

Hyperbolic phonon polaritons in periodic structures

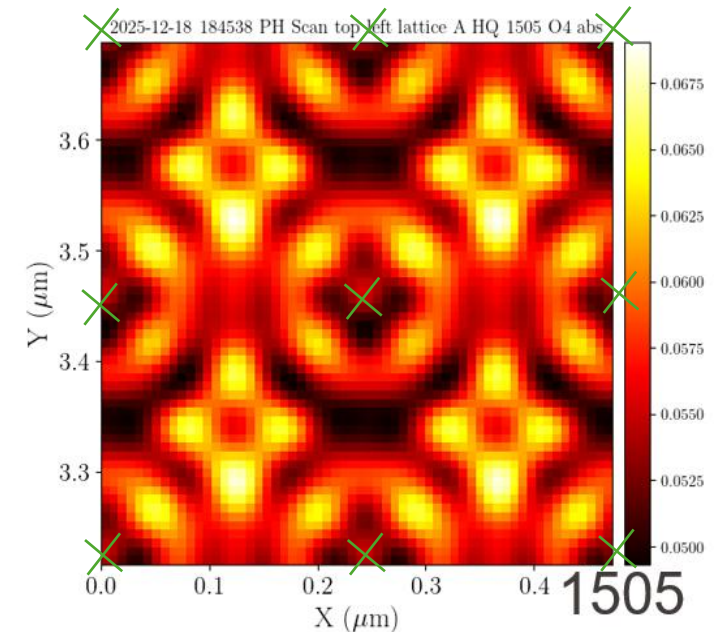
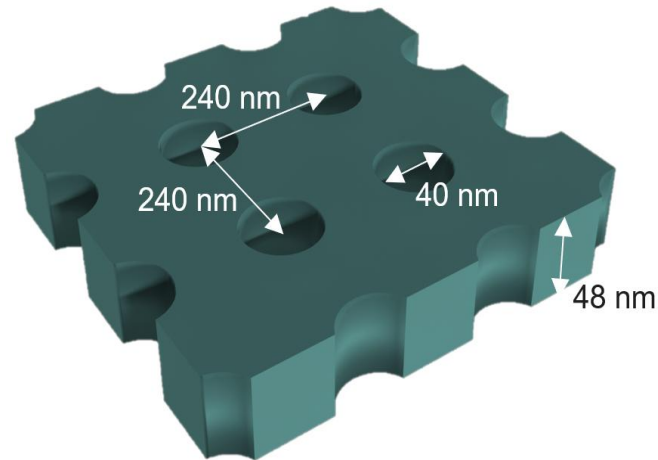
- Martin van Exter,
- Lorenzo Orisini,
- Elisa Mendels,
- Bianca Turini,
- Zoe Velluire-Pellat,
- Frank Koppens



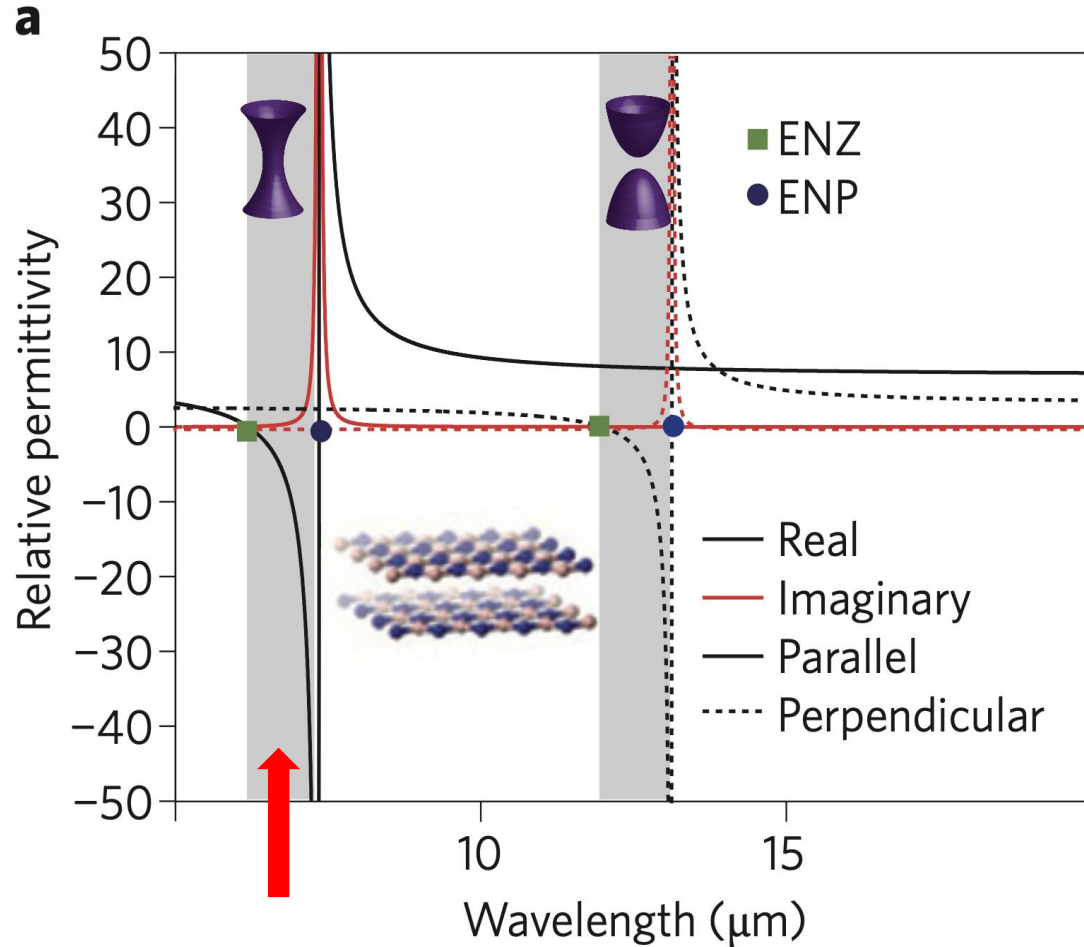
Elisa Mendels



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Hyperbolic phonon polaritons (HPhPs) in hBN



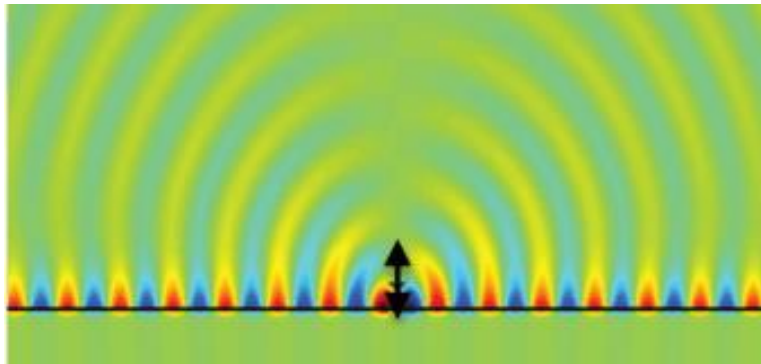
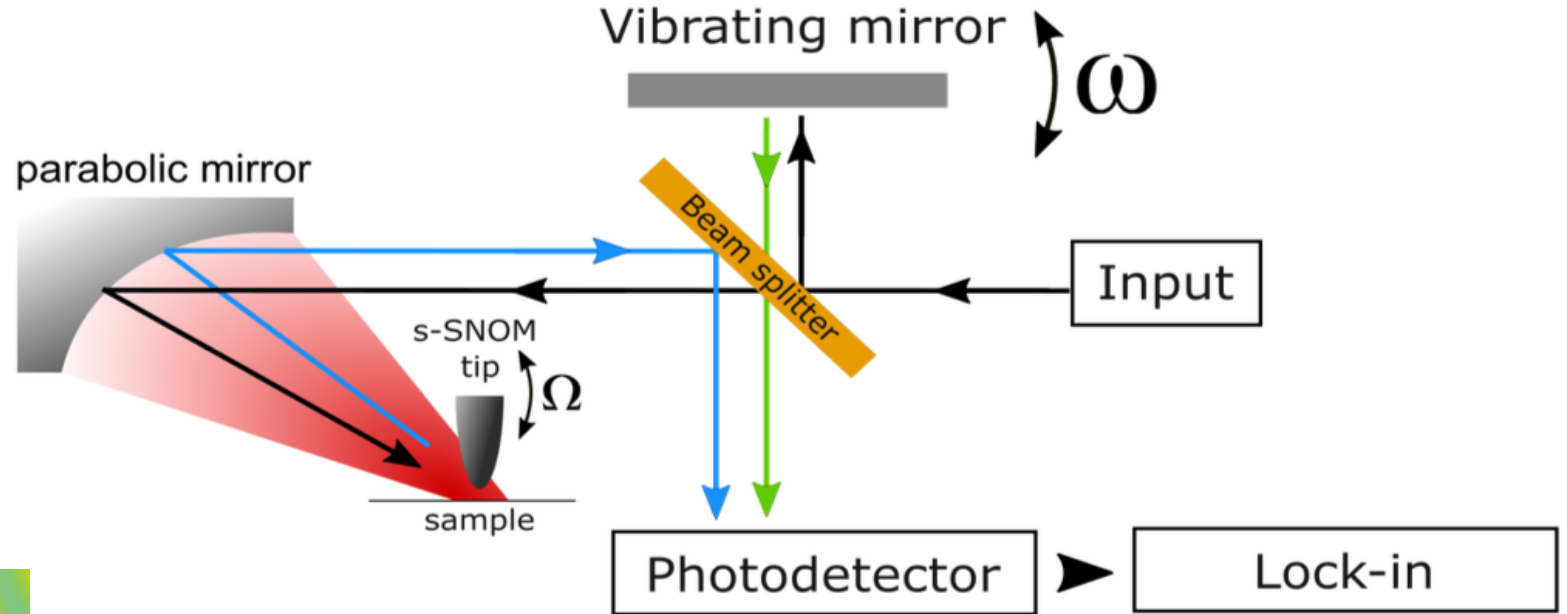
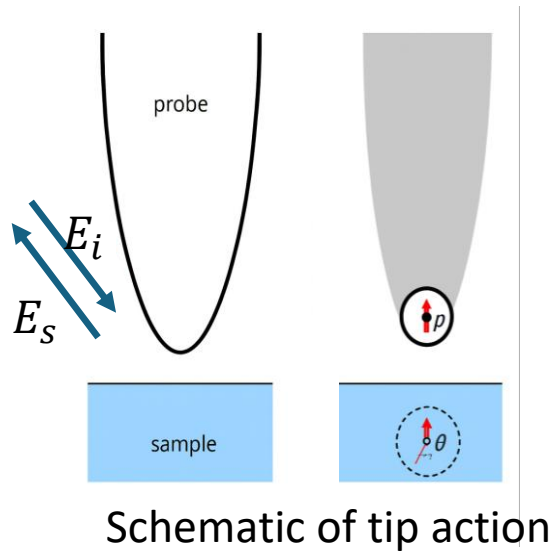
$$\lambda \approx 6 - 7.5 \mu\text{m} ; 1/\lambda \approx 1350-1650 \text{ cm}^{-1}$$

Type II: In-plane $\epsilon_{xx} = \epsilon_{yy} < 0$

$$\epsilon(\omega) \approx -\epsilon_x^\infty \left(\frac{\omega_{LO}^2 - \omega^2}{\omega^2 - \omega_{TO}^2} \right) (1 - i\delta)$$

$$\frac{k_x^2}{\epsilon_{zz}} + \frac{k_z^2}{\epsilon_{xx}} = k_0^2$$

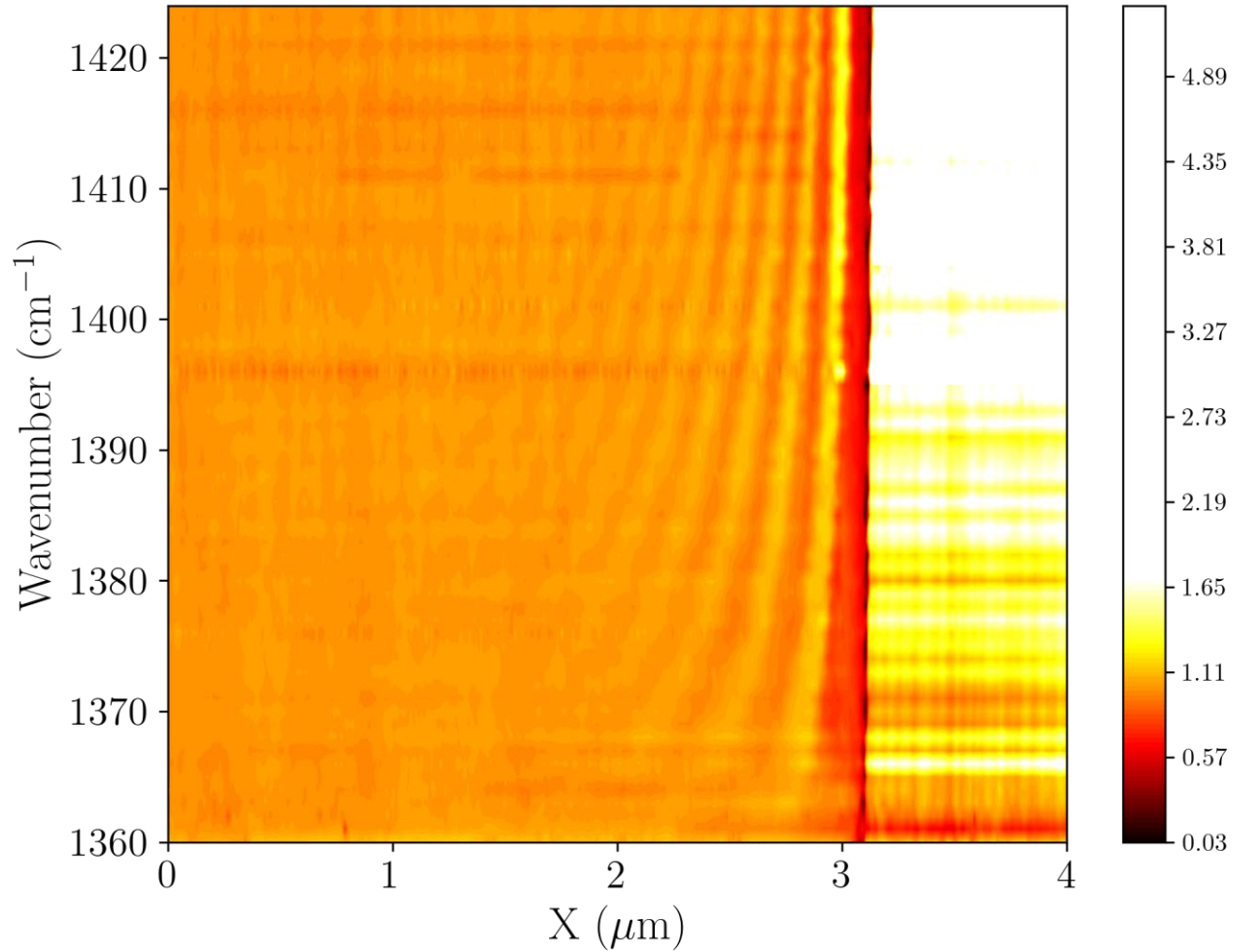
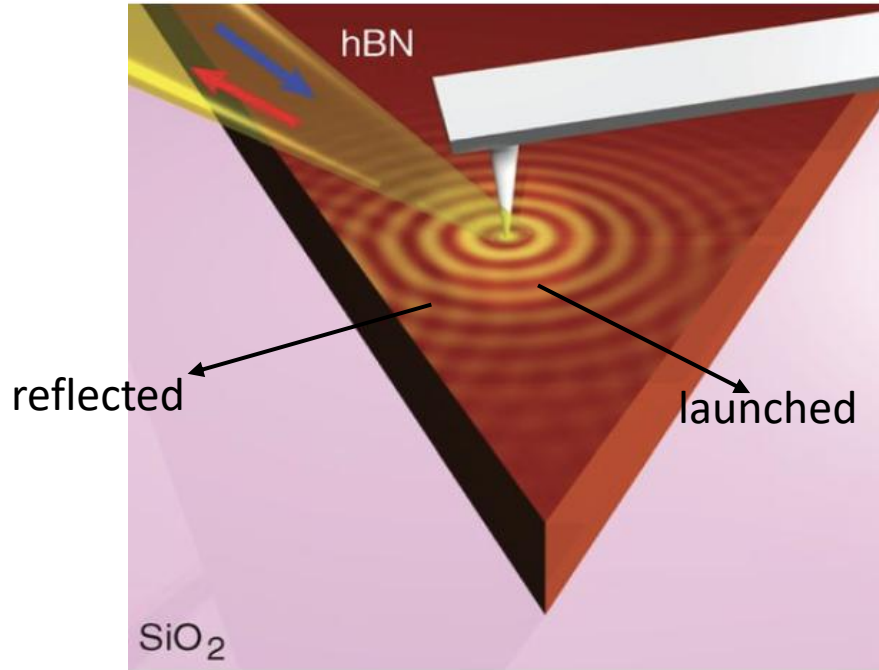
Scanning Near-field Optical Microscope (SNOM)



Schematics of propagation of polaritons from sSNOM tip

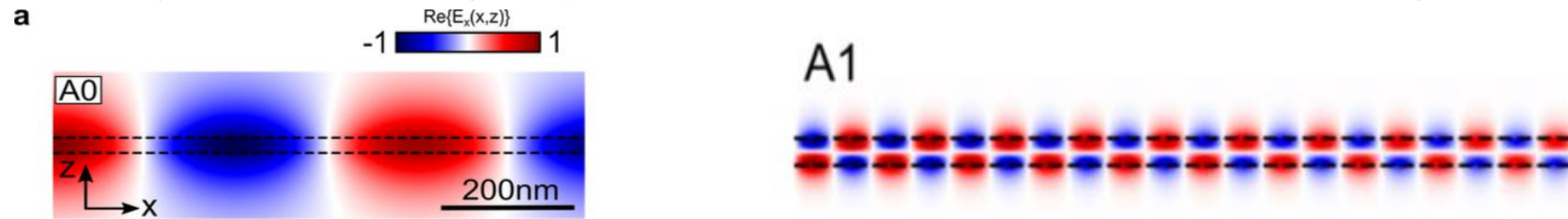
Earlier observations of HPhPs in hBN

2025-09-16 162150 PH h11BN gold chip flake A right edge frequencysweep HQ 1360to1460 O4 abs

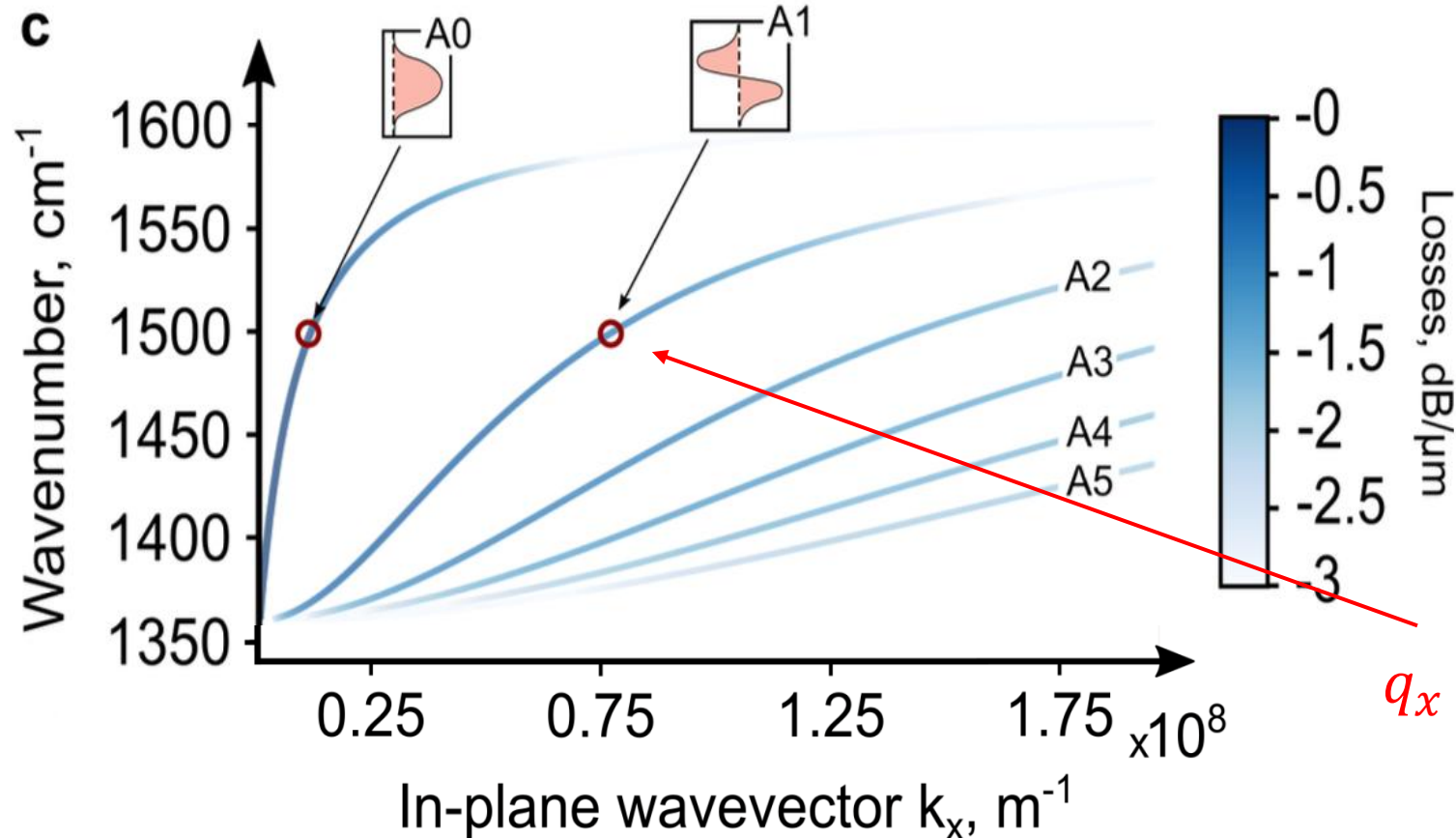


Frequency sweep on an hBN edge

Why? Strong spatial confinement of light

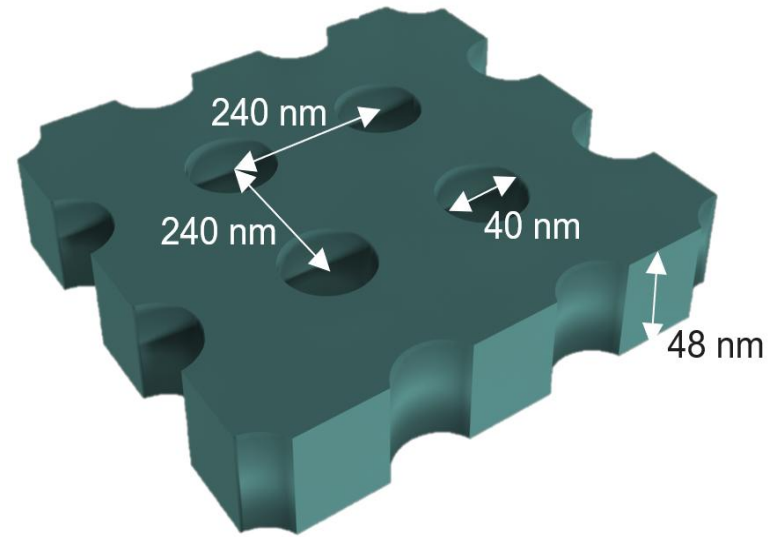
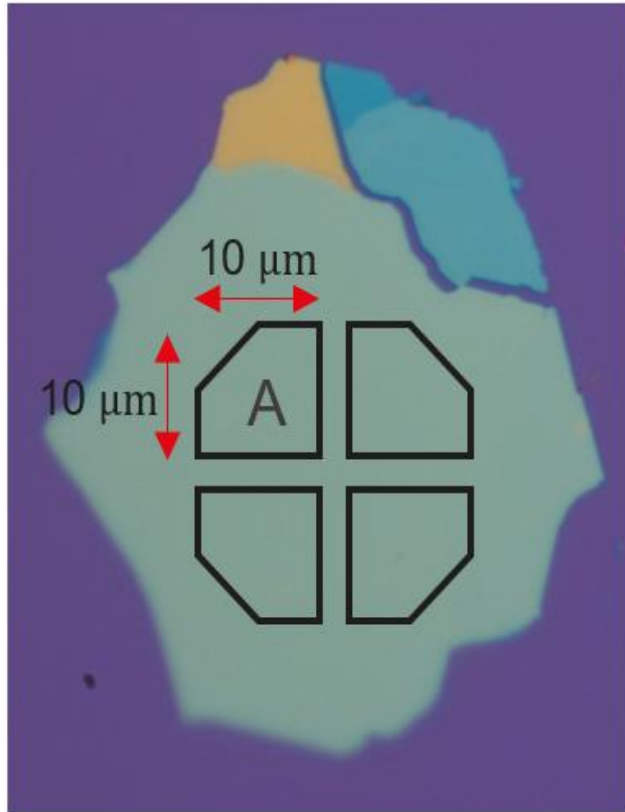


Higher-order
HPhPs (A1, ...) have stronger confinement

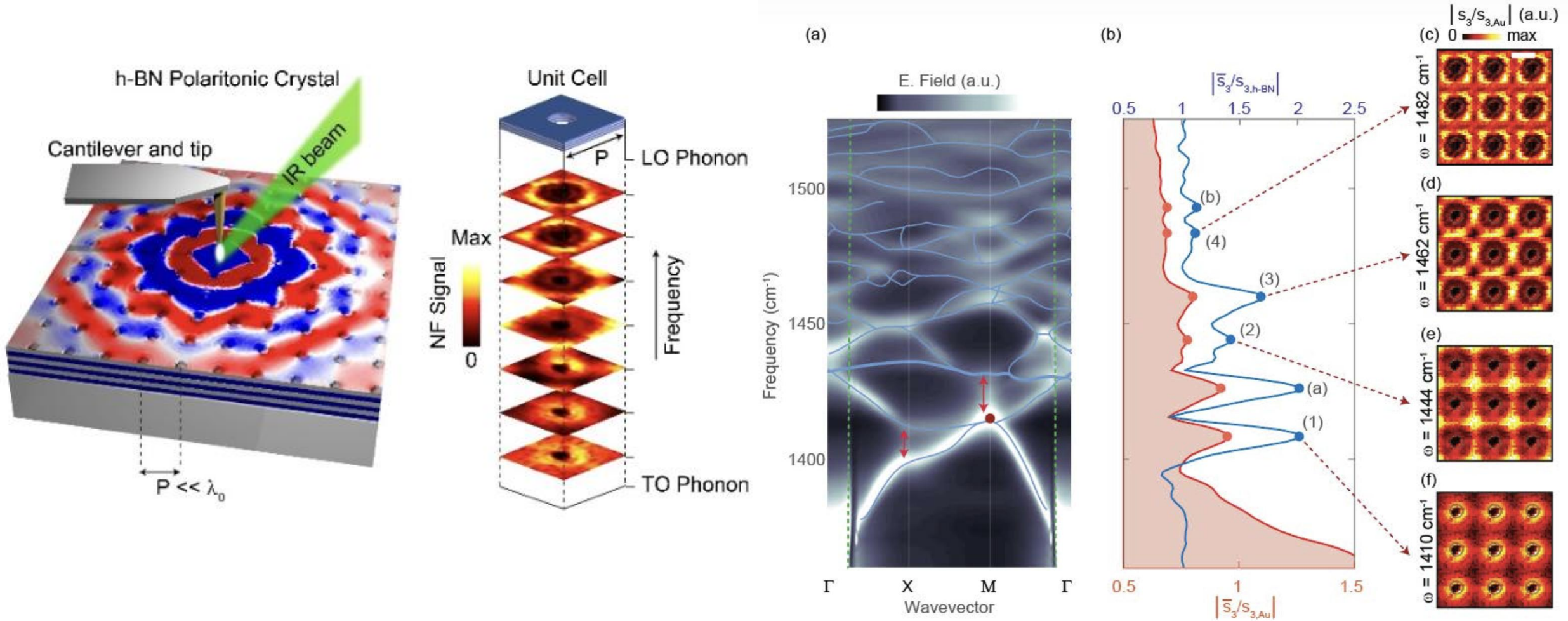


$$q_x = \frac{1}{\lambda_x} = \frac{k_x}{2\pi} \approx 120,000 \text{ cm}^{-1} \approx 12 \mu\text{m}^{-1}$$

Geometry: periodic array of holes in hBN film



Earlier work on ‘Hole arrays in hBN = polaritonic crystals’



F.J. Alfaro-Mozaz, ..., L. Martin-Moreno, R. Hillenbrand, A.Y. Nikitin, 'Hyperspectral nanoimaging of van der Waals polaritonic crystals', Nano Lett. 21, 7109 (2021)

Our SNOM image of hole array in hBN @ 1520 cm⁻¹

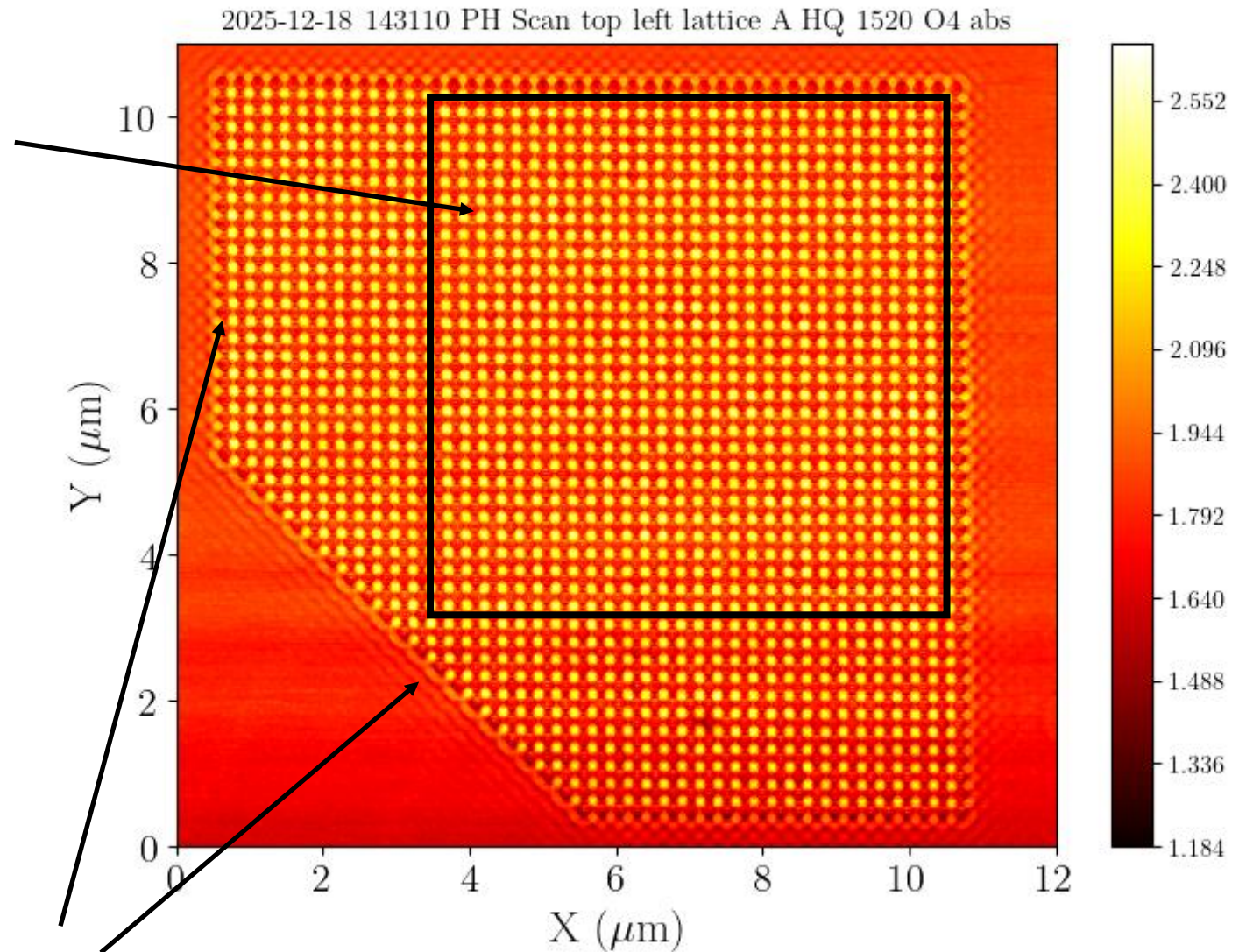
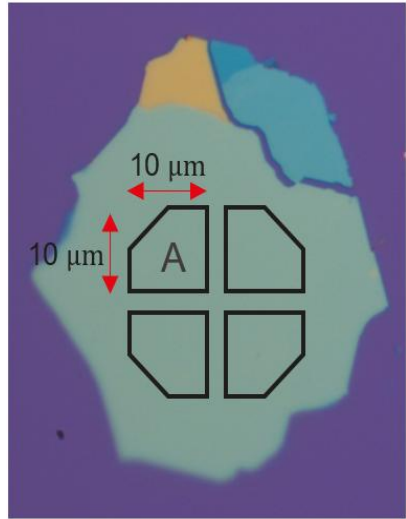
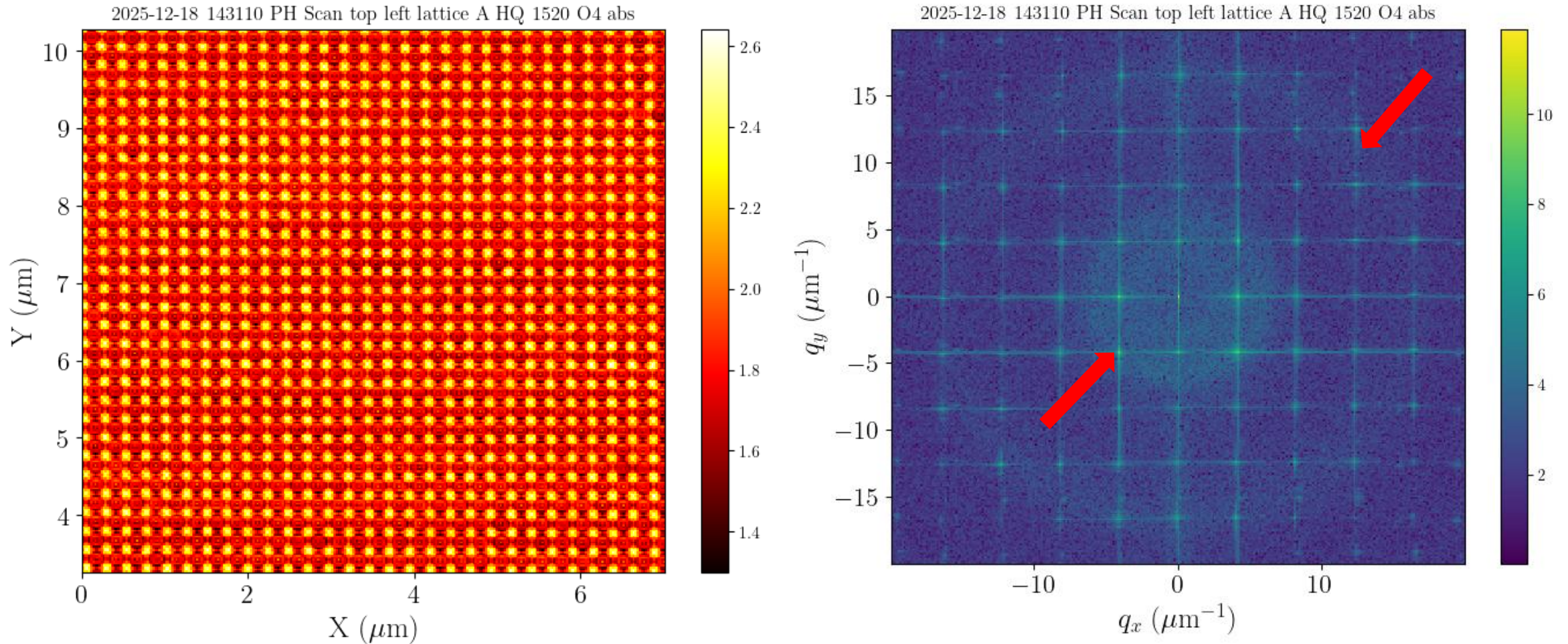


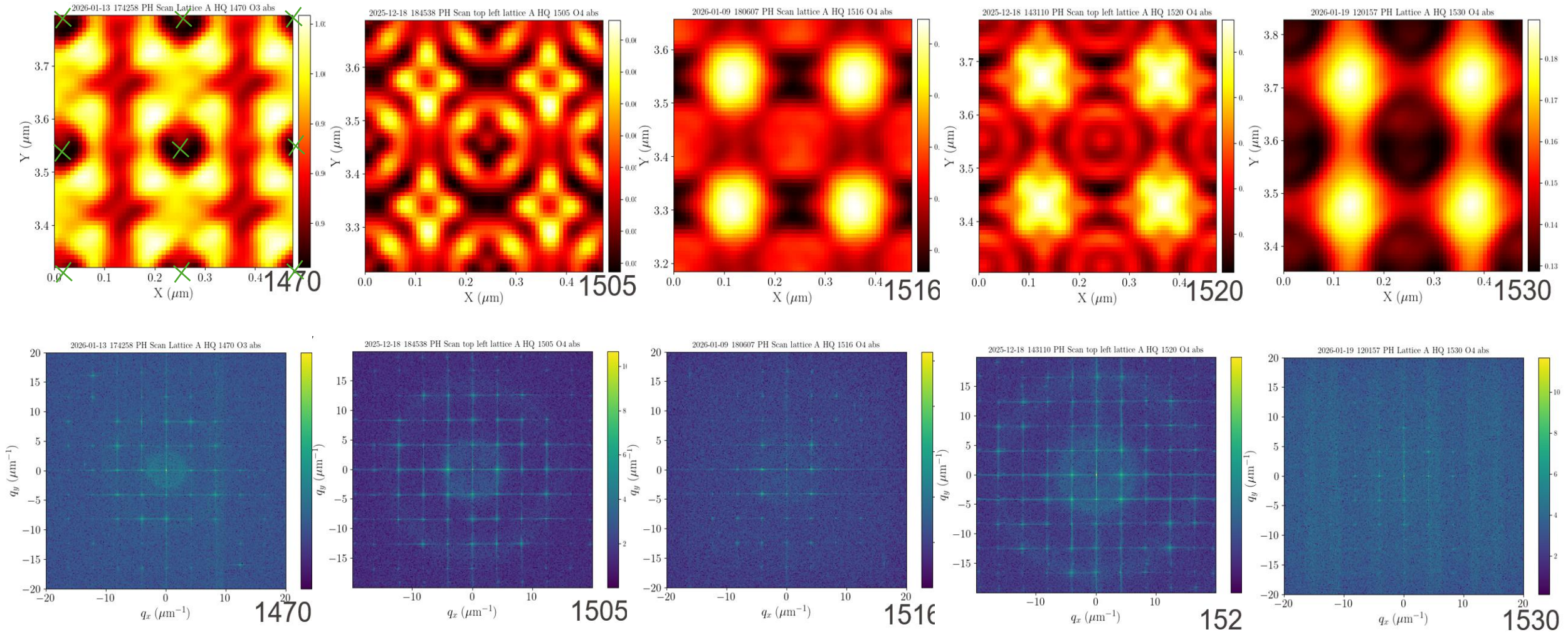
Image processing: Cut & apply Fourier transform



Fourier lattice: $(q_x, q_y) = (m_x, m_y)/a$

Angle (deg): -0.02 ± 0.44 , FFT Lattice const (μm^{-1}): 4.13 ± 0.04 , Real-space lattice const (μm): 0.242 ± 0.002

SNOM & Fourier images at different wavelength

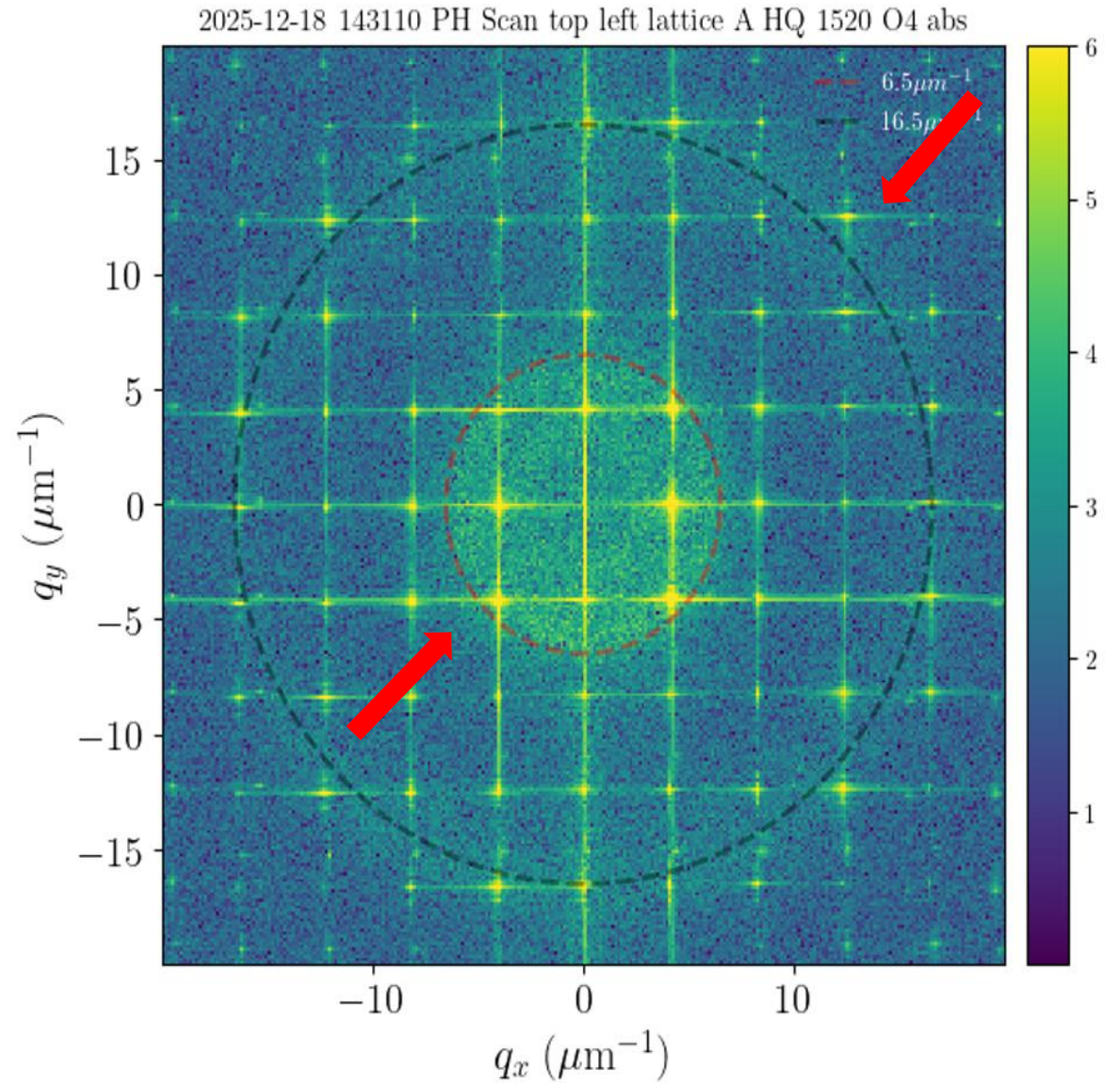


Faint rings in Fourier images

Sketched rings at:

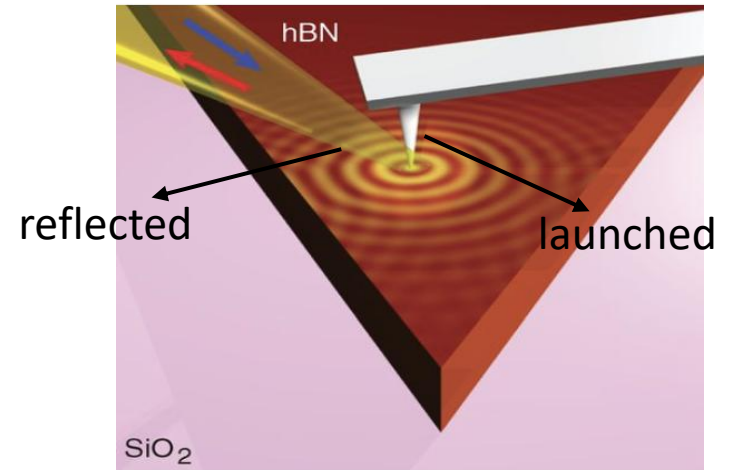
$$q_x = 6.5 \mu\text{m}^{-1} \text{ (A0)}$$

$$q_x = 16.5 \mu\text{m}^{-1} \text{ (A1)}$$



Towards a simple theory

- Traditional theory: excitation & detection of HPhPs



- Alternative theory: Green's function & LDOS

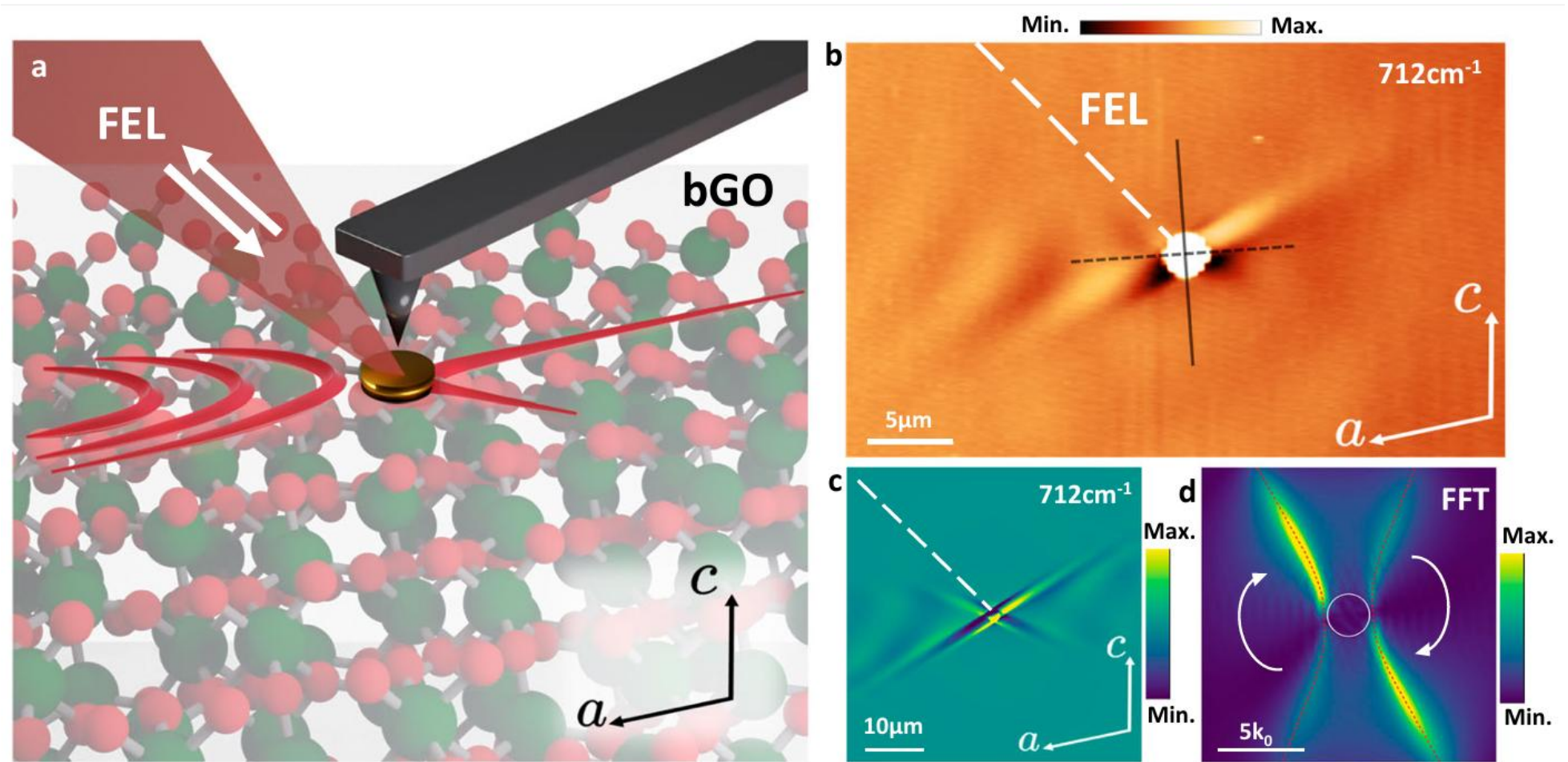
- Hypothesis 1: $E_{SNOM}(\vec{r}, \omega) \propto G_{2D}(\vec{r}, \vec{r}, \omega)$

- Hypothesis 2: $E_{SNOM}(\vec{r}, \omega) \propto \sum_j \frac{|\psi_j(\vec{r})|^2}{1 - i(\omega - \omega_j)/\gamma_j}$

Suggestions for future experiments

- Quantitative comparison theory-experiment
- Randomly positioned holes?
- Single hole?

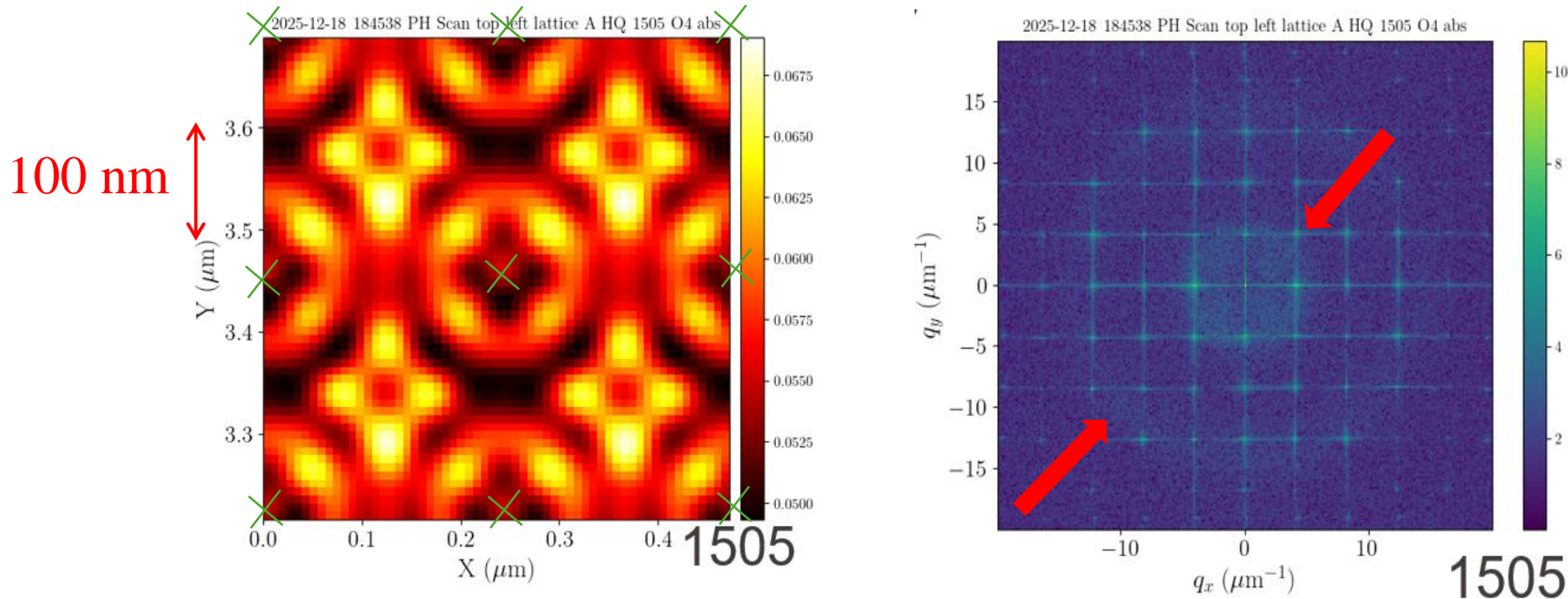
Link to talk of Alex Paarmann on ‘hyperbolic shear polaritons’



J. Matson, ..., A. Paarmann, J.D. Caldwell, ‘Controlling the propagation asymmetry of hyperbolic shear polaritons in beta-gallium oxide’, Nature Comm. 14, 5240 (2023)

Concluding summary

- SNOM images show fascinating details, $< 40 \text{ nm}$ ($\lambda_{SNOM} \approx 6 \mu\text{m}$)



- Higher-order hyperbolic phonon polaritons are visible
- Different lattice modes are visible
- Theoretical support would be appreciated 😊