

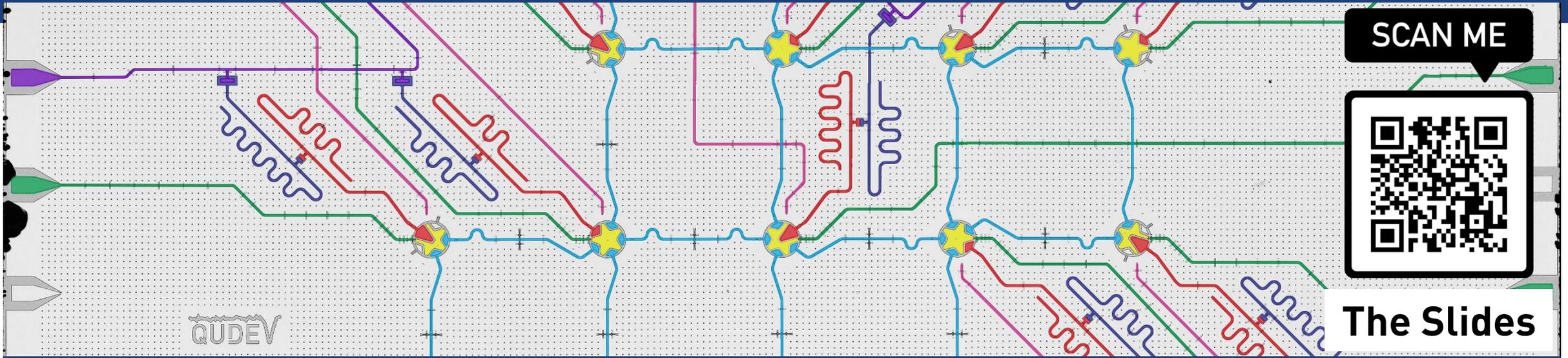
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QUDEV

SCAN ME



The Slides



Quantum Error Correction with Superconducting Circuits (Lecture 1)

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Confederaziun svizra
Swiss Confederation
Innosuisse – Swiss Innovation Agency

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www.qudev.ethz.ch

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Collaborations (last 5 years) with groups of

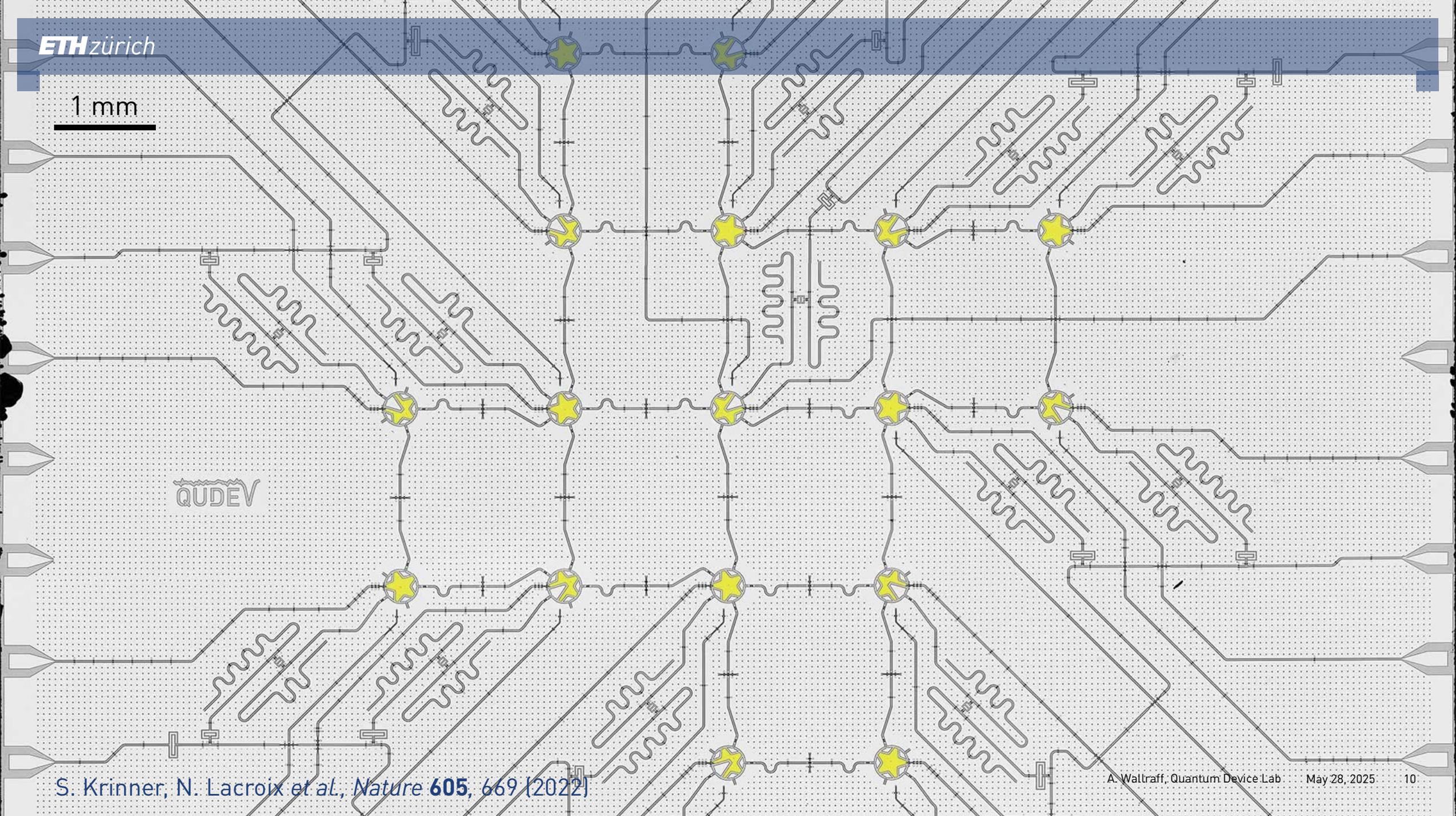
C. Abellan (Quside)
P. Bertet (CEA Saclay)
A. Blais (Sherbrooke)
J. Bylander (Chalmers)
H. J. Carmichael (Auckland)
A. Chin (Cambridge)
I. Cirac (MPQ)
K. Ensslin (ETH Zurich)

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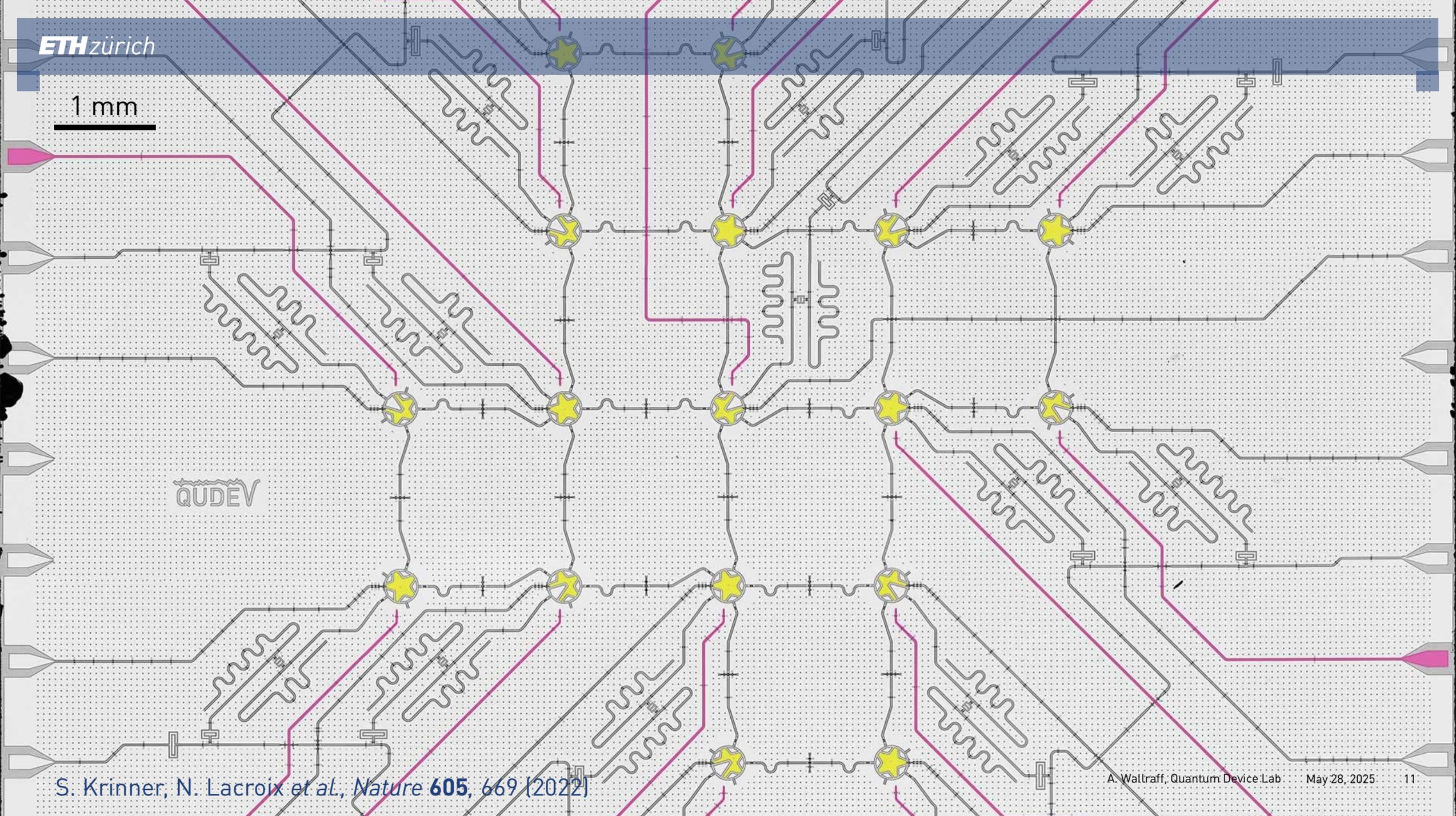
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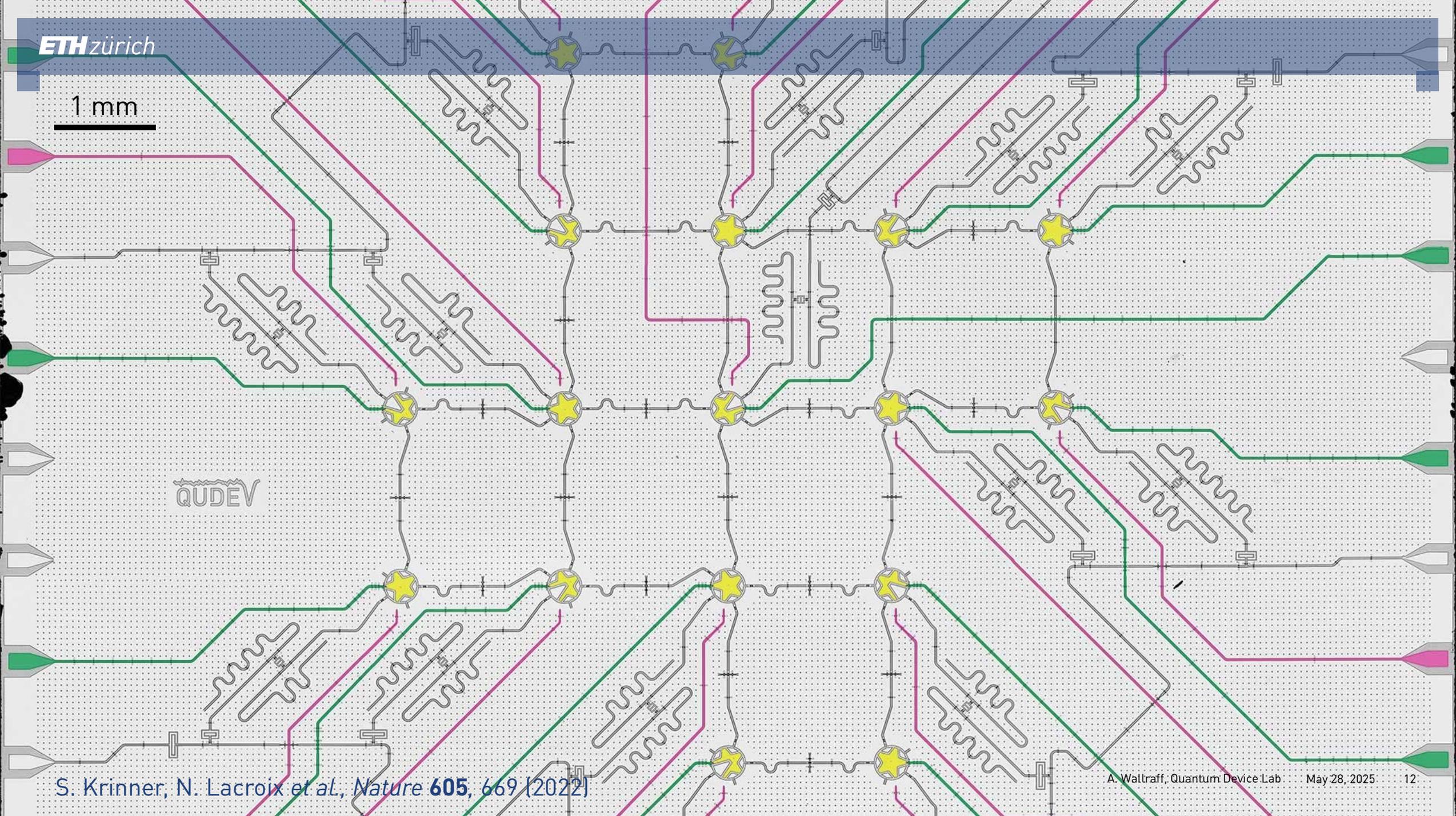
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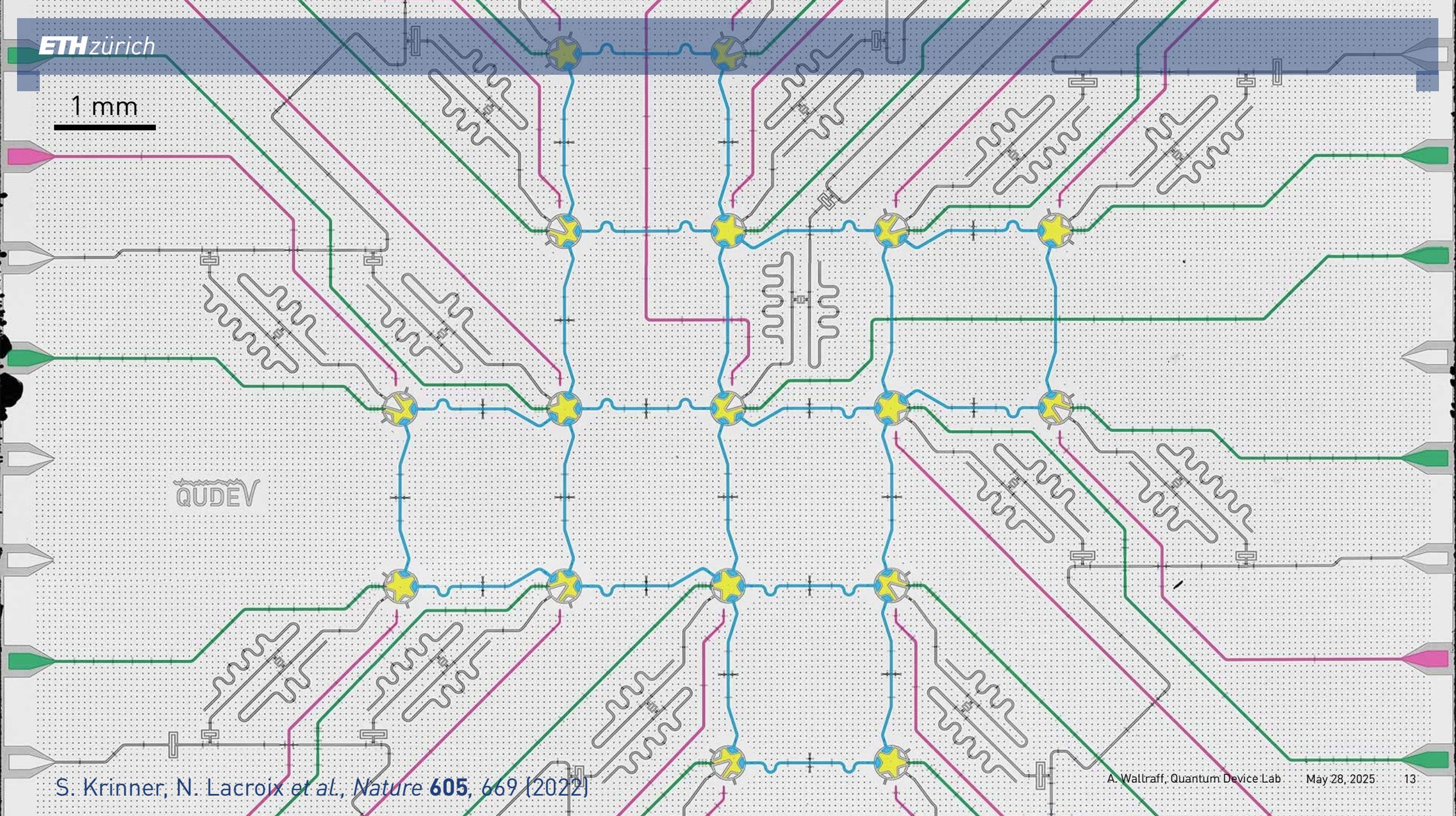


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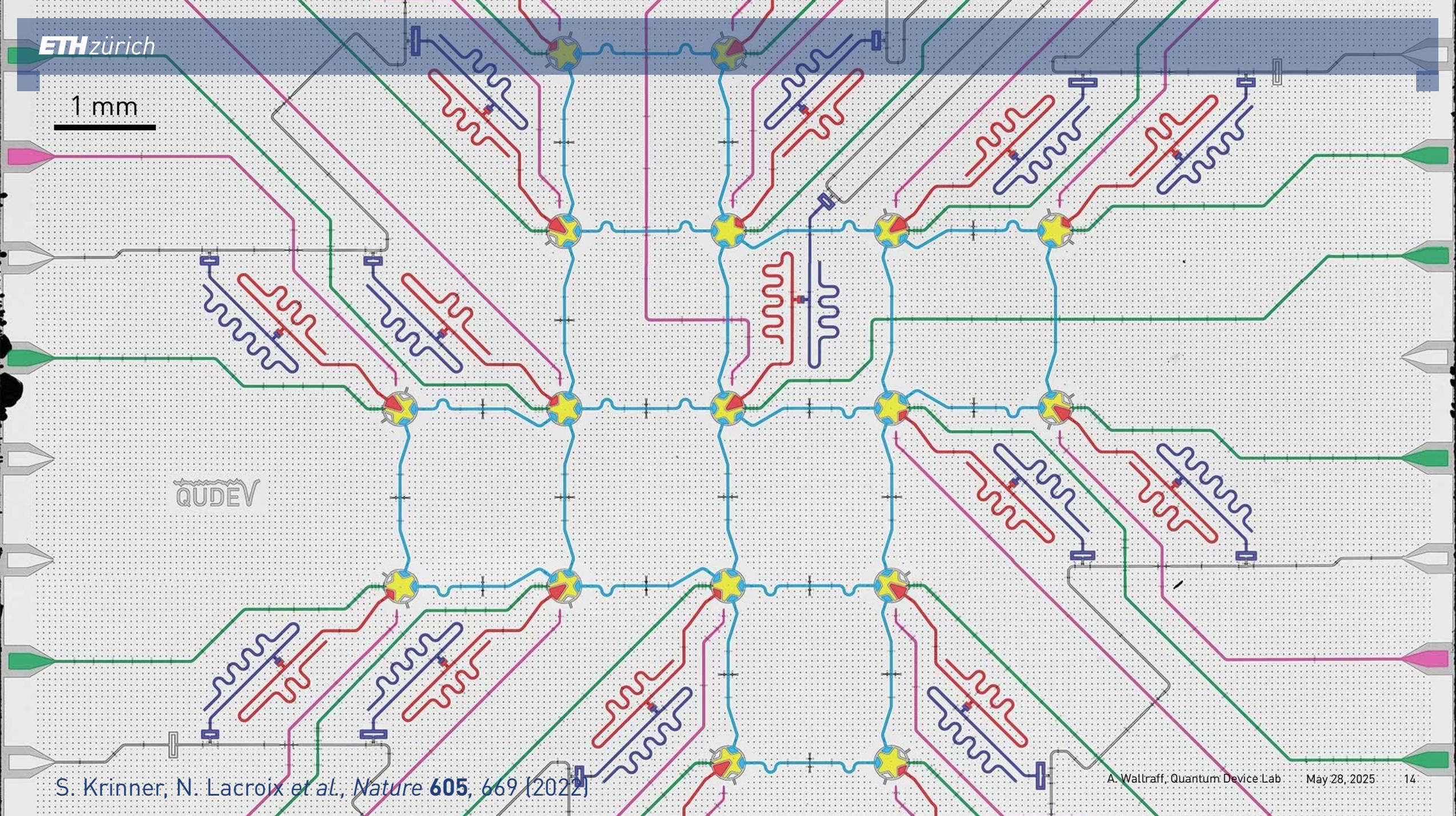


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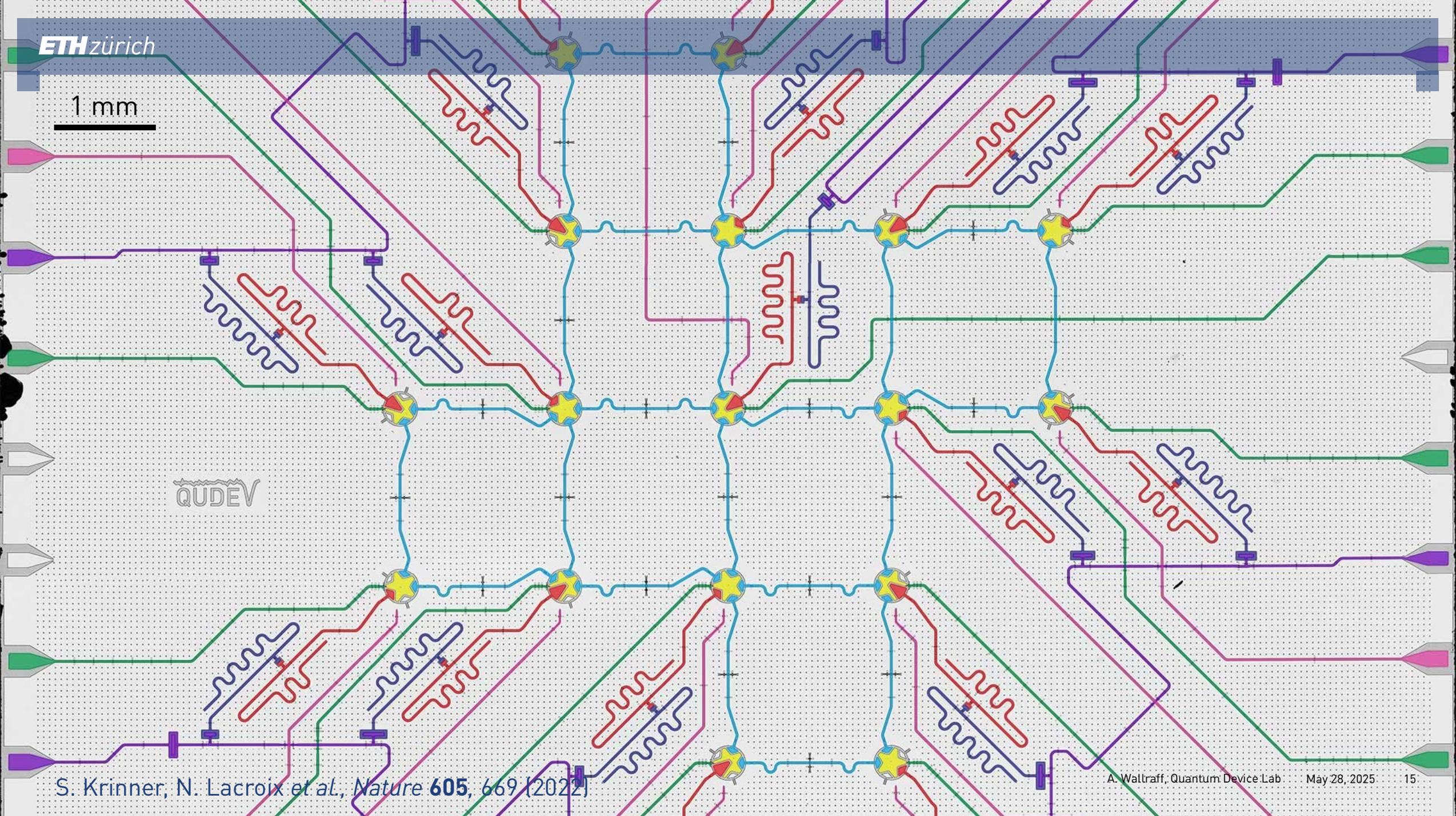
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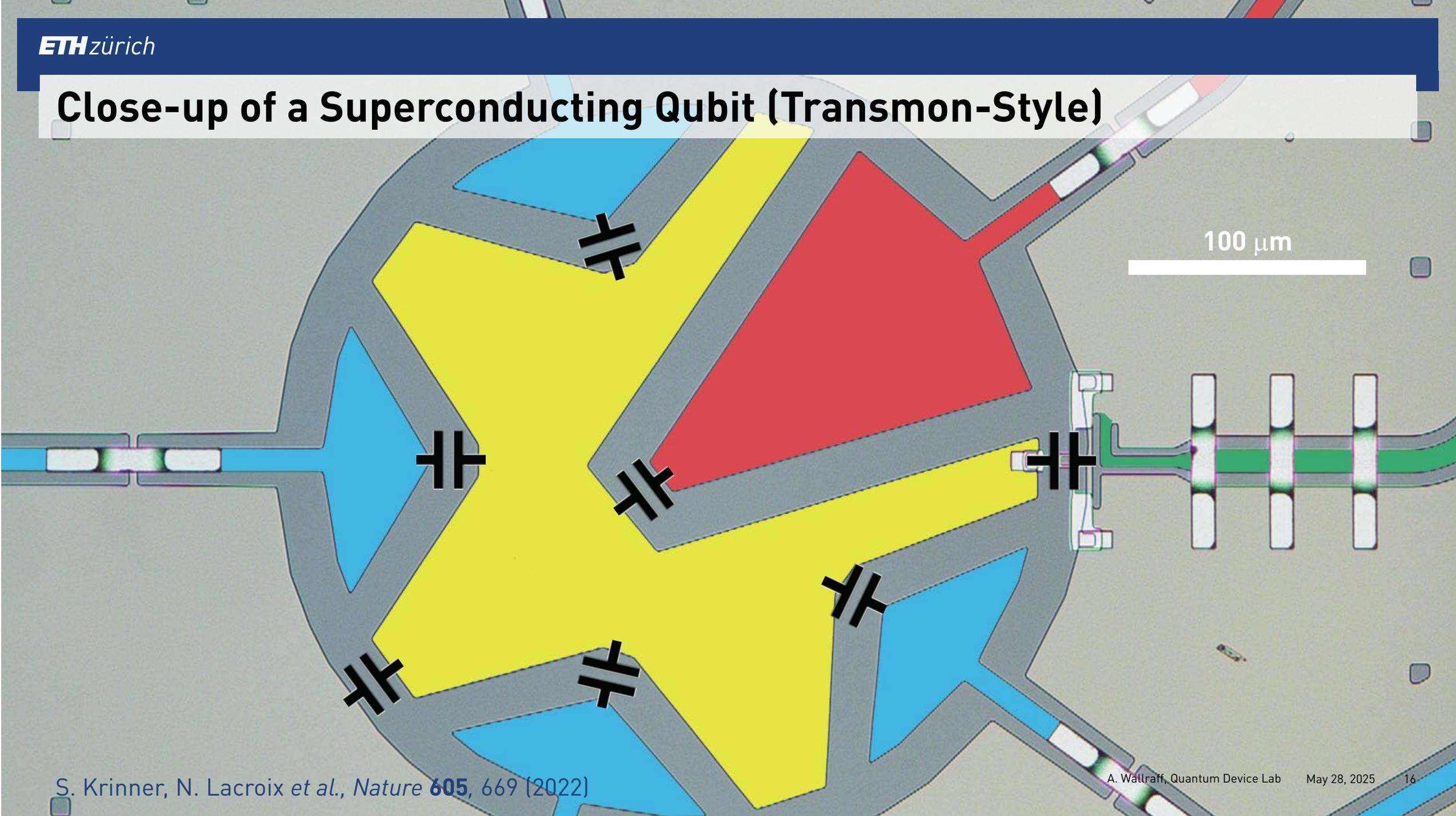


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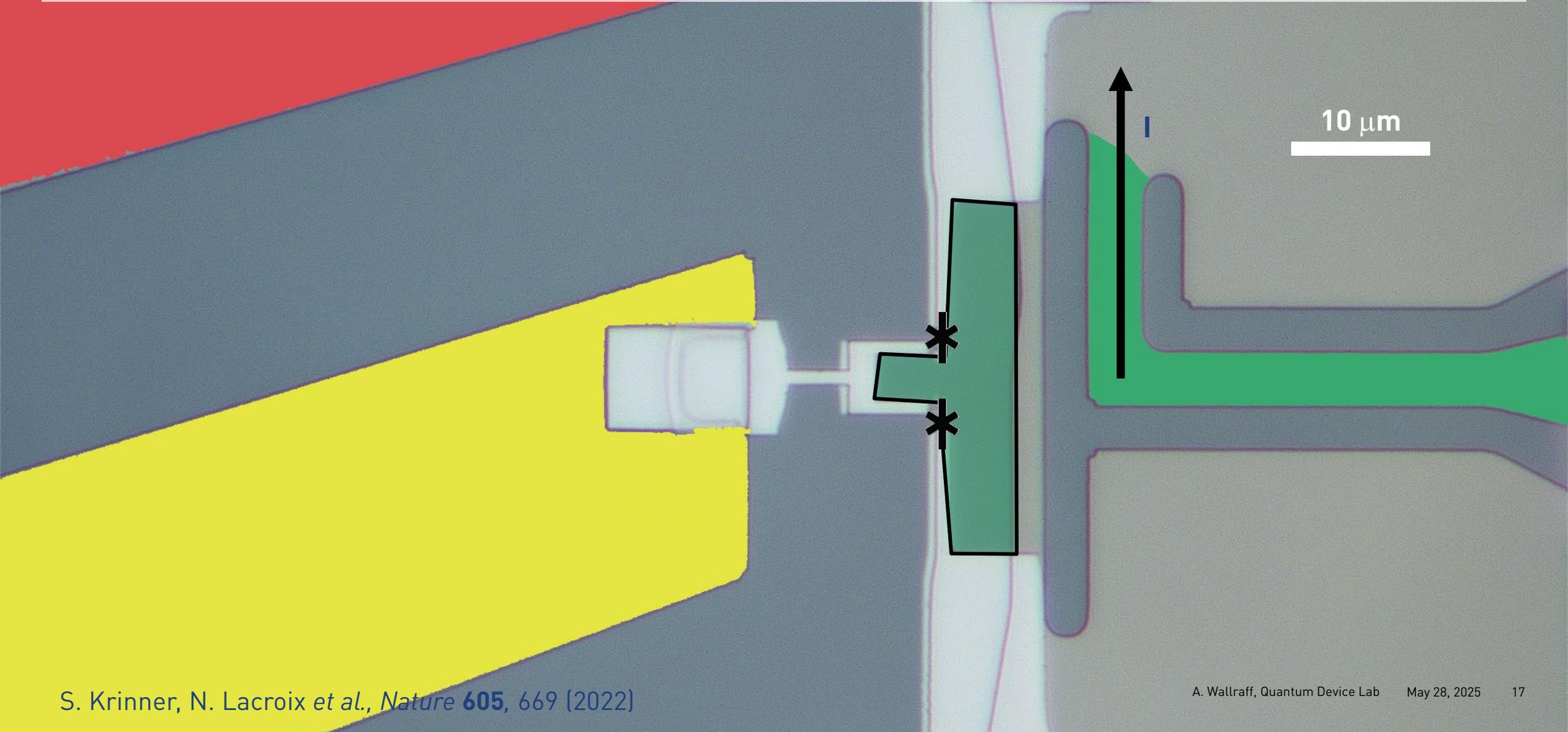


Close-up of a Superconducting Qubit (Transmon-Style)



100 μm

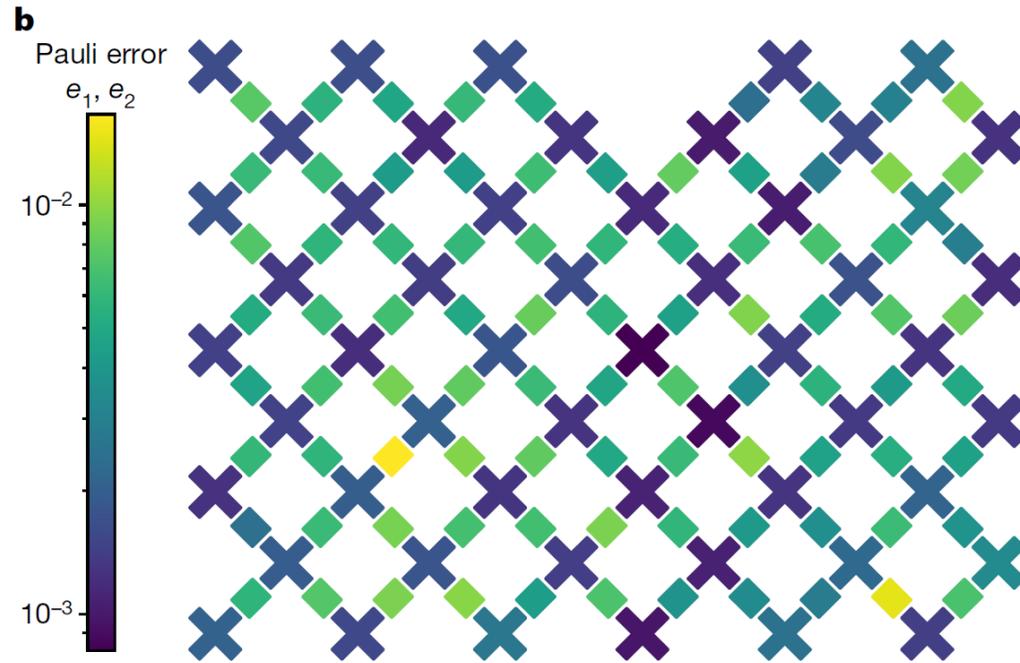
Tunnel Junctions, SQUID, and Fluxline



Two of the Major Goals in Quantum Information Processing ...

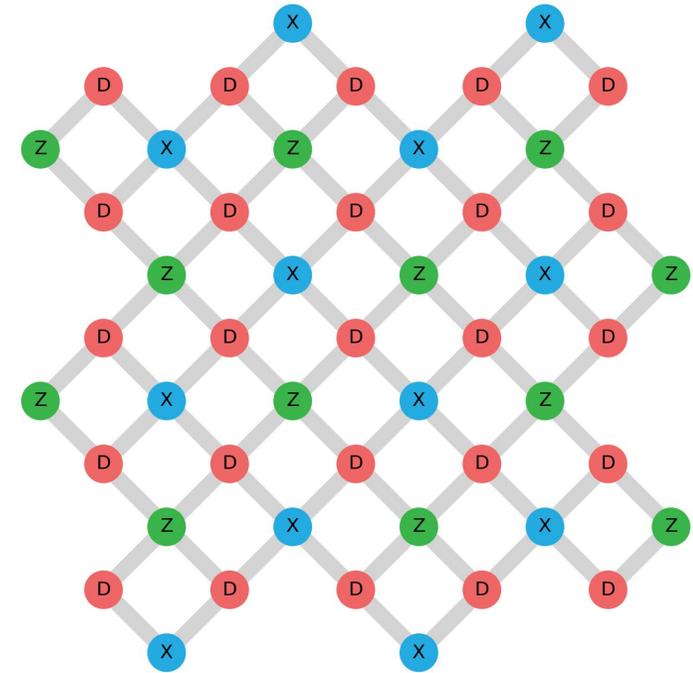
... with superconducting circuits

Noisy Intermediate Scale Quantum (NISQ) algorithms displaying a quantum advantage



F. Arute, ..., J. M. Martinis *et al.*, *Nature* **574**, 505 (2019)

Fault-tolerant, error-corrected, universal quantum information processor

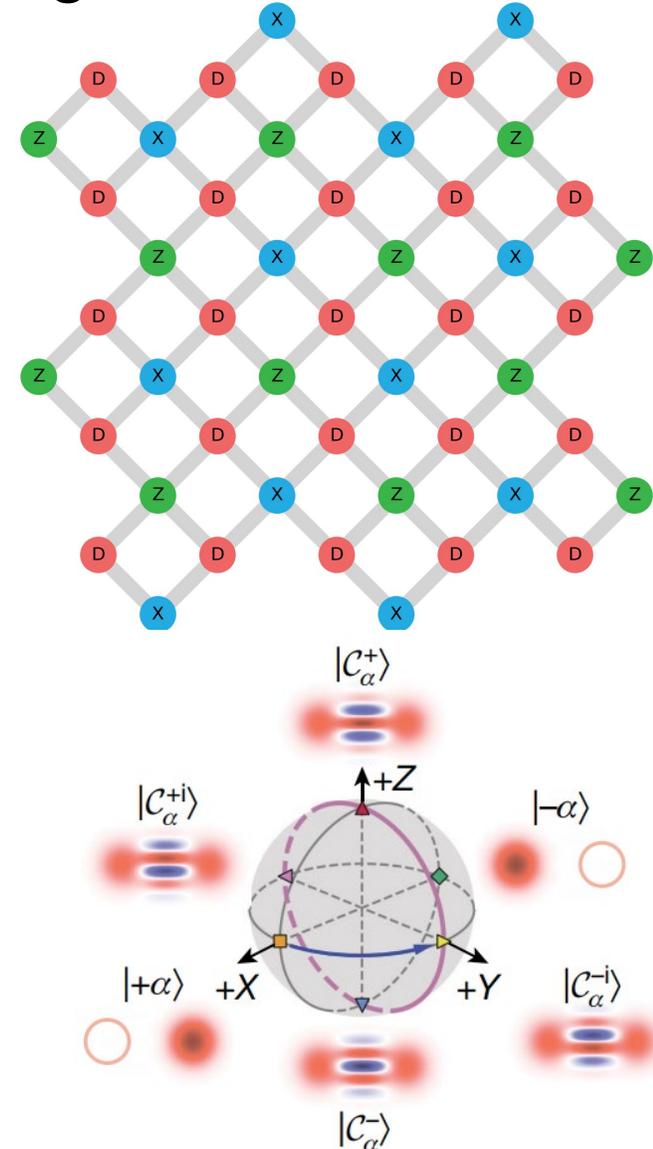


Fowler *et al.*, *Phys. Rev. A* **86**, 032324 (2012)

Quantum Error Correction with Superconducting Circuits

Approaches:

- Digital, qubit-based encodings: e.g. surface code, color code
- Continuous variable encodings in harmonic oscillator states: e.g. cat states, GKP states



Preskill, *Quantum* **2**, 79 (2020)

Review: Terhal, *Rev. Mod. Phys.* **87**, 307 (2015)

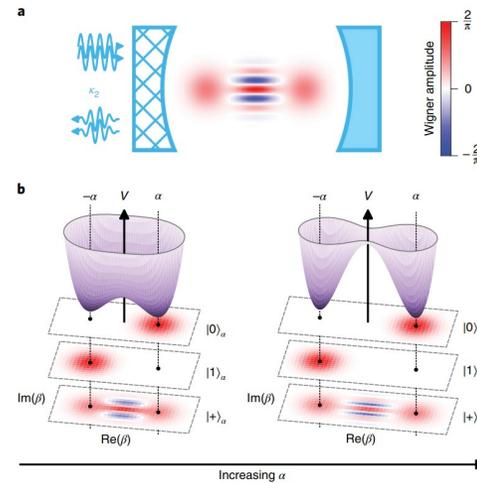
Bosonic Quantum Error Correction Experiments

Continuous QEC

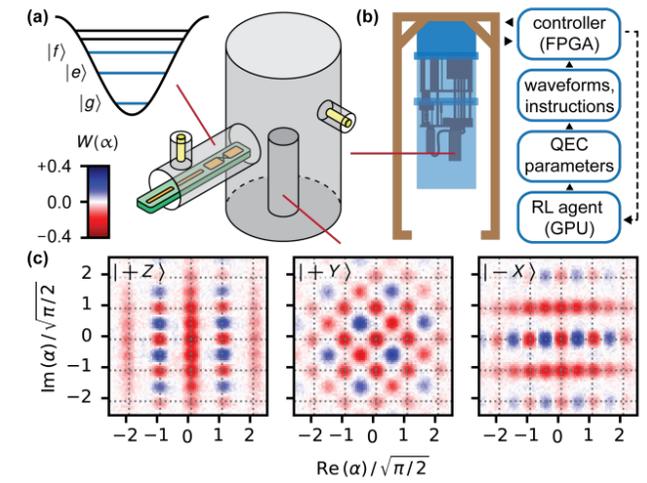
- Dissipative-cat codes
Leghtas, et. al. Science 347, 853 (2015)
Lescanne, et. al. Nature Physics 16, 509 (2020)
Gertler et. al. Nature 590, 243 (2021)
- Kerr-cat codes
Grimm, et. al. Nature 584, 205 (2020)

Discrete QEC

- Binomial bosonic codes
Ni, Z. et al., Nature 616, 56 (2023).
Hu et al., Nature Physics 15, 503 (2019).
- Cat-Codes
Ofek et. al., Nature 536, 441 (2016)



Lescanne et. al. Nat. Phys. 16, 509 (2020)



Sivak et. al. arXiv:2211.09116 (2022)

GKP codes

- Trapped ions
Flühmann et. al., Nature 566, 513 (2019)
de Neeve et. al., Nature Physics 18, 296 (2022)
- Superconducting circuits
Campagne-Ibarcq et. al., Nature 584, 368 (2020)
Sivak et al., Nature 616, 50 (2023).

Why is Error Correction Needed?

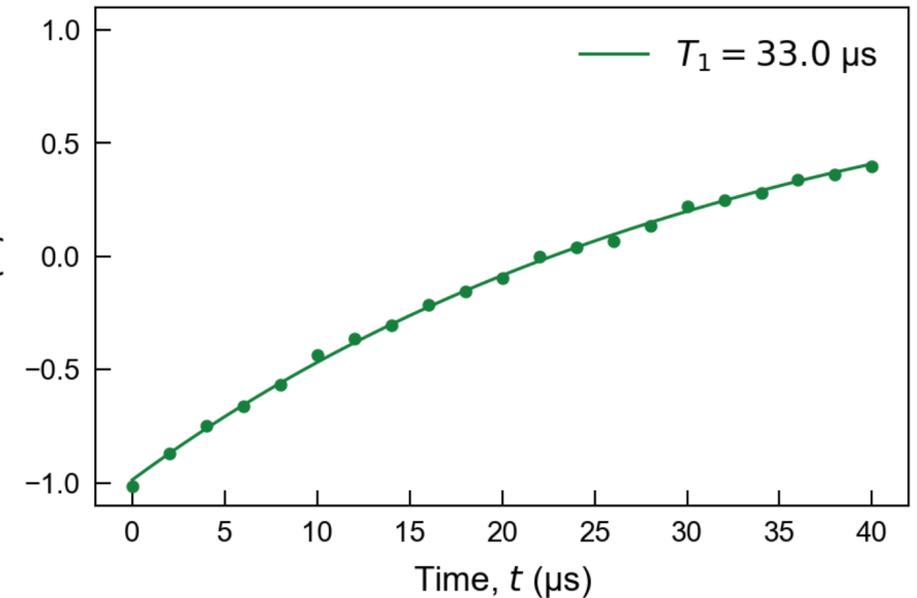
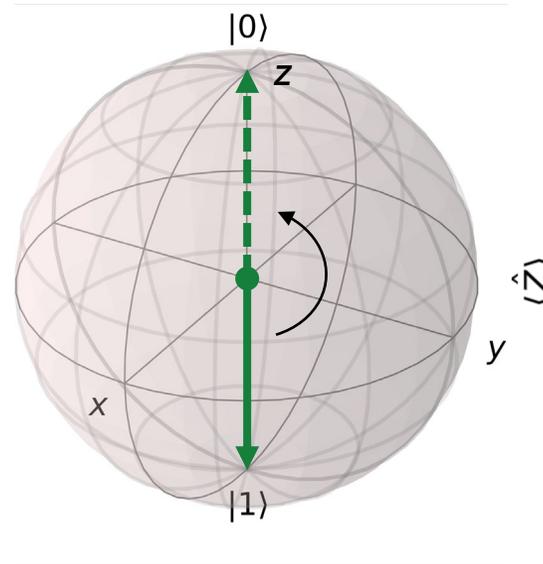
- Computational basis states are eigenstates of the Pauli Z operator

$$\hat{Z} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\hat{Z}|0\rangle = +1 |0\rangle$$

$$\hat{Z}|1\rangle = -1 |1\rangle$$

- Every excited quantum system undergoes spontaneous emission $|1\rangle \rightarrow |0\rangle$
- Bit flip errors** also occur due to
 - Thermal excitation
 - Control inaccuracies
- The expectation value of \hat{Z} characterizes the decay of the excited state on average



A Second Type of Error: Phase Flips

- Quantum computers make use of superposition states $|\pm\rangle = \frac{1}{\sqrt{2}}(|0\rangle \pm |1\rangle)$

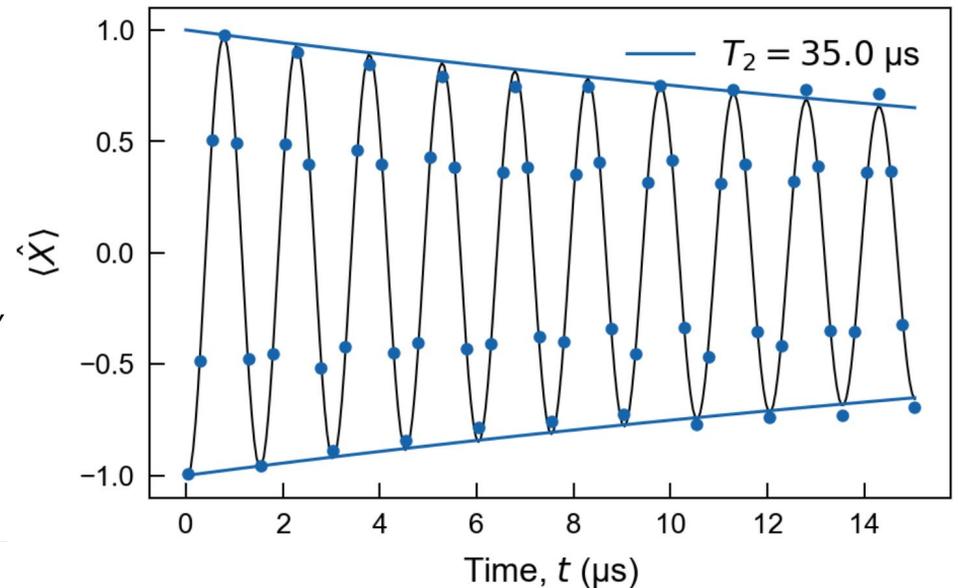
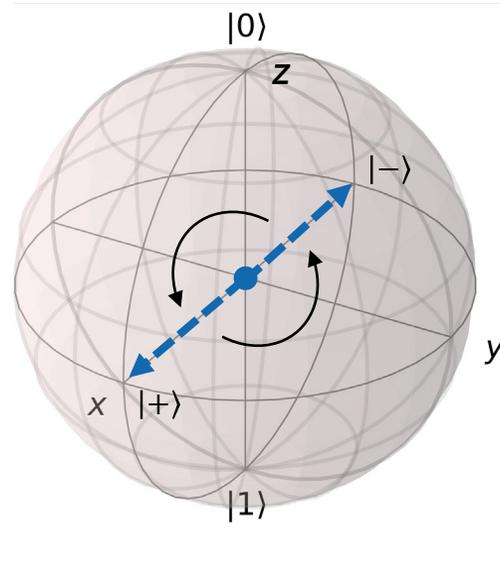
- Eigenstates of

$$\hat{X} = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

$$\hat{X}|+\rangle = +1|+\rangle$$

$$\hat{X}|-\rangle = -1|-\rangle$$

- Phase flip errors** occur due to
 - Environmental field fluctuations
 - Control inaccuracies
 - Energy relaxation
- Expectation value of \hat{X} characterizes the decay of the quantum phase on average



The Challenge of Quantum Error Correction

Detect and correct two types of errors:

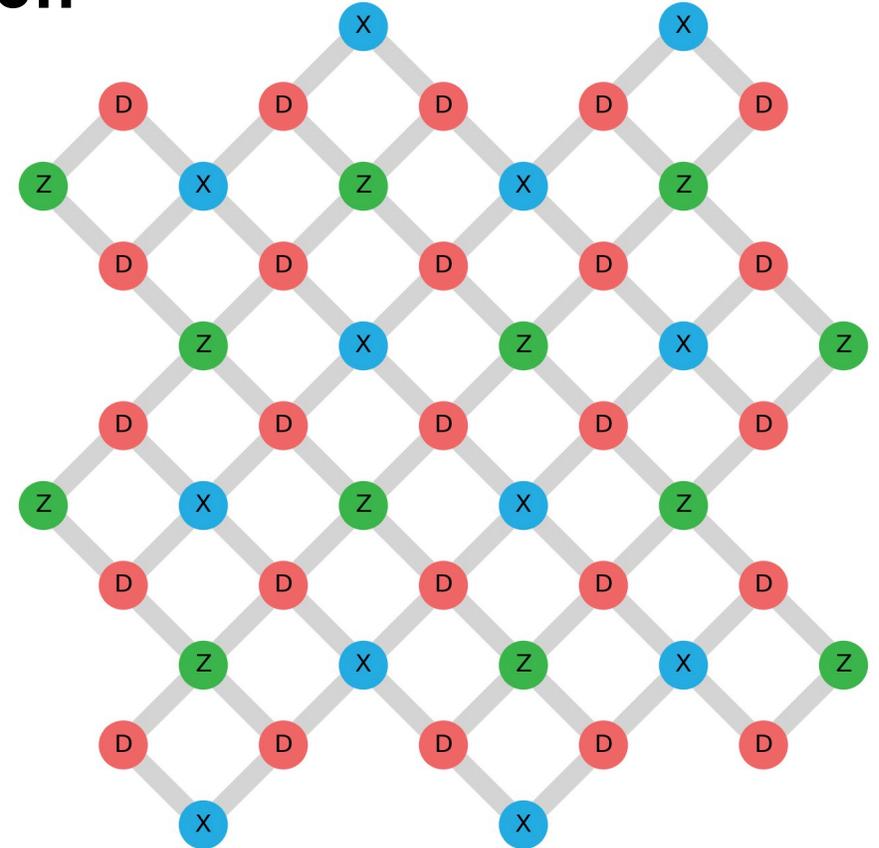
- Bit flips
- Phase flips

Preserve stored quantum states while detecting and correcting errors:

- Measurements collapse quantum (superposition) states

Solution: Use encoding

- Store **logical qubit** state $|\psi\rangle$ in a system of many **physical qubits**
- Make use of **symmetry properties (parity)** of logical qubit states
 - revealing errors ...
 - ... but not the encoded quantum state



Kitaev, *Annals of Physics* **303**, 2 (2003),
 Dennis et al., *Journ. of Math. Physics* **43**, 4452 (2002)
 Raussendorff, Harrington, *Phys. Rev. Lett.* **98**, 190504 (2007)
 Fowler et al., *Phys. Rev. A* **86**, 032324 (2012)

The Surface Code – Main Features

Large error threshold $\epsilon_{\text{th}} \sim 1\%$

- Logical error rate $\epsilon_L \propto (\epsilon_{\text{phys}}/\epsilon_{\text{th}})^{(d+1)/2}$

ϵ_{phys} : Physical error rate per step

ϵ_{th} : Threshold error rate

d : Distance of the code

Two-dimensional architecture

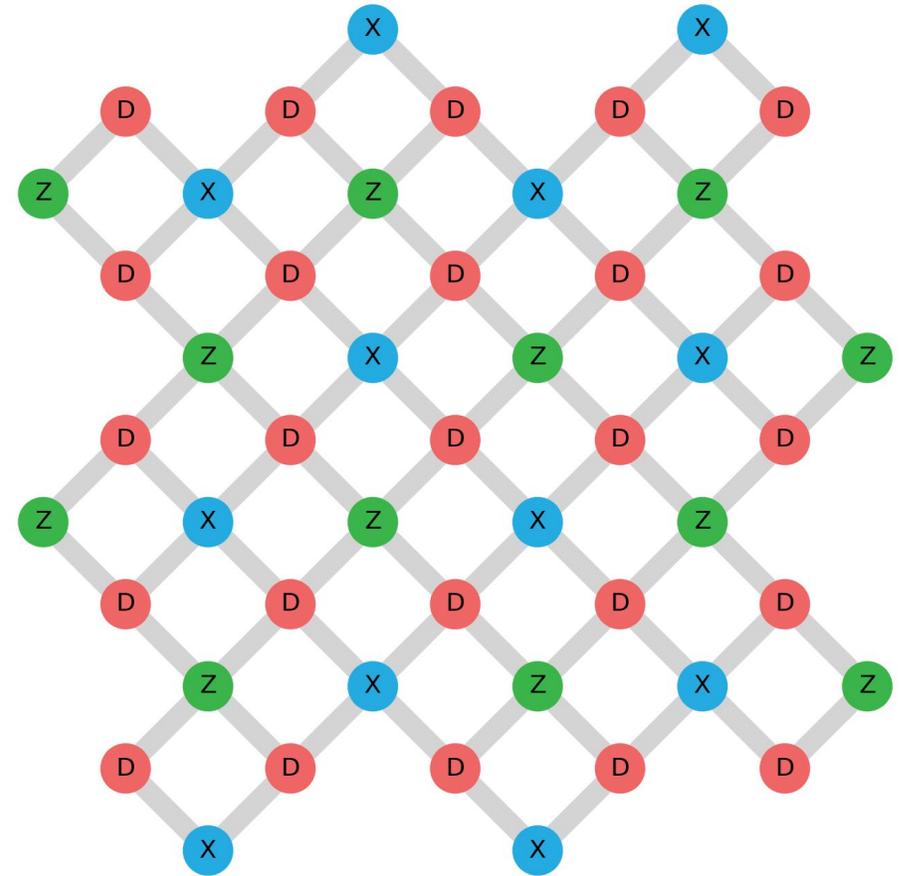
- All operations realizable on a planar qubit lattice
- Topological code: only local operations needed for error correction process

Kitaev, *Annals of Physics* **303**, 2 (2003),

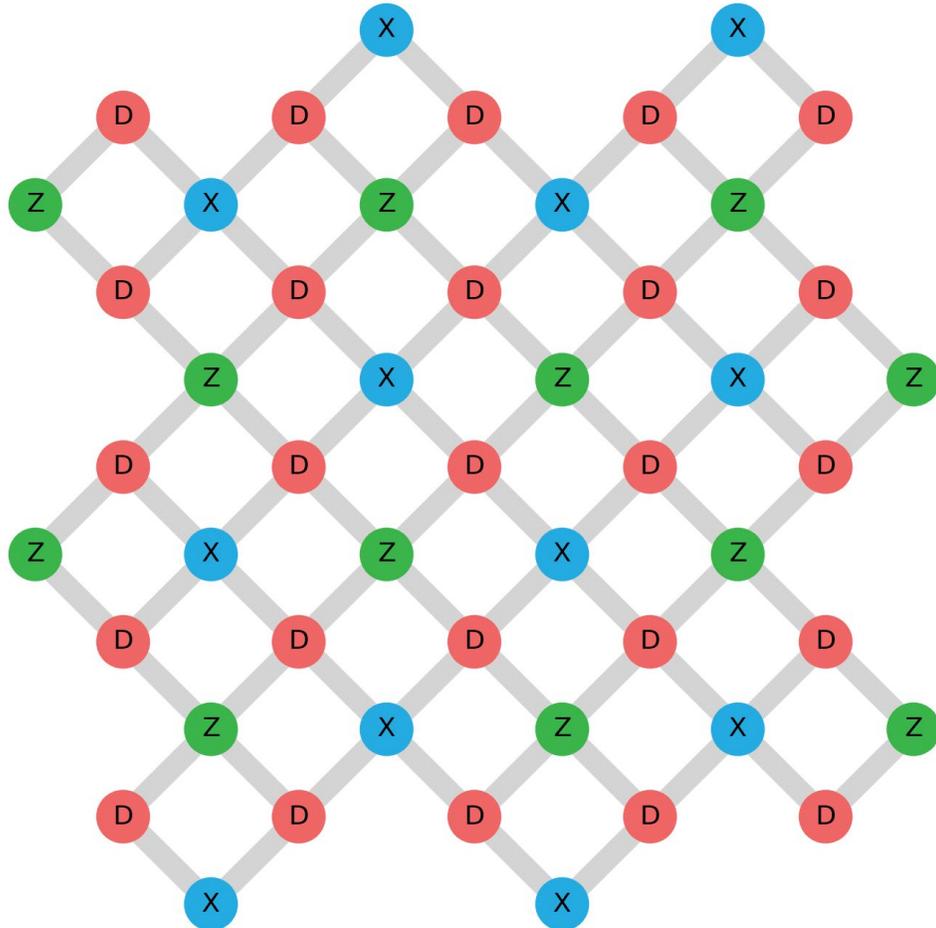
Dennis et al., *Journ. of Math. Physics* **43**, 4452 (2002)

Raussendorff, Harrington, *Phys. Rev. Lett.* **98**, 190504 (2007)

Fowler et al., *Phys. Rev. A* **86**, 032324 (2012)



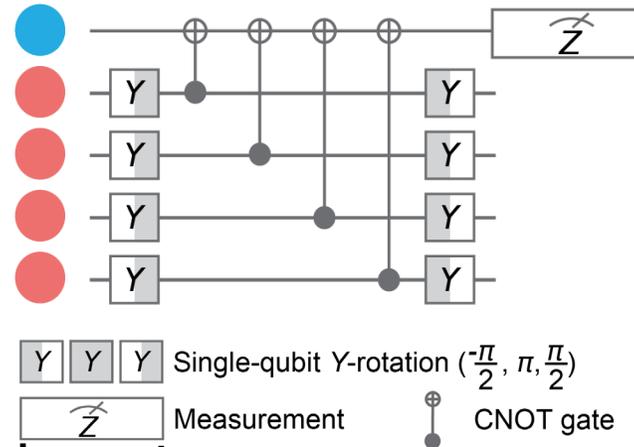
Elements of the Surface Code



Fowler *et al.*, *Phys. Rev. A* **86**, 032324 (2012)
 Versluis *et al.*, *Phys. Rev. Applied* **8**, 034021 (2017)

Features:

- Two-dimensional ($d \times d$) grid of **data qubits**
- **X-type** and **Z-type** auxiliary qubits
- Auxiliary-qubit-assisted stabilizer measurement
 - $Z_1 Z_2 Z_3 Z_4$ (or $Z_1 Z_2$ at the edges)
 - $X_1 X_2 X_3 X_4$ (or $X_1 X_2$ at the edges)



Requirements:

- High-fidelity entangling gates between data and ancilla qubits
- Fast high-fidelity measurements of the ancilla qubits
- Low readout crosstalk between ancilla and data qubits
- Ability to do repeated gates and mid-cycle measurements

Distance-Two Surface Code for Error Detection

- Distance-two code: detect 1 error, correct 0 errors
- Stabilizers for parity measurement:

$$\underbrace{\hat{X}_1 \hat{X}_2 \hat{X}_4 \hat{X}_5, \quad \hat{Z}_1 \hat{Z}_4, \quad \hat{Z}_2 \hat{Z}_5}_{\text{Stabilizers commute, common eigenstates}}$$

Stabilizers commute, common eigenstates

- Logical eigenstates and their equal superpositions:

$$|0\rangle_L = \frac{1}{\sqrt{2}} (|0000\rangle + |1111\rangle)$$

$$|1\rangle_L = \frac{1}{\sqrt{2}} (|0101\rangle + |1010\rangle)$$

$$|+\rangle_L = \frac{1}{2} (|0000\rangle + |1111\rangle + |0101\rangle + |1010\rangle)$$

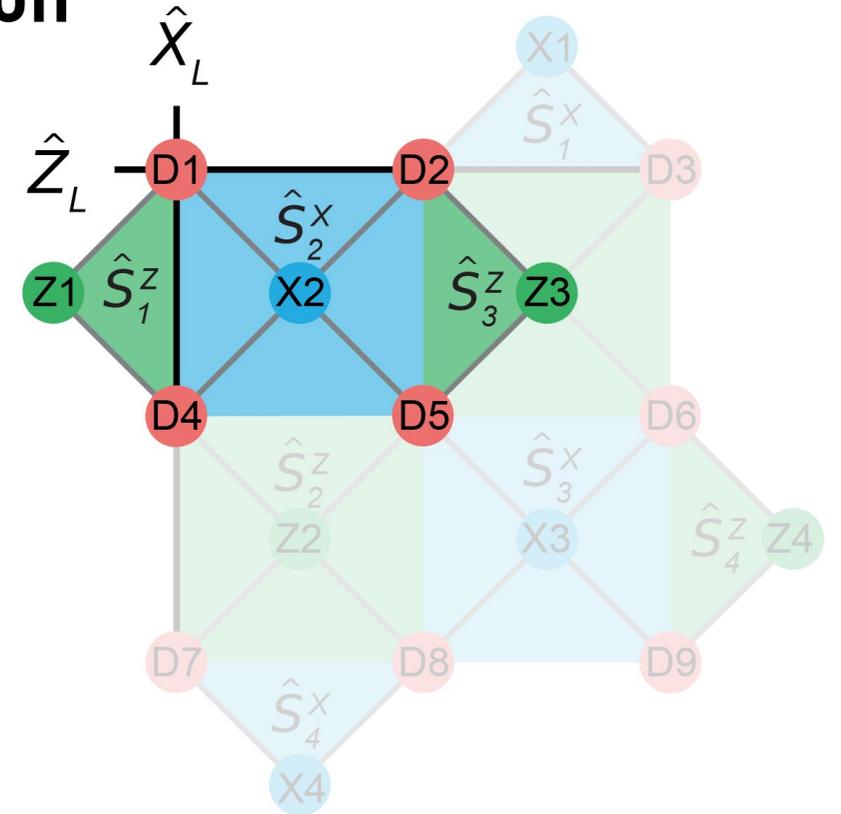
$$|-\rangle_L = \frac{1}{2} (|0000\rangle + |1111\rangle - |0101\rangle - |1010\rangle)$$

- Logical operators:

- $\hat{X}_L = \hat{X}_1 \hat{X}_4$ or $\hat{X}_L = \hat{X}_2 \hat{X}_5$

- $\hat{Z}_L = \hat{Z}_1 \hat{Z}_2$ or $\hat{Z}_L = \hat{Z}_4 \hat{Z}_5$

Anti-commute with each other
and commute with stabilizers
(as needed for logical operators
in a stabilizer code)



Andersen *et al.*, *Nat. Phys.* **16**, 875 (2020)

Chen *et al.*, *Nature* **595**, 7867 (2021)

Marques *et al.*, *Nat. Phys.* **18**, 80 (2022)

Distance-Three Surface Code for Error Correction

Two-dimensional square lattice of qubits

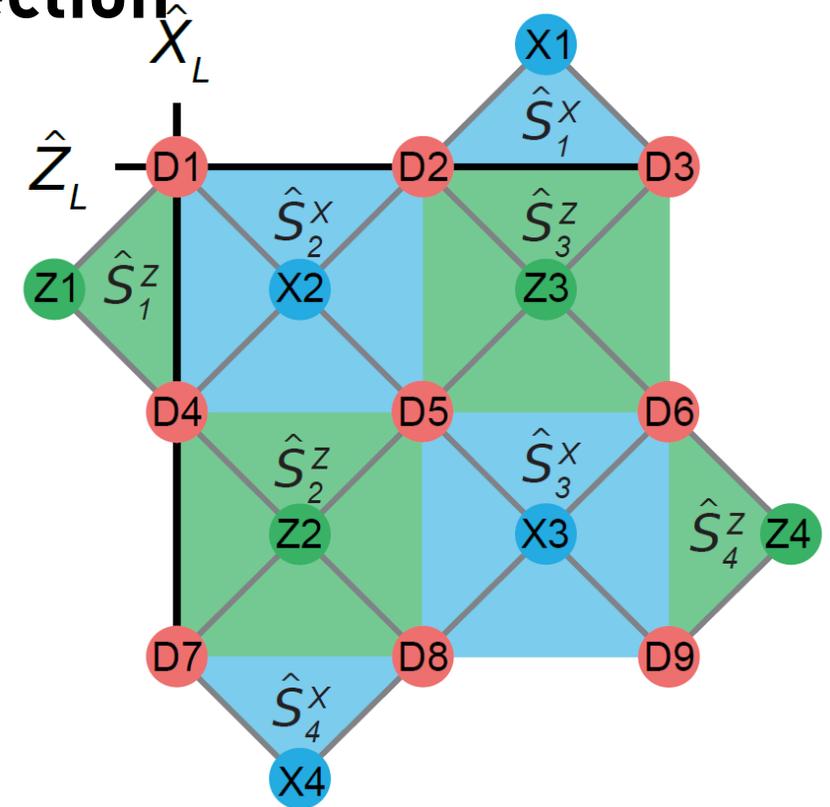
- $d^2 = 9$ Data qubits: encode single (logical) qubit
 - Logical operators: $\hat{Z}_L = \hat{Z}_1 \hat{Z}_2 \hat{Z}_3$ $\hat{X}_L = \hat{X}_1 \hat{X}_4 \hat{X}_7$
 - Distance d : min. number of Pauli operators in \hat{Z}_L, \hat{X}_L
 - Number of correctable errors: $\lfloor (d - 1)/2 \rfloor = 1$
- $d^2 - 1 = 8$ Auxiliary qubits: for parity measurements

Parity/Stabilizer measurements

- Detect errors without collapsing data-qubit state (Stabilizer operators commute with \hat{Z}_L, \hat{X}_L)
- 4 Z-type Stabilizers \hat{S}^{Zi} to detect bit-flip errors
- 4 X-type Stabilizers \hat{S}^{Xi} to detect phase-flip errors

Bombin, Delgado, *Phys. Rev. A* **76**, 012305 (2007)

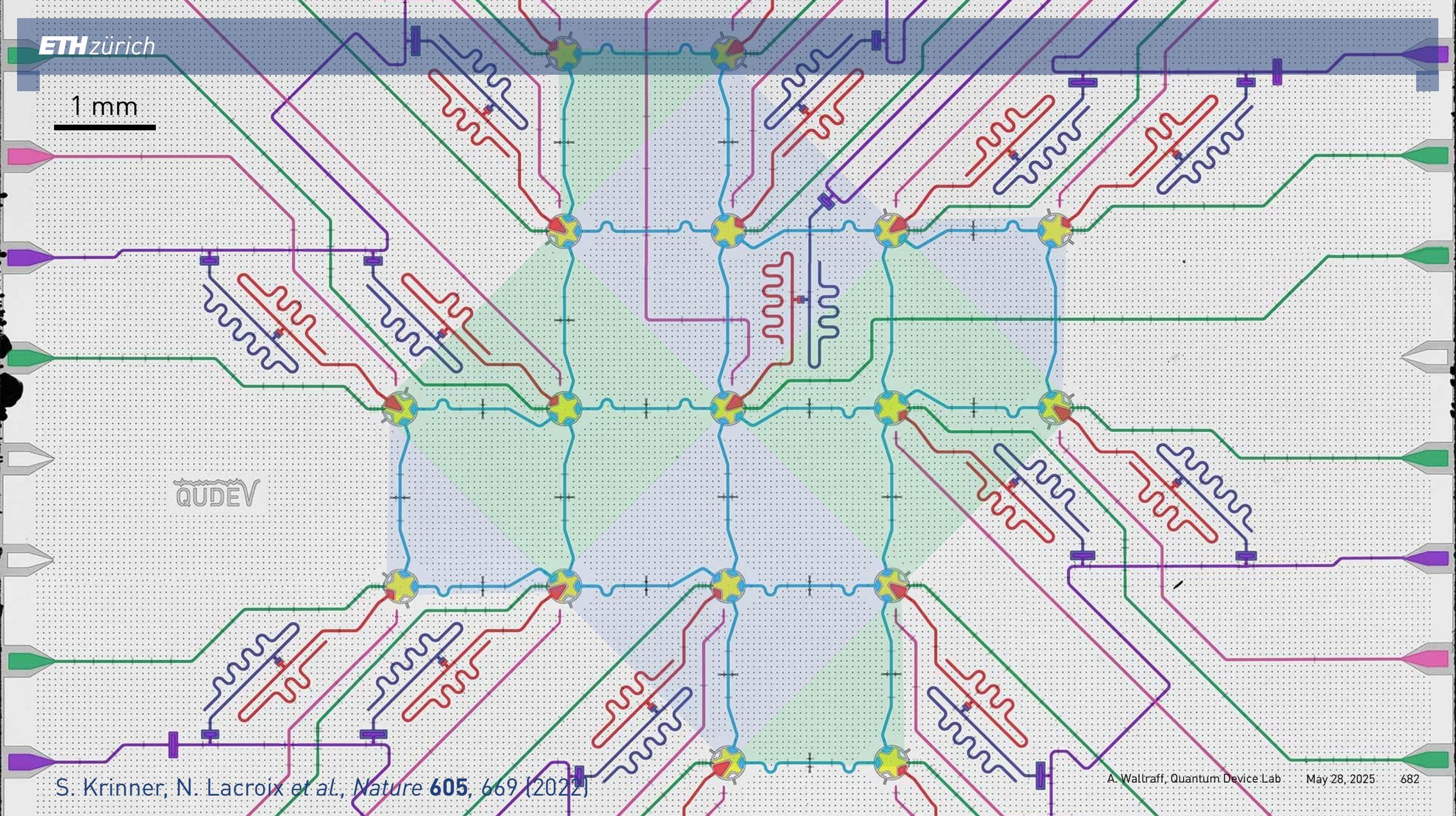
Tomita, Svore, *Phys. Rev. A* **90**, 062320 (2014)



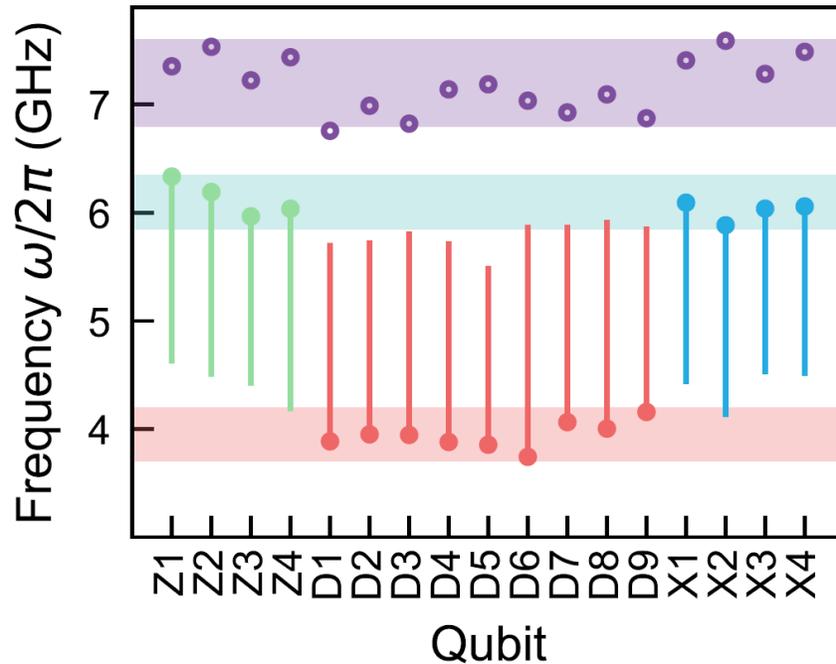
\hat{S}^{Z1}	$\hat{Z}_1 \hat{Z}_4$	\hat{S}^{X1}	$\hat{X}_2 \hat{X}_3$
\hat{S}^{Z2}	$\hat{Z}_4 \hat{Z}_5 \hat{Z}_7 \hat{Z}_8$	\hat{S}^{X2}	$\hat{X}_1 \hat{X}_2 \hat{X}_4 \hat{X}_5$
\hat{S}^{Z3}	$\hat{Z}_2 \hat{Z}_3 \hat{Z}_5 \hat{Z}_6$	\hat{S}^{X3}	$\hat{X}_5 \hat{X}_6 \hat{X}_8 \hat{X}_9$
\hat{S}^{Z4}	$\hat{Z}_6 \hat{Z}_9$	\hat{S}^{X4}	$\hat{X}_7 \hat{X}_8$

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Device Architecture



Frequency tunable qubits in two bands

- **Data qubits** at ~ 4 GHz
- **Auxiliary qubits** at ~ 6 GHz

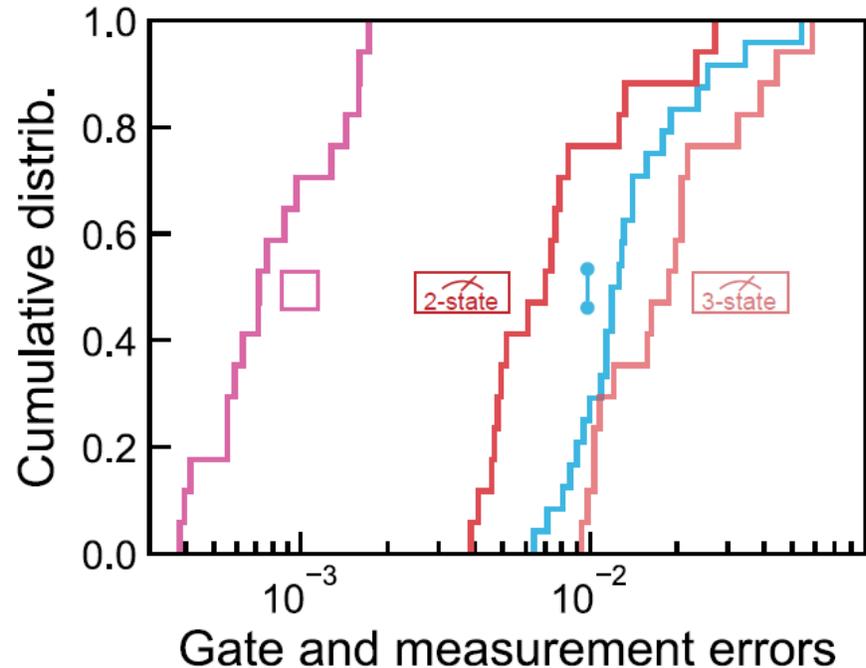
Features

- Small residual-ZZ couplings (≤ 8 kHz)
- Improved coherence using asymmetric SQUIDs creating upper and lower-frequency sweet spots
- Two-qubit CZ gates initiated by tuning both qubits
- Tuning range indicated by vertical bars
- Only auxiliary qubits evolve through $|2\rangle$ during a two-qubit gate

Readout resonators

- Single frequency band ~ 7 GHz

Device Performance



Averaged qubit coherence

- Energy relaxation time $T_1 \sim 33 \mu\text{s}$
- Ramsey decay time $T_2^* \sim 38 \mu\text{s}$

Single-qubit gates

- Mean gate error of $0.9(4) \cdot 10^{-3}$
- Duration of 40 ns

Two-qubit gates

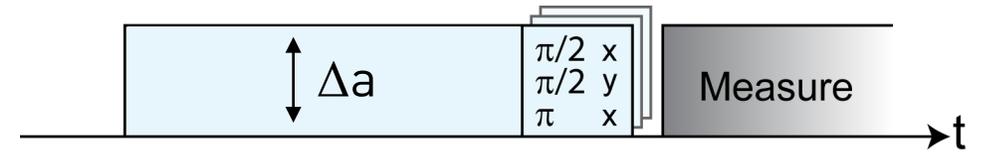
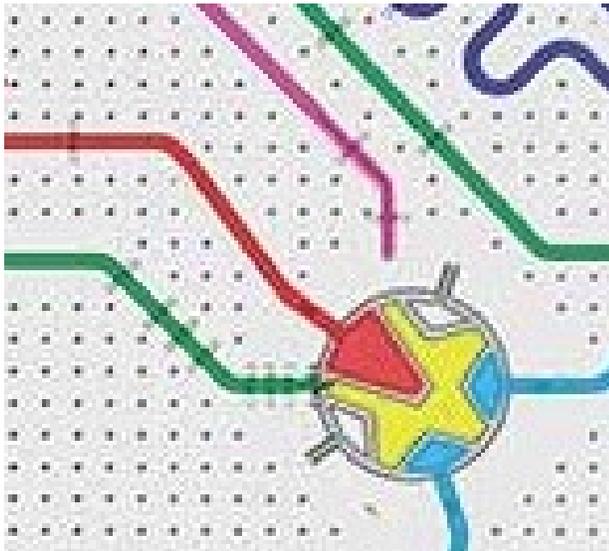
- Mean gate error of $15(10) \cdot 10^{-3}$
- Mean duration of 98(7) ns (including buffers)

Readout:

- Mean **two-state** assignment error: $9(7) \cdot 10^{-3}$
and **three-state** assignment error: $22(14) \cdot 10^{-3}$
- Duration: 300 ns (aux.) to 400 ns (data)

Controlling Single Qubits (Y Rotation)

- apply microwave pulse
- followed by read-out pulse
- both with controlled length, amplitude and phase
- Characterize gates by randomized benchmarking
- $F > 99\%$

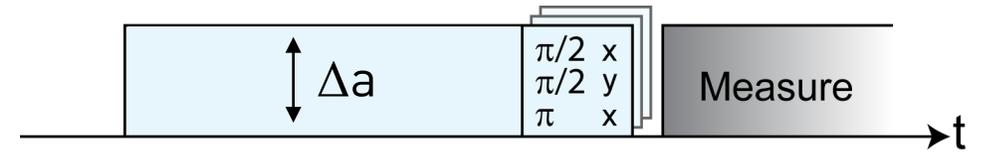


experimental density matrix and Pauli set:



Controlling Single Qubits (X Rotation)

- apply microwave pulse
- followed by read-out pulse
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- Characterize gates by randomized benchmarking
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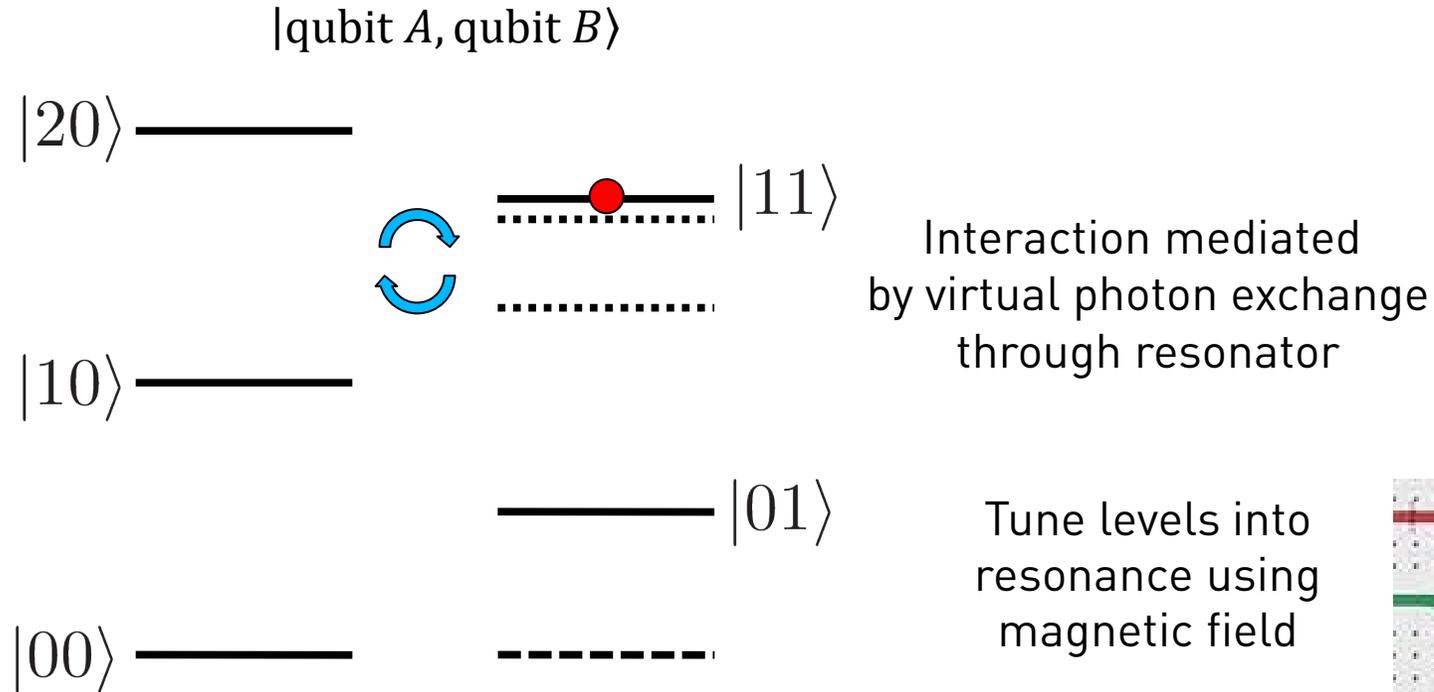


experimental density matrix and Pauli set:



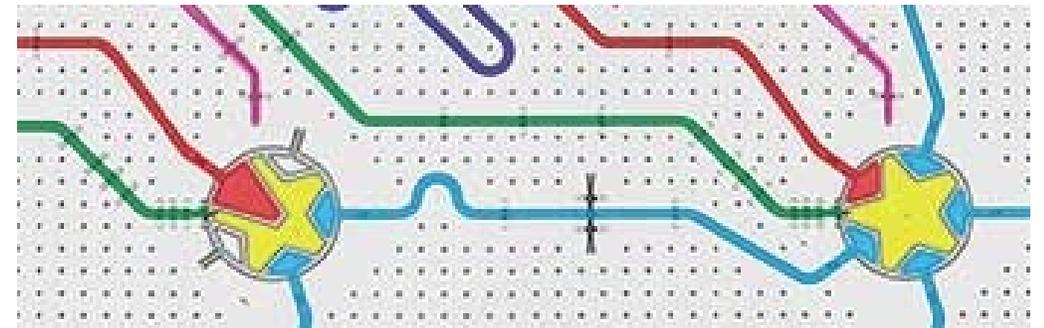
Universal Two-Qubit Controlled Phase Gate

Make use of qubit states beyond 0, 1



$$|11\rangle \longrightarrow i|20\rangle \longrightarrow -|11\rangle$$

Full 2π rotation induces phase factor -1

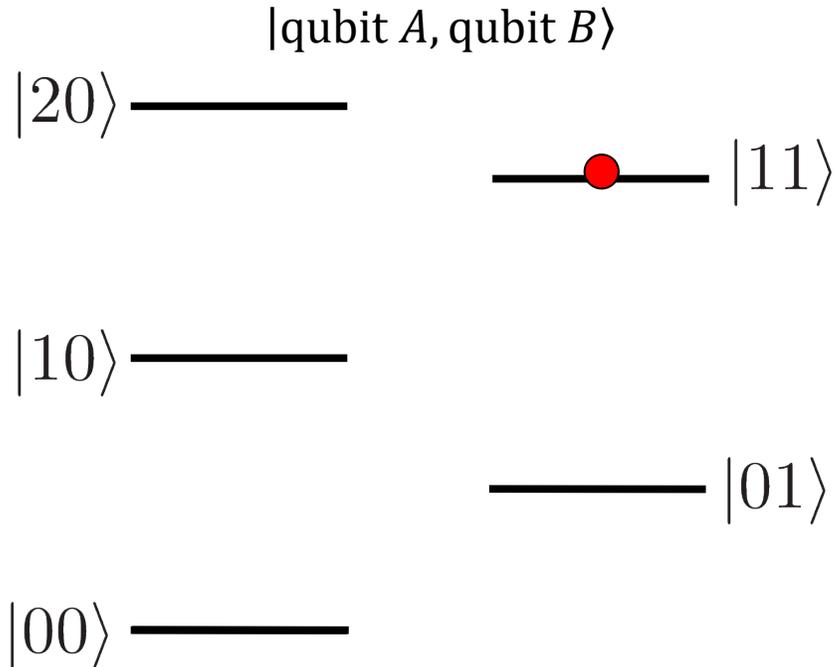


proposal: F. W. Strauch *et al.*, *Phys. Rev. Lett.* **91**, 167005 (2003).

first implementation: L. DiCarlo *et al.*, *Nature* **460**, 240 (2010).

Universal Two-Qubit Controlled Phase Gate

Make use of qubit states beyond 0, 1



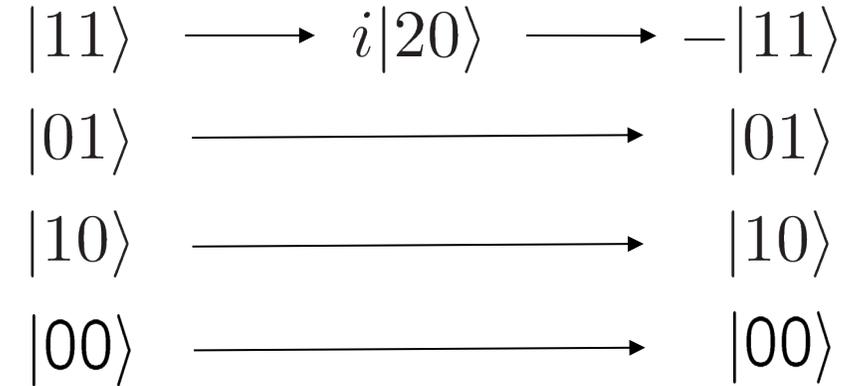
Qubits in states 01, 10 and 00 do not interact and thus acquire no phase shift

Universal two-qubit gate.

Test performance with process tomography or randomized benchmarking.

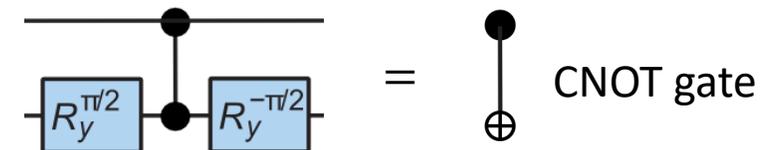
proposal: F. W. Strauch *et al.*, *Phys. Rev. Lett.* **91**, 167005 (2003).

first implementation: L. DiCarlo *et al.*, *Nature* **460**, 240 (2010).



C-Phase gate:

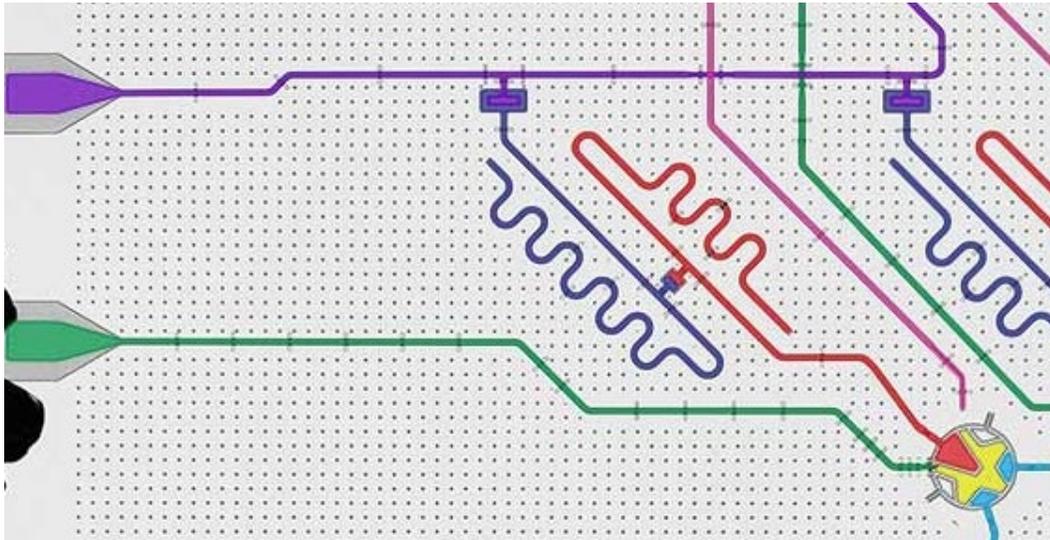
$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$



Qubit Readout

Circuit design

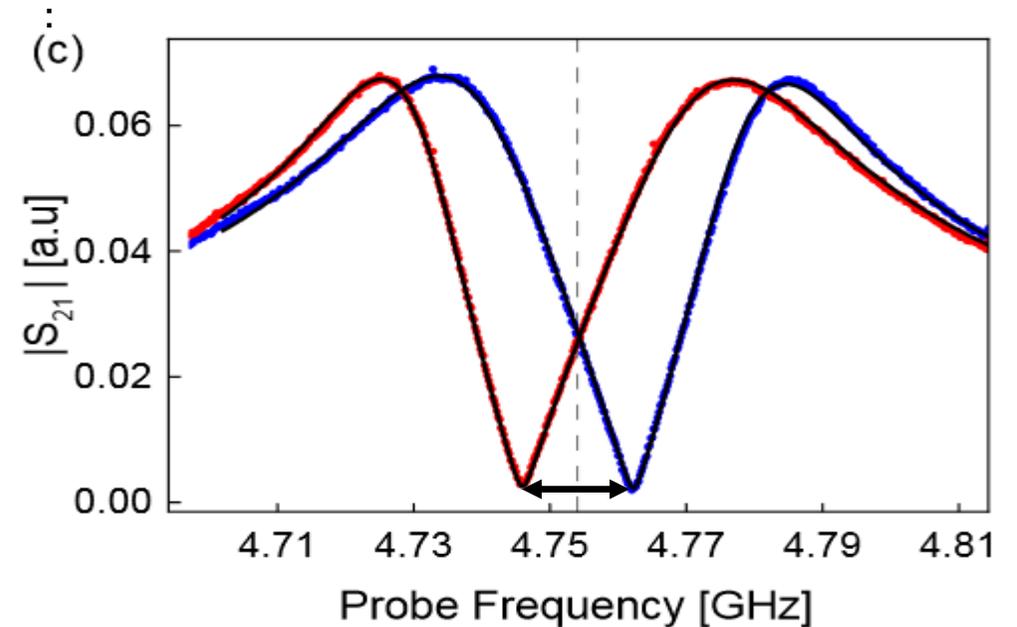
- $\lambda/4$ readout resonator & $\lambda/4$ Purcell filter



Performance

- $F \sim 99.2\%$ at 88 ns integration time
- Optimized sample design
- Low-noise phase-sensitive JP-Amplifier

Transmission amplitude of readout circuit for qubit prepared in **ground (g)** or **excited (e)** state

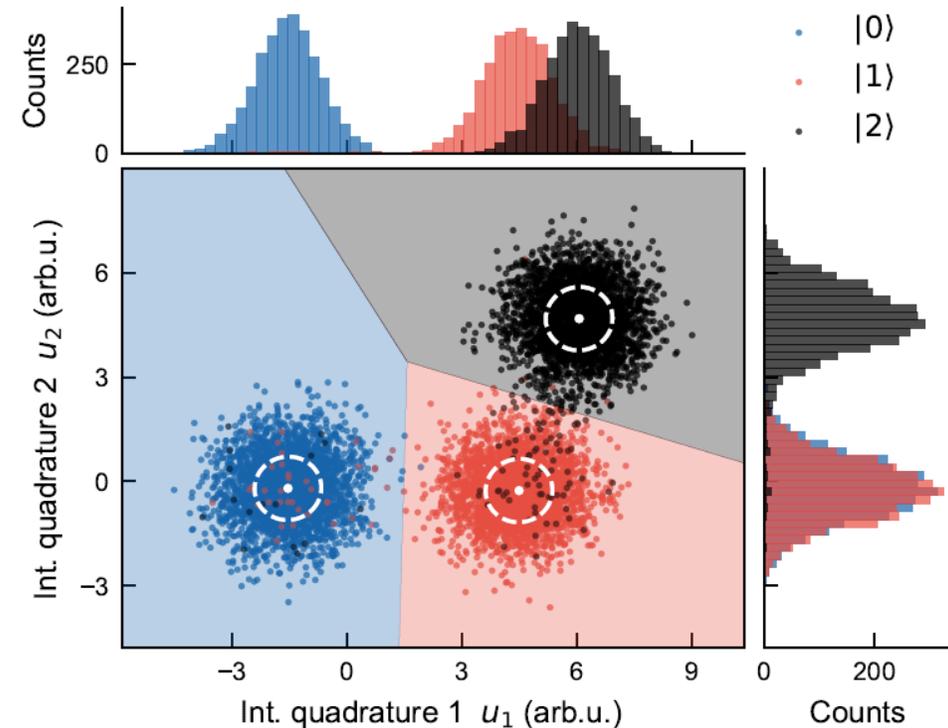


Features:

- large dispersive shift χ
- large resonator BW κ
- Purcell protection
- Low cross-talk when multiplexed

Leakage Detection and Rejection

- Leakage errors are detrimental for quantum error correction
- Device designed to minimize leakage on data qubits: $< 2 \cdot 10^{-3}$ per qubit and per cycle
- Detect residual leakage using three-state readout
 - Auxiliary qubits: in each cycle
 - Data qubits: after final cycle
- Rejected fraction per qubit per cycle
 - Auxiliary qubits: $9.4(4) \cdot 10^{-3}$
 - Data qubits: $1.7(2) \cdot 10^{-3}$
- Some contribution from false positives



S. Krinner, N. Lacroix *et al.*, *Nature* **605**, 669 (2022)

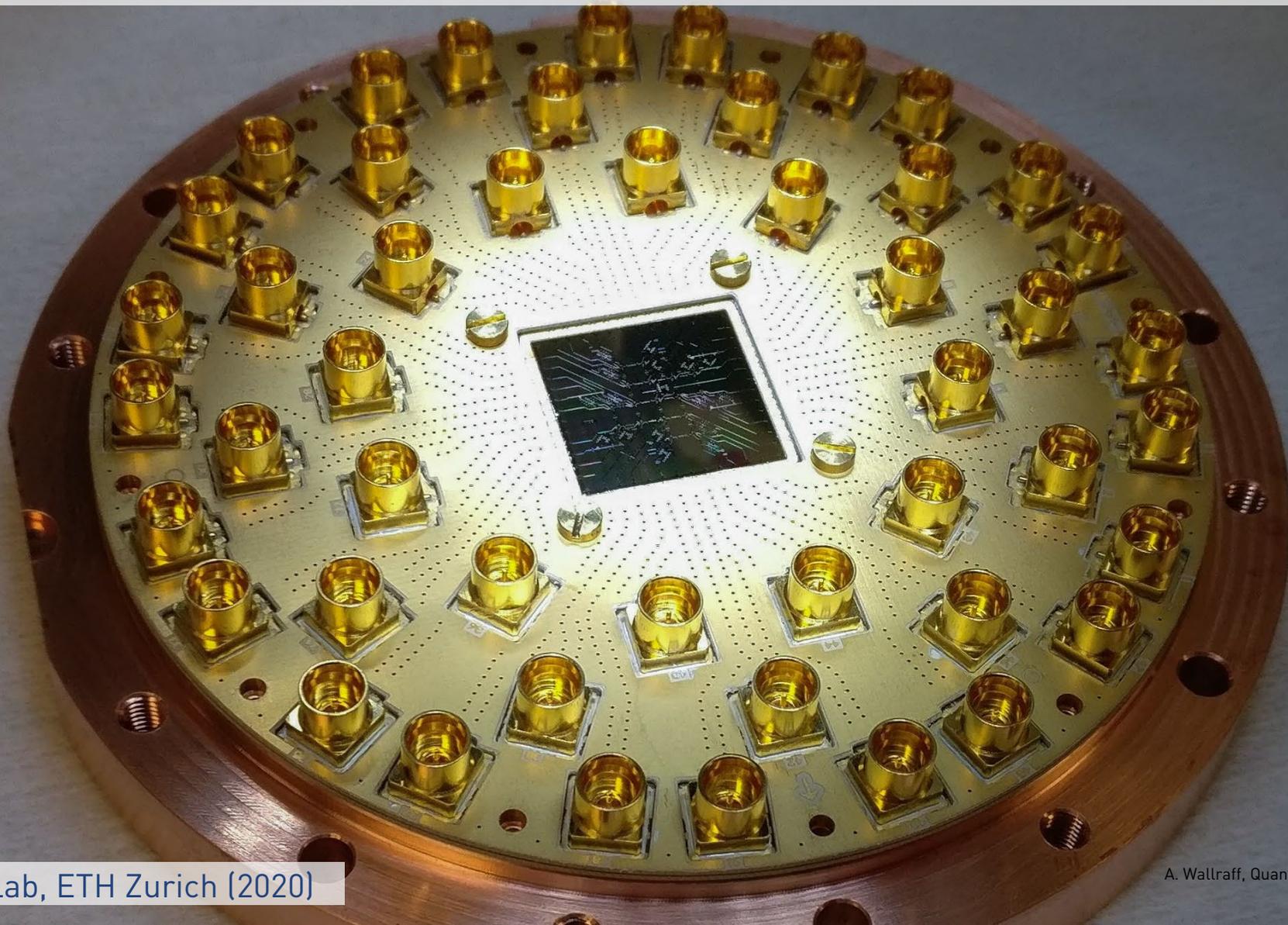
Alferis, Terhal, *Quant. Info. Comp.* **7**, 139 (2007)

Fowler, *PRA* **88**, 042308 (2013)

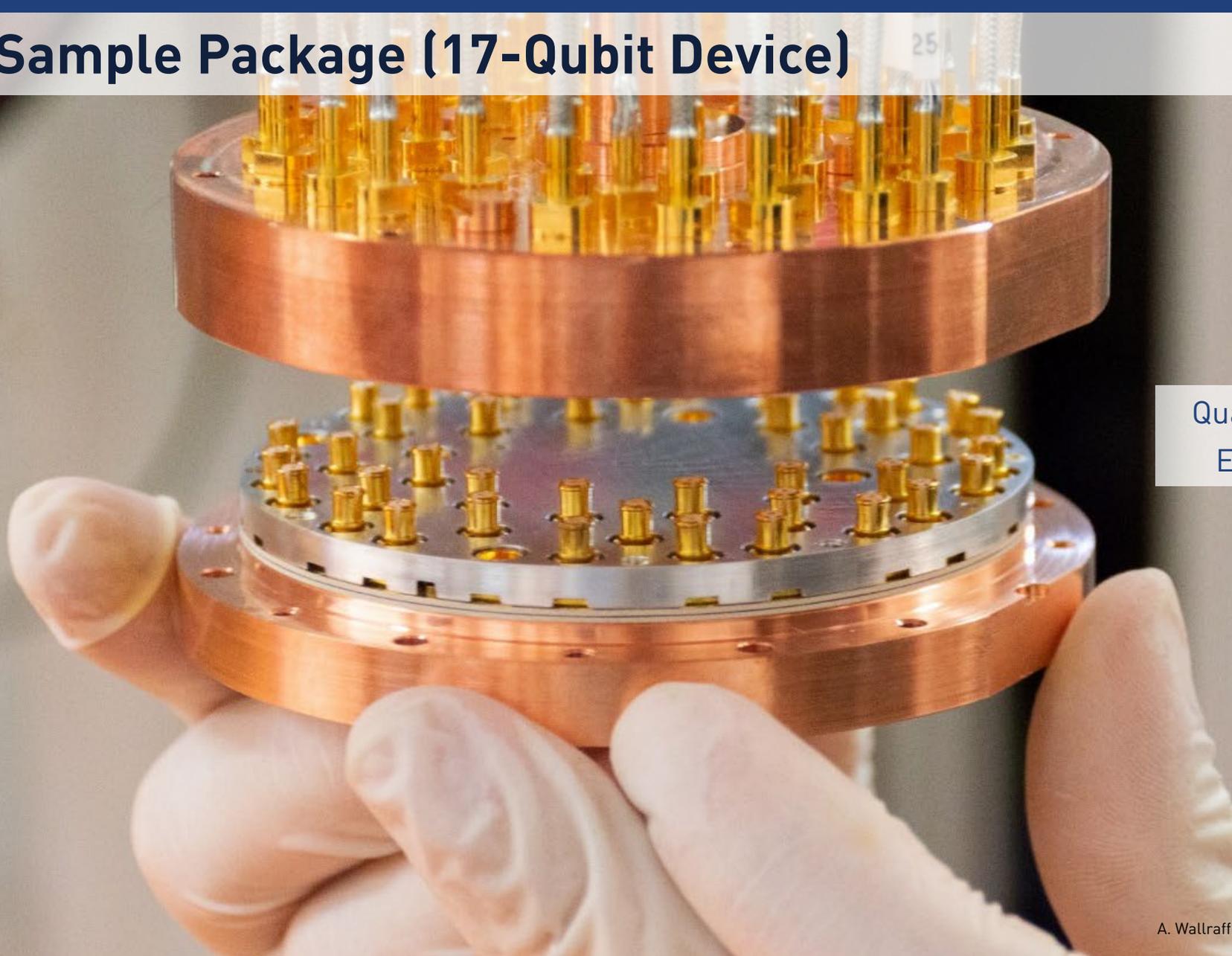
Bultink *et al.*, *Science Advances* **6**, eaay3050 (2020)

Varbanov *et al.*, *npj Quantum Information* **15**, 997 (2020)

Distance-Three Surface-Code Device Mounted in Sample Holder



48-Port Sample Package (17-Qubit Device)



Quantum Device Lab,
ETH Zurich (2020)



Quantum Device Lab, ETH Zurich (2021)



Room-Temperature Electronics

- Close collaboration with Zurich Instruments

Qubit control (7x HDAWG)

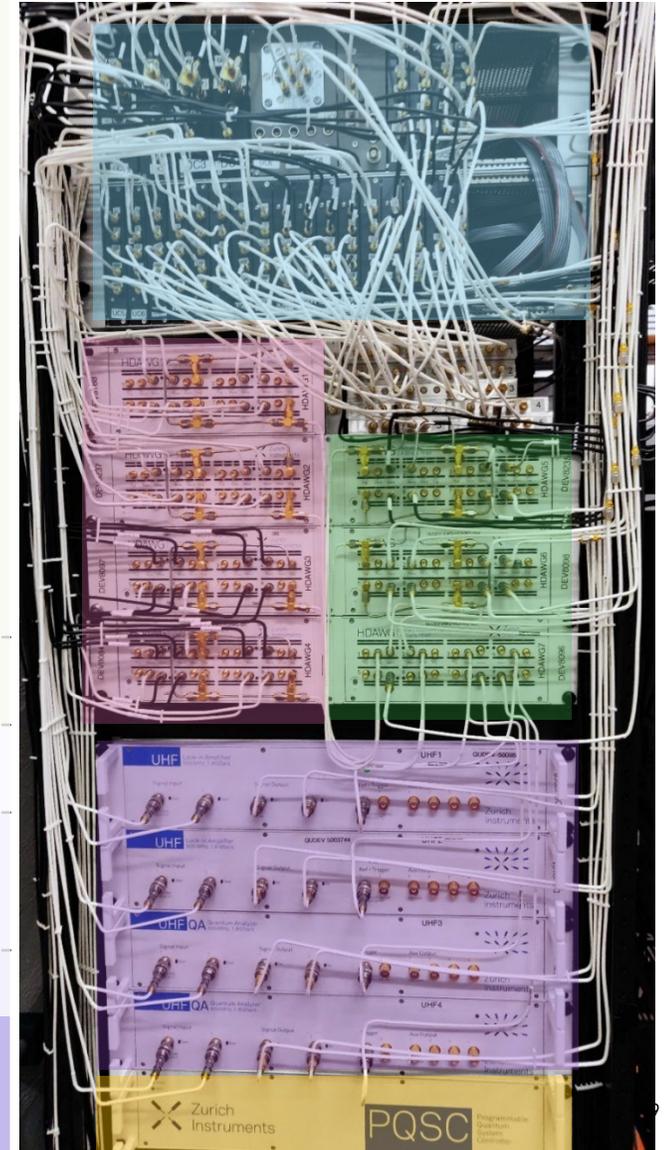
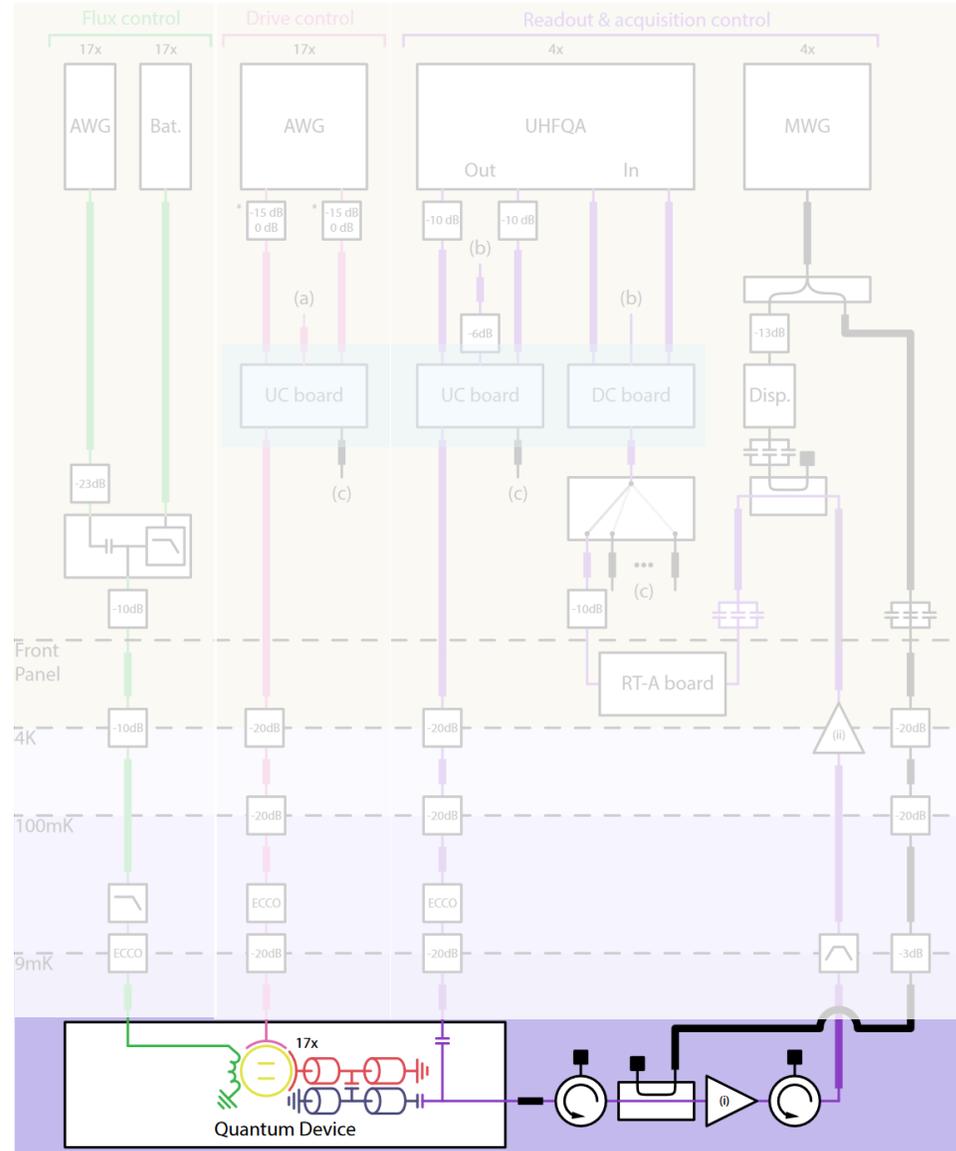
- Flux drives (17x)
- Baseband RF drives (17x)

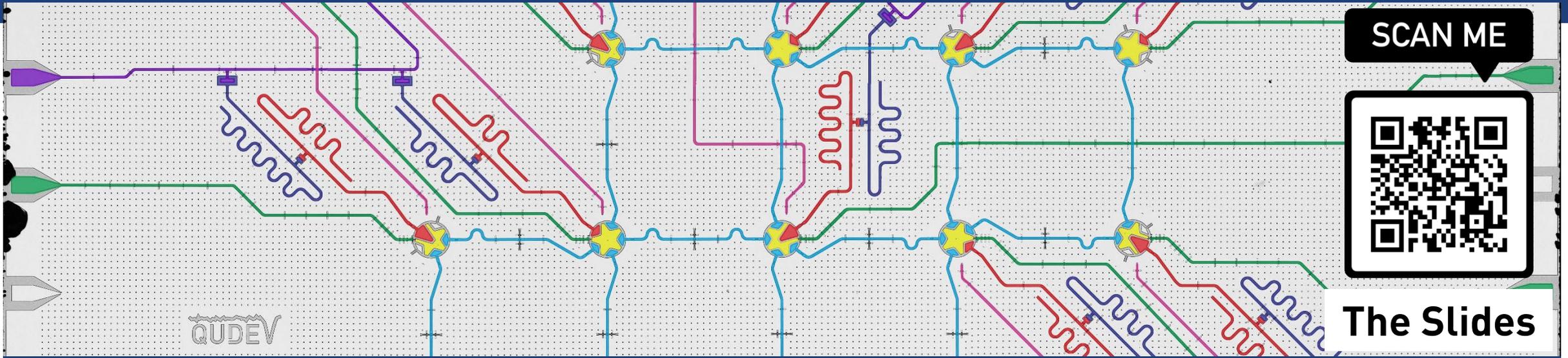
Qubit Readout (4x UHFQA)

- FPGA Baseband signal generation & analysis

Up- and down-conversion electronics for qubit drive and readout

Synchronization using PQSC





SCAN ME



The Slides

Quantum Error Correction with Superconducting Circuits (Lecture 2)

Sci. Team: E. Al-Tavil, L. Beltran, I. Besedin, J.-C. Besse, D. Colao Zanuz, Xi Dai, K. Dalton, J. Ekert, S. Frasca, A. Grigorev, D. Hagmann, C. Hellings, A. Hernandez-Anton, I. Hesner, L. Hofele, M. Kerschbaum, S. Krinner, A. Kulikov, N. Lacroix, M. Pechal, K. Reuer, A. Rosario, C. Scarato, J. Schaer, Y. Song, F. Swiadek, F. Wagner, A. Wallraff *(ETH Zurich)*

Eng. & Tech. Team: A. Akin, M. Bahrani, A. Flasby, A. Fauquex, R. Keller, N. Kohli, R. Siegbert, M. Werner *(ETH Zurich)*



Innovation project
supported by



Schweizerische Eidgenossenschaft
Confédération suisse
Confederazione Svizzera
Confederaziun svizra

Swiss Confederation

Innosuisse – Swiss Innovation Agency

Qubit-Encoded Quantum Error Correction Experiments

Bit or phase-flip codes (only X or Z errors):

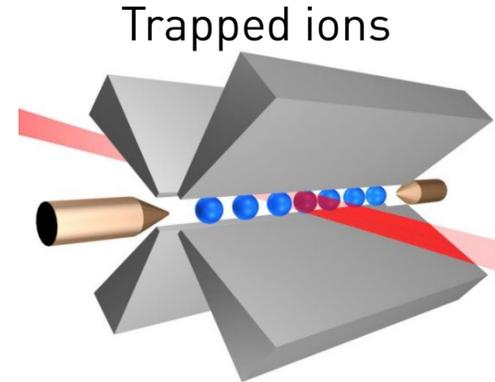
- NMR [Cory et al. Phys. Rev. Lett. 81, 2152 (1998)]
- Ions [Chiaverini et al. Nature 432, 602 (2004), Schindler et al. Science 322, 1059 (2011)]
- NV-Centers [Cramer et al. Nature Comm. 7, 11526 (2016)]
- Superconducting qubits [Riste et al. Nature Comm. 6, 6983 (2015), Kelly et al. Nature 519, 66 (2015), Chen et al., Nature 595, 7867 (2021)]

Quantum codes, single-cycle experiments:

- Five-qubit code [Knill et al., PRL 86, 5811 (2001), Abobeih et al., arXiv:2108.01646 (2021)]
- Bacon-Shor code [Egan et al., Nature 598, 281 (2021)]

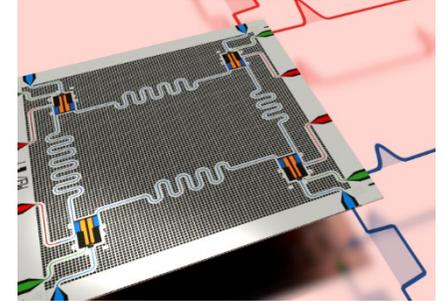
Repeated error detection in the surface code

- Andersen et al., Nat. Phys. 16, 875 (2020)
- Chen et al., Nature 595, 7867 (2021)
- Marques et al., Nat. Phys. 18, 80 (2022)



e.g. Blatt & Roos, Nat. Phys. 8, 277 (2012)

Supercond. circuits



Picture: Y. Salathé
Review: e.g. Krantz et al., Appl. Phys. Rev. 6, 021318 (2019)

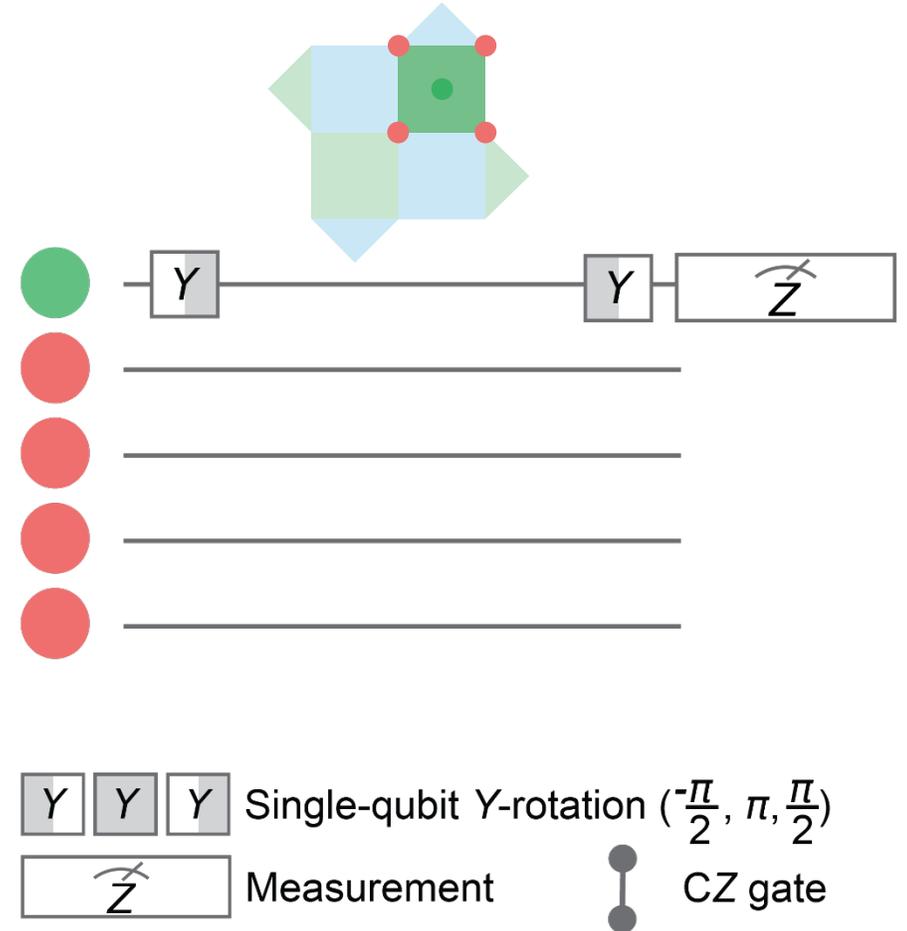
Repeated quantum error correction

- Color code (trapped ions) Ryan-Anderson et al., PRX 11, 041058 (2021)
- Distance-3 surface code (s.c.) Krinner, Lacroix et al., Nature 605, 669 (2022) Zhao et al., PRL 129, 030501 (2022)
- Distance-3 heavy-hexagon code (s.c.) Sundaresan et al., Nat. Commun. 14, 2852 (2023)
- Distance-3 to 5 scaling of the surface code (s.c.) Google AI, Nature 614, 676 (2023)

Stabilizer Measurements

Quantum circuit

- Ramsey measurement on auxiliary qubit A_i

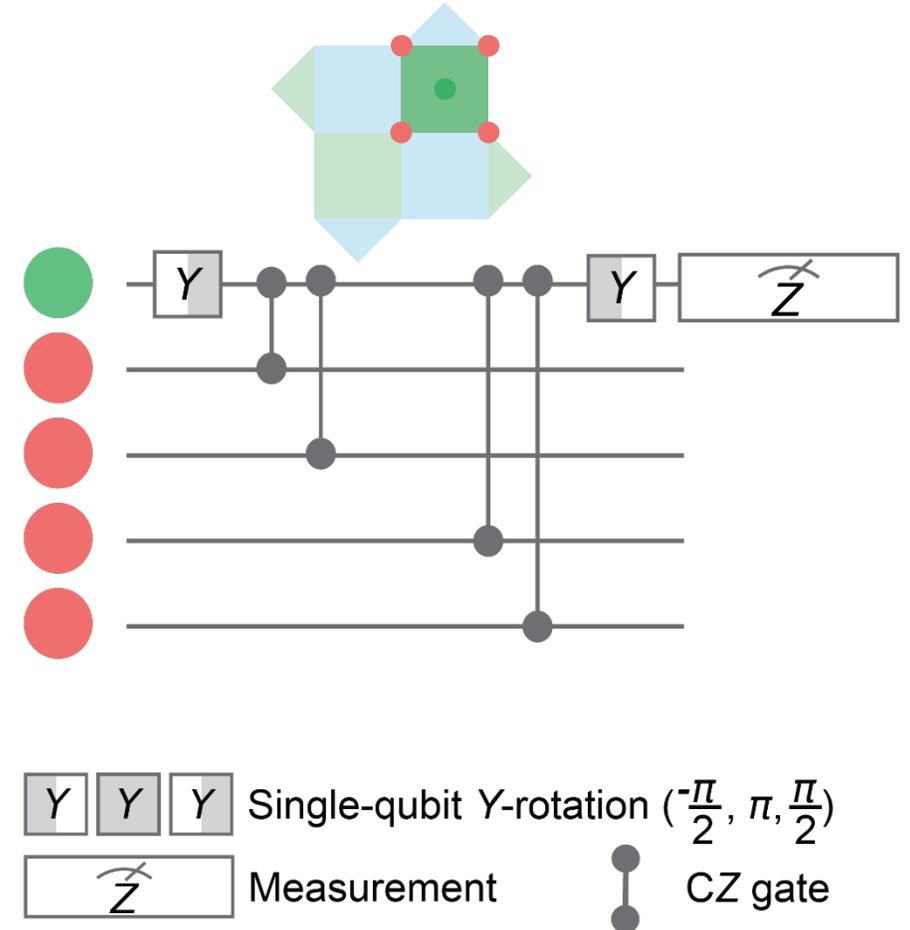


Stabilizer Measurements

Quantum circuit

- Ramsey measurement on auxiliary qubit A_i
- Controlled-phase (CZ) gates between A_i and four data qubits D_j
 - If D_j in $|1\rangle$: phase of A_i changes by π
- Resulting mapping:

Number of D_j in $ 1\rangle$:	Final phase of A_i	Final state of A_i	Stabilizer value s^{A_i}
Even	0	Unchanged	+1
Odd	π	Changed	-1



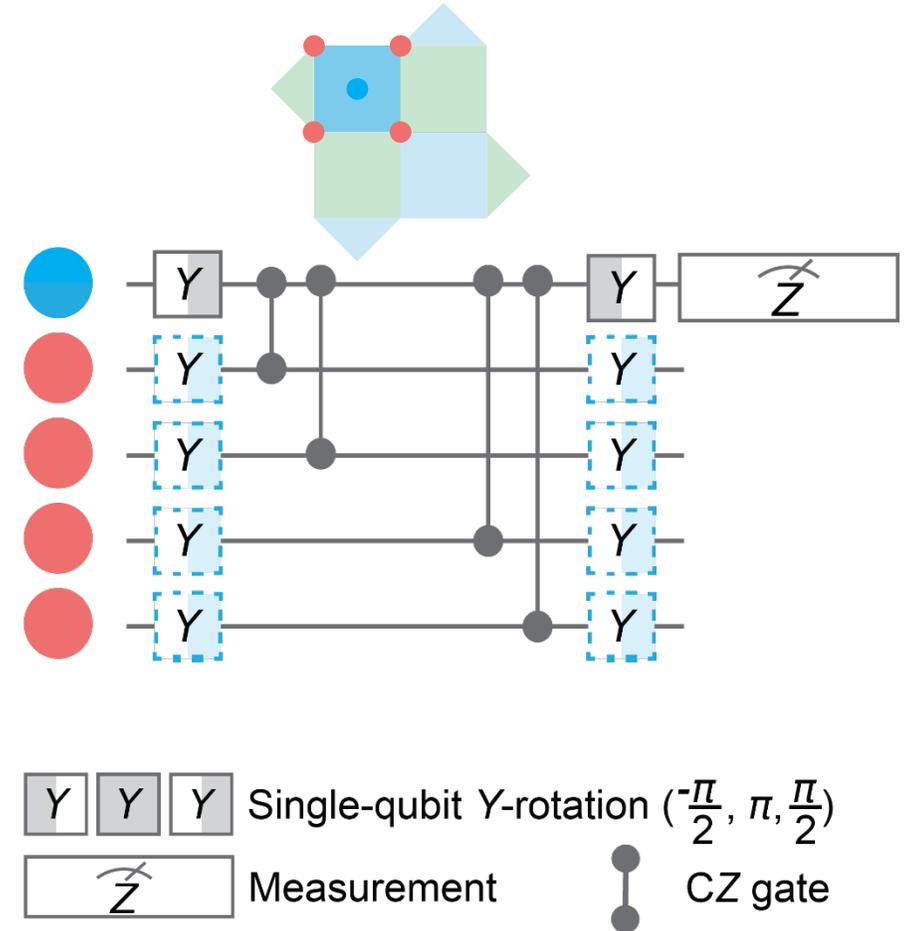
Stabilizer Measurements

Quantum circuit

- Ramsey measurement on auxiliary qubit A_i
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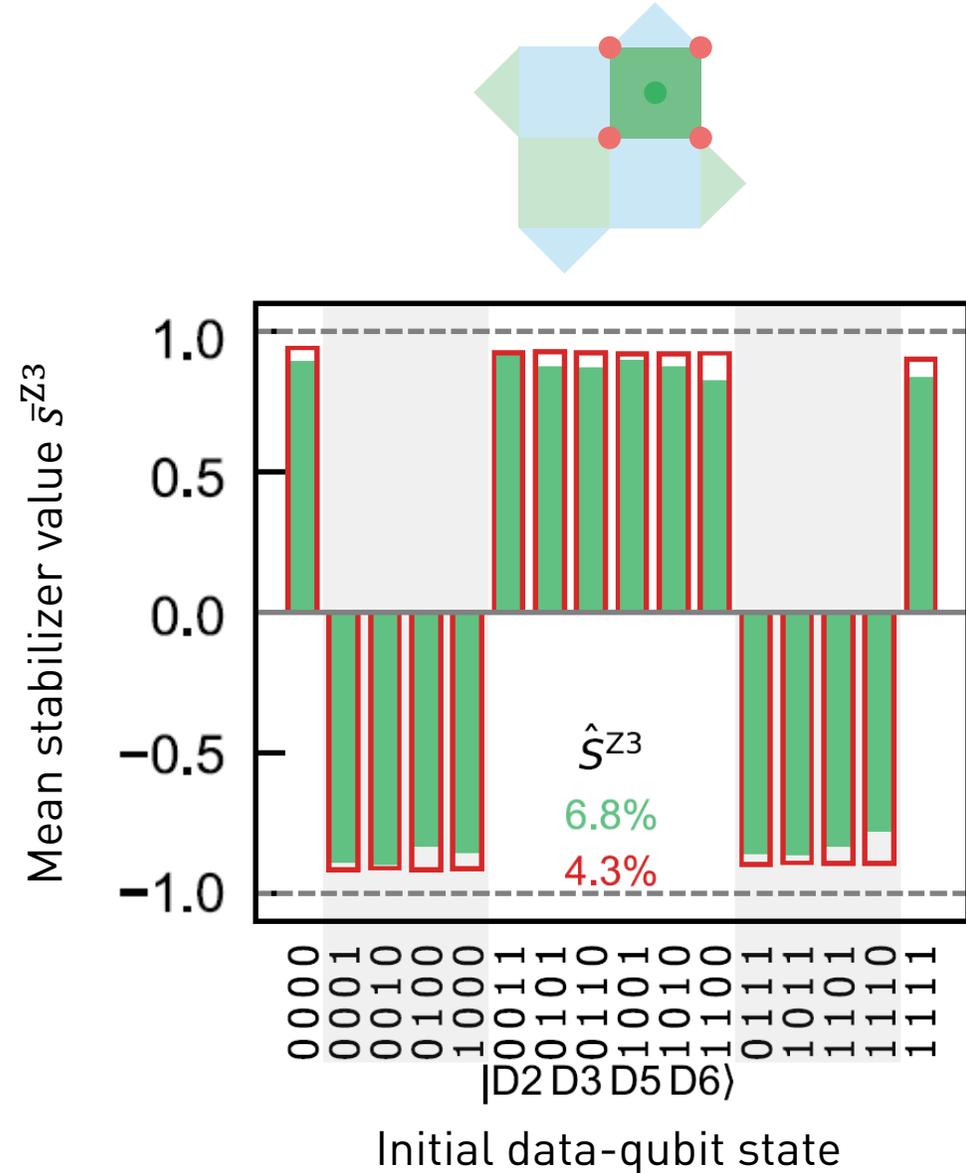
- X-type stabilizer with basis change on data qubits



Stabilizer Characterization

Individual characterization

- Prepare data qubits of plaquette in all 4 (weight-2) or 16 (weight-4) basis states
- Stabilizer execution yields $s^{Ai} = \pm 1$
- Average over $\sim 4 \times 10^4$ measurements to obtain \bar{s}^{Ai}
- Measured and calculated error



Stabilizer Characterization

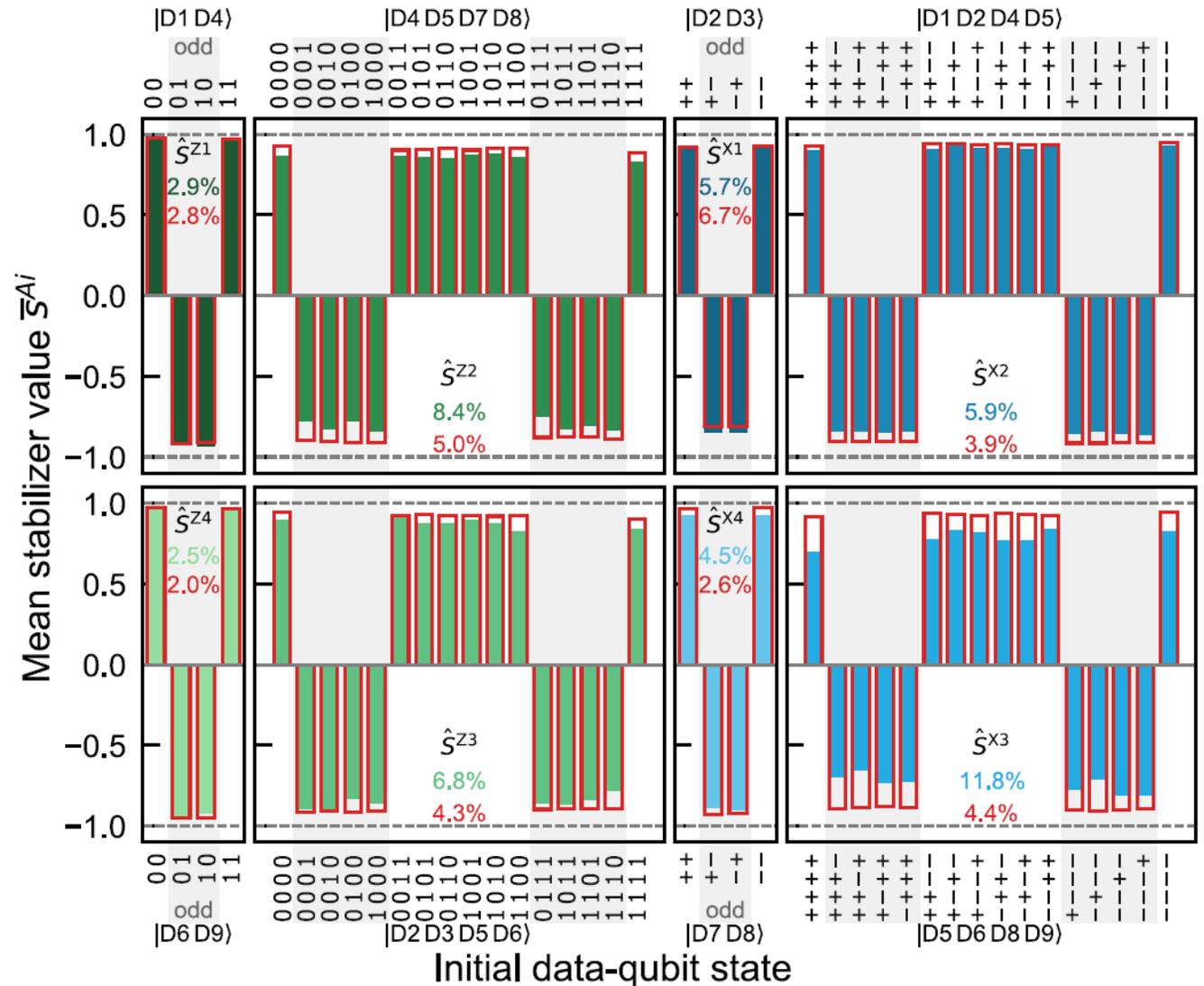
Individual characterization

- Prepare data qubits of plaquette in all 4 (weight-2) or 16 (weight-4) basis states
- Stabilizer execution yields $s^{Ai} = \pm 1$
- Average over $\sim 4 \times 10^4$ measurements to obtain \bar{s}^{Ai}
- Measured and calculated error

Average parity error

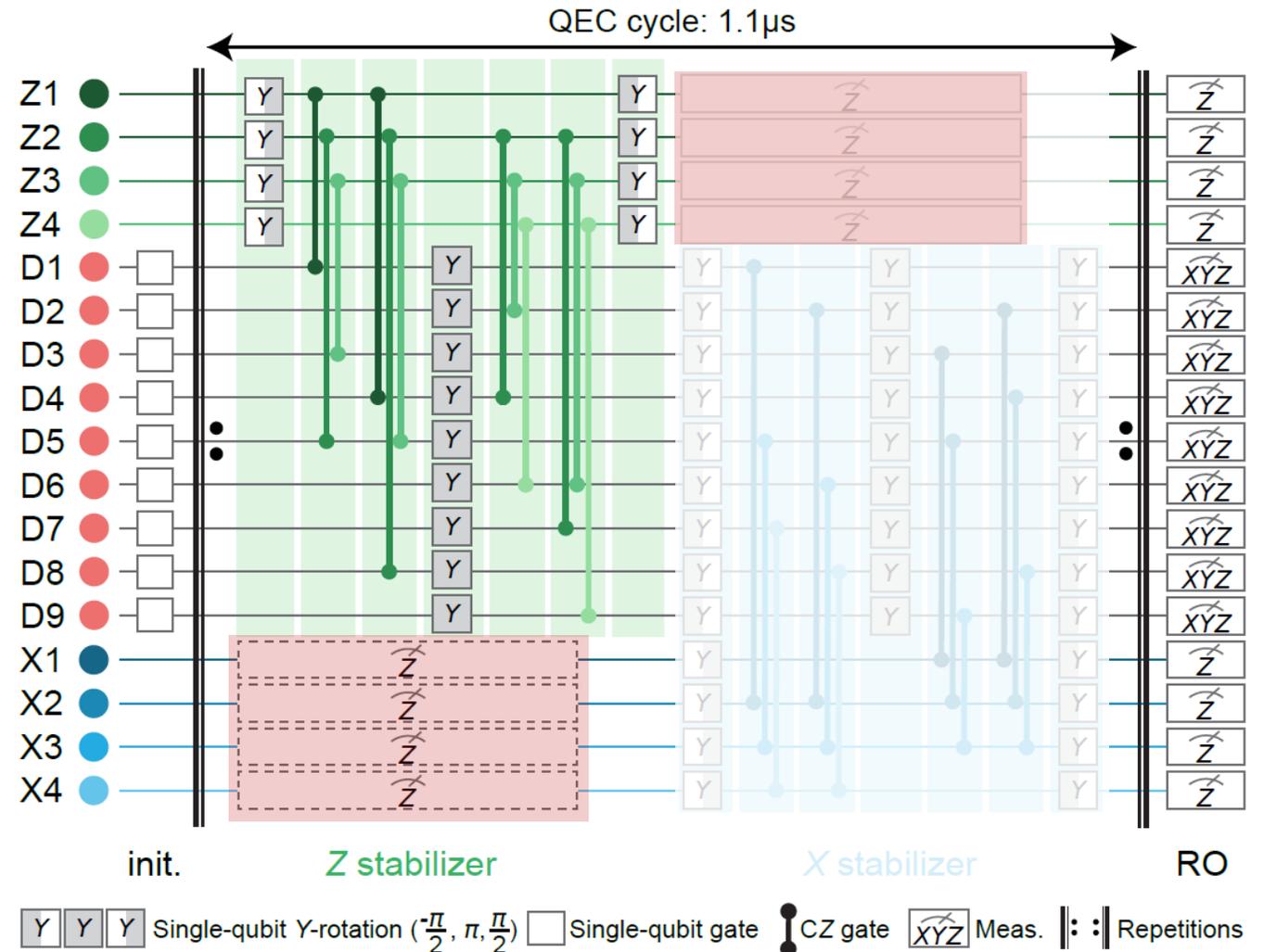
- Weight-2 stabilizers: 3.9(1.3) %
- Weight-4 stabilizers: 8.2(2.2) %

Qualitative agreement with **master-equation simulations**



The Surface Code Cycle

- All four \hat{S}^{Zi} measured in parallel
- All four \hat{S}^{Xi} measured in parallel
- Pipelining: **Read out** one stabilizer type while running gates of the other.
- Logical state preparation: $|0\rangle_L$, $|1\rangle_L$ and $|\pm\rangle_L = (|0\rangle_L \pm |1\rangle_L)/\sqrt{2}$ in single cycle.
- State preservation over n cycles
 - Cycle duration: 1.1 μ s
 - Leakage detection and rejection executed in every cycle
 - circuits with ~ 800 single-qubit gates and ~ 400 two-qubit gates

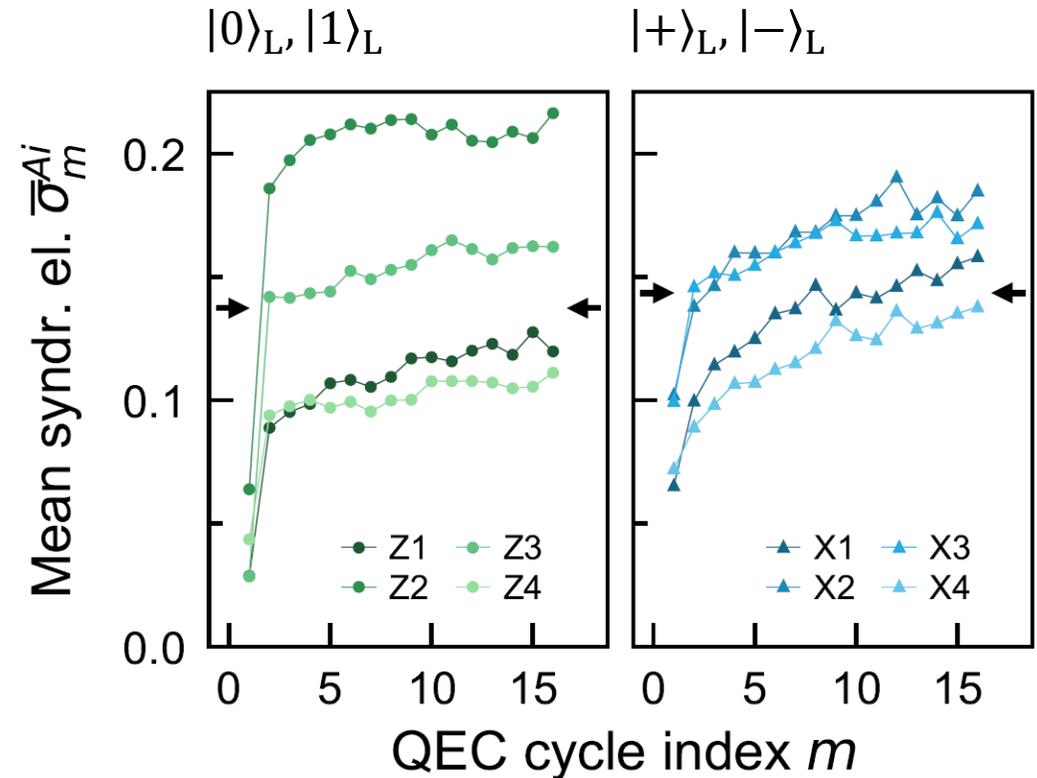


Versluis et al., *PR Applied* **8**, 034021 (2017)

S. Krinner, N. Lacroix et al., *Nature* **605**, 669 (2022)

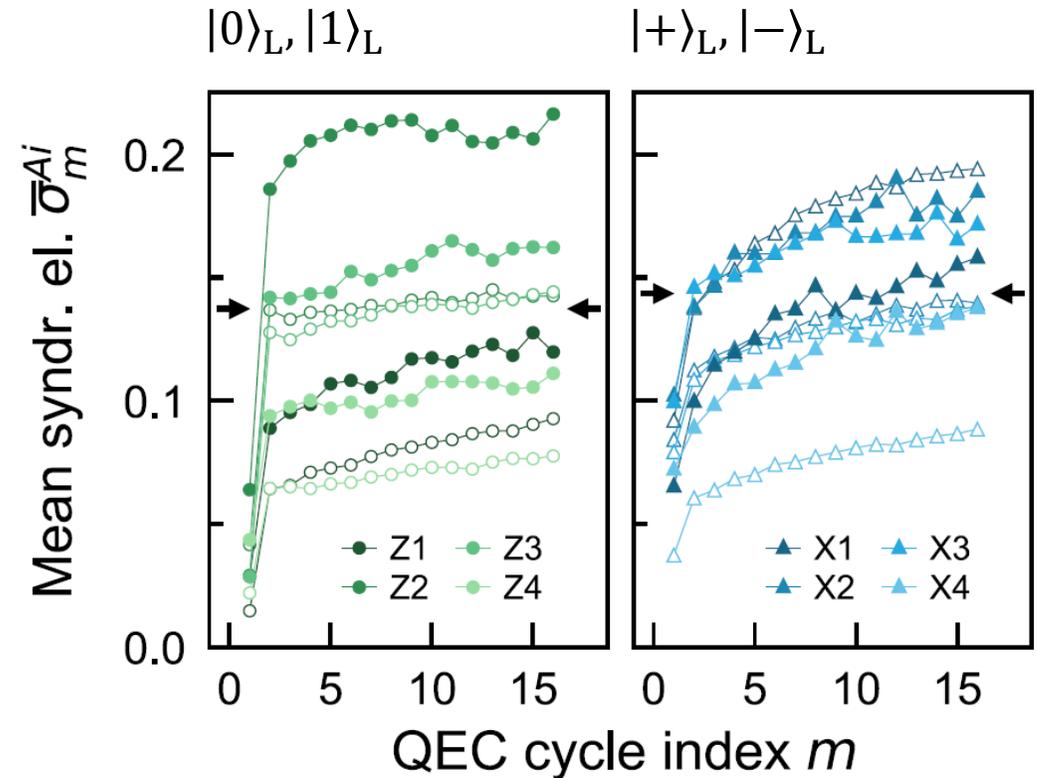
Syndrome Measurements

- Average σ_m^{Ai} over experimental repetitions: $\bar{\sigma}_m^{Ai}$
- Average over Ai and m : $\bar{\sigma} = 0.14 \ll 1$
- For $m \geq 2$: $\bar{\sigma}_m^{Ai}$ approximately constant
- Finite remaining slope due to increasing excited state population of auxiliary qubits



Syndrome Measurements

- Average σ_m^{Ai} over experimental repetitions: $\bar{\sigma}_m^{Ai}$
- Average over Ai and m : $\bar{\sigma} = 0.14 \ll 1$
- For $m \geq 2$: $\bar{\sigma}_m^{Ai}$ approximately constant
- Finite remaining slope due to increasing excited state population of auxiliary qubits
- Qualitative agreement with simulations



Decoding of Syndromes

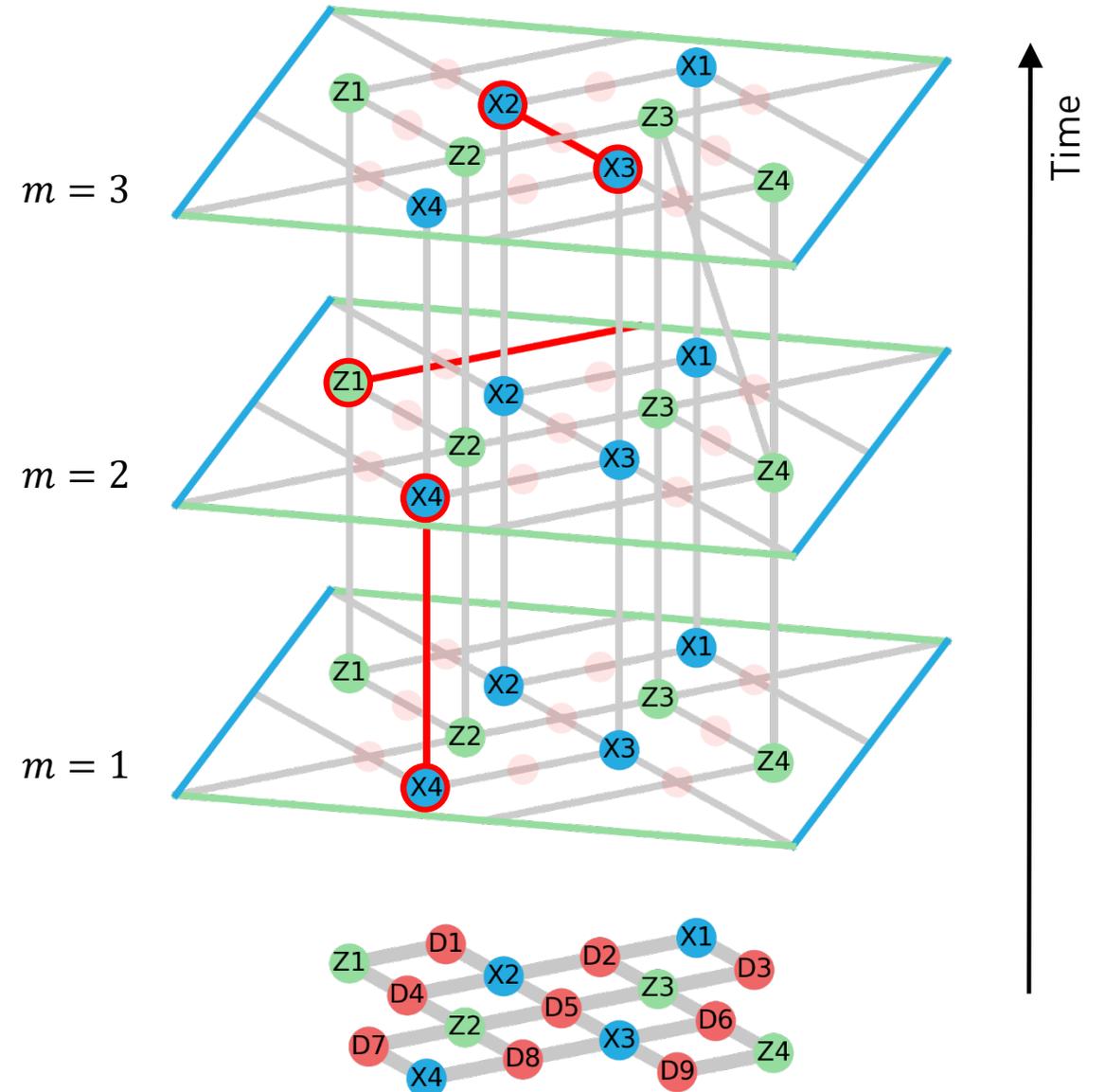
Decoder:

- Determine most likely errors given observed sequence of syndromes
- Mapping to minimum-weight-perfect-matching algorithm
 - Syndrome graph
 - Weights determined in error-model-free approach

Spitz et al., *Adv. Quantum Techn.* **1**, 1800012 (2018)

Chen et al., *Nature* **595**, 383 (2021)

Reimm et al., arXiv:2502.17722 (2025)



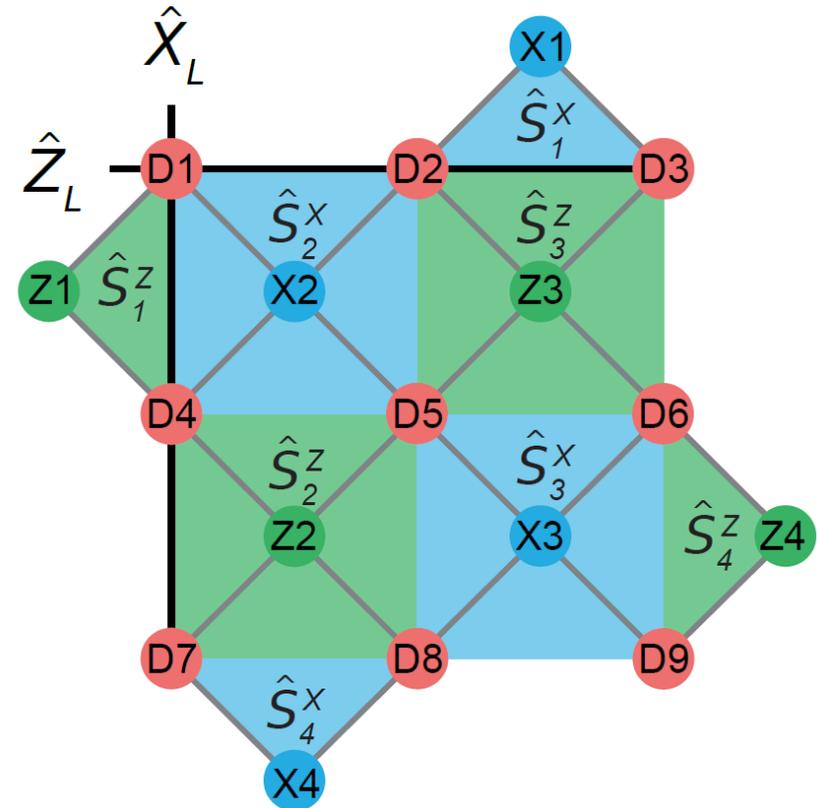
Repeated Quantum Error Correction

Measurement of Logical Z and Logical X Operators

- Initialization
 - $|0\rangle_L$: prepare data qubits in $|0\rangle^{\otimes 9}$
 - $|1\rangle_L$: prepare data qubits in $X_L|0\rangle^{\otimes 9}$
 - $|+\rangle_L$: prepare data qubits in $|+\rangle^{\otimes 9}$
 - $|-\rangle_L$: prepare data qubits in $Z_L|+\rangle^{\otimes 9}$
- Perform n QEC cycles
- Read out all data qubits in Z-basis (X-basis)

Analysis

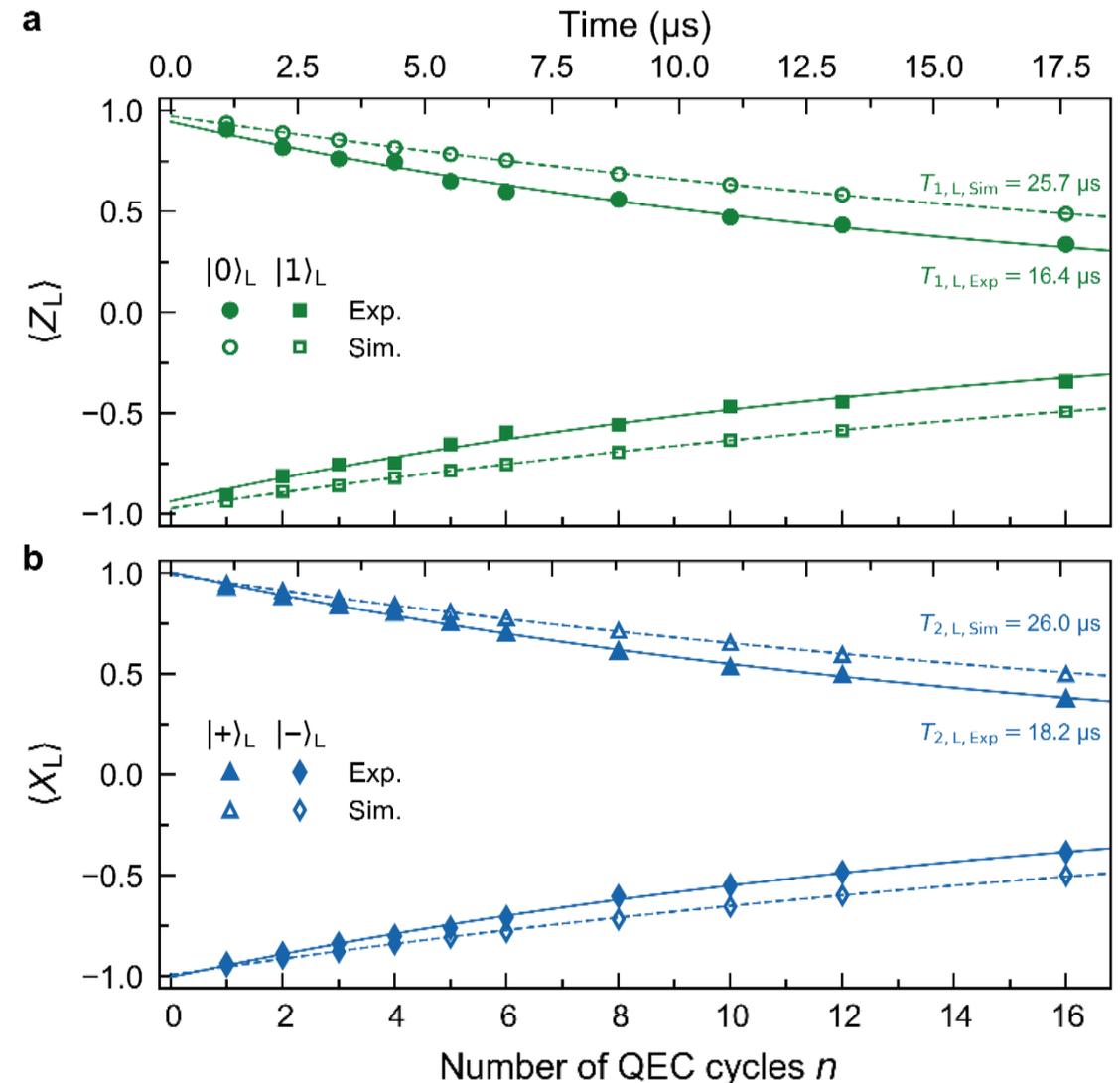
- Determine logical operator $z_L = z_1 z_2 z_3 = \pm 1$ ($x_L = x_1 x_4 x_7 = \pm 1$) for each run with up to n repeated cycles
- Apply correction conditioned on decoded syndromes for each run
- Average over runs with n repeated cycles to compute $\bar{z}_L = \langle \hat{Z}_L \rangle$ ($\bar{x}_L = \langle \hat{X}_L \rangle$)



Repeated Quantum Error Correction

Outcomes Logical Z and Logical X

- Exponential decay of logical expectation values
- Logical lifetime
 $T_{1,L} = 16.4(8) \mu\text{s} \gg t_c = 1.1 \mu\text{s}$
- Logical coherence time
 $T_{2,L} = 18.2(5) \mu\text{s} \gg t_c = 1.1 \mu\text{s}$
- Master equation simulation of logical lifetimes of $\sim 26 \mu\text{s}$ provide upper bound for achievable lifetimes with our device performance



Logical Error Probability and Logical Error per Cycle

Logical error probability:

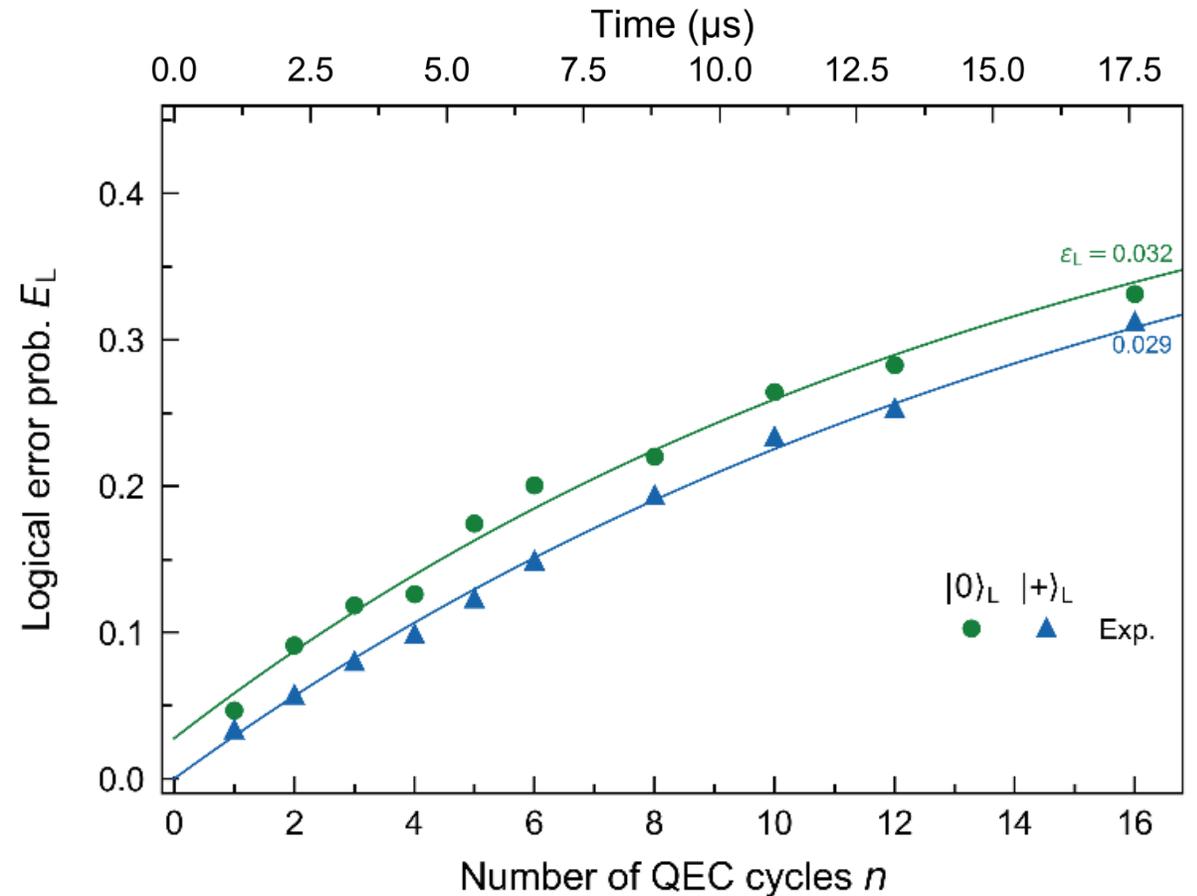
- $E_L = (1 - \langle \hat{Z}_L \rangle) / 2$ for eigenstates of \hat{Z}_L
- $E_L = (1 - \langle \hat{X}_L \rangle) / 2$ for eigenstates of \hat{X}_L

Logical error per cycle:

- Extracted from fit to $E_L(n)$ or from $T_{1/2,L}$:

$$\epsilon_L = \frac{1}{2} [1 - \exp(-t_c / T_{1/2,L})] \approx t_c / 2T_{1/2,L}$$

- $\epsilon_L \sim 0.03$



Repeated Quantum Error Correction Experiments with $d=3$ or Larger

Published work:

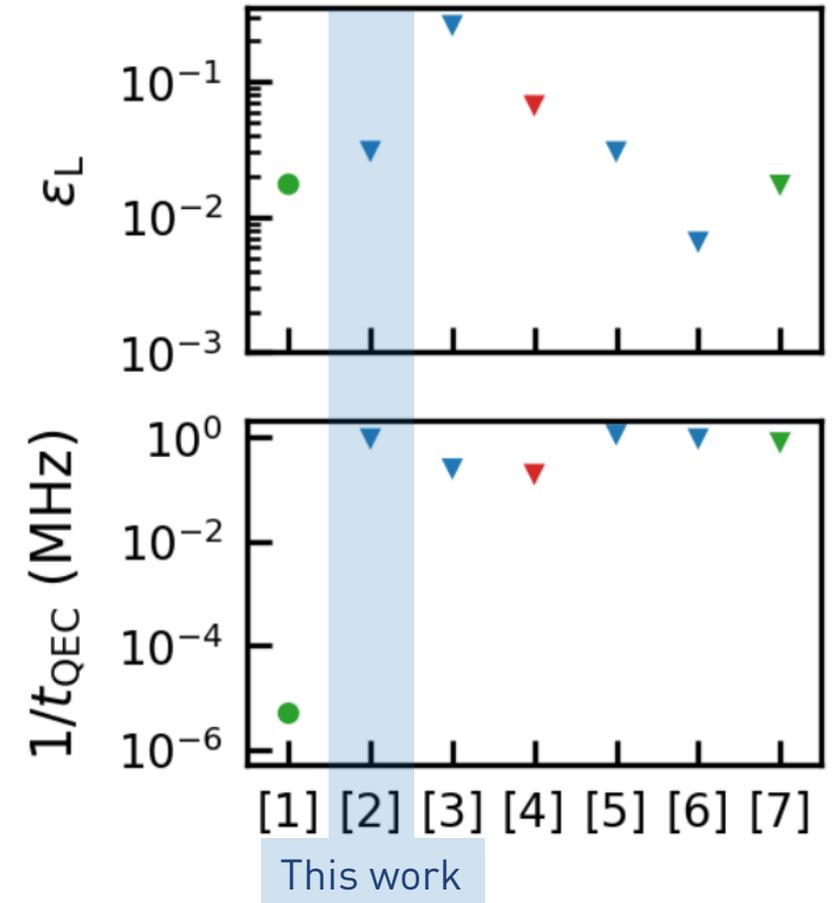
- Honeywell: [1] Ryan-Anderson *et al.*, *Phys. Rev. X* **11**, 041058 (2021)
- ETHZ: [2] Krinner, Lacroix *et al.* *Nature* **605**, 669 (2022)
- USTC: [3] Zhao *et al.*, *PRL* **129**, 030501 (2022)
- IBM: [4] Sundaresan *et al.*, *Nat. Commun.* **14**, 2852 (2023)
- Google: [5] Google Quantum AI, *Nature* **614**, 676 (2023)
- Google: [6] Google Quantum AI, *Nature* **638**, 920 (2025)
- Google: [7] Lacroix *et al.*, *arXiv:2412.14256* (2024)

Implementations:

- superconducting-circuits (∇) and trapped-ions (0)
- Color code, surface code and heavy-hexagon code

Performance criteria

- Small logical error per cycle ϵ_L
- High QEC cycle rate $1/t_{\text{QEC}}$



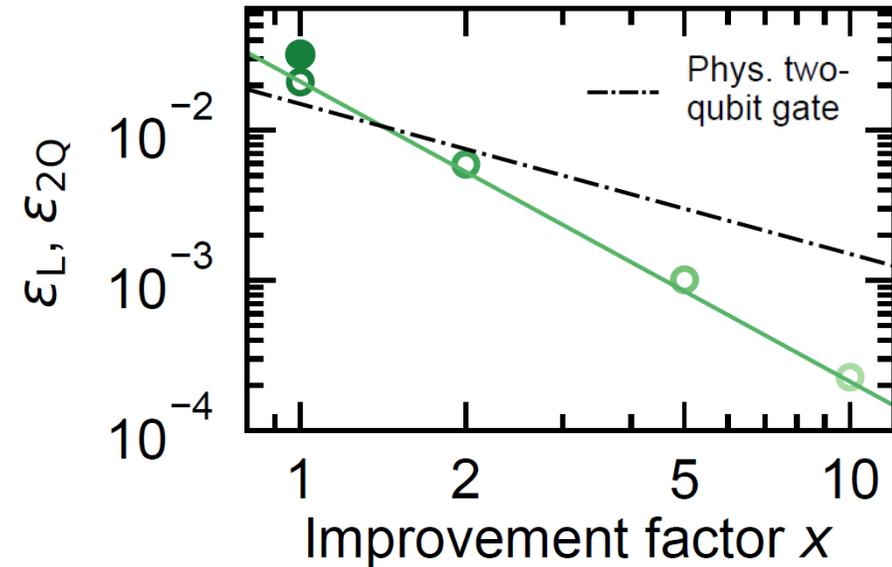
Performance Assessment and Projection

Two-qubit-gate break-even

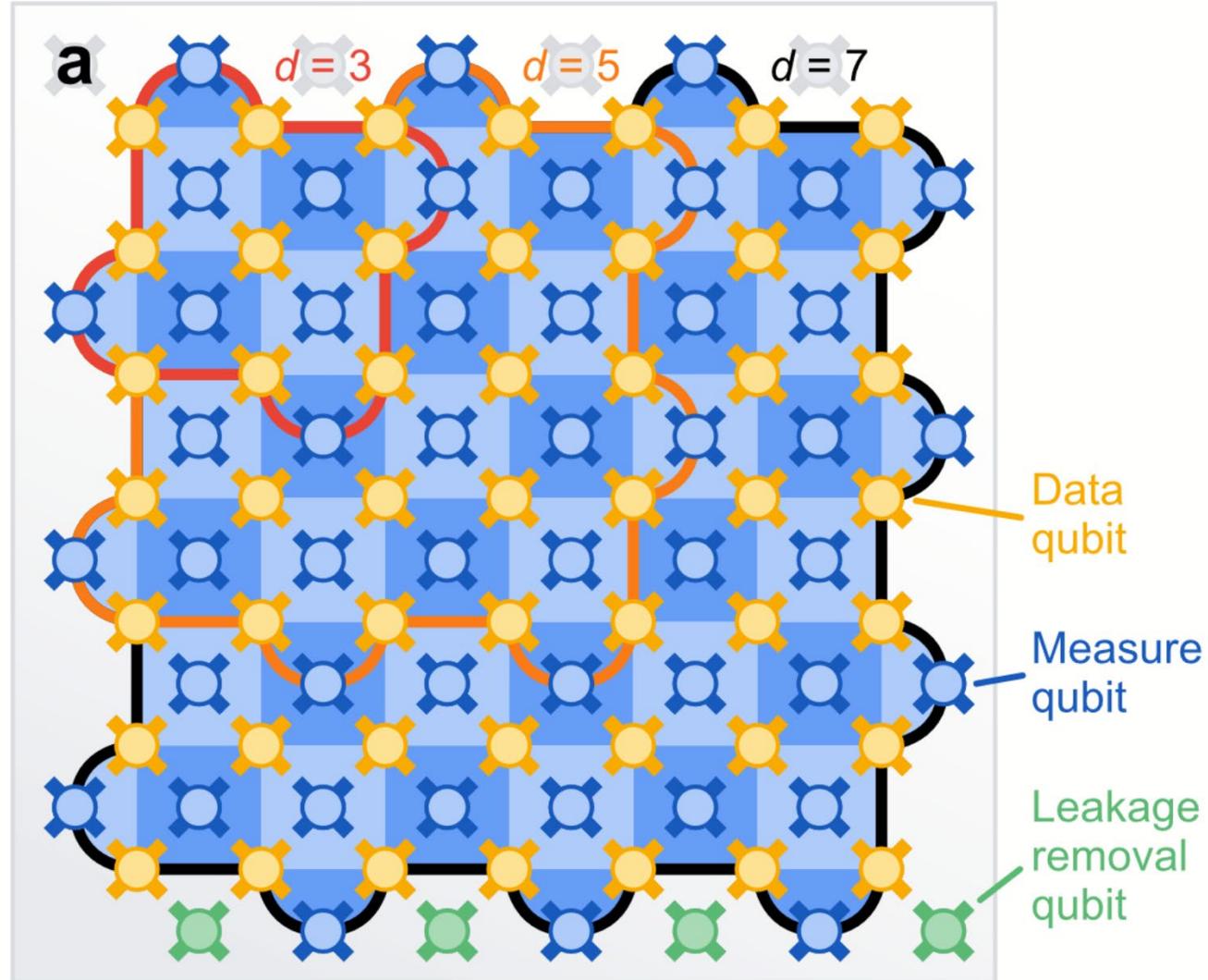
- Compare $\epsilon_L = 0.03$ to dominant physical error
 - Two-qubit gate error $\epsilon_{2Q} = 0.015$
 - Logical two-qubit gate error is expected to be dominated by ϵ_L
- Used simulations to project performance with physical error rates reduced by factor x
 - $\epsilon_L \propto 1/x^2$
 - Break-even within reach

Error threshold

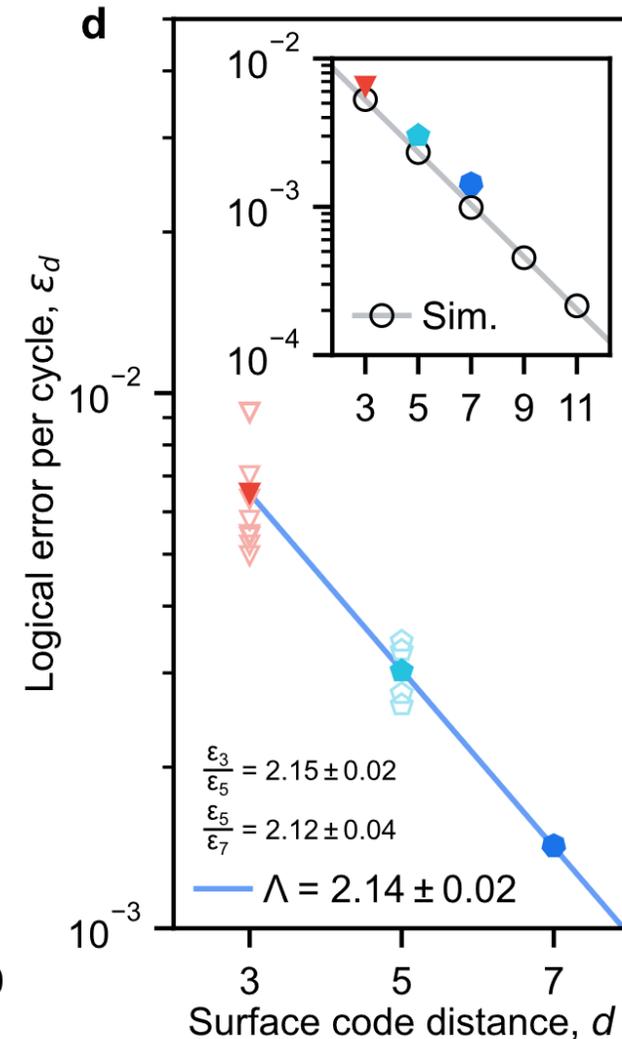
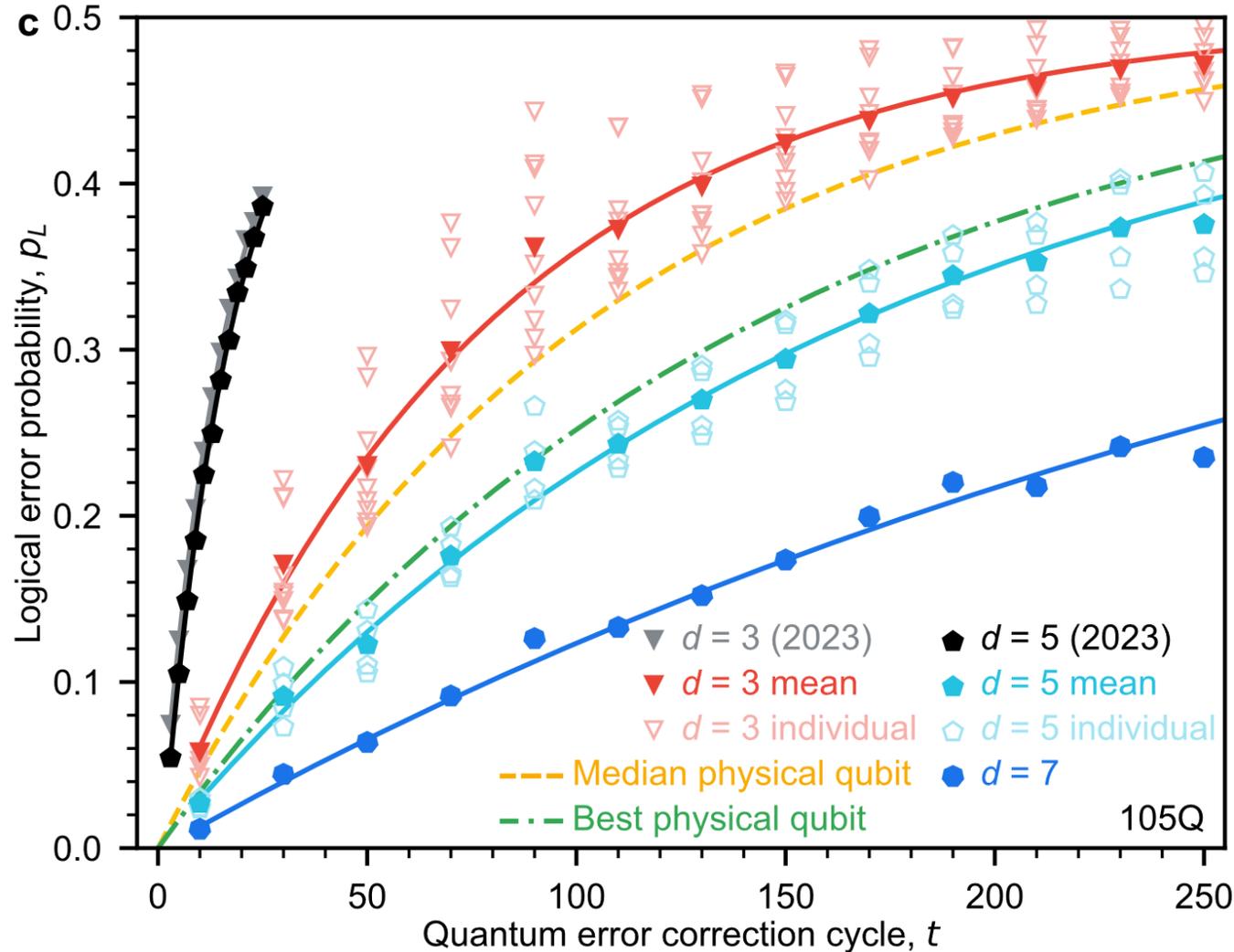
- $\epsilon_L \sim 0.03$ comparable to predicted logical error per cycle at error threshold
 Fowler *et al.*, *Phys. Rev. A* **86**, 032324 (2012)
 Stephens, *Phys. Rev. A* **89**, 022321 (2014).



Distance-Three, -Five and -Seven Surface Code Layout



Distance Scaling and Logical Error Suppression



Surface Code and Lattice Surgery

- Surface code promising candidate for implementation of logical qubits in superconducting circuits

Kitaev, A. *Ann. Phys.* 303 1 (2003)

Fowler, A. et al. *Phys. Rev. A* 86, 032324 (2012)

- Experimental realizations of logical state preservation close to the threshold

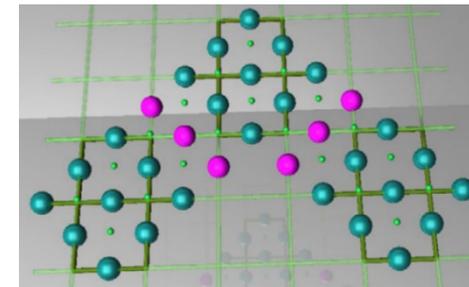
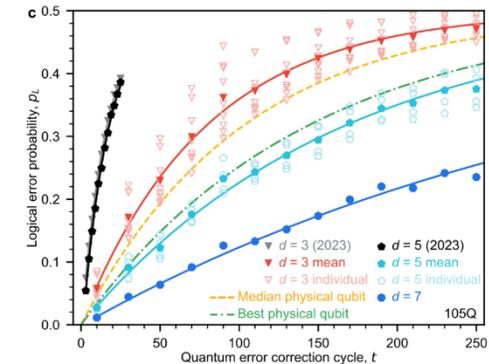
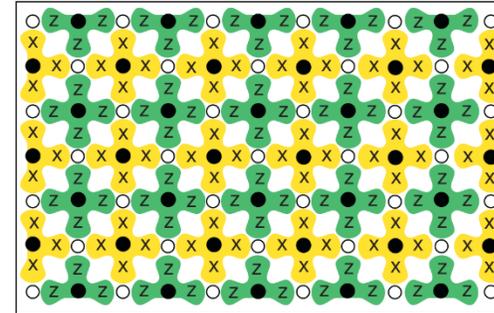
Krinner, S. et al. *Nature* 605, pages 669–674 (2022)

Google Quantum AI, *Nature* 614, pages 676–681 (2023)

Google Quantum AI and Collaborators, *Nature* (2024)

- Lattice surgery allows realization of non-transversal interactions between encoded qubits with low qubit-overhead

Horsman, D. et al. *New J. Phys.* 14 123011 (2012)



Experimental Work on Logical Qubit Operations

Logical operations on **encoded qubits**:

- Fault-tolerant subset of Clifford group on [4,2,2] code (s.c.)
Harper, R. et al. Phys. Rev. Lett. **122**, 080504 (2019)
- Transversal CNOT on two [7,1,3] color codes (ions)
Postler, L. et al. Nature **605**, 675 (2022)

Non-fault-tolerant **arbitrary state preparation**

- $d = 3$ Bacon-Shor code (ions)
Egan, L. et al. Nature **598**, 281 (2021)
- $d = 3$ surface code (s.c.)
Ye, Y. et al. Phys. Rev. Lett. **131**, 210603 (2023)

Lattice surgery ...

- ... on a $d = 2$ surface code (ions)
Erhard, A. et al. Nature **589**, 220 (2021)
- ... on interleaved $d = 3$ 3CX and Bacon-Shor code (s.c.)
Hetenyi, B. et al. PRX Quantum **5**, 040334 (2024)
- ... on a $d = 3$ color code (s.c.)
Lacroix, N. et al. arXiv:2412.14256v1 (2024)

Independent logical qubits during idling (modularity):

- transversal implementation of various QEC codes (ryd.)
Bluvstein, D. et al. Nature **626**, 58 (2024)
- state teleportation on three $d = 3$ color codes (ions)
Ryan-Anderson, C. et al. Science **385**, 1327 (2024)

Here: Modular lattice surgery on surface code with partial decoding from repeated syndrome extraction on superconducting qubits

Transversal Gates vs. Lattice Surgery

All-to-all connectivity (ions, Rydberg atoms)

- Allows for transversal logical two-qubit gates

2D square lattice connectivity (s.c.)

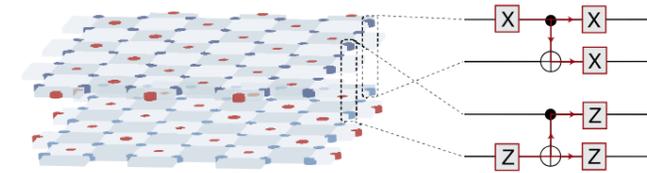
- Requires lattice surgery

Lattice surgery operations:

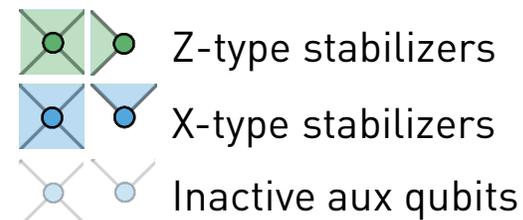
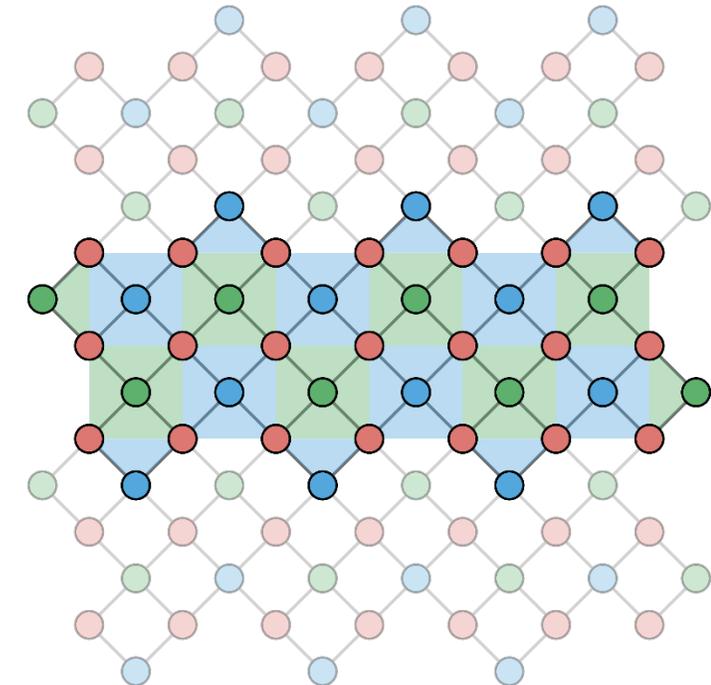
- Merge
- Split
- Measurement of logical two-qubit observables $\hat{X}_{L1}\hat{X}_{L2}$ (or $\hat{Z}_{L1}\hat{Z}_{L2}$)

Horsman, D. et al. *New J. Phys.* **14** 123011 (2012)

Austin G. Fowler, Craig Gidney arXiv:1808.06709 (2018)



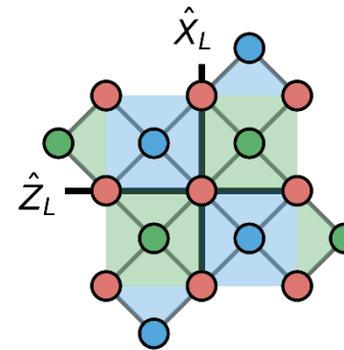
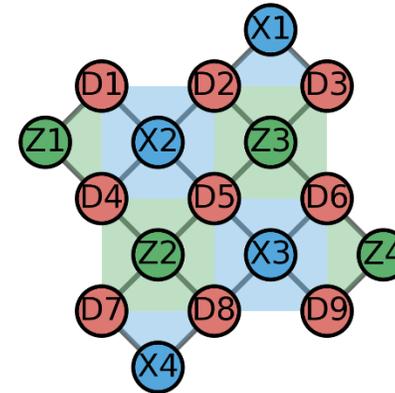
D. Bluvstein et al, *Nature* **626**, pages 58–65 (2024)



● Data qubit
● Data qubit (inactive)

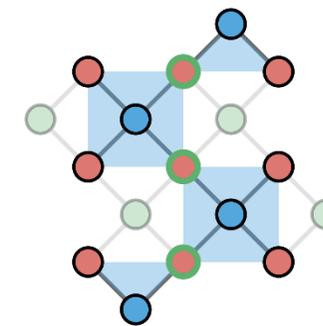
Logical Operators of the Surface and the Repetition Codes

- Distance-three surface code qubit:
 - 3×3 patch on the data qubit lattice,
 - single bit-flip and phase-flip errors correctable
 - Logical operator definitions
- Lattice split operation transforms the $d = 3$ surface code into two $d = 3$ bit-flip codes:
 - Stop measuring X-type stabilizers
 - Readout of middle column of data qubits \bullet in Z-basis
- Two $d = 3$ bit-flip repetition codes:
 - Two 1×3 patches
 - Single bit-flip error correctable
 - Logical operator definitions

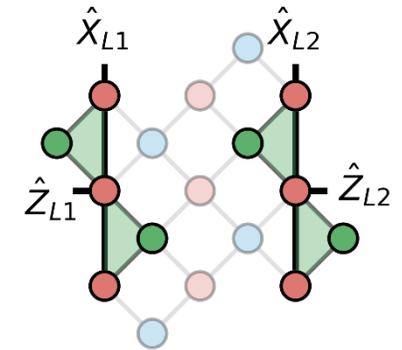


$$\begin{aligned}\hat{Z}_L &= \hat{Z}_{D4}\hat{Z}_{D5}\hat{Z}_{D6} \\ \hat{X}_L &= \hat{X}_{D2}\hat{X}_{D5}\hat{X}_{D8} \\ \hat{Y}_L &= \hat{Z}_L\hat{X}_L = \hat{X}_{D2}\hat{Z}_{D4}\hat{Y}_{D5}\hat{Z}_{D6}\hat{X}_{D8}\end{aligned}$$

$$\begin{aligned}\hat{Z}_{L2} &= \hat{Z}_{D6} \\ \hat{X}_{L2} &= \hat{X}_{D3}\hat{X}_{D6}\hat{X}_{D9} \\ \hat{Y}_{L2} &= \hat{X}_{D3}\hat{Y}_{D6}\hat{X}_{D9}\end{aligned}$$



$$\begin{aligned}\hat{Z}_{L1} &= \hat{Z}_{D4} \\ \hat{X}_{L1} &= \hat{X}_{D1}\hat{X}_{D4}\hat{X}_{D7} \\ \hat{Y}_{L1} &= \hat{X}_{D1}\hat{Y}_{D4}\hat{X}_{D7}\end{aligned}$$



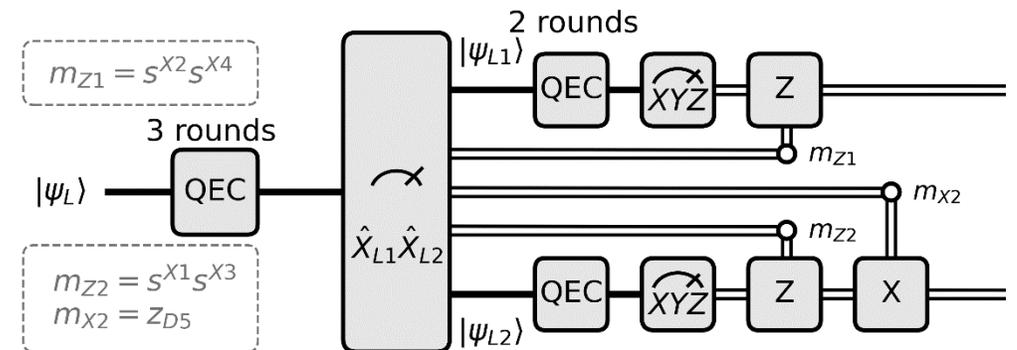
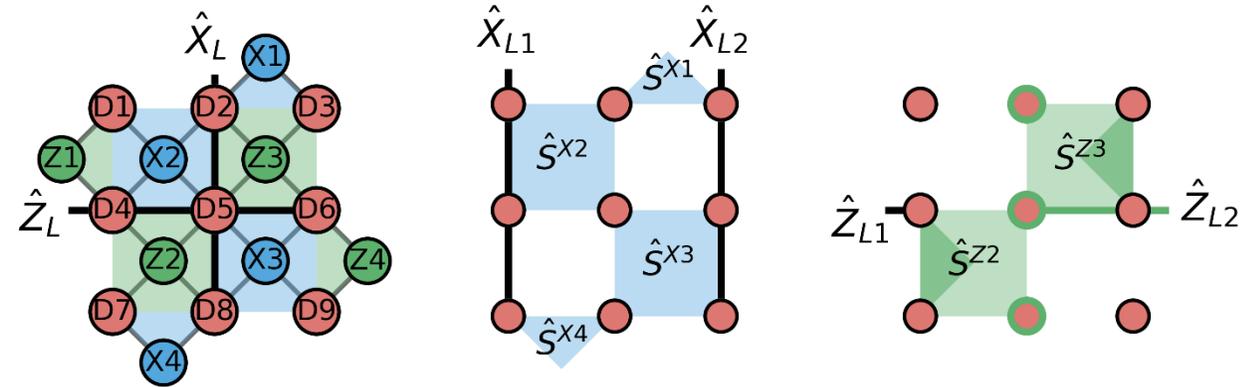
Pauli Frame Update

- Logical states after split depend on measurement outcomes
- Relation between repetition and surface code logical operators
 - Logical X-operators:

$$\hat{X}_{L1} = \hat{X}_L \hat{S}^{X2} \hat{S}^{X4}$$

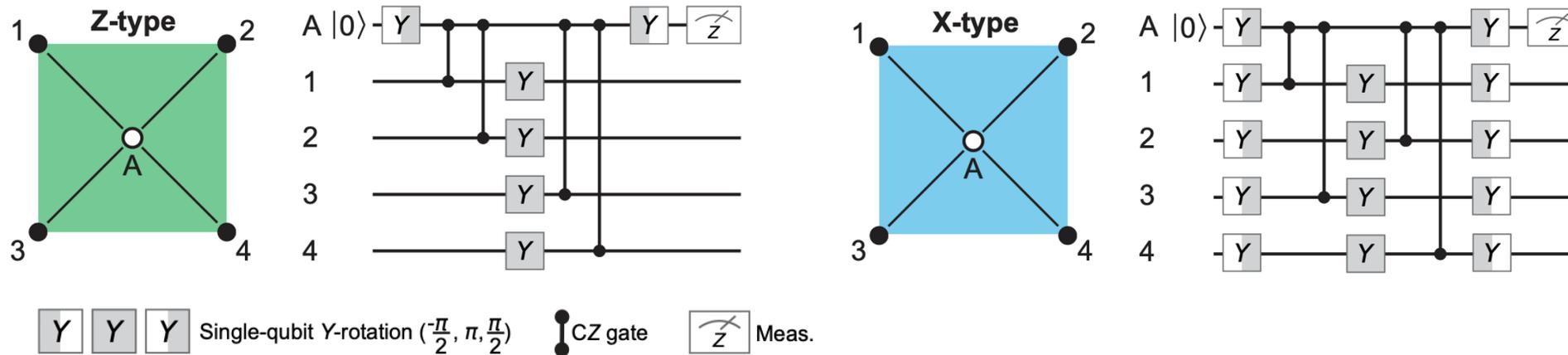
$$\hat{X}_{L2} = \hat{X}_L \hat{S}^{X1} \hat{S}^{X3}$$
 - Logical Z-operators:

$$\hat{Z}_L = \hat{Z}_{D4} \hat{Z}_{D5} \hat{Z}_{D6} = \hat{Z}_{L1} (\hat{Z}_{L2} \hat{Z}_{D5})$$
- Deterministic operation realized by feed-forward Pauli-Frame update:
 - $\hat{X}_L \rightarrow \hat{X}_{L1}, \hat{X}_{L2}$
 - $\hat{Z}_L \rightarrow \hat{Z}_{L1}, \hat{Z}_{L2}$
 - performed in post-processing
- Weight-4 Z-type stabilizers become weight-2, value updated by data qubit readout outcome



Stabilizer Measurement and Syndrome Extraction

Auxiliary-qubit-based stabilizer measurement



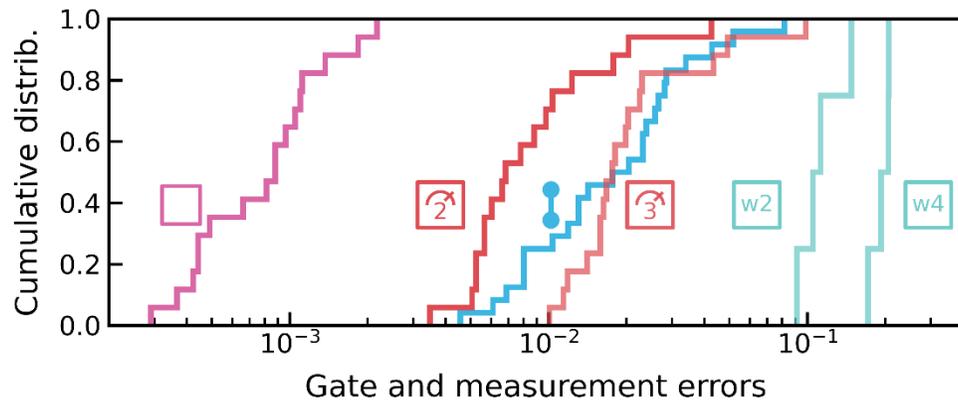
- Z- or X-parity measurement of data qubits on vertices of plaquette
- Bit-flip detected when Z-stabilizer s_N^Z switches from +1 to -1 in round N
- Phase-flip detected when X-stabilizer s_N^X switches from +1 to -1 in round N
- syndrome element of round N for operator A_i :

$$\sigma_N^{A_i} = (1 - s_N^{A_i} s_{N-1}^{A_i})/2$$

17-Qubit Device

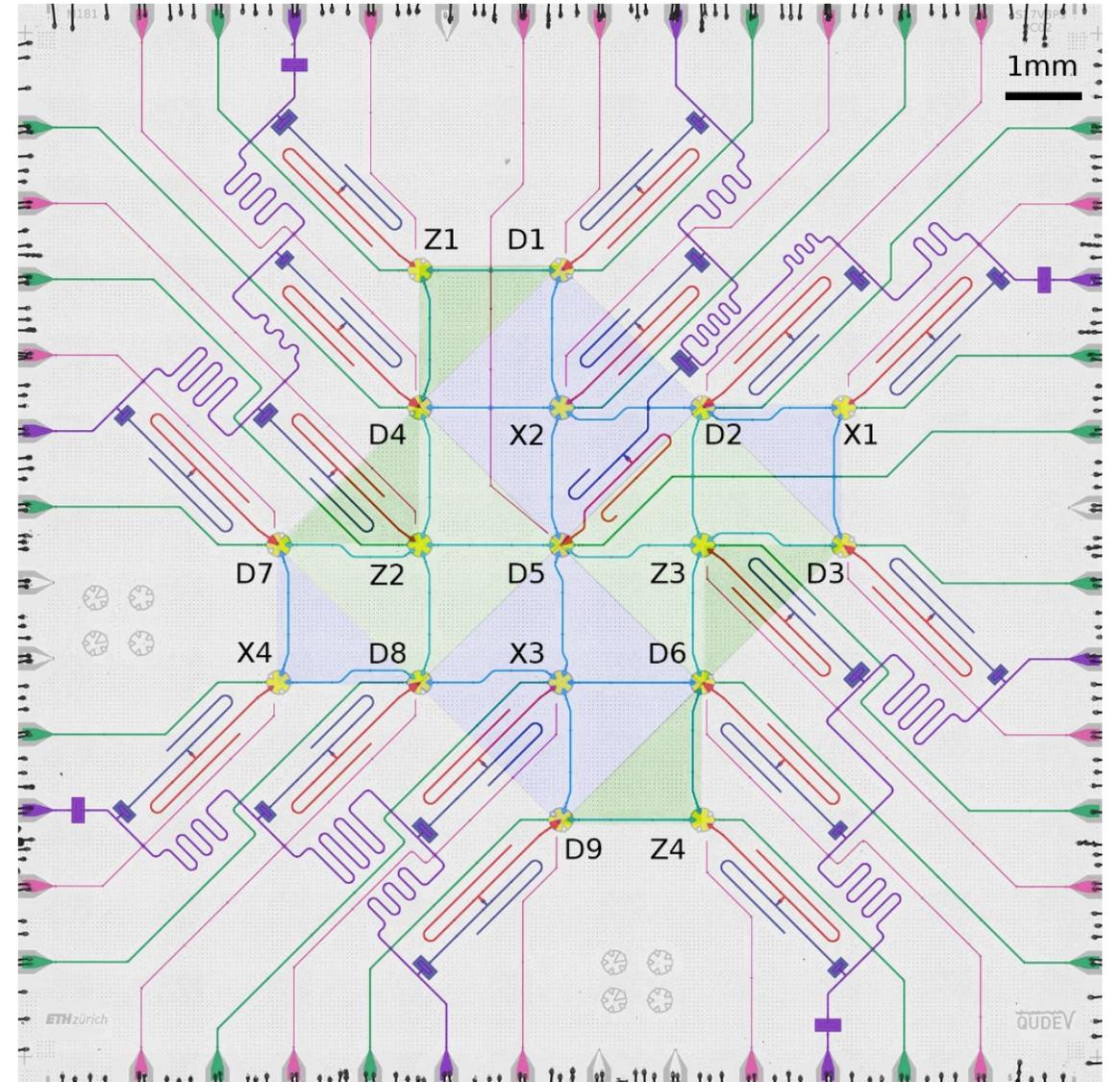
- flux-tunable transmon qubits
- Readout resonators and Purcell filters coupled to joint feedline

Device performance metrics

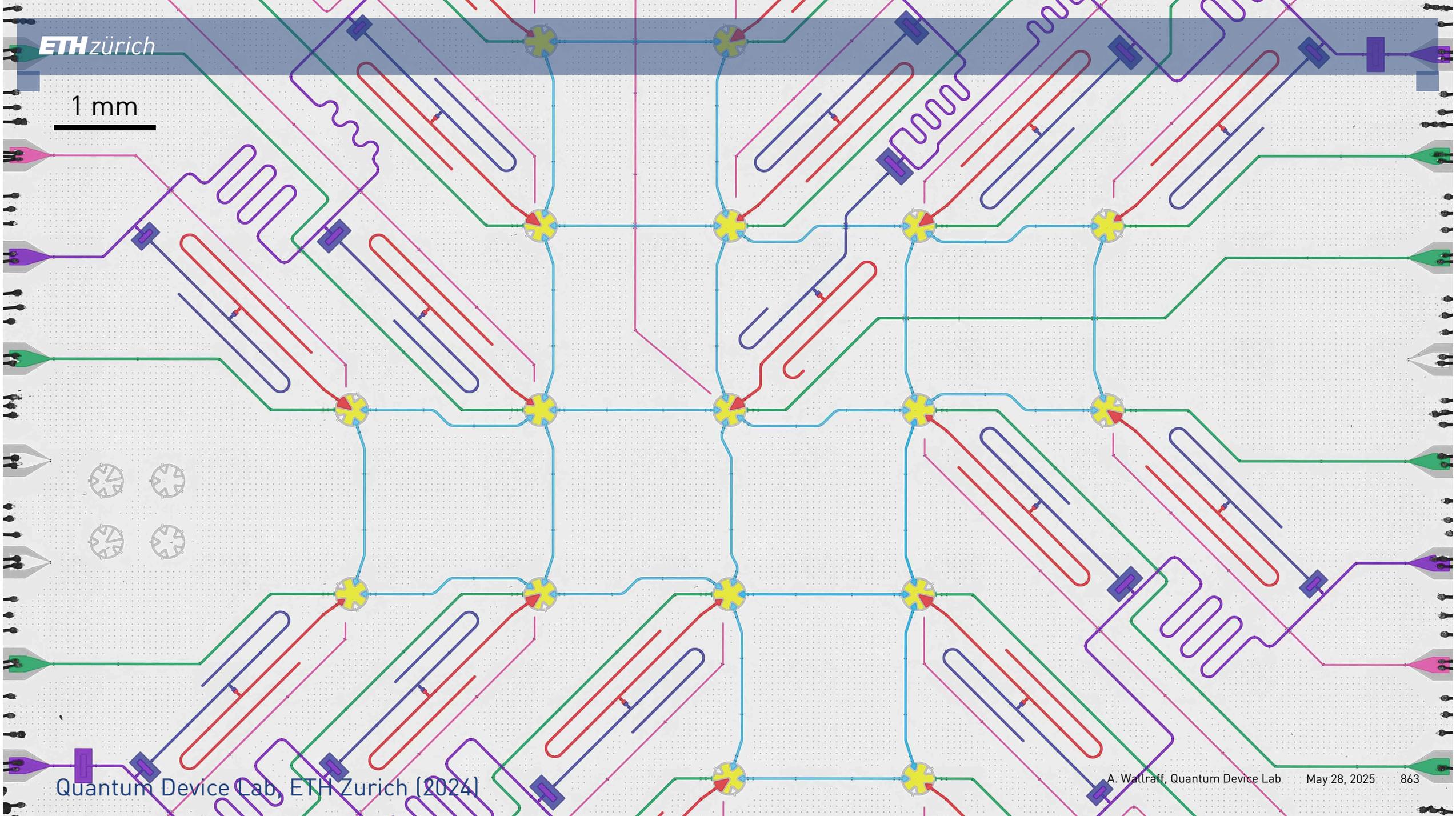


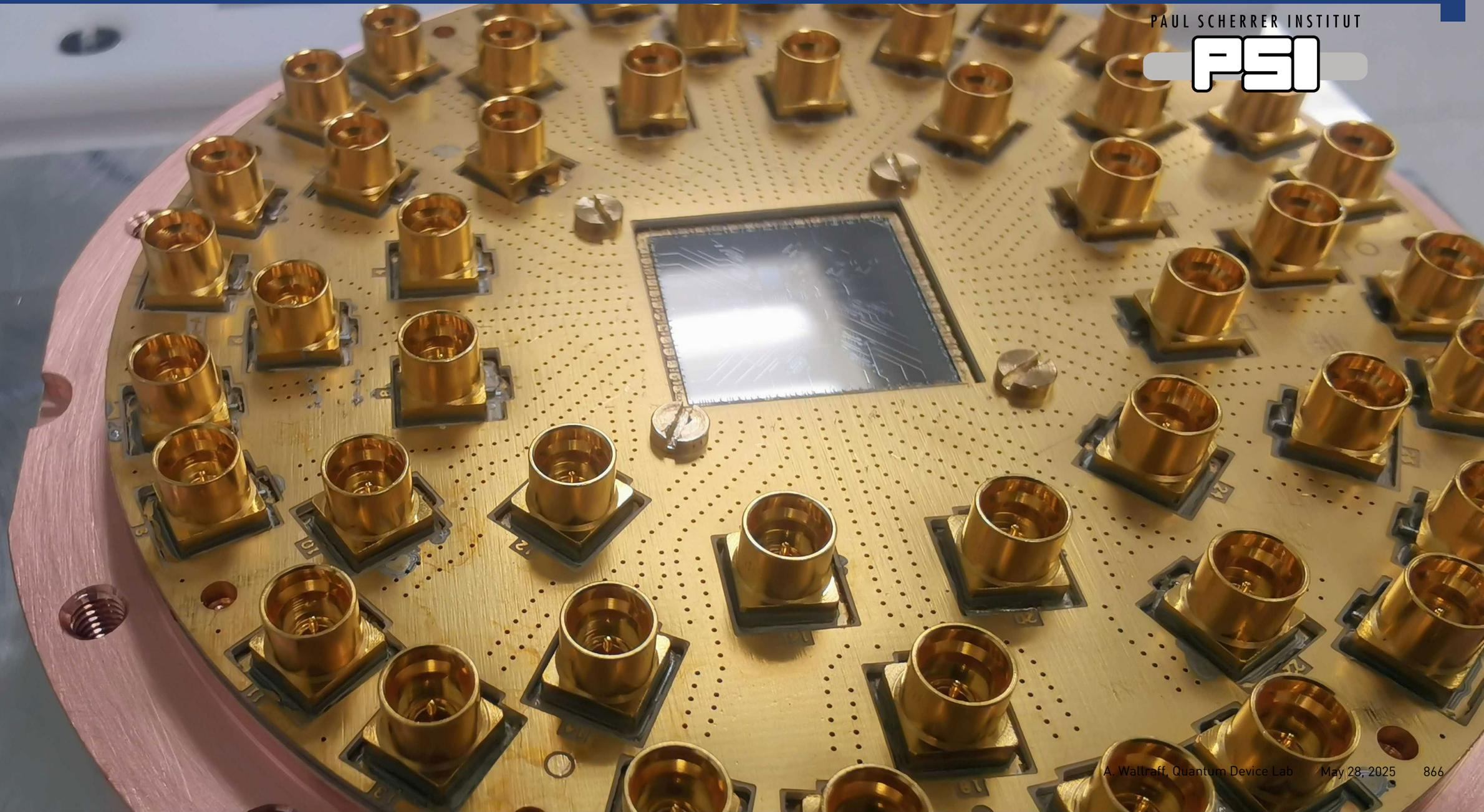
- Single-qubit gate error 0.1%
- Two-qubit gate error 2%
- Two-/three-state readout error 1.1% / 2.5%
- Weight-2/-4 syndrome element 11.6% / 18.5%

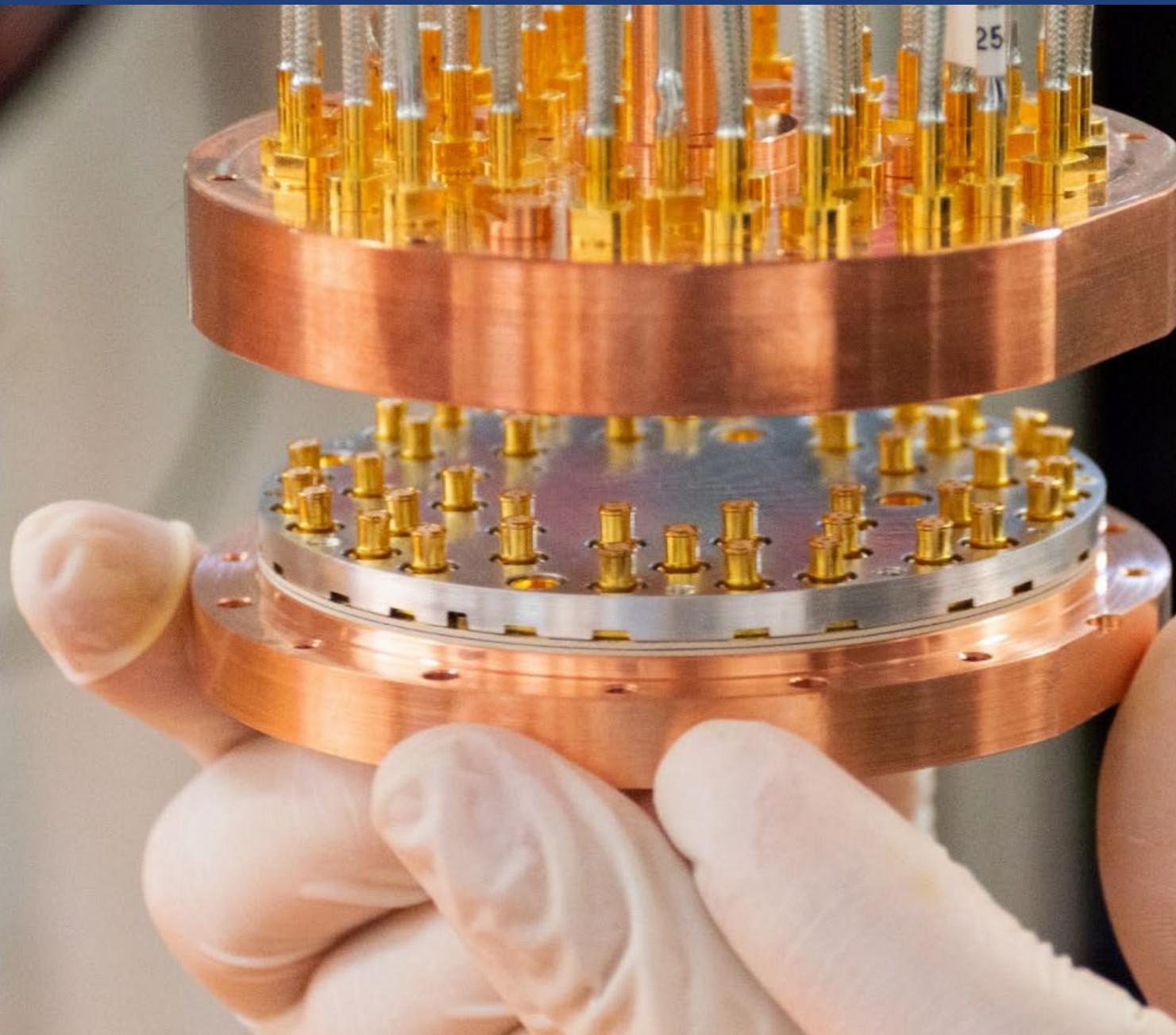
Besedin, I., Kerschbaum M. *et al.*, arXiv: 2501.04612 (2025)



1 mm











Surface-Code State-Preservation Experiment

Surface code

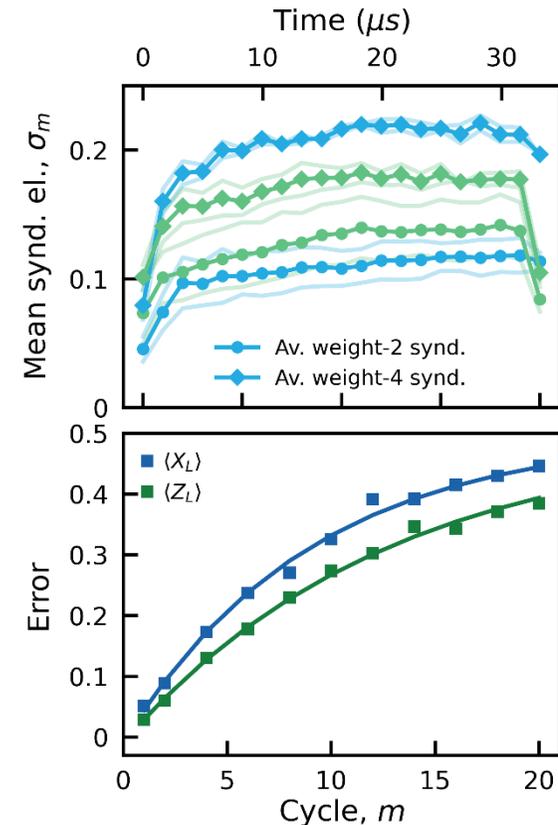
- 20 rounds of X and Z stabilizer measurements for $|0\rangle_L, |1\rangle_L, |+\rangle_L, |-\rangle_L$ initial states

Fault-tolerant state preparation:

- preparing all data qubits in \hat{Z} (\hat{X}) eigenstates yields well-defined S^{Zi} (S^{Xi}) and Z_L (X_L)
- 1 Preparation syndrome, 19 state preservation and 1 readout syndrome: $\sigma_N^{Ai} = (1 - s_N^{Ai} s_{N-1}^{Ai})/2$

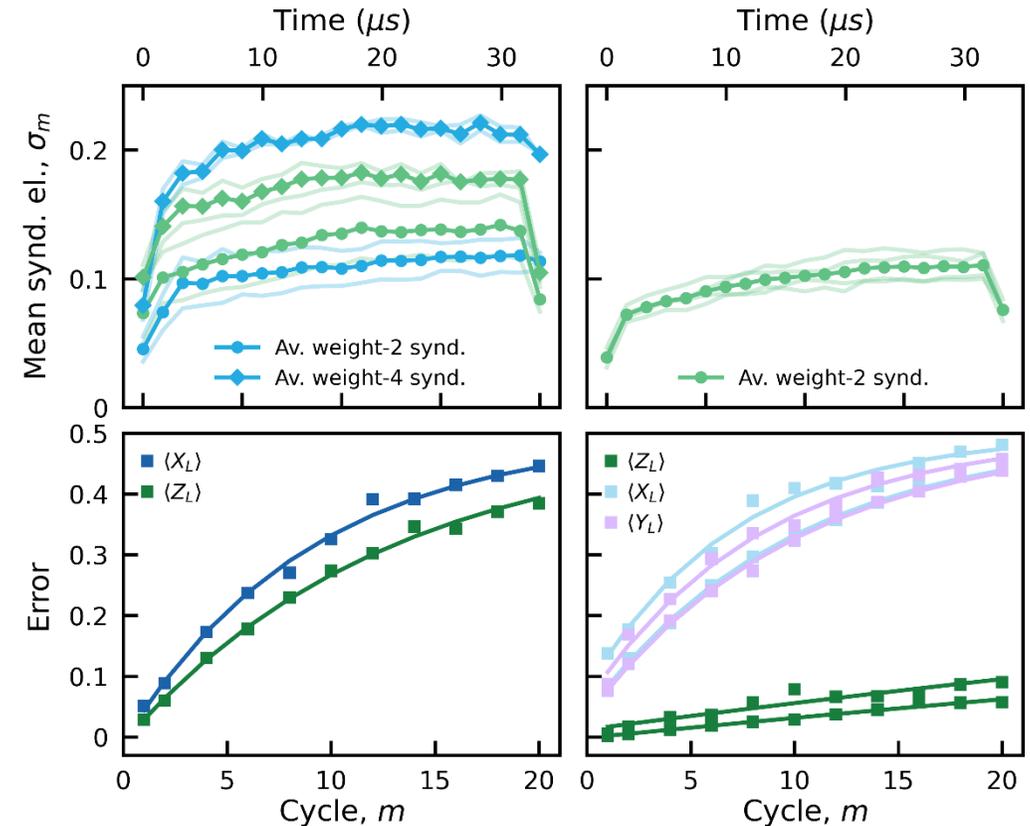
Errors

- evaluate Z_L (X_L) from final data qubit readout
- use syndrome data with MWPM decoder to correct errors
- Error per cycle: $\epsilon_X = 11.1(4)\%$, $\epsilon_Z = 7.8(2)\%$

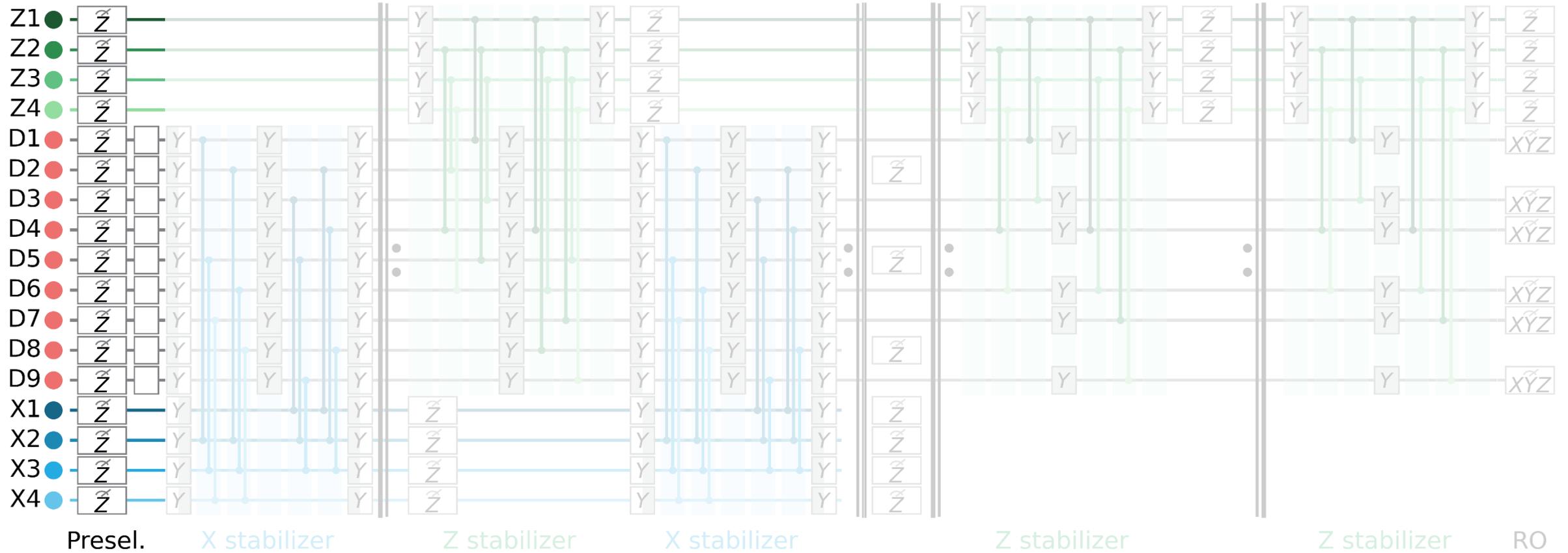


Repetition-Code State-Preservation Experiment

- For repetition codes, only Z syndromes
- Error correction only for Z_{L1} , Z_{L2} observables
- error per cycle: $\epsilon_{Z1} = 0.68(3)\%$, $\epsilon_{Z2} = 0.93(11)\%$
- For X observables, we compare raw outcomes.
Errors per cycle: $\epsilon_{X1} = 10.1(2)\%$, $\epsilon_{X2} = 14.0(8)\%$
- For bit flip-code: $\epsilon_{Y1} = 9.9(2)\%$, $\epsilon_{Y2} = 11.8(5)\%$
- Logical error per cycle in X observable for surface code similar to non-corrected observable in bit-flip code
- Near-threshold regime**



Gate Sequence of Lattice-Split Operation

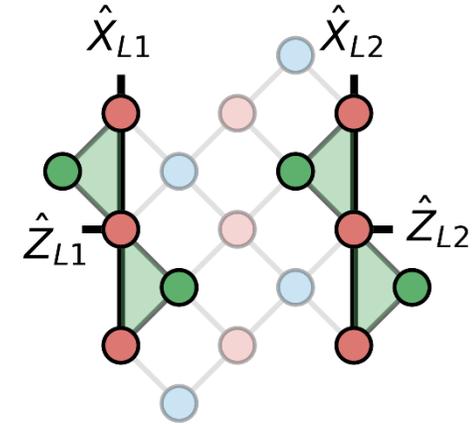


Y Y Y Single-qubit Y rotation $(-\frac{\pi}{2}, \pi, \frac{\pi}{2})$
 ⊗ CZ gate
 ⊗ Meas.
 ||: :|| Repetitions

- **Qubit initialization**
- **X-syndrome extraction to initialize $d = 3$ qubit**
- **Three rounds of syndrome extraction**
- **Lattice split**
- **Two rounds of syndrome extraction**
- **Logical observable readout**

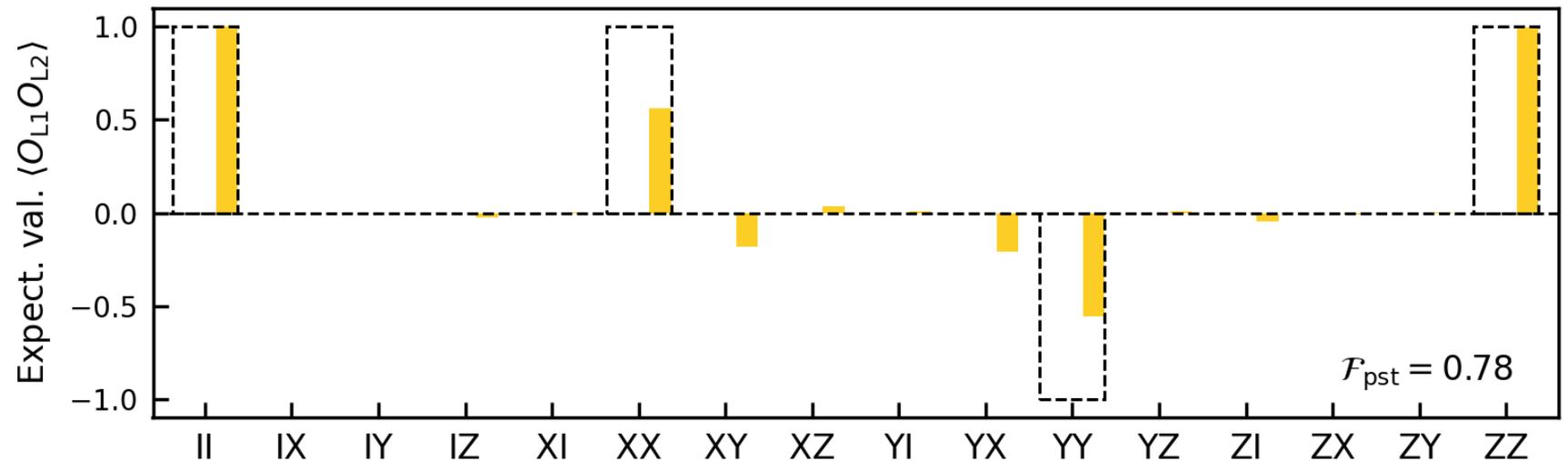
Logical Bell State Creation

- Prepare surface-code $|0\rangle_L$ and perform lattice split
- Fault-tolerant ($d = 3$) with respect to **bit-flip errors**
- Non-fault-tolerant ($d = 1$) with respect to **phase-flip errors**
- Evaluate Logical Bell state after **Pauli-frame update**:
 - Ideally $X_{L1}X_{L2} = Z_{L1}Z_{L2} = 1$ and $Y_{L1}Y_{L2} = -1$
- ~70'000 shots per logical operator, reject leakage, and calculate **expectation values**



Logical State Tomography

- Measure **all nine basis combinations of repetition code logical qubits** to perform **logical quantum state tomography**
- Use extracted syndromes to **post-select** on zero syndrome elements (no error)
 - $Z_{L1}Z_{L2}$ error <1%:
fault tolerant with respect to **bit-flips**
 - Expectation value of $X_{L1}X_{L2}$ and $Y_{L1}Y_{L2}$ limited by repetition code

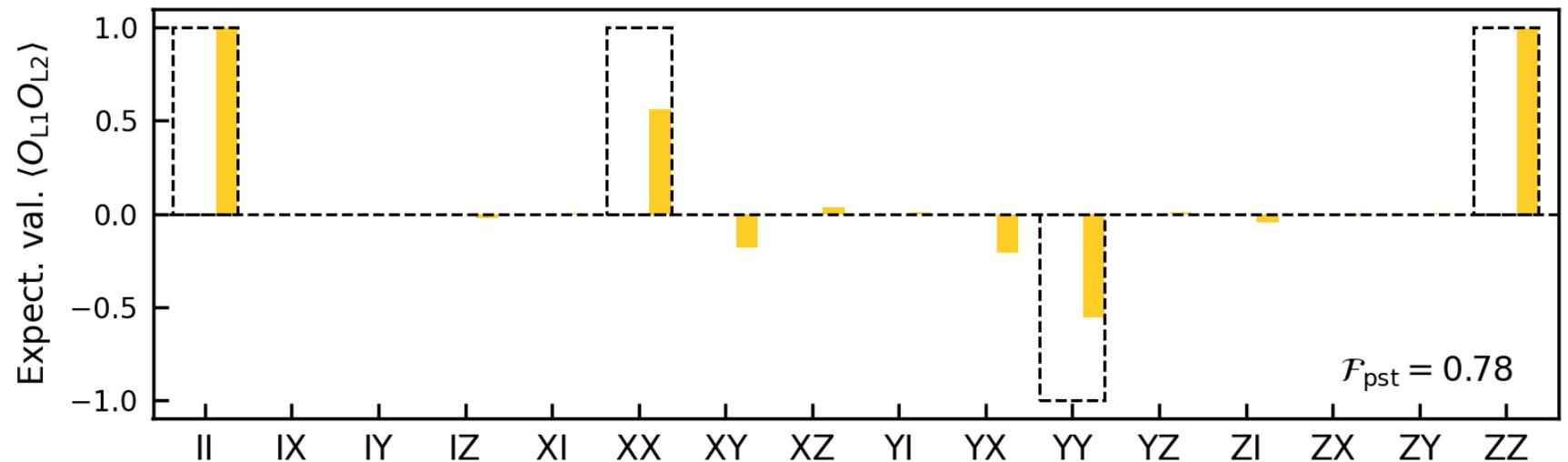


Logical State Tomography

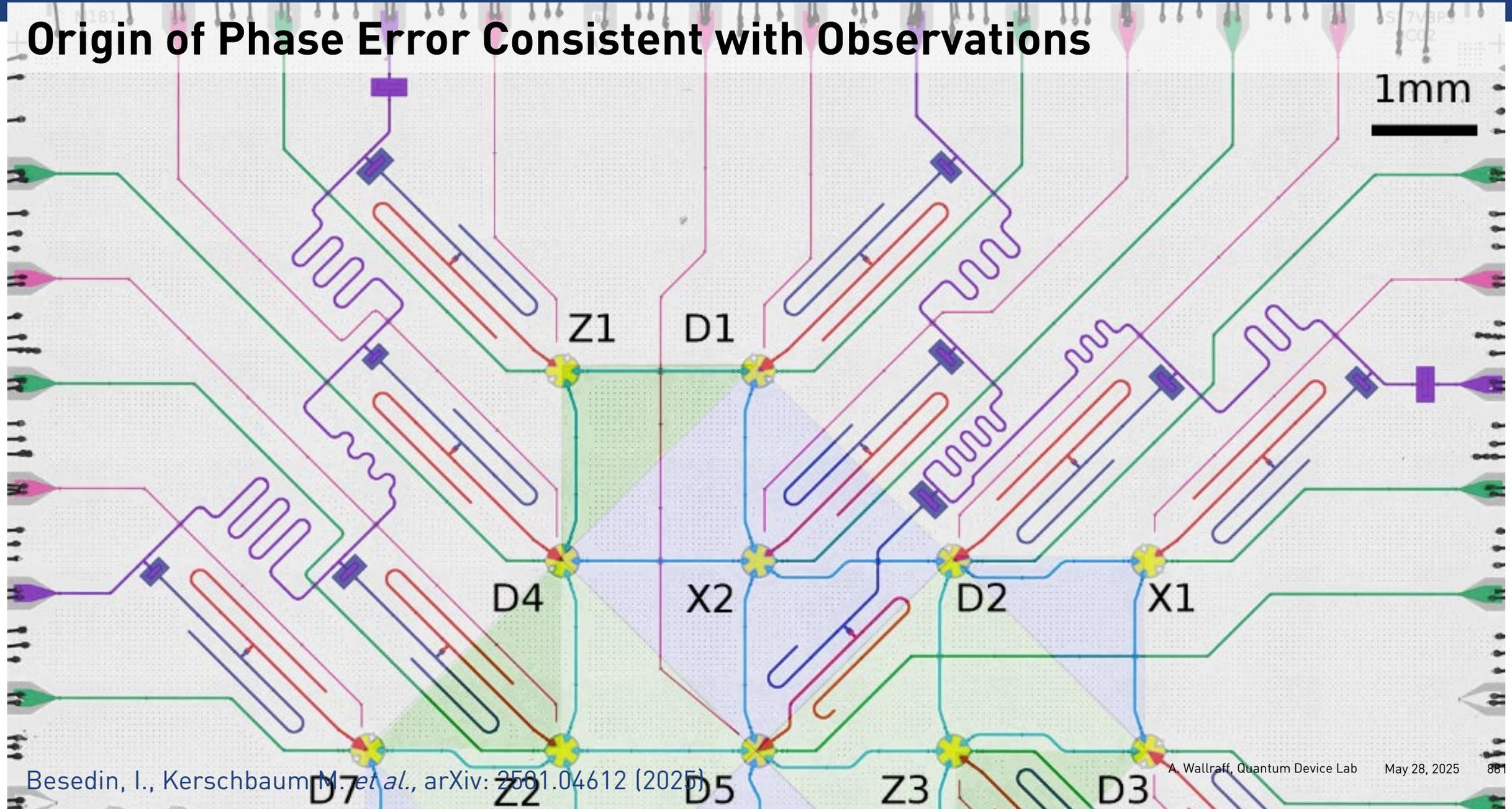
- Measure **all nine basis combinations of repetition code logical qubits** to perform **logical quantum state tomography**

Note

- Non-zero $X_{L1}Y_{L2}$ and $Y_{L1}X_{L2}$ expectation values
- Consistent with a 0.11π phase error on the first logical qubit state

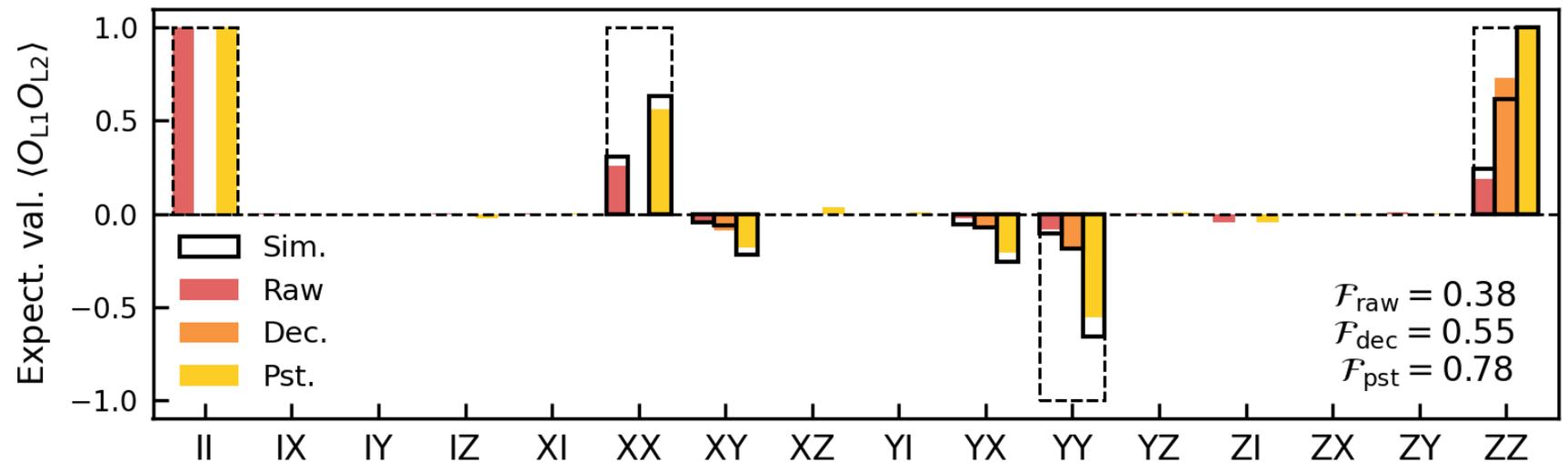


Origin of Phase Error Consistent with Observations



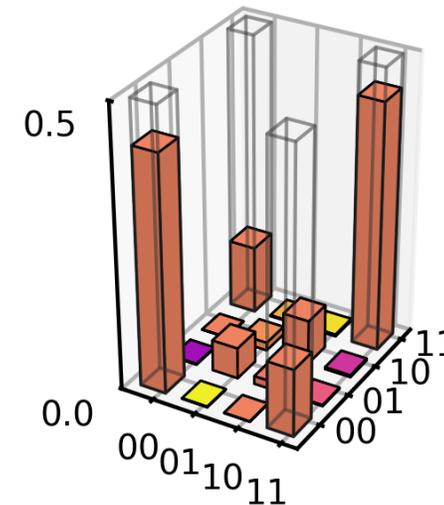
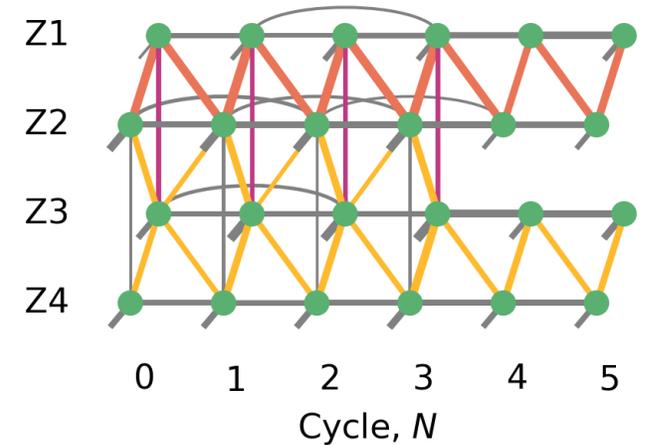
Logical State Tomography

- Measure **in all nine combinations of bases of logical qubits** to perform **logical quantum state tomography**
- Use **MWPM decoder**:
 - raw $Z_{L1} Z_{L2} = 0.19$ is improved to 0.73
- Reasonable agreement of data with Pauli error model **simulations** based on randomized benchmarking (RB) and coherence measurements (+ coherent error on D1)

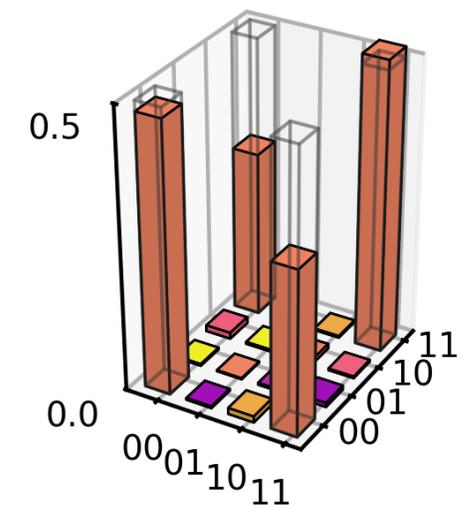


Decoding Logical Operators

- Extract **weights based on correlations** in experimentally acquired syndrome data
Spitz et al., Adv. Quantum Technol. 1 (2018)
Remm et al., arXiv:2502.17722 (2025)
- connectivity of graph changed after lattice-split operation
→ **no strong correlations between repetition codes**
- Matched syndromes in **orange (yellow)** flip Z_{L1} (Z_{L2}) operator
- Decoded and post-selected logical density matrices



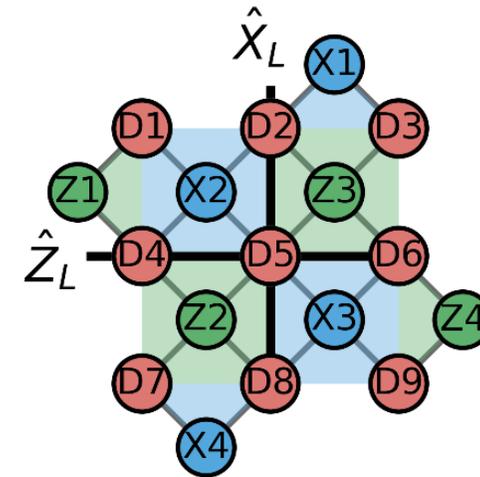
Decoded fidelity 55.3%



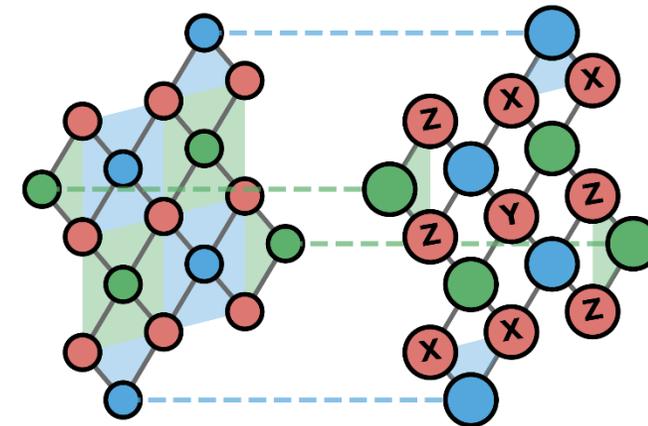
Postselected fidelity 78.8%

Logical State Tomography

- Readout of X_L and Z_L observables of logical surface code qubits can be performed fault-tolerantly
- Final set of stabilizer outcomes determined from data qubit readout
- We also measure \hat{Y}_L to reconstruct the full logical state (density matrix, Pauli sets)
- We read out the corner data qubits in a basis that allows the weight-2 stabilizers to be determined.
- An incomplete subset of stabilizers can't be used to correct errors, but can help identifying some errors



- $\hat{X}_L = \hat{X}_{D2}\hat{X}_{D5}\hat{X}_{D8}$
- $\hat{Z}_L = \hat{Z}_{D4}\hat{Z}_{D5}\hat{Z}_{D6}$
- $\hat{Y}_L = \hat{X}_{D2}\hat{Z}_{D4}\hat{Y}_{D5}\hat{Z}_{D6}\hat{X}_{D8}$



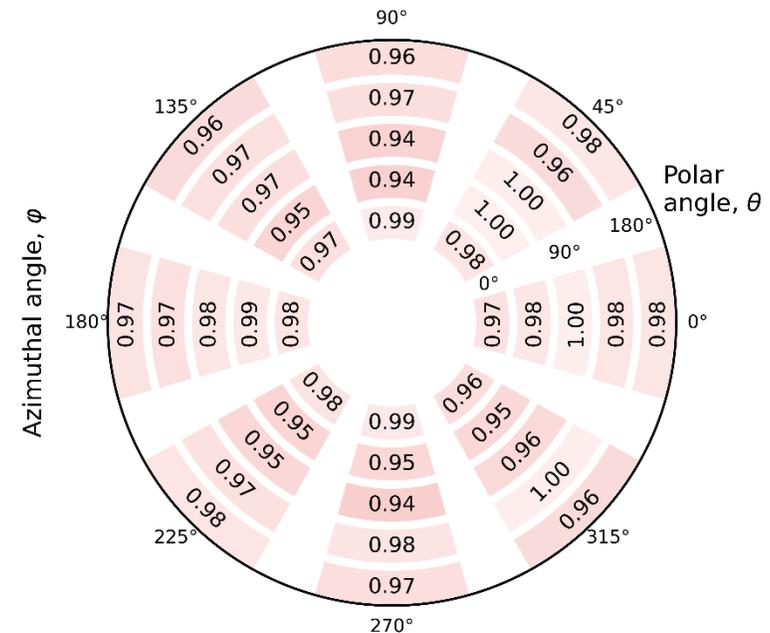
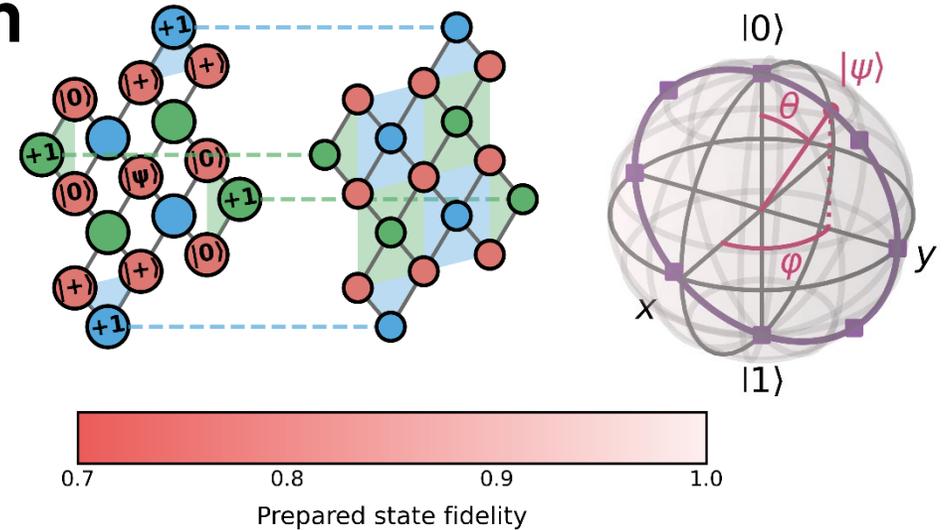
Ye, Y. et al. Phys. Rev. Lett. **131**, 210603 (2023)

L. Postler et al. Nature **605**, 675 (2022)

R. S. Gupta et al. Nature **625**, 259 (2024)

Parametrized Logical State Preparation

- Arbitrary state preparation scheme:
Ye, Y. et al. Phys. Rev. Lett. **131**, 210603 (2023)
 - Central data qubit prepared in target state $|\psi\rangle$
 - Other data qubits prepared such that weight-2 stabilizers are in the +1 eigenstate
- We prepare states $|\psi\rangle = \cos\frac{\theta}{2}|0\rangle + \sin\frac{\theta}{2}e^{i\varphi}|1\rangle$
- After 1 cycle of error correction, we perform tomographic measurements, and determine the fidelity $\mathcal{F} = \langle\psi|\hat{\rho}_{\text{tom}}|\psi\rangle$, average 83.5%
- Postselected** average fidelity: 97.0%



Splitting of Parametrized Logical Qubit States

- Experiment combining arbitrary **logical-state preparation**, **logical-split operation** and **logical tomography**

- Consider initial states $|\psi\rangle$ in yz -plane

- Split operation after Pauli frame update:
 $\alpha|+\rangle_L + \beta|-\rangle_L \rightarrow \alpha|++\rangle_{L1L2} + \beta|--\rangle_{L1L2}$

- Consider non-zero logical two-qubit operators:

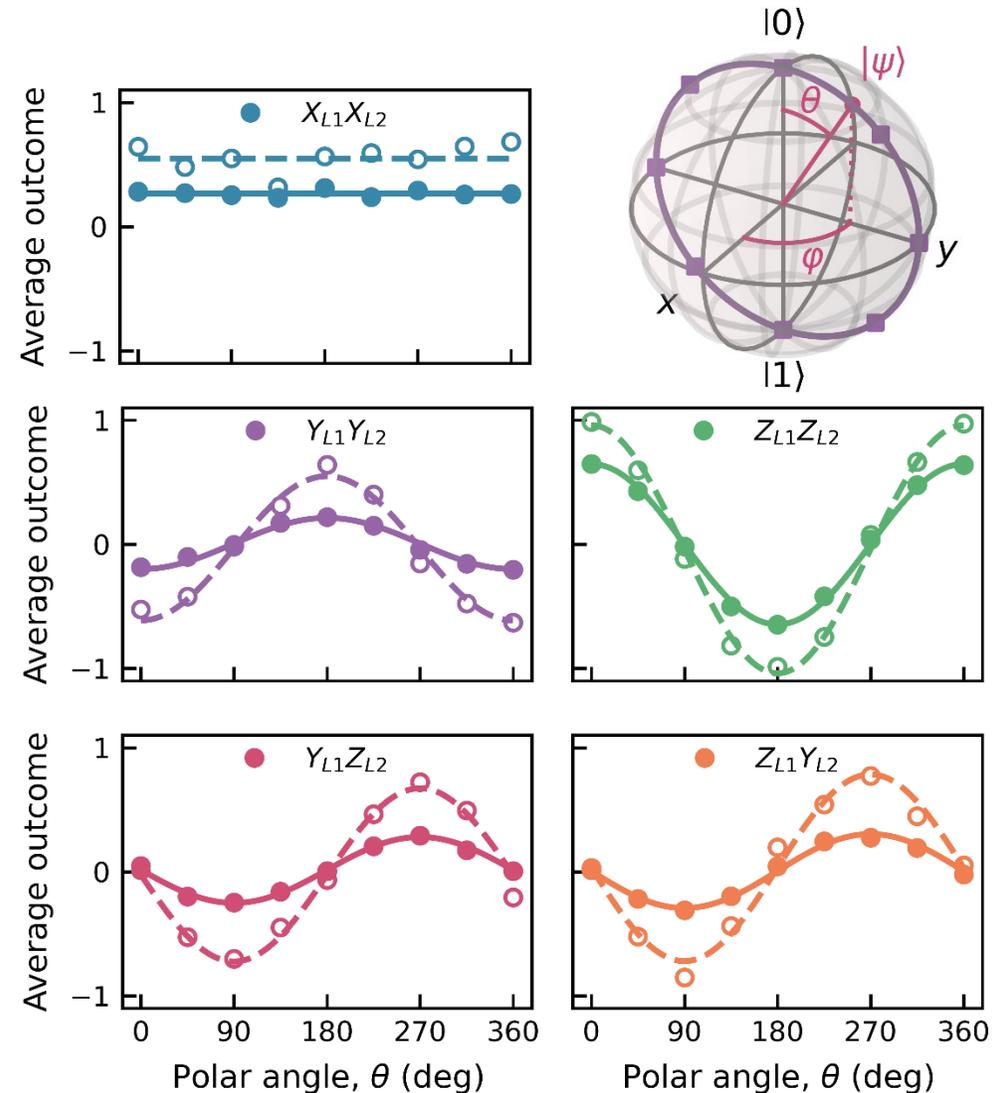
$$\hat{X}_{L1}\hat{X}_{L2} = +1$$

$$\hat{Z}_L \rightarrow \hat{Z}_{L1}\hat{Z}_{L2} = -\hat{Y}_{L1}\hat{Y}_{L2}$$

$$\hat{Y}_L \rightarrow \hat{Z}_{L1}\hat{Y}_{L2} = \hat{Y}_{L1}\hat{Z}_{L2}$$

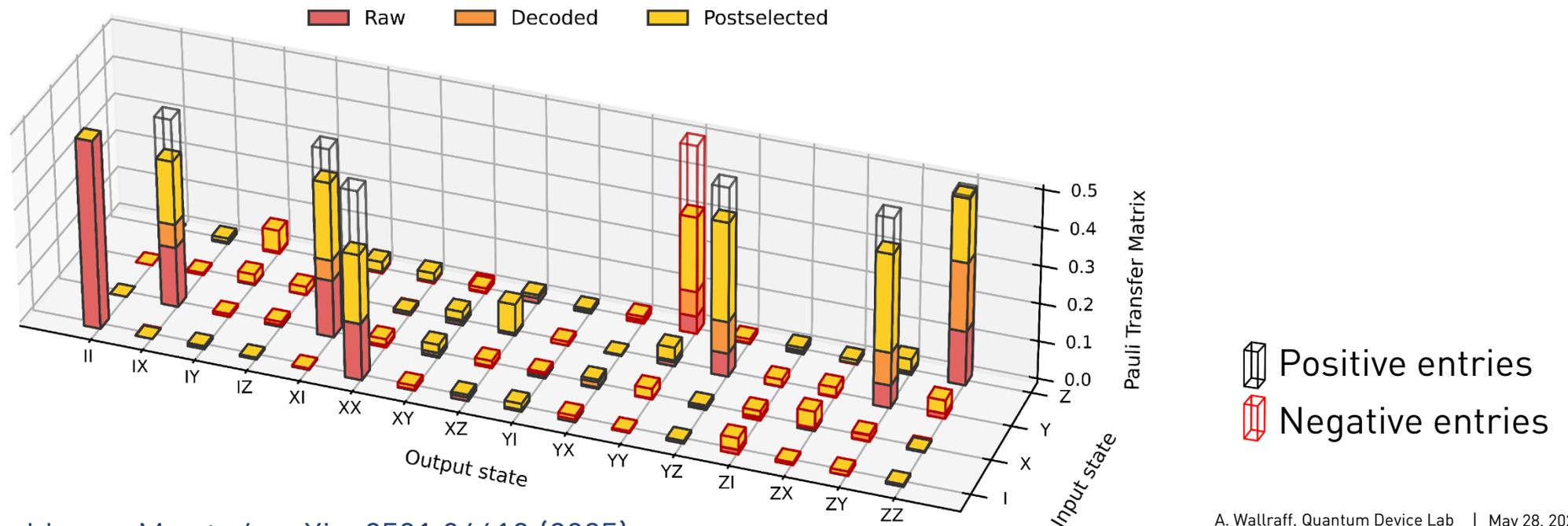
● ● ● ● Error-corrected

○ ○ ○ ○ Post selected on no syndrome events



Logical Quantum Process Tomography

- Split acting on logical input states $|0\rangle_L, |1\rangle_L, |+\rangle_L, |-\rangle_L, |+i\rangle_L, |-i\rangle_L$ states
- Split operation maps Pauli operators to Pauli operators
- Note: single-qubit phase rotation of 0.11π on logical qubit 1 corrected for.
- Pauli transfer matrix (PTM) representation
 - ideal values $\pm 1/2$
- Process fidelity
 - raw: $\mathcal{F} = 0.310(12)$
 - decoded: $\mathcal{F} = 0.442(12)$
 - post-selected: $\mathcal{F} = 0.80(3)$

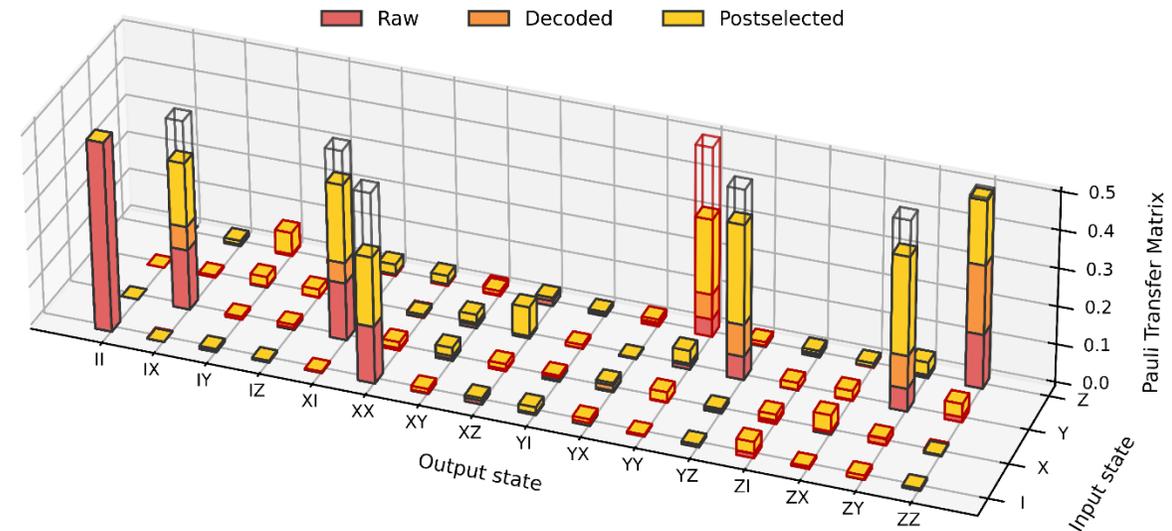
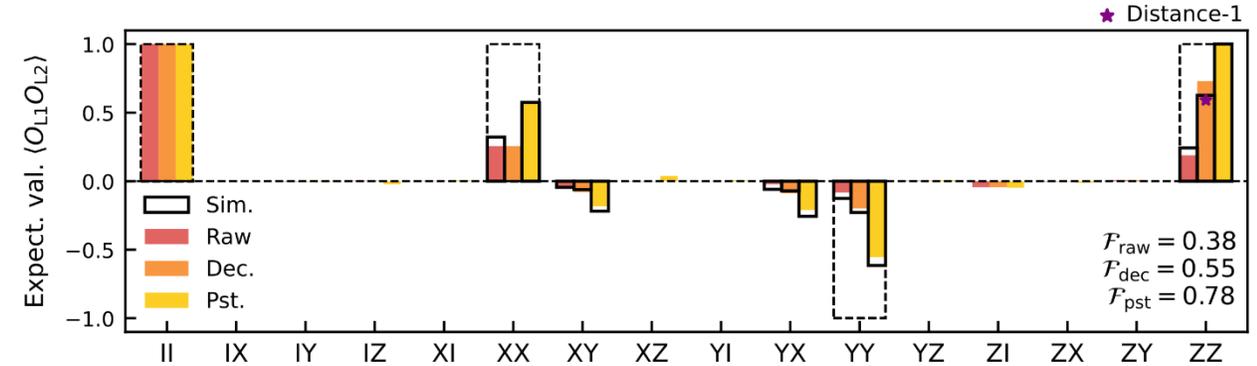


Summary and Outlook

- Demonstrated **lattice surgery** on a distance-three surface code, **creating a logical Bell state** of two distance-three repetition codes
- **Increased decoded observable expectation value** compared to non-encoded variant
- Measured **logical Pauli-transfer matrix** for lattice split operation

Outlook

- Deploy full scheme on two distance-three surface codes and integrate in **logical state teleportation protocol**



The Quantum Device Lab



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