

# Clusters of Primordial Black Holes

Dawn GW Cosmology, Benasque, 9<sup>th</sup> May 25

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IFT-UAM/CSIC

# Outline

- Fundamental Physics and PBH:
  - Critical Higgs Inflation
  - Quantum Diffusion and PNG tails
- PBH cluster dynamics:
  - Binary parameter distributions
  - Spin induction in dense clusters
- Observational Evidences:
  - Gravitational Waves (GWTC-3)

## Density perturbations and black hole formation in hybrid inflation

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The resulting density inhomogeneities lead to a copious production of black holes.

quantum fluctuations at the time corresponding to the phase transition between the two inflationary stages can

for certain values of parameters these black holes may constitute the dark matter in the Universe.

these models can be made extremely small, but in general it could be sufficiently large to have important cosmological and astrophysical implications. In particular, for certain values of parameters these black holes may constitute the dark matter in the Universe. It is also possible to have hybrid models with two stages of inflation where the black hole production is not suppressed, but where the typical masses of the black holes are very small. Such models lead to a completely different thermal history of the Universe, where postinflationary reheating occurs via black hole evaporation. [S0556-2821(96)00522-X]

PACS number(s): 98.80.Cq

## Steven Weinberg

*“our problem is not that we  
take our theories too seriously,  
but that we  
don't take them seriously enough”*

## Massive primordial black holes from hybrid inflation as dark matter and the seeds of galaxies

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(Received 9 March 2015; published 16 July 2015)

In this paper we present a new scenario where massive primordial black holes (PBHs) are produced from the collapse of large curvature perturbations generated during a mild-waterfall phase of hybrid inflation. We determine the values of the inflaton potential parameters leading to a PBH mass spectrum peaking on planetarylike masses at matter-radiation equality and producing abundances comparable to those of dark matter today, while the matter power spectrum on scales probed by cosmic microwave background (CMB) anisotropies agrees with Planck data. These PBHs could have acquired large stellar masses today, via merging, and the model passes both the constraints from CMB distortions and microlensing. This scenario is supported by Chandra observations of numerous BH candidates in the central region of Andromeda. Moreover, the tail of the PBH mass distribution could be responsible for the seeds of supermassive black holes at the center of galaxies, as well as for ultraluminous x-ray sources. We find that our effective hybrid

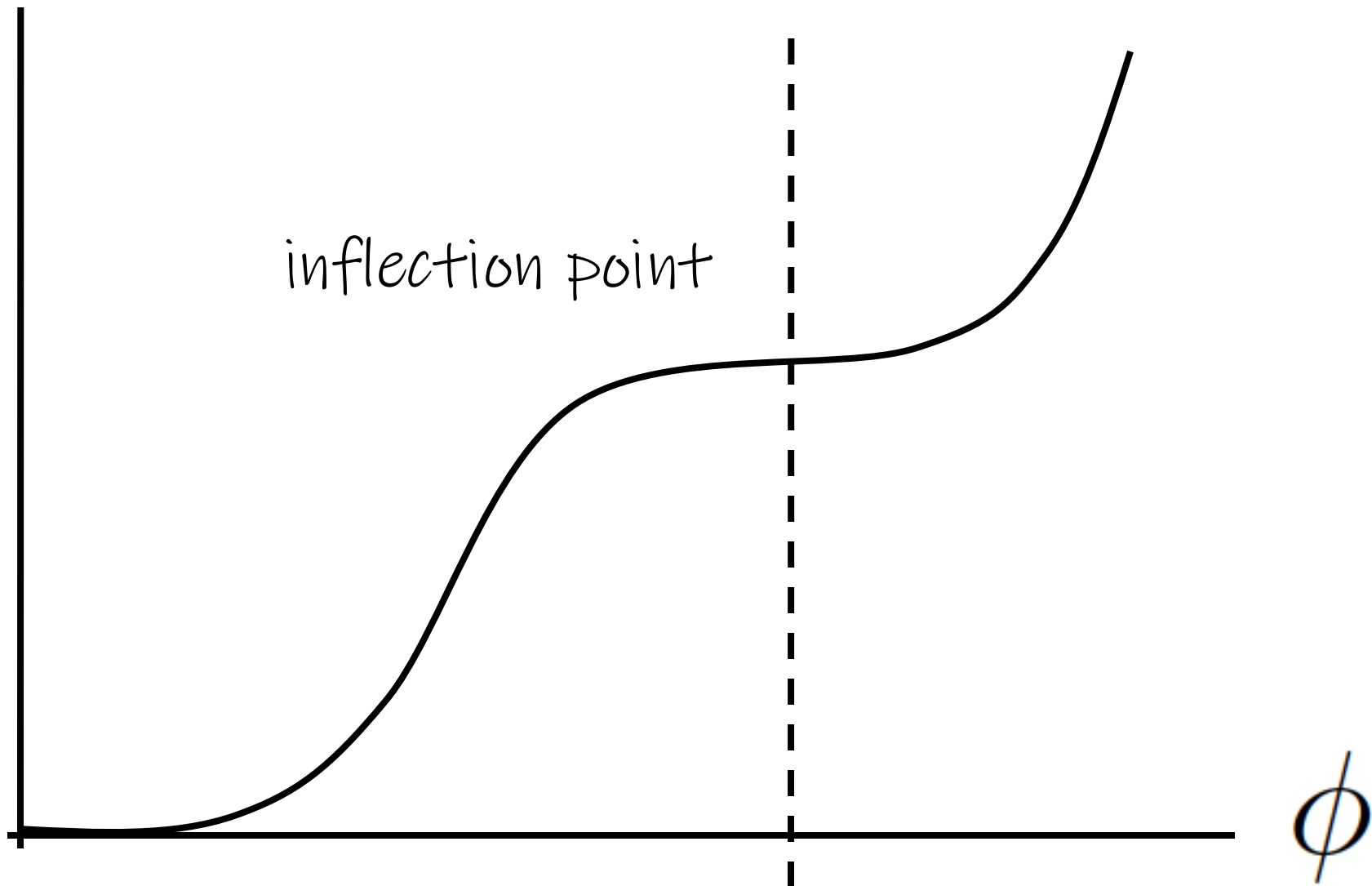
These PBHs could have acquired large stellar masses today, via merging, the model passes both the constraints from CMB distortions and microlensing. the tail of the PBH mass distribution could be responsible for the seeds of supermassive black holes at the center of galaxies, as well as for ultraluminous x-ray sources.

Moreover, PBH binaries should emit gravitational waves that could be detected by future gravitational wave experiments such as LIGO, DECIGO and eLISA [70,71].

Binaries of PBHs forming a fraction of dark matter should emit gravitational waves; this results in a background of gravitational waves that could be observed by LIGO, DECIGO and eLISA [70–72].

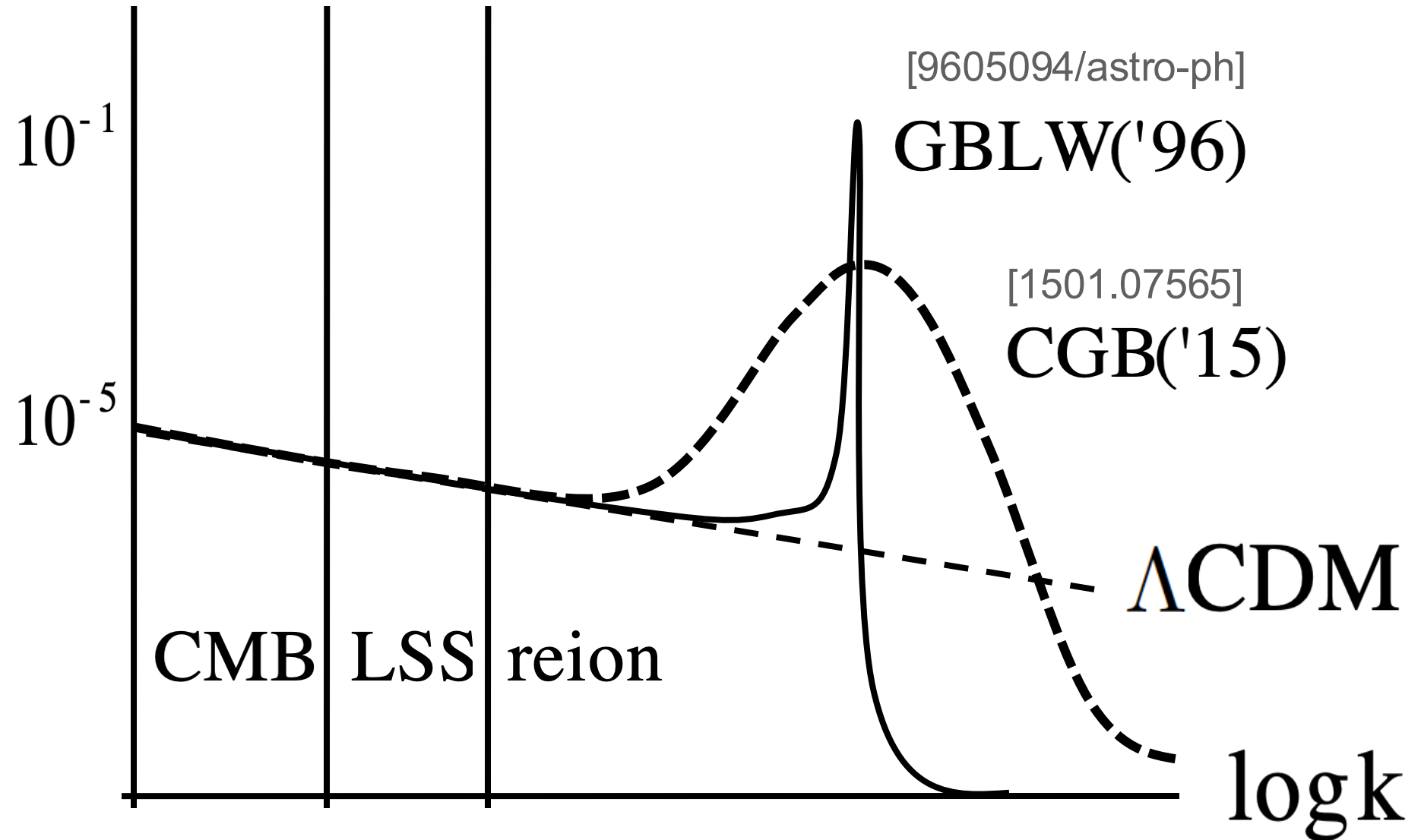
$V(\phi)$

Potential



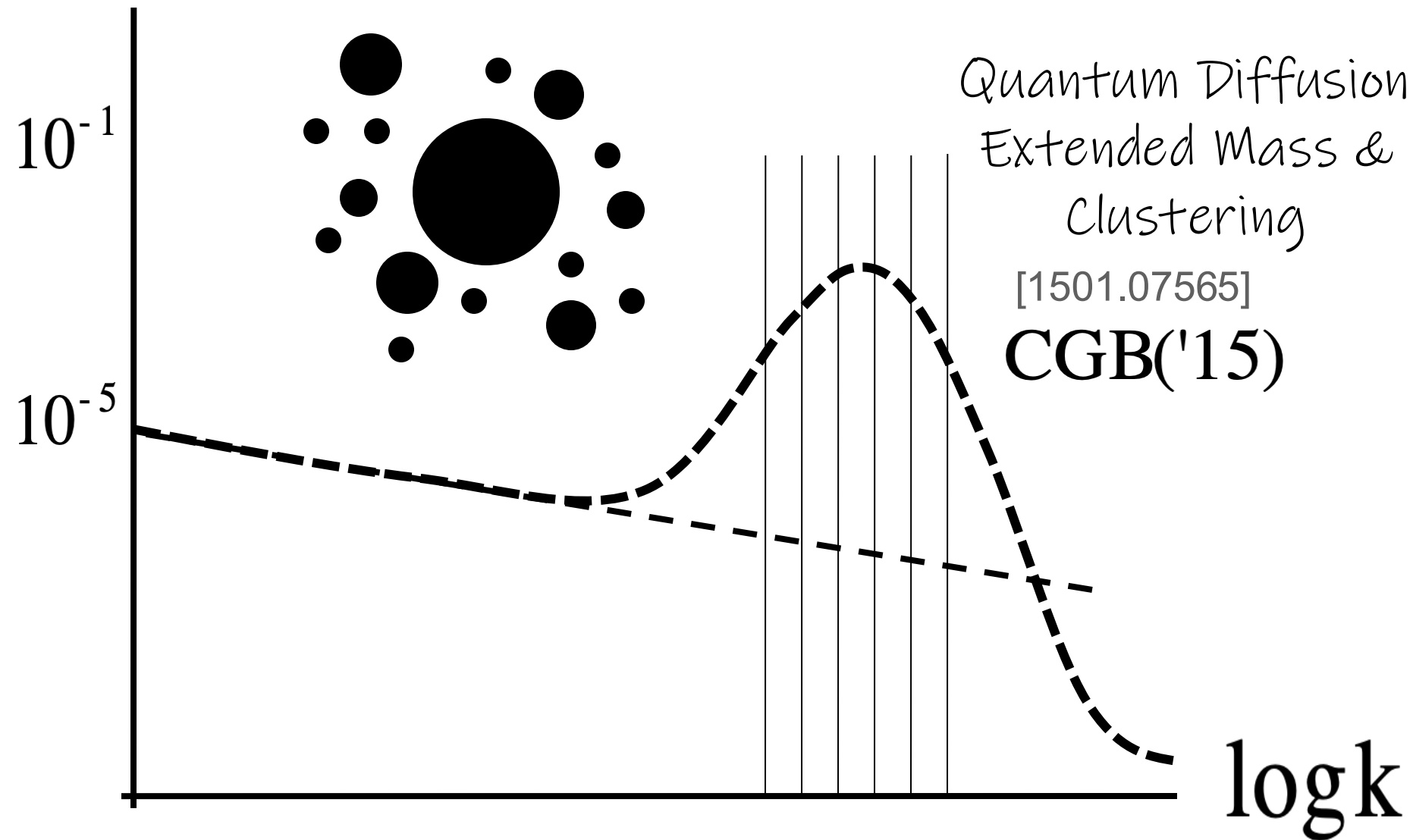
$\log P(k)$

Power spectrum



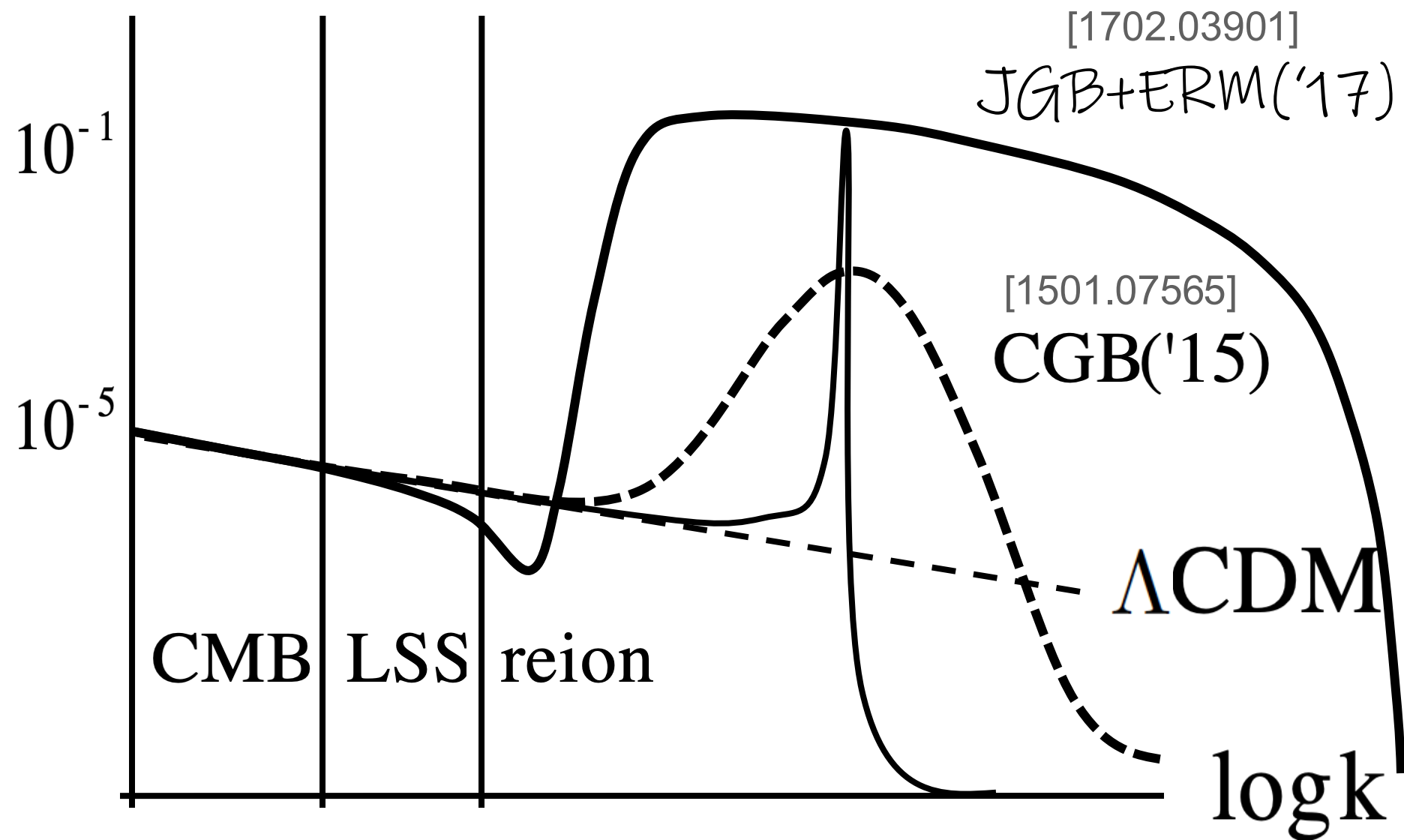
$\log P(k)$

Power spectrum

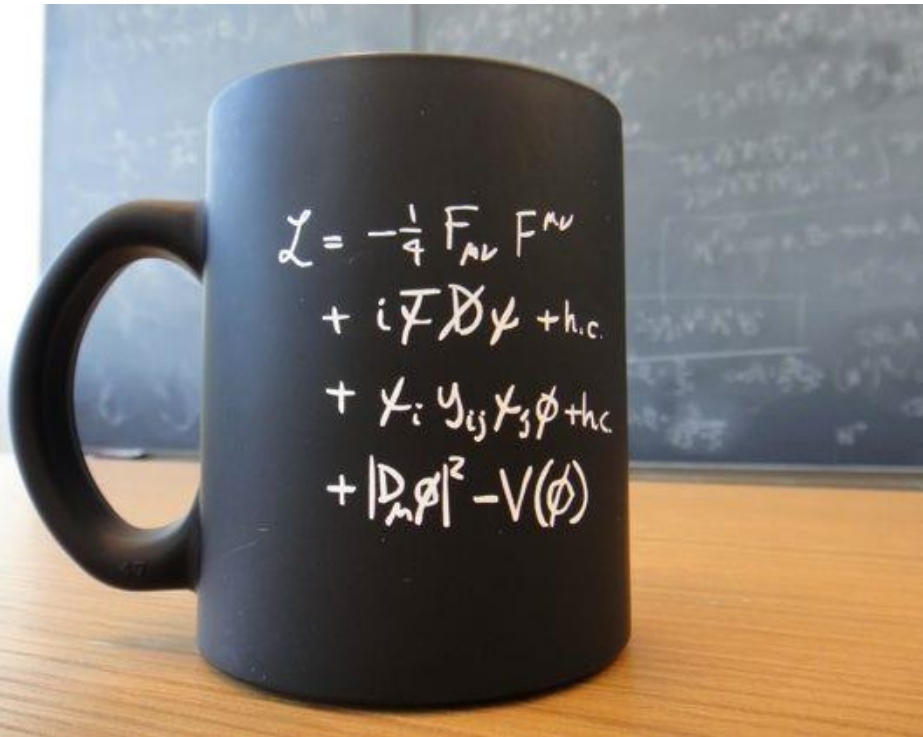


$\log P(k)$

# Single Field Inflation



# Standard Model Lagrangian

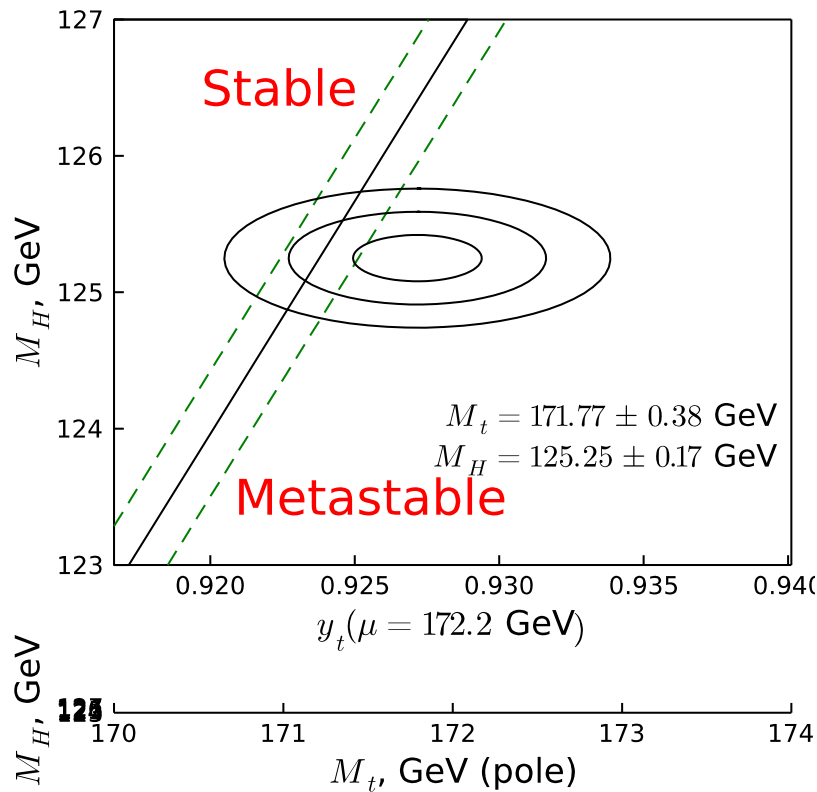


$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \not{D} \psi + \text{h.c.} \\ & + \bar{\chi}_i y_{ij} \chi_j \phi + \text{h.c.} \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$

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$$R = 12H^2 + 6\dot{H} \rightarrow R_0 = 9.2 H_0^2 \rightarrow m_H = \sqrt{\xi R_0} = 2 \times 10^{-32} \text{ eV}$$

# EW vacuum metastability



$$m_t^{\text{pole}} = 170.5 \pm 0.8 \text{ GeV}$$

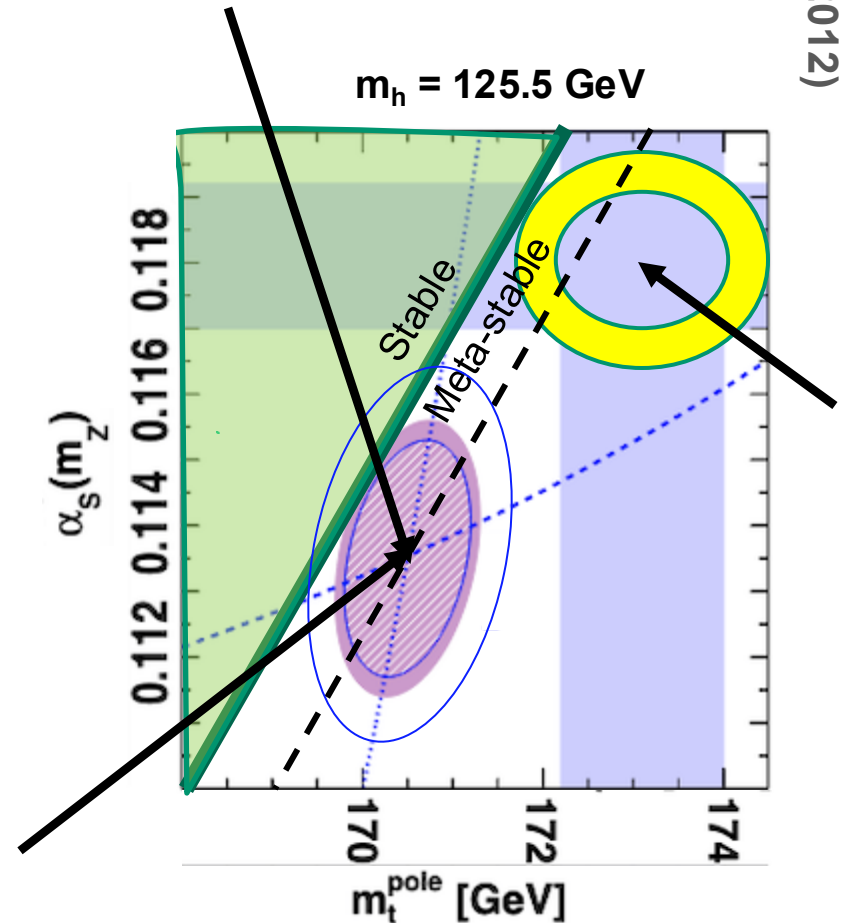
$$\alpha_S(m_Z) = 0.1135^{+0.0021}_{-0.0017}$$

LHC-CMS Collab. (2020)

<https://arxiv.org/abs/1904.05237>

Buttazzo et al. (2012)

<https://arxiv.org/pdf/1112.3022.pdf>



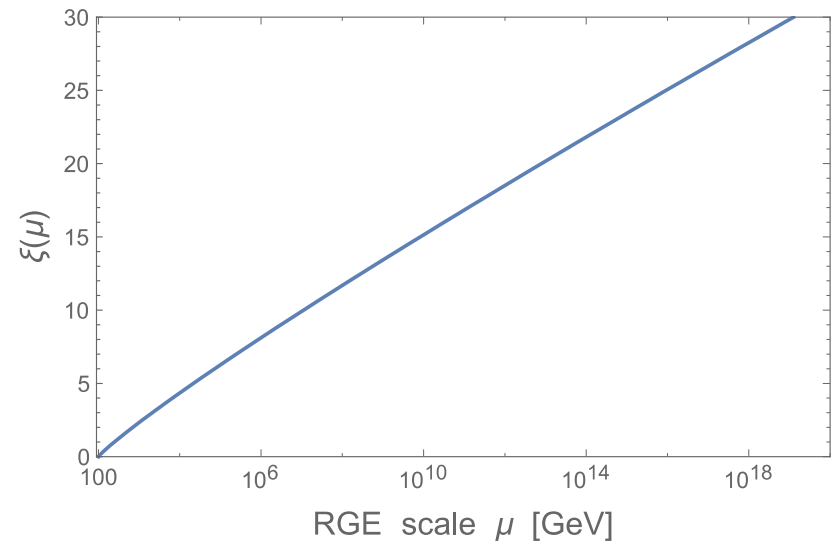
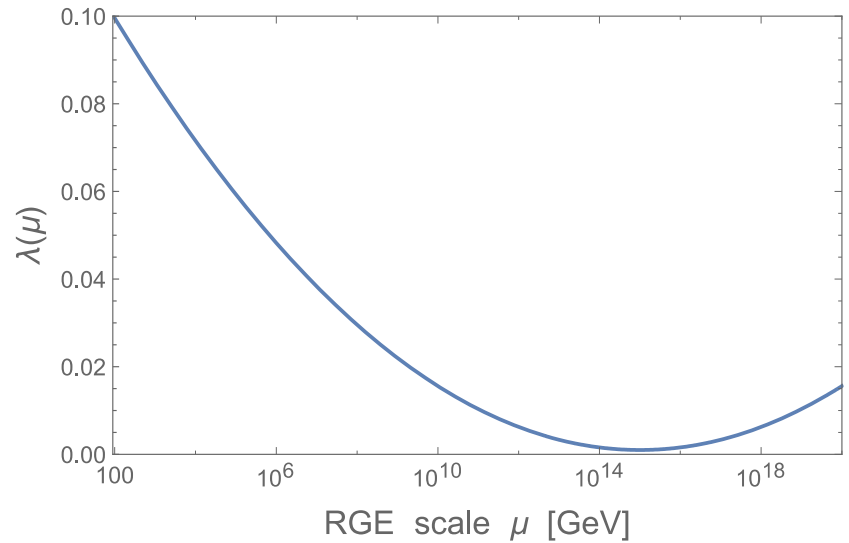
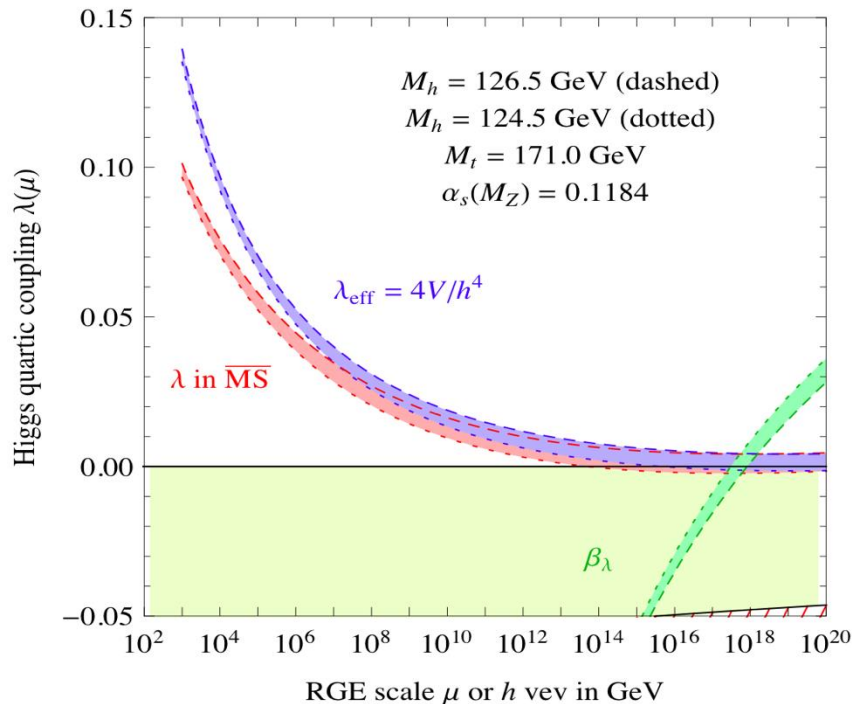
# Renormalization of Higgs couplings

Ezquiaga, JGB, Ruiz [1705.04861]

$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu) ,$$

$$\xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu) ,$$

Buttazzo et al (2014)



# Critical Higgs Inflation

Ezquiaga, JGB, Ruiz Morales [1705.04861]

$$S = \int d^4x \sqrt{g} \left[ \left( \frac{1}{2\kappa^2} + \frac{\xi(\phi)}{2} \phi^2 \right) R - \frac{1}{2} (\partial\phi)^2 - \frac{1}{4} \lambda(\phi) \phi^4 \right]$$

$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu) ,$$

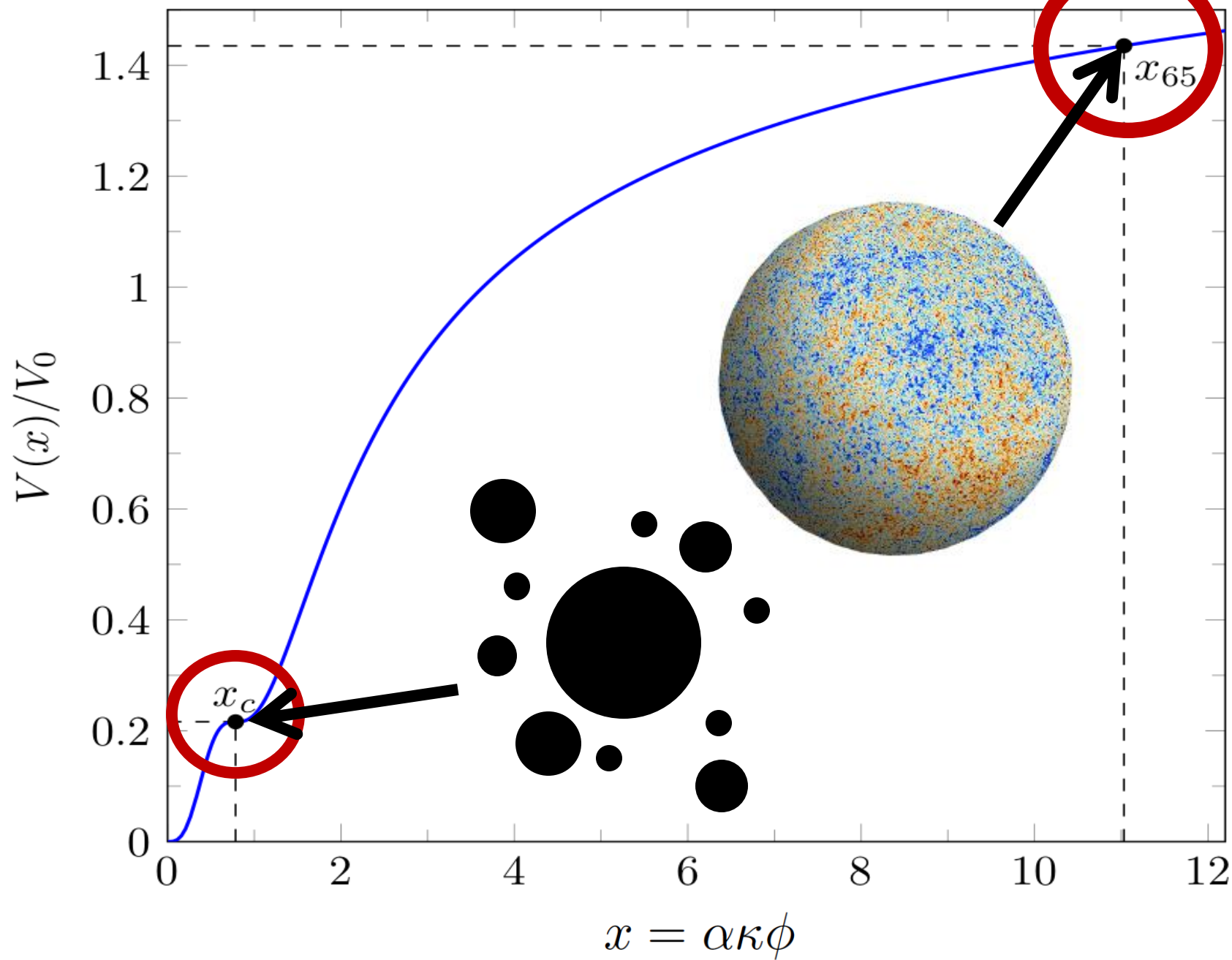
$$g_{\mu\nu} \rightarrow h_{\mu\nu} = (1 + \xi\phi^2) g_{\mu\nu}$$

$$\xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu) ,$$

$$\frac{d\varphi}{d\phi} = \frac{\sqrt{1 + \xi(\phi) \phi^2 + 6 \phi^2 (\xi(\phi) + \phi \xi'(\phi)/2)^2}}{1 + \xi(\phi) \phi^2}$$

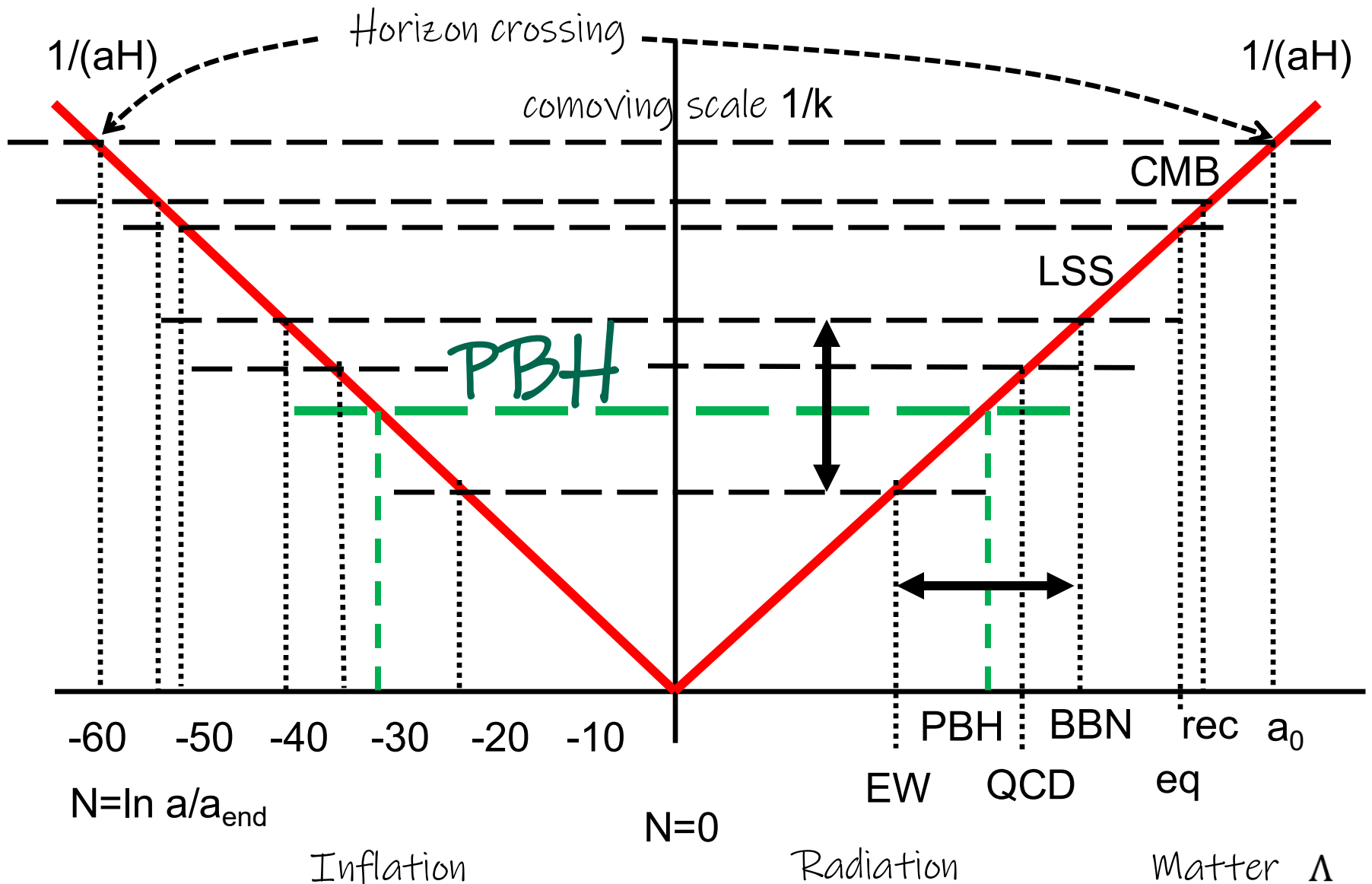
$$V(x) = \frac{V_0 (1 + a \ln^2 x) x^4}{(1 + c (1 + b \ln x) x^2)^2} \quad x = \phi/\mu$$

$$V_0 = \lambda_0 \mu^4 / 4, \quad a = b_\lambda / \lambda_0, \quad b = b_\xi / \xi_0 \quad \text{and} \quad c = \xi_0 \kappa^2 \mu^2$$



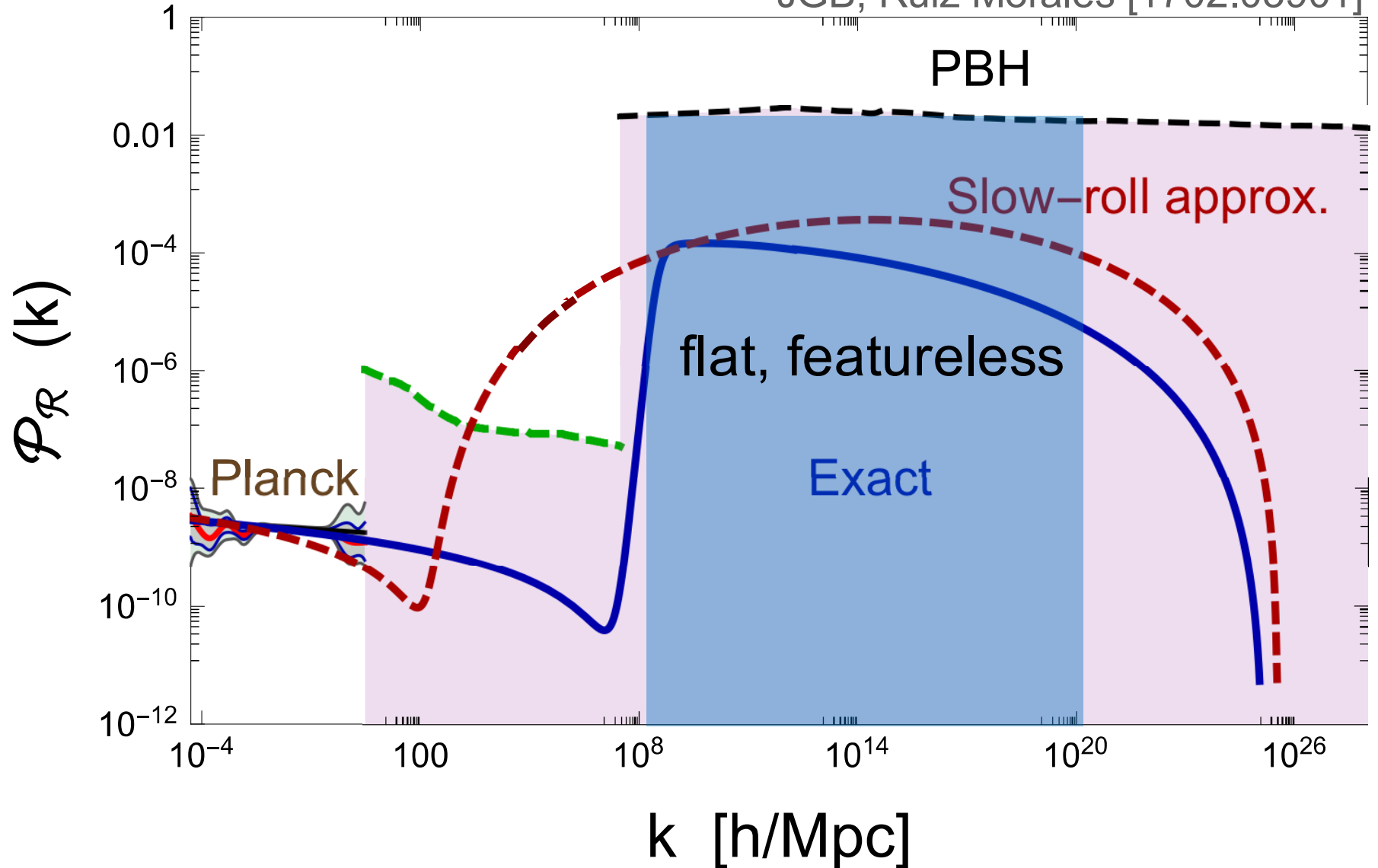
# Inflation

JGB [1702.08275]



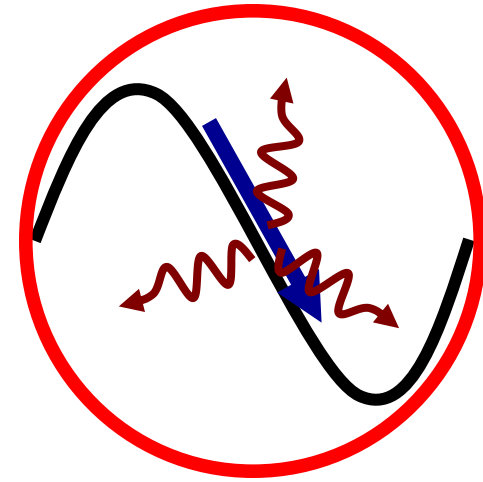
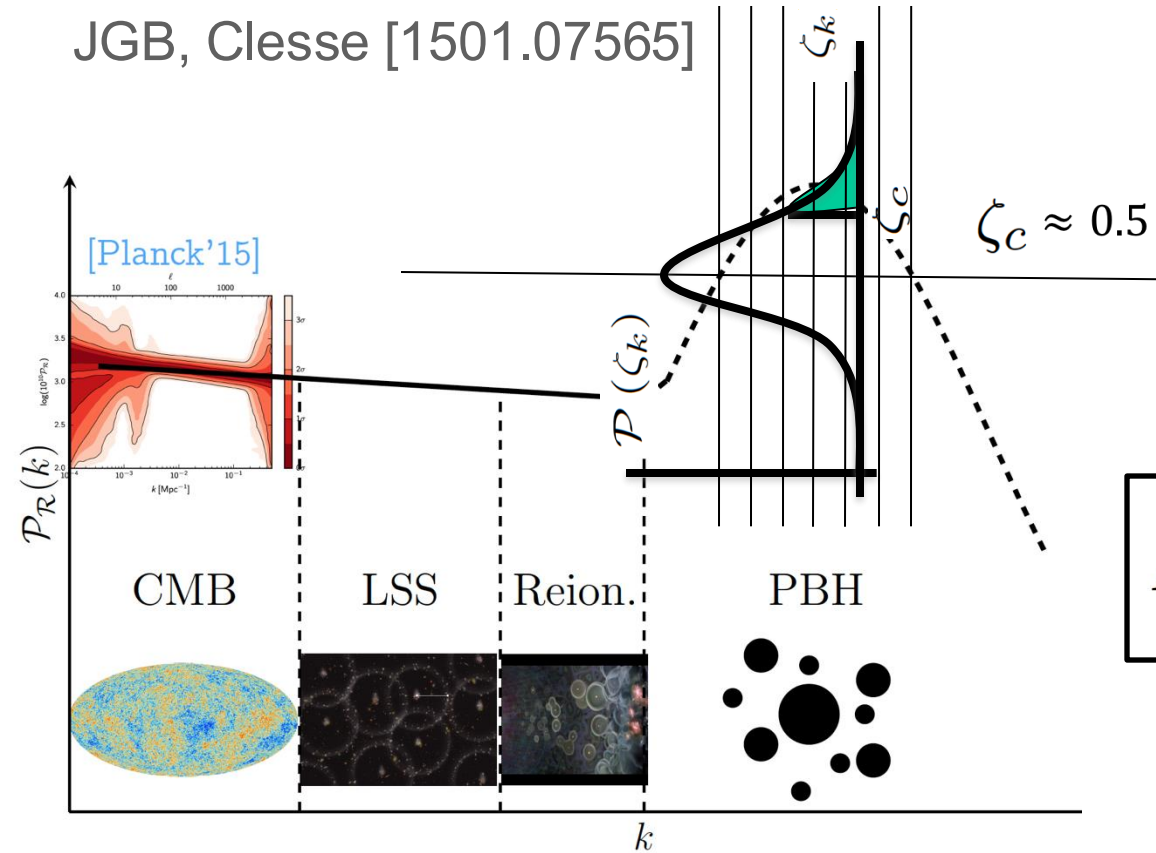
# Primordial Power Spectrum

JGB, Ruiz Morales [1702.03901]



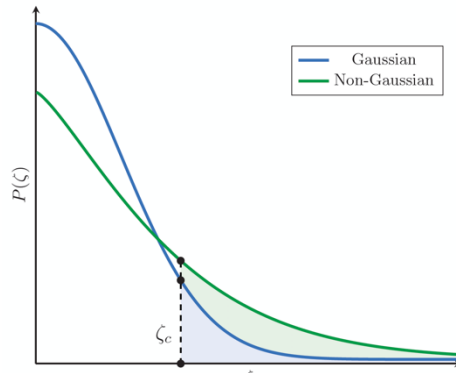
# Extended Mass Function of PBH

JGB, Clesse [1501.07565]



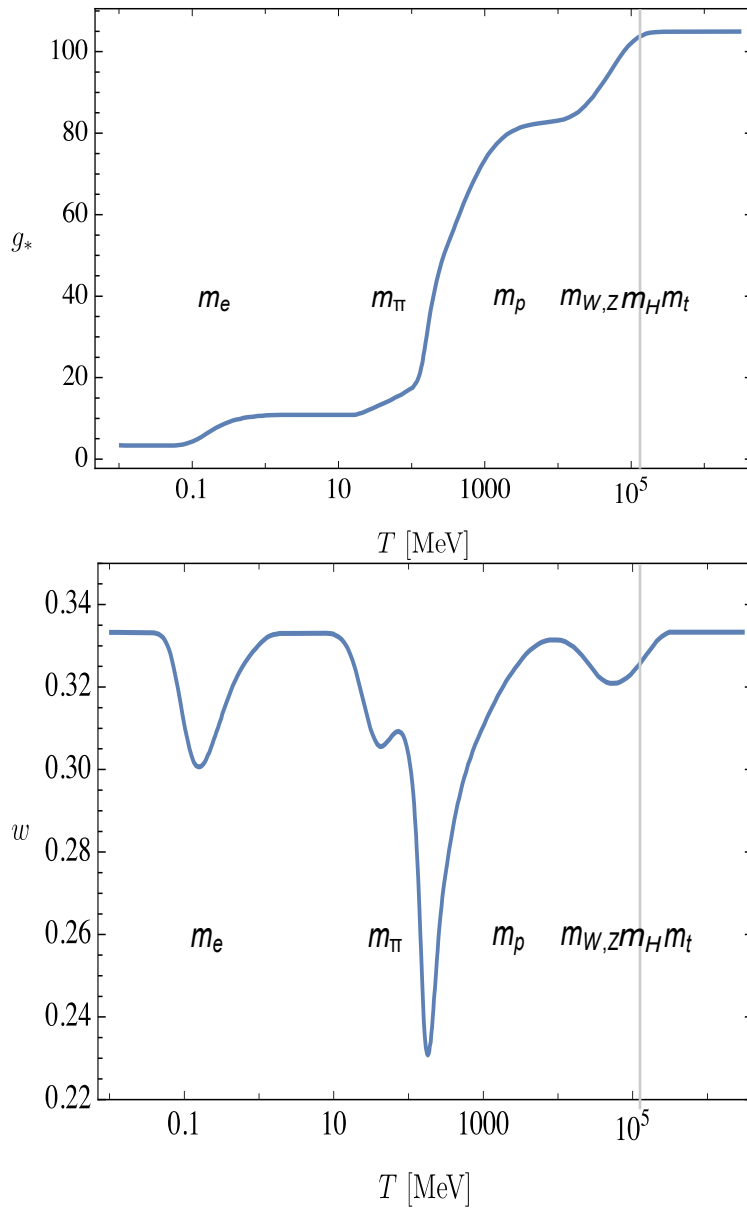
$$M_{\text{PBH}} \simeq 30 M_{\odot} e^{2(N-36)}$$

$$\beta^{\text{form}}(M_k) = \int_{\zeta_c}^{\infty} \mathcal{P}(\zeta_k) d\zeta_k$$



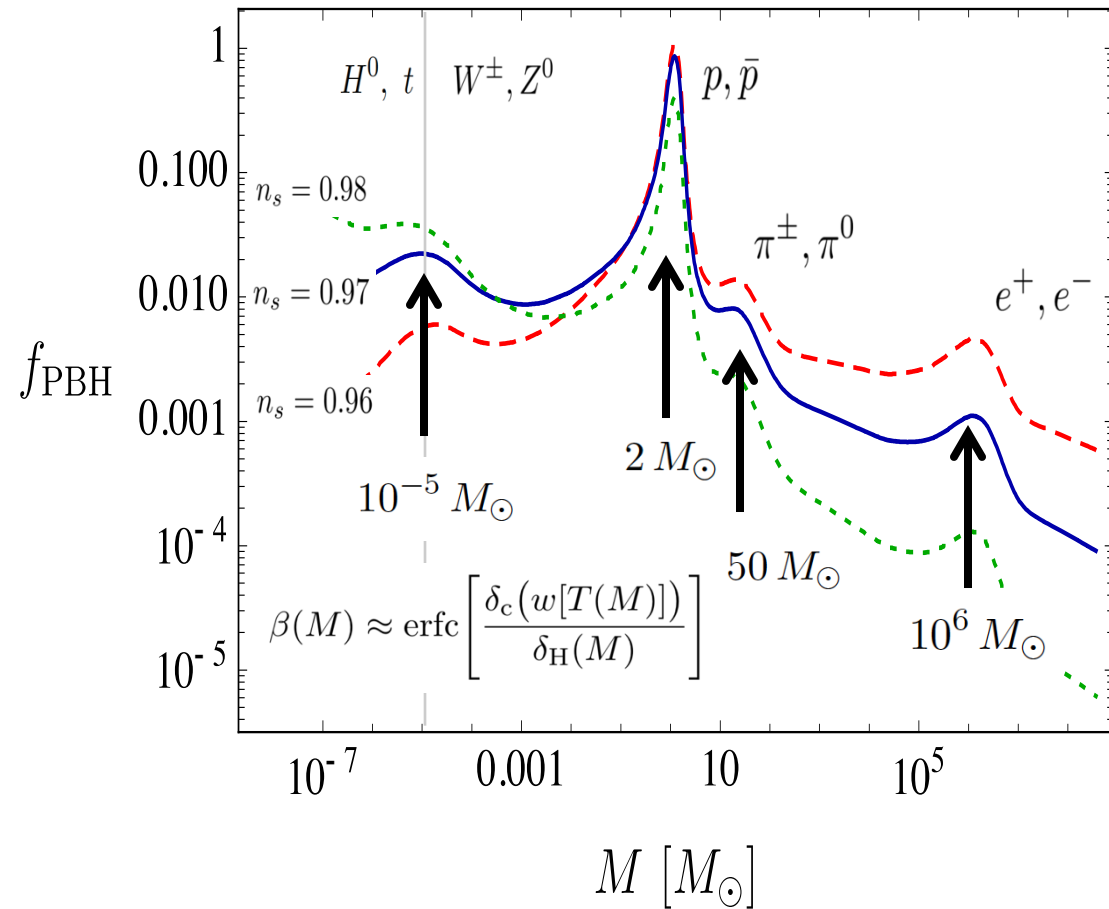
$$\beta(N) = \begin{cases} \text{Erfc} \left( \frac{\zeta_c}{\sqrt{2P_{\zeta}(N)}} \right), & \text{Gaussian statistics,} \\ \text{Erfc} \left( \sqrt{\frac{1}{2} + \frac{\zeta_c}{\sqrt{2P_{\zeta}(N)}}} \right), & \chi^2 \text{ statistics} \end{cases}$$

# Thermal history of the universe

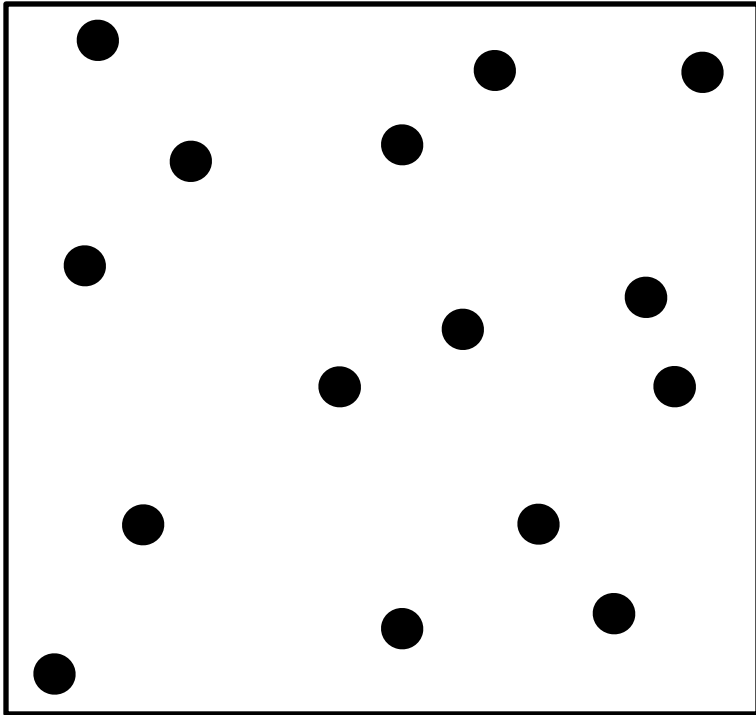


Carr, Clesse, JGB, Kühnel [1906.08217]

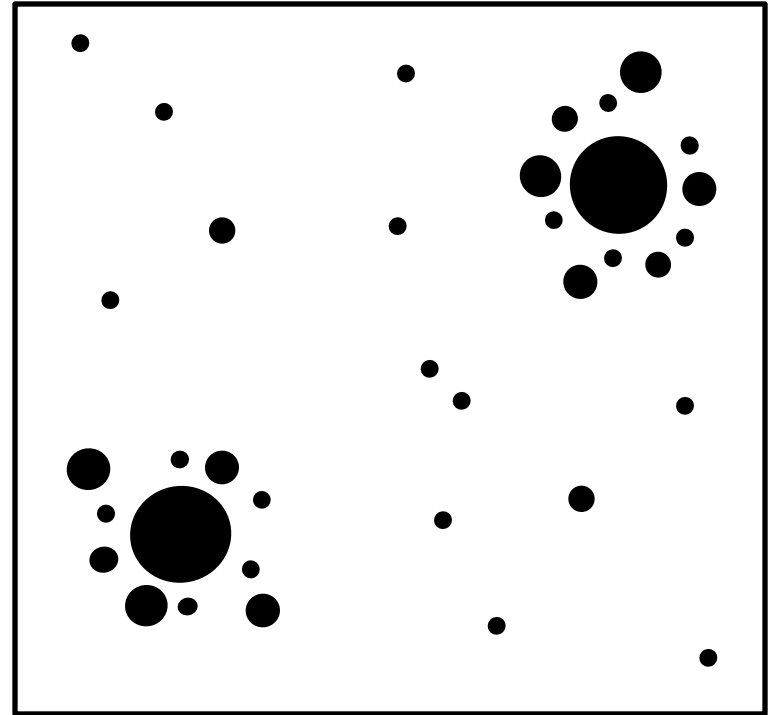
## PBH mass spectrum



# What about clusters of PBH?



- Monochromatic ( $m$ )
- Uniformly distributed
- Gaussian statistics



- Broad range of masses
- PBH in dense clusters
- Non-Gaussian tails

# Stochastic $\delta N$ - formalism

## Coarse-grained curvature perturbation

$$ds^2 = -dt^2 + a^2(t)e^{2\zeta(t,\mathbf{x})}\delta_{ij}dx^i dx^j \quad \zeta_{\text{cg}}(\mathbf{x}) = \delta N_{\text{cg}}(\mathbf{x}) = \mathcal{N}(\mathbf{x}) - \langle \mathcal{N} \rangle$$

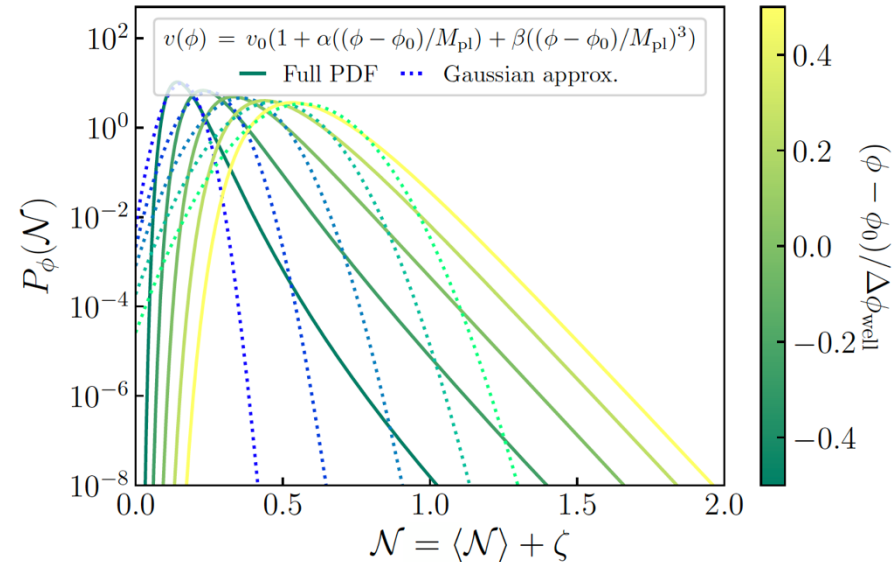
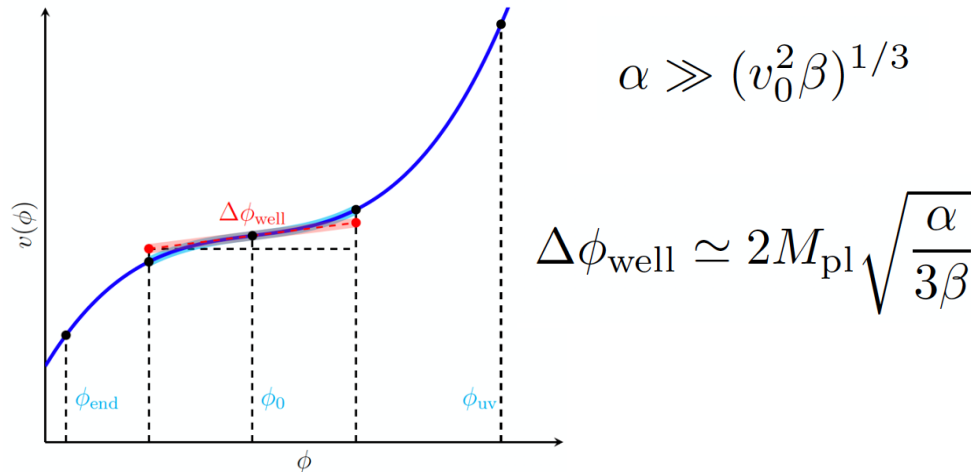
$$\frac{1}{M_{\text{pl}}^2} \frac{d}{d\mathcal{N}} P_{\Phi}(\mathcal{N}) = \left( - \sum_i \frac{v_{\phi_i}}{v} \frac{\partial}{\partial \phi_i} + v \sum_i \frac{\partial^2}{\partial \phi_i^2} \right) \cdot P_{\Phi}(\mathcal{N}) \quad \text{Fokker-Planck Diffusion Eq.}$$

## Determined by the poles of the characteristic function

$$P_{\phi}(\mathcal{N}) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-it\mathcal{N}} \chi_{\mathcal{N}}(t, \phi) dt = \sum_n a_n(\phi) e^{-\Lambda_n \mathcal{N}}$$

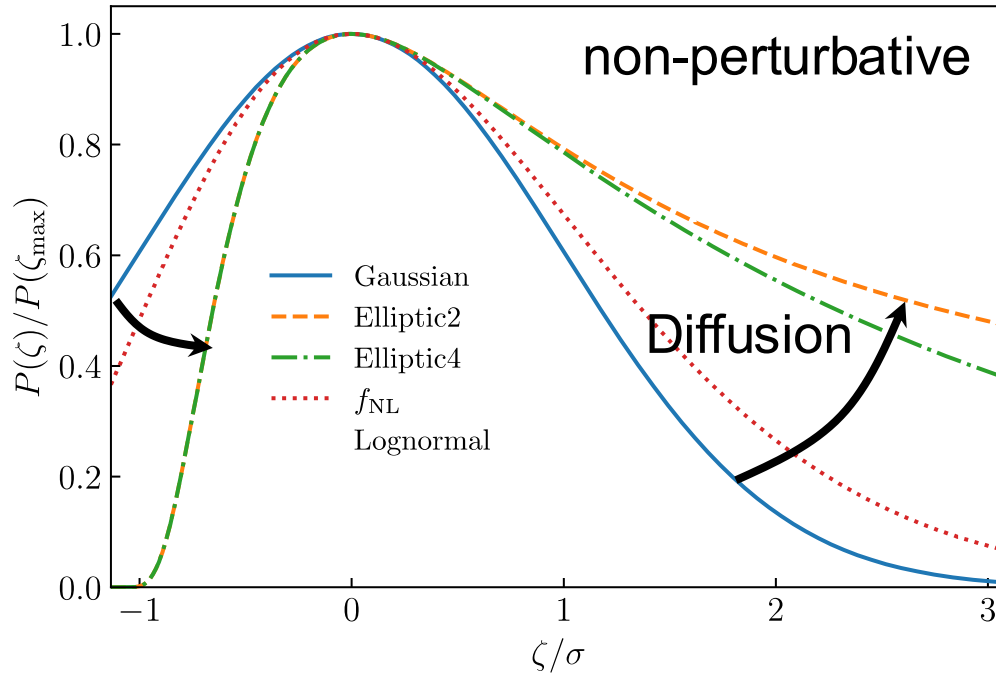
$$\chi_{\mathcal{N}}(t, \phi) = \sum_n \frac{a_n(\phi)}{\Lambda_n - it} + \text{regular func.}$$

Ezquiaga, JGB, Vennin [1912.05399]



# Quantum Diffusion $\leadsto$ CMB & LSS

Ezquiaga, JGB, Vennin [2207.06317]



Elliptic Functions

$$P_2(\zeta_k) = -\frac{\pi}{2\mu^2} \vartheta'_2 \left( \frac{\pi\alpha_k}{2}, e^{-\frac{\pi^2}{\mu^2} \mathcal{N}_k} \right)$$

$$P_4(\zeta_k) = \frac{\pi}{2\mu^2\alpha_k} \vartheta'_4 \left( \frac{\pi\alpha_k}{2}, e^{-\frac{\pi^2}{\mu^2} \mathcal{N}_k} \right)$$

$f_{\text{NL}}$  – expansion (not enough)

$$\zeta(x) = \zeta_{\text{G}}(x) + \frac{3}{5} f_{\text{NL}} \left[ \zeta_{\text{G}}^2(x) - \sigma_{\text{G}}^2(x) \right]$$

Lognormal distributions

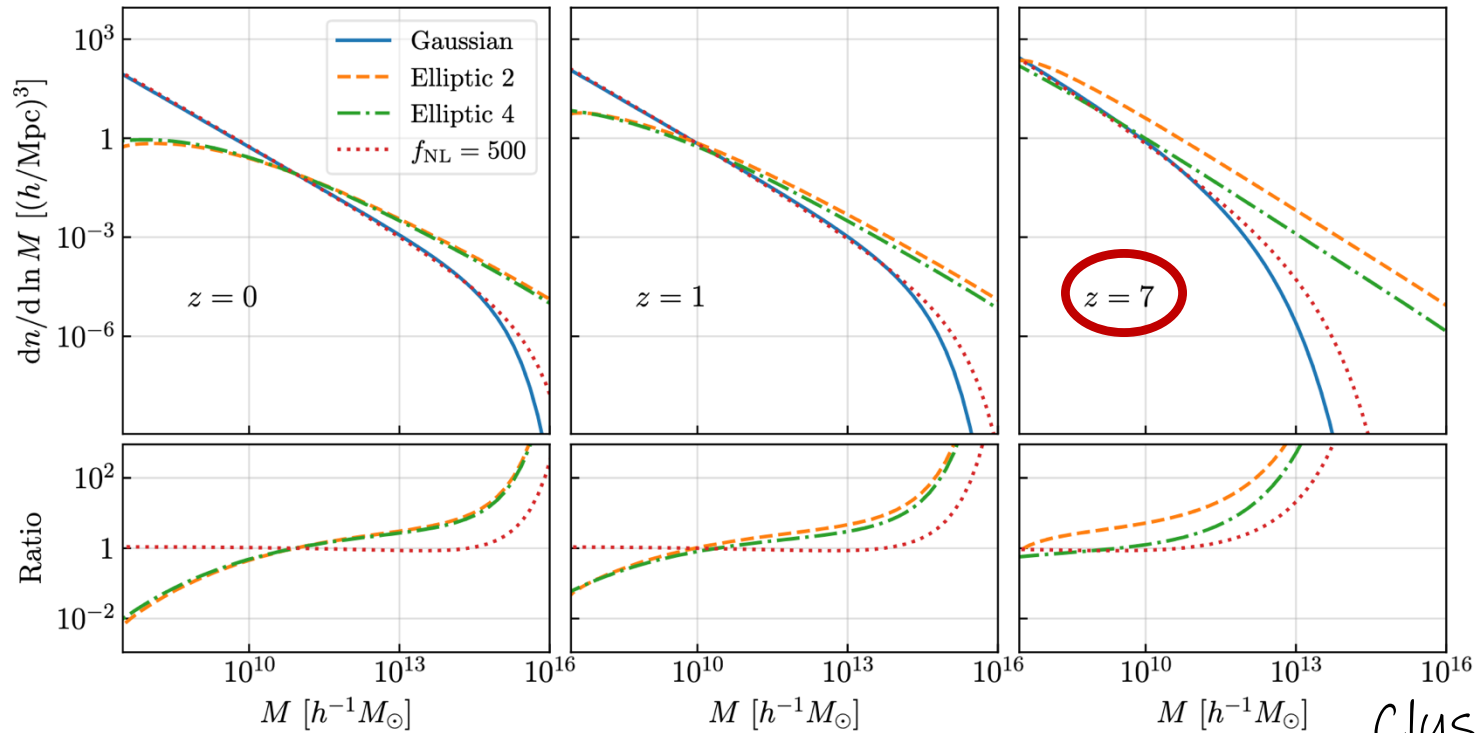
$$\text{LN}(x, \rho, \sigma) = \frac{1}{\rho \sigma \sqrt{2\pi}} \exp \left[ -\frac{\ln(x/\rho)^2}{2\sigma^2} - \frac{\sigma^2}{2} \right]$$

$$\text{G}(x, \rho, \sigma_{\text{G}}) = \frac{1}{\sigma_{\text{G}} \sqrt{2\pi}} \exp \left[ -\frac{(x - \rho)^2}{2\sigma_{\text{G}}^2} \right]$$

$$P_{\text{NL}}(\zeta) = \frac{1}{\sqrt{2\pi\sigma_{\text{G}}^2\Delta}} \left[ e^{-\frac{25(\sqrt{\Delta}-1)^2}{72f_{\text{NL}}^2\sigma_{\text{G}}^2}} + e^{-\frac{25(\sqrt{\Delta}+1)^2}{72f_{\text{NL}}^2\sigma_{\text{G}}^2}} \right]$$

where  $\Delta(\zeta) = 1 + \frac{12}{5} f_{\text{NL}} \zeta + \frac{36}{25} f_{\text{NL}}^2 \sigma_{\text{G}}^2$ .

# Quantum Diffusion $\leadsto$ CMB & LSS



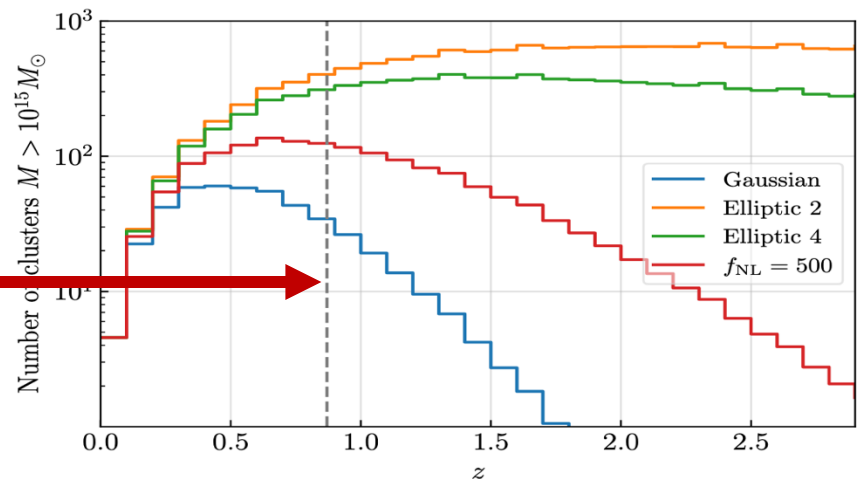
Halo  
Mass  
Function

Cluster Abundance

Ezquiaga, JGB, Vennin [2207.06317]

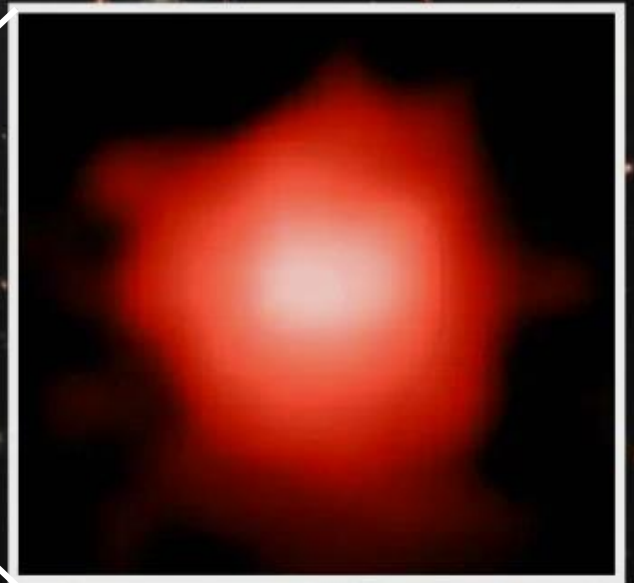
El Gordo

$$M \sim 3 \cdot 10^{15} M_{\odot} \text{ at } z = 0.87$$



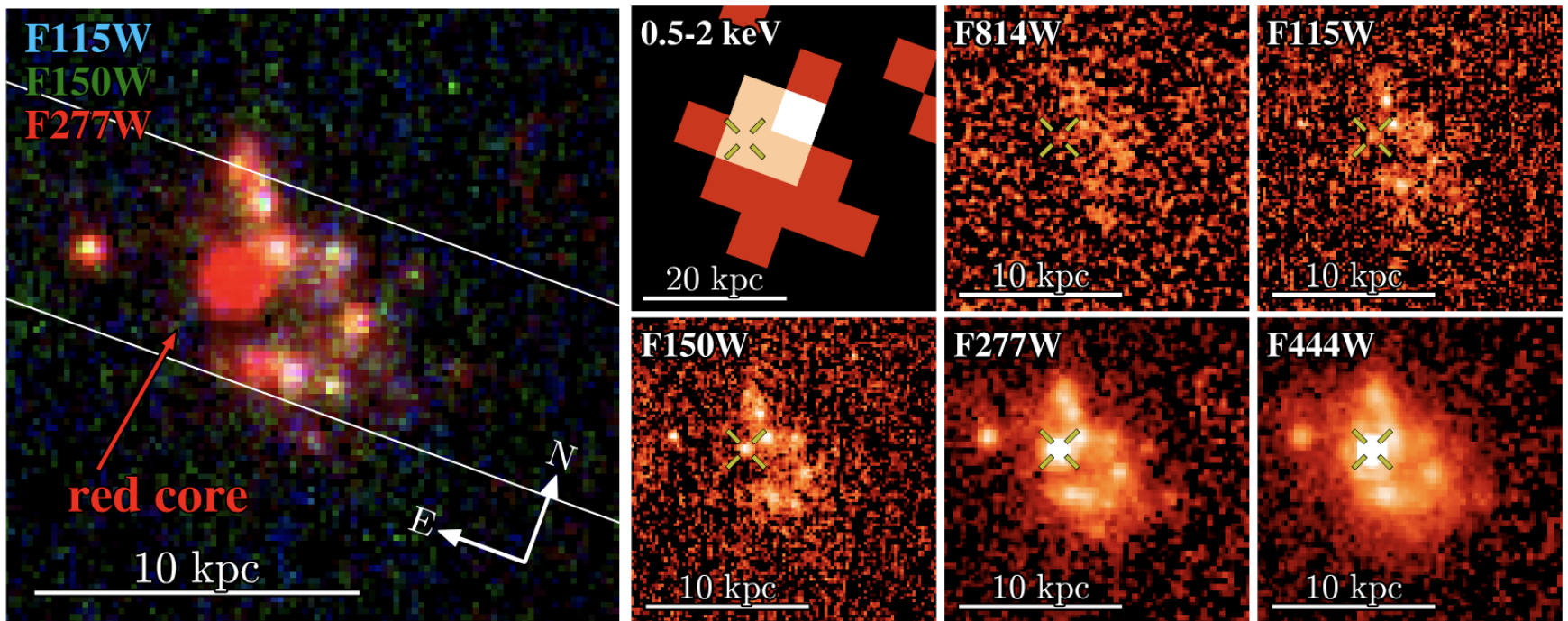
PBH could explain the SMBH in the  
center of galaxies seen by JWST at  
 $z \sim 13-16$

JGB, Clesse [1501.07565]  
Ezquiaga, JGB, Vennin [2207.06317]



# PBH clusters explain the cumplly Nature of "Little Red Dots"

Tanaka et al. [2410.00104]

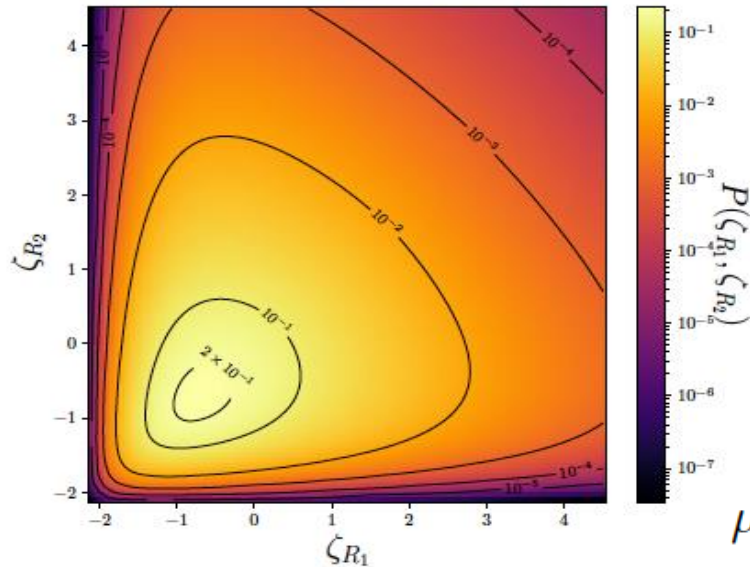


**Fig. 1.** Three-color (JWST/NIRCam F277W, F150W, and F115W for RGB) image and separate filter images of CID-931. The slit position of Keck-II/DEIMOS observation is shown by the white lines. Note that the Chandra 0.5-2 keV image has a different cutout size ( $6'' \times 6''$ ) due to a much lower pixel scale ( $0.''984/\text{pixel}$ ) than the HST and JWST images ( $3'' \times 3''$  cutout with the pixel scale of  $0.''03/\text{pixel}$ ). Yellow bars in right panels indicate the position of the red core.

# Clusters from Quantum Diffusion

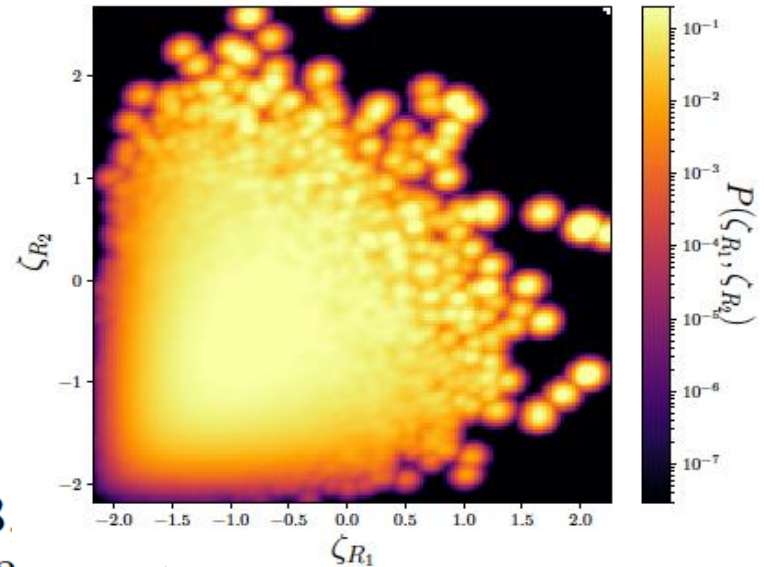
2-pt distribution function

Animali, Vennin [2402.08642]

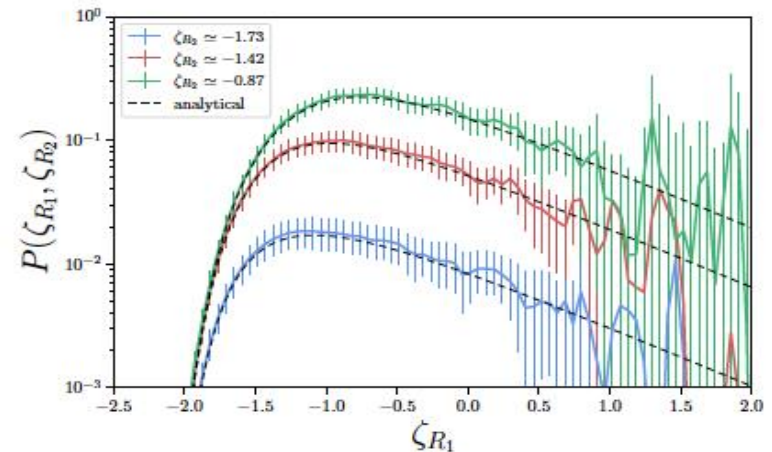
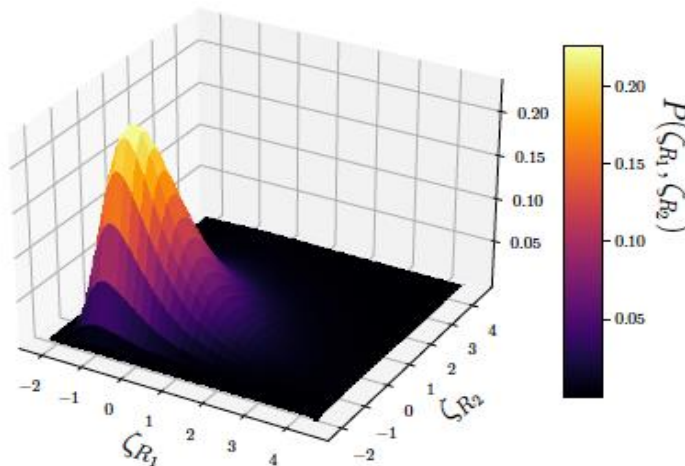


Tilted-well potential

$\mu = 13$   
 $d = 0.3$

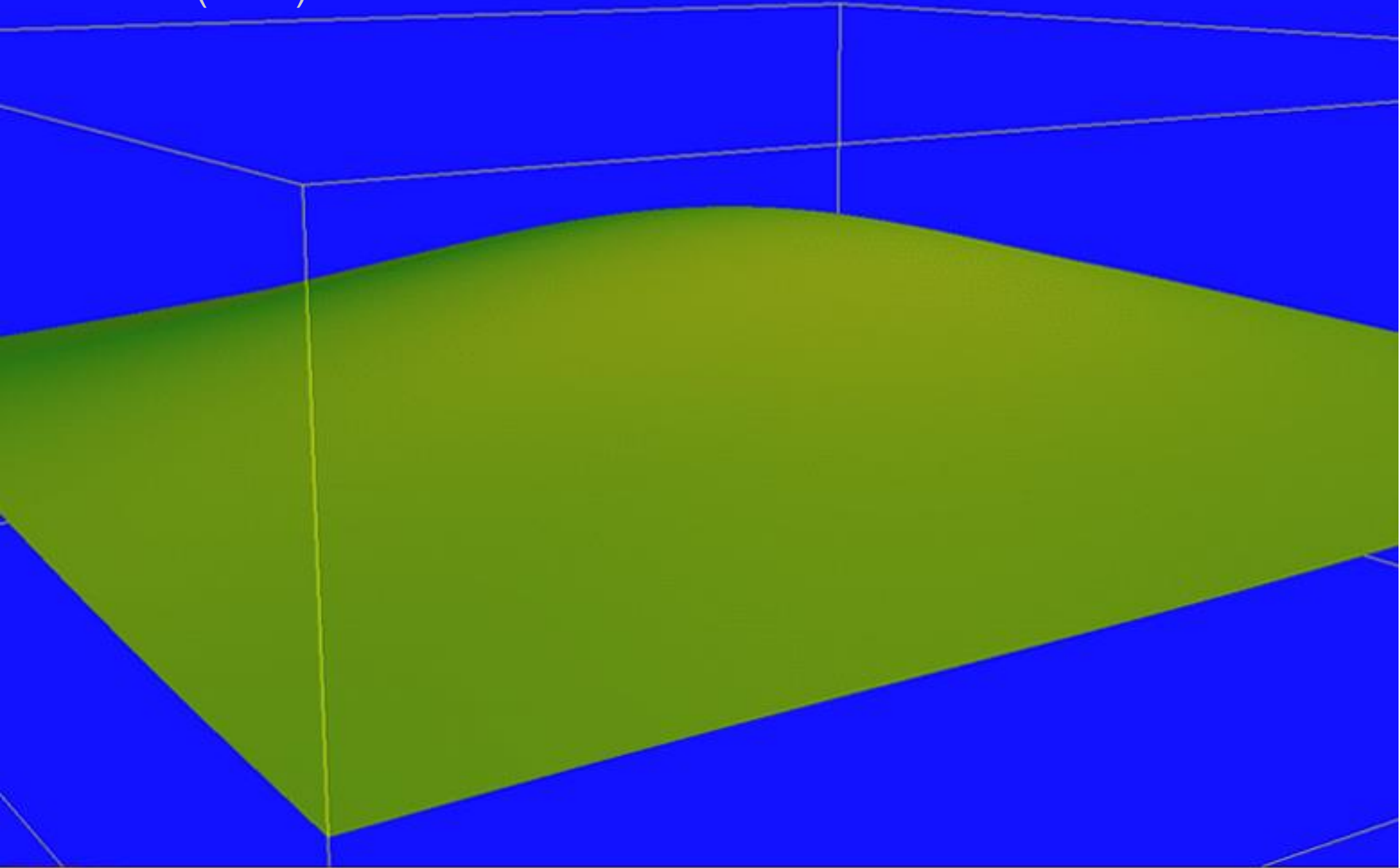


$10^6$  numerical simulations

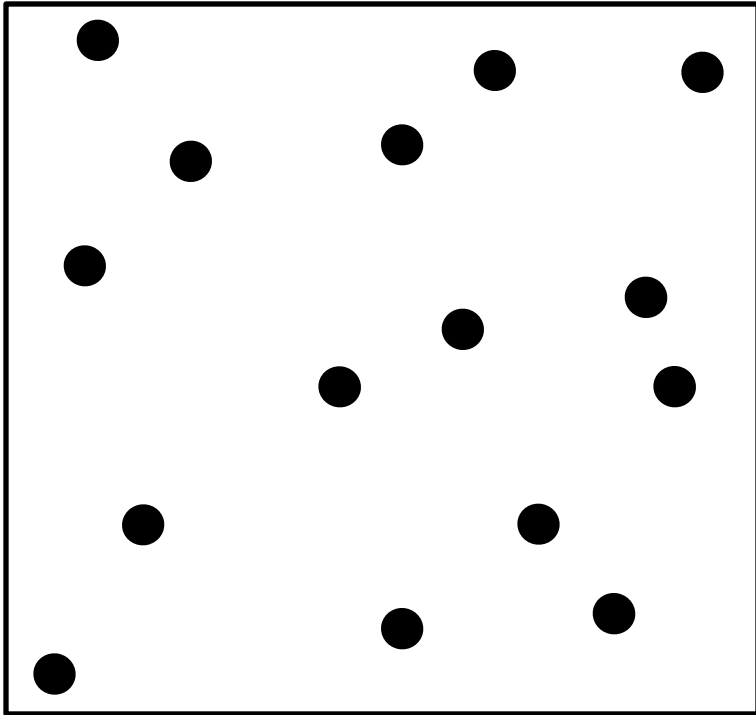


# PBH and Stochastic Inflation

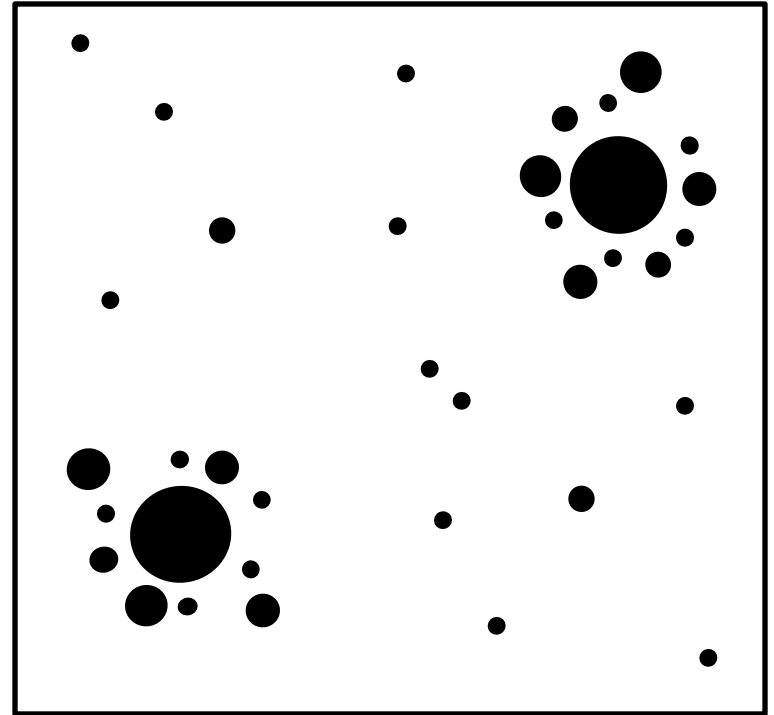
A. Linde (1994)



# Spatial Distribution PBH



- Monochromatic
- Uniformly distributed



- Broad range of masses
- PBH in dense clusters



JGB [1702.08275]

# Cluster Dynamics

- Initial conditions
- Binary parameter distributions
- Hierarchical mergers (w/ kicks)
- Merger rates
- Spin induction

# Cluster Dynamics

J.F. Nuño Siles, JGB [2405.06391]

Lognormal mass distribution

$$N \sim \mathcal{O}(10^3 - 20 \cdot 10^3)$$

$$M_{\text{tot}} \sim \mathcal{O}(10^3 - 10^5) M_{\odot}$$

Maxwellian velocity distribution

Plummer density profile

Galactic potential MW

(point-mass galaxy)

$$M = 4.36953 \times 10^4 M_{\odot}$$

with circular orbit at  $R = 34$  kpc

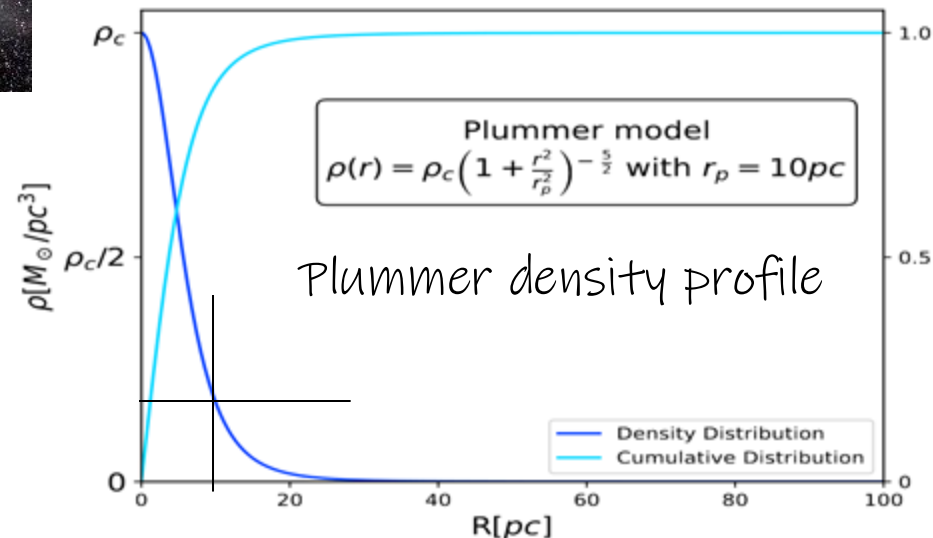
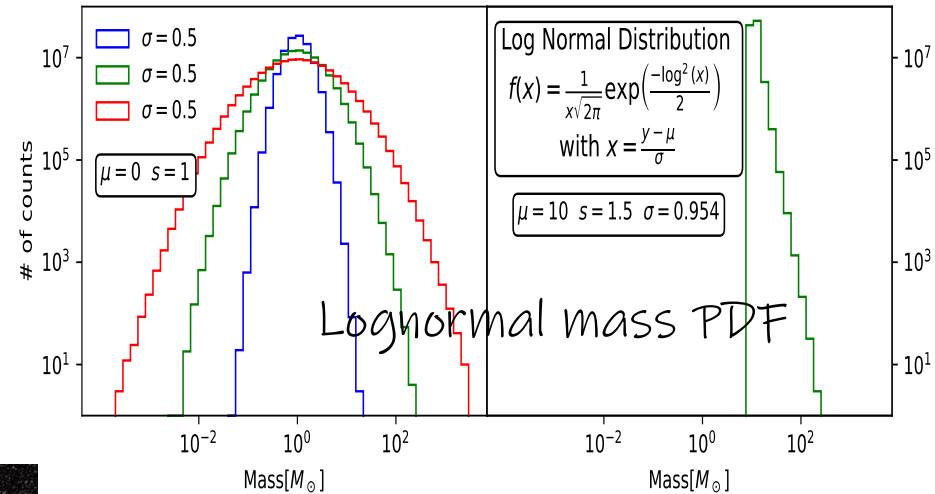
No primordial binaries

Zero natal spin

Code used: [Nbody6++GPU](#)



$$\{M\&A, \sigma_{0.5}, \sigma_1, \sigma_{1.5}\}$$



# Multiple simulations

J.F. Nuño Siles, JGB [2405.06391]

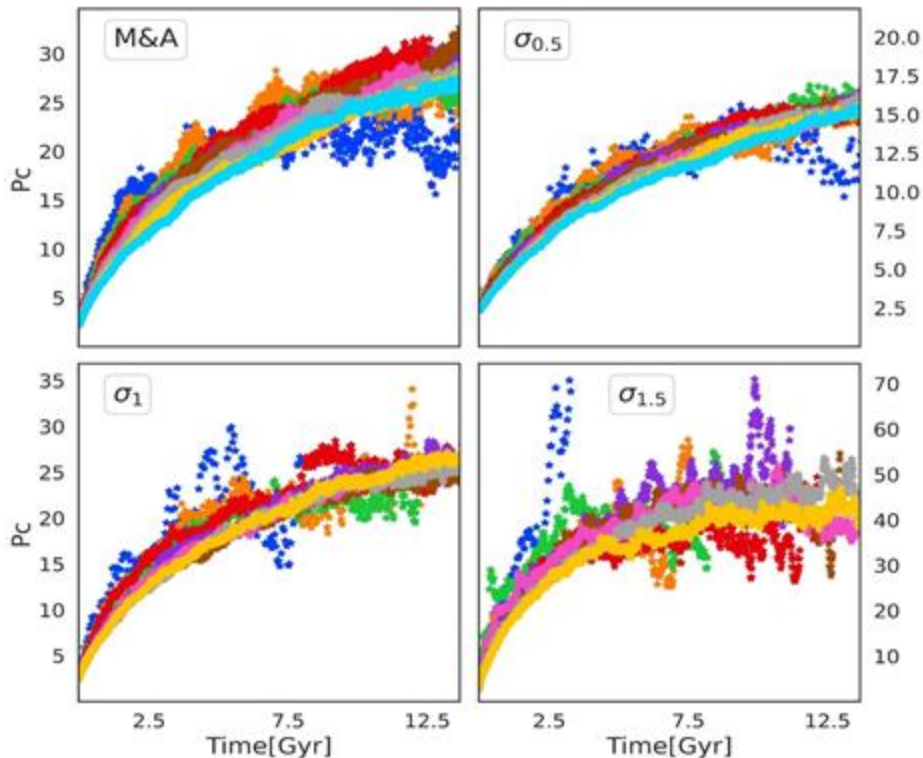
| ID<br>M&A        | $M_{\text{total}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = T_U$ | $R_{\text{HM}}[\text{pc}]$<br>$t = 0$ | $R_{\text{HM}}[\text{pc}]$<br>$t = T_U$ | ID<br>$\sigma_{0.5}$ | $M_{\text{total}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = T_U$ | $R_{\text{HM}}[\text{pc}]$<br>$t = 0$ | $R_{\text{HM}}[\text{pc}]$<br>$t = T_U$ |
|------------------|------------------------------------------|----------------------------------------|------------------------------------------|---------------------------------------|-----------------------------------------|----------------------|------------------------------------------|----------------------------------------|------------------------------------------|---------------------------------------|-----------------------------------------|
| 1295             | 16140                                    | 46.54                                  | 46.54                                    | 2.20                                  | 27.04                                   | 1520                 | 1389                                     | 5.03                                   | 5.03                                     | 9.72                                  | 12.25                                   |
| 2570             | 32166                                    | 66.10                                  | 97.80                                    | 2.38                                  | 27.17                                   | 3345                 | 3007                                     | 4.50                                   | 5.08                                     | 3.23                                  | 15.55                                   |
| 4046             | 50088                                    | 63.64                                  | 91.98                                    | 4.27                                  | 26.74                                   | 5480                 | 5009                                     | 6.67                                   | 6.67                                     | 0.77                                  | 16.21                                   |
| 5199             | 64280                                    | 69.98                                  | 74.80                                    | 2.20                                  | 28.39                                   | 7678                 | 7008                                     | 5.69                                   | 7.52                                     | 1.92                                  | 15.15                                   |
| 8077             | 100116                                   | 78.27                                  | 78.27                                    | 12.53                                 | 29.50                                   | 9937                 | 9001                                     | 5.48                                   | 5.48                                     | 1.25                                  | 15.85                                   |
| 8922             | 110196                                   | 76.15                                  | 81.52                                    | 13.31                                 | 32.01                                   | 12201                | 11001                                    | 5.00                                   | 7.77                                     | 2.90                                  | 15.29                                   |
| 10372            | 128337                                   | 104.26                                 | 104.26                                   | 6.20                                  | 27.54                                   | 14366                | 13005                                    | 5.42                                   | 8.22                                     | 2.65                                  | 16.04                                   |
| 10535            | 130198                                   | 68.50                                  | 74.35                                    | 9.72                                  | 28.20                                   | 16428                | 14912                                    | 7.72                                   | 7.72                                     | 0.48                                  | 16.04                                   |
| 16159            | 200392                                   | 57.75                                  | 113.59                                   | 4.44                                  | 27.24                                   | 18776                | 17007                                    | 5.40                                   | 6.51                                     | 2.29                                  | 15.00                                   |
| 20738            | 256346                                   | 134.10                                 | 145.70                                   | 1.37                                  | 26.65                                   | 20866                | 18918                                    | 5.31                                   | 7.36                                     | 3.91                                  | 15.35                                   |
| ID<br>$\sigma_1$ | $M_{\text{total}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = T_U$ | $R_{\text{HM}}[\text{pc}]$<br>$t = 0$ | $R_{\text{HM}}[\text{pc}]$<br>$t = T_U$ | ID<br>$\sigma_{1.5}$ | $M_{\text{total}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = 0$ | $M_{\text{max}}[M_{\odot}]$<br>$t = T_U$ | $R_{\text{HM}}[\text{pc}]$<br>$t = 0$ | $R_{\text{HM}}[\text{pc}]$<br>$t = T_U$ |
| 1505             | 2003                                     | 32.07                                  | 32.07                                    | 1.93                                  | 27.07                                   | 1220                 | 3020                                     | 63.67                                  | 63.67                                    | 3.37                                  | 58.92                                   |
| 3090             | 4004                                     | 18.56                                  | 18.56                                    | 7.52                                  | 22.21                                   | 3423                 | 8010                                     | 105.74                                 | 105.74                                   | 7.15                                  | 41.00                                   |
| 5288             | 7007                                     | 34.14                                  | 34.14                                    | 7.60                                  | 21.97                                   | 5258                 | 13014                                    | 541.18                                 | 541.18                                   | 1.95                                  | 40.15                                   |
| 7507             | 10001                                    | 25.82                                  | 34.29                                    | 3.95                                  | 24.77                                   | 8025                 | 20021                                    | 157.23                                 | 157.23                                   | 0.41                                  | 41.62                                   |
| 10663            | 14000                                    | 46.77                                  | 46.77                                    | 6.64                                  | 26.96                                   | 10011                | 24187                                    | 179.83                                 | 280.36                                   | 1.45                                  | 60.33                                   |
| 12834            | 17004                                    | 32.81                                  | 58.06                                    | 4.41                                  | 23.91                                   | 12409                | 30007                                    | 114.51                                 | 114.51                                   | 0.07                                  | 55.98                                   |
| 15136            | 20000                                    | 58.31                                  | 58.31                                    | 0.47                                  | 25.47                                   | 14691                | 38027                                    | 731.69                                 | 1004.13                                  | 1.40                                  | 37.81                                   |
| 17554            | 23008                                    | 45.68                                  | 64.90                                    | 0.82                                  | 25.62                                   | 17182                | 43013                                    | 554.27                                 | 554.27                                   | 5.59                                  | 46.36                                   |
| 20590            | 27008                                    | 51.60                                  | 76.41                                    | 4.70                                  | 26.64                                   | 20261                | 49021                                    | 657.47                                 | 784.02                                   | 3.52                                  | 41.41                                   |

# Cluster Dynamics

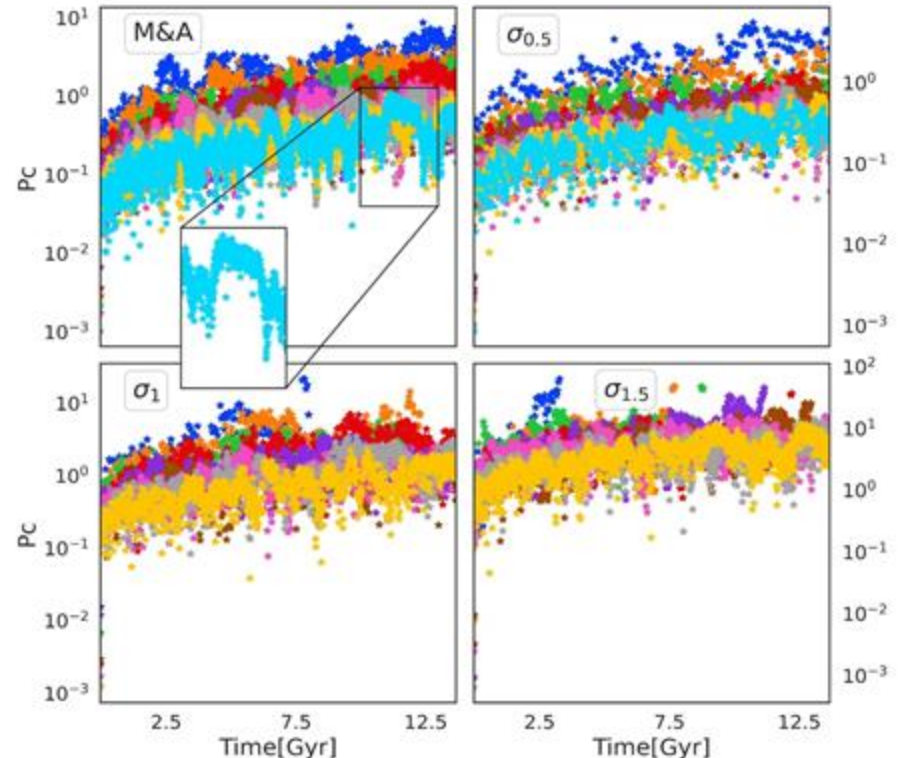
Clusters expand with time while core radius stays almost constant

JFN+JGB [2405.06391]

$R_{HM}(t)$



$R_c(t)$

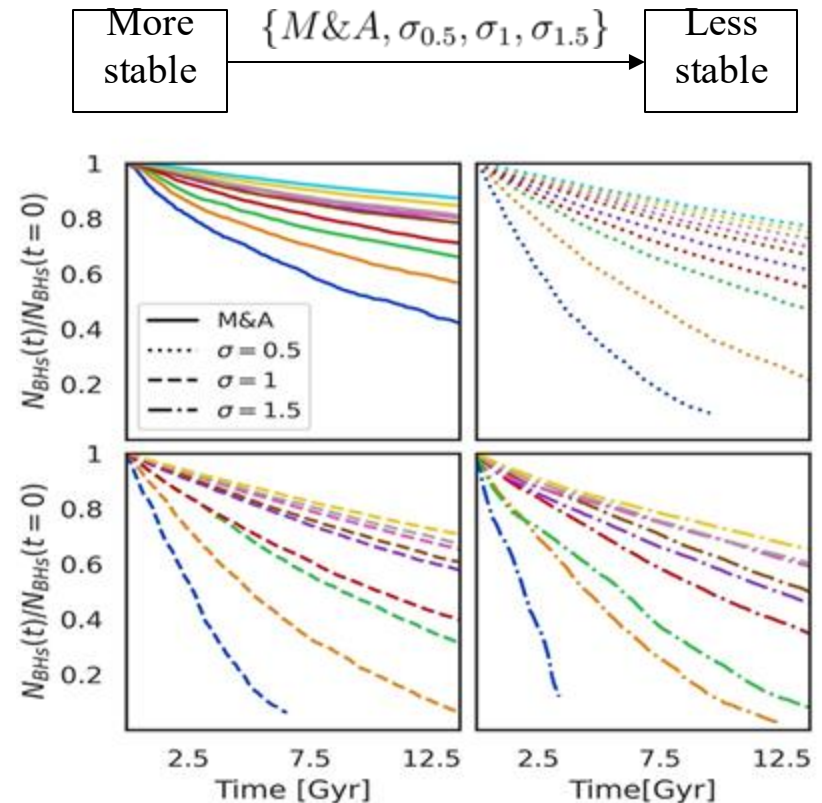


# Cluster Dynamics

J.F. Nuño Siles, JGB [2405.06391]

All the clusters are metastable or directly unstable, that is, they dissolved in a time comparable with the age of the Universe or will do so in the future

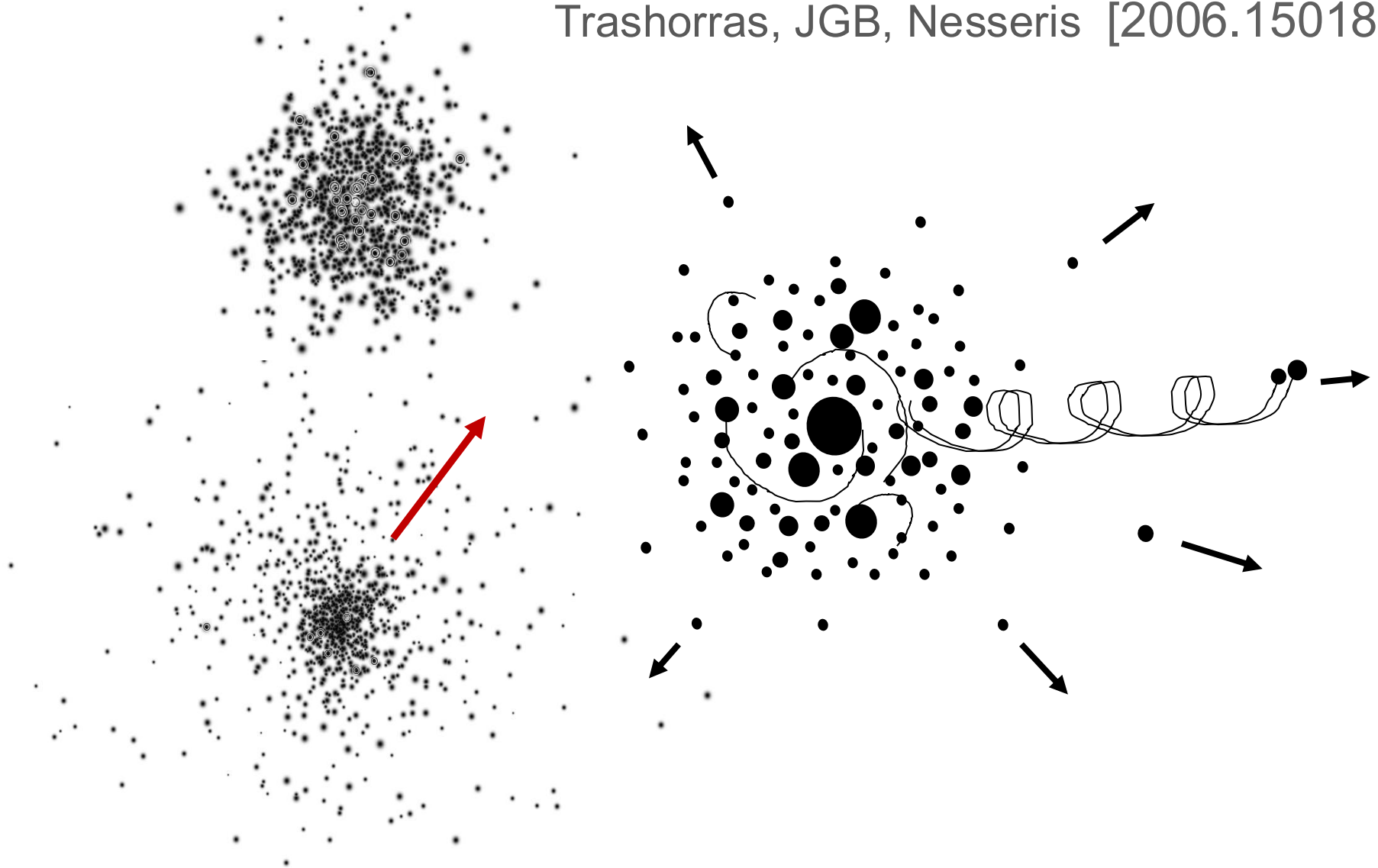
Some types of clusters are more stable than others, depending on the mass ratio distribution of the pairwise interactions.



BHs remaining in clusters within 13.6 Gyr

# Cluster Dynamics

Trashorras, JGB, Nesseris [2006.15018]

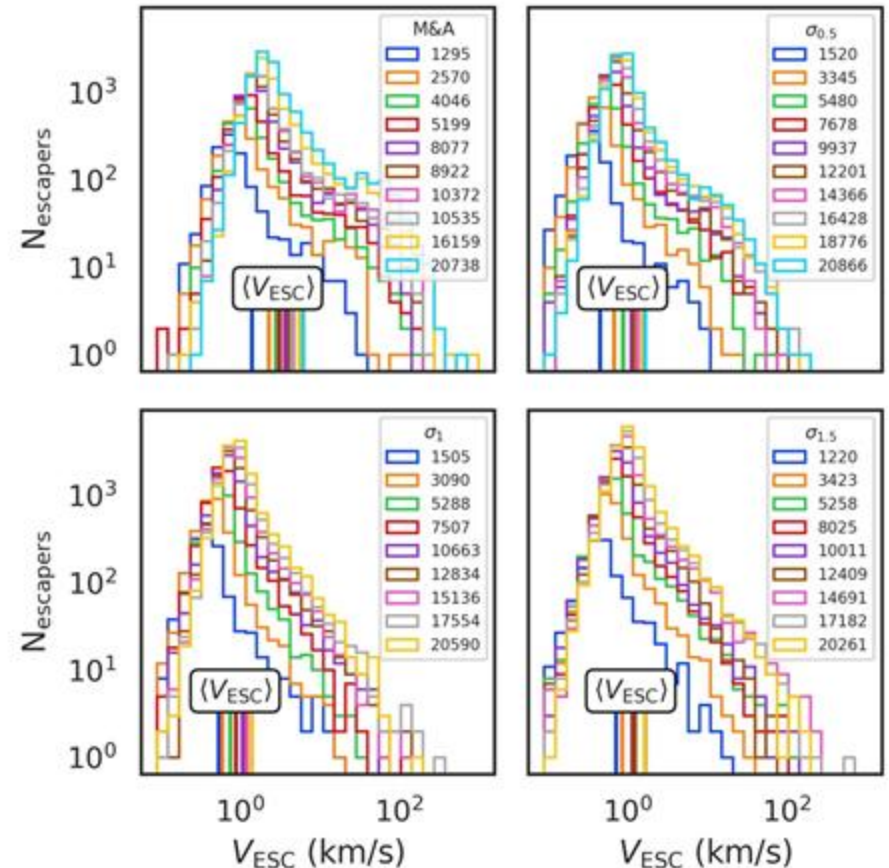
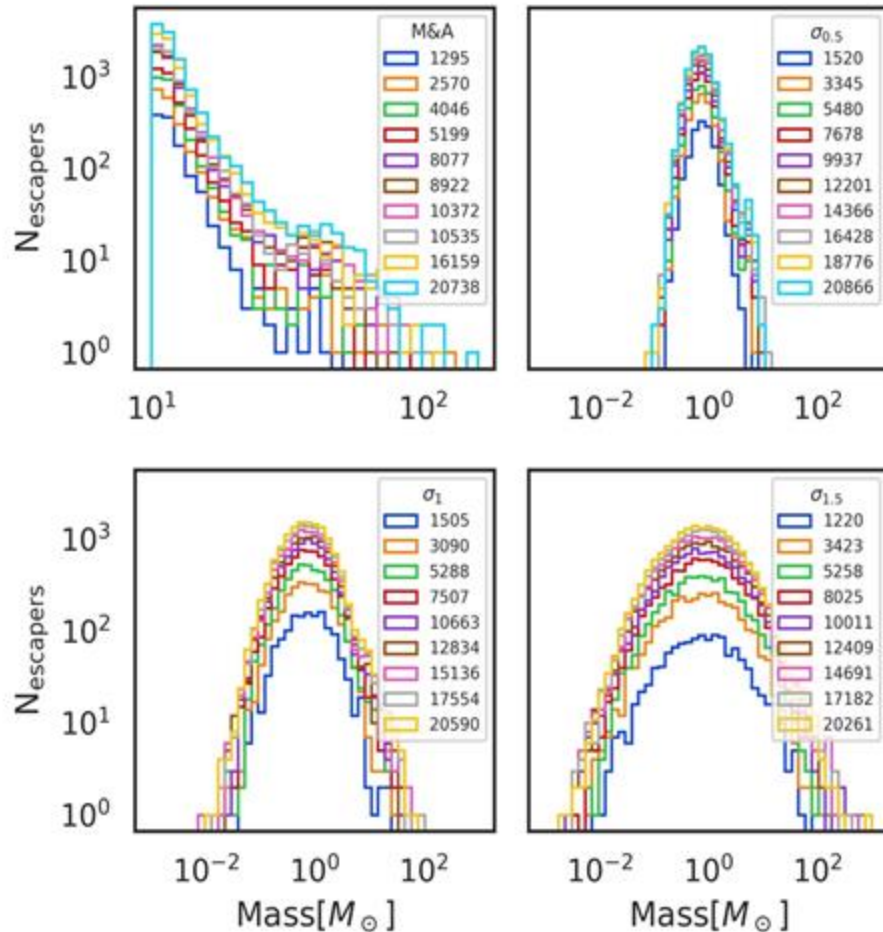


# Distribution of escapers

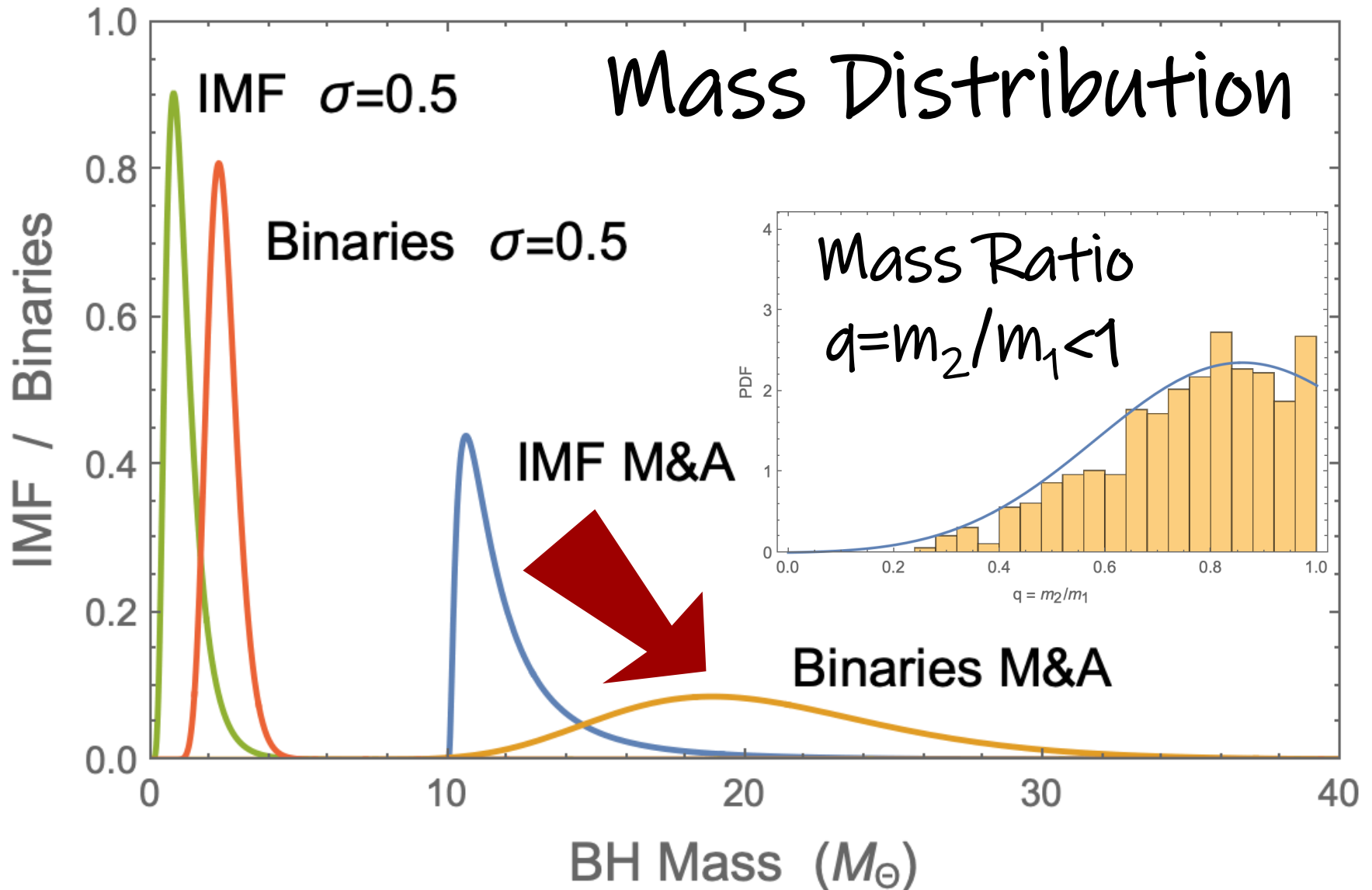
JFN+JGB [2405.06391]

Mass

Escape velocity



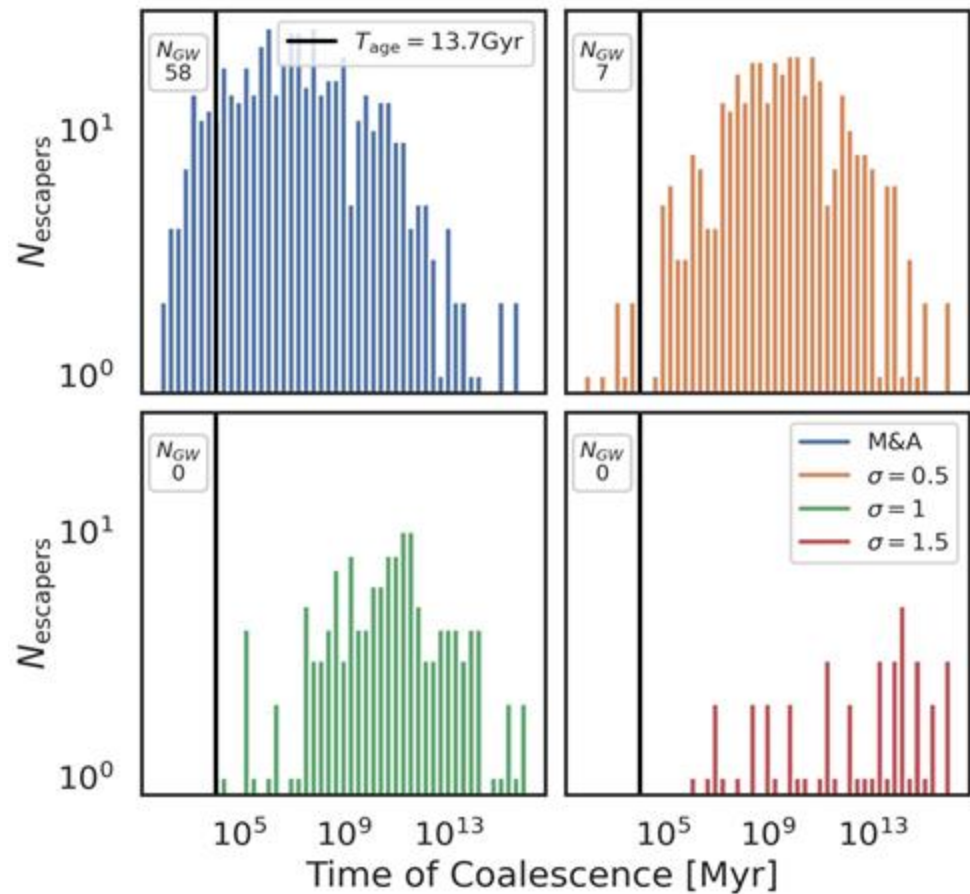
# Binary escapers



# Binary escapers

- The larger the initial  $N$ , the harder the binary needs to be to escape.
- Mainly highly eccentric (at birth) binaries coalesce in a Hubble time.
- Most binaries would not have merged by now. Only  $\{58, 7, 0, 0\}$  of the  $\{504, 371, 153, 60\}$  binary escapers are off-cluster mergers within the age of the universe.
- Binary escapers merger rate lognormal in time

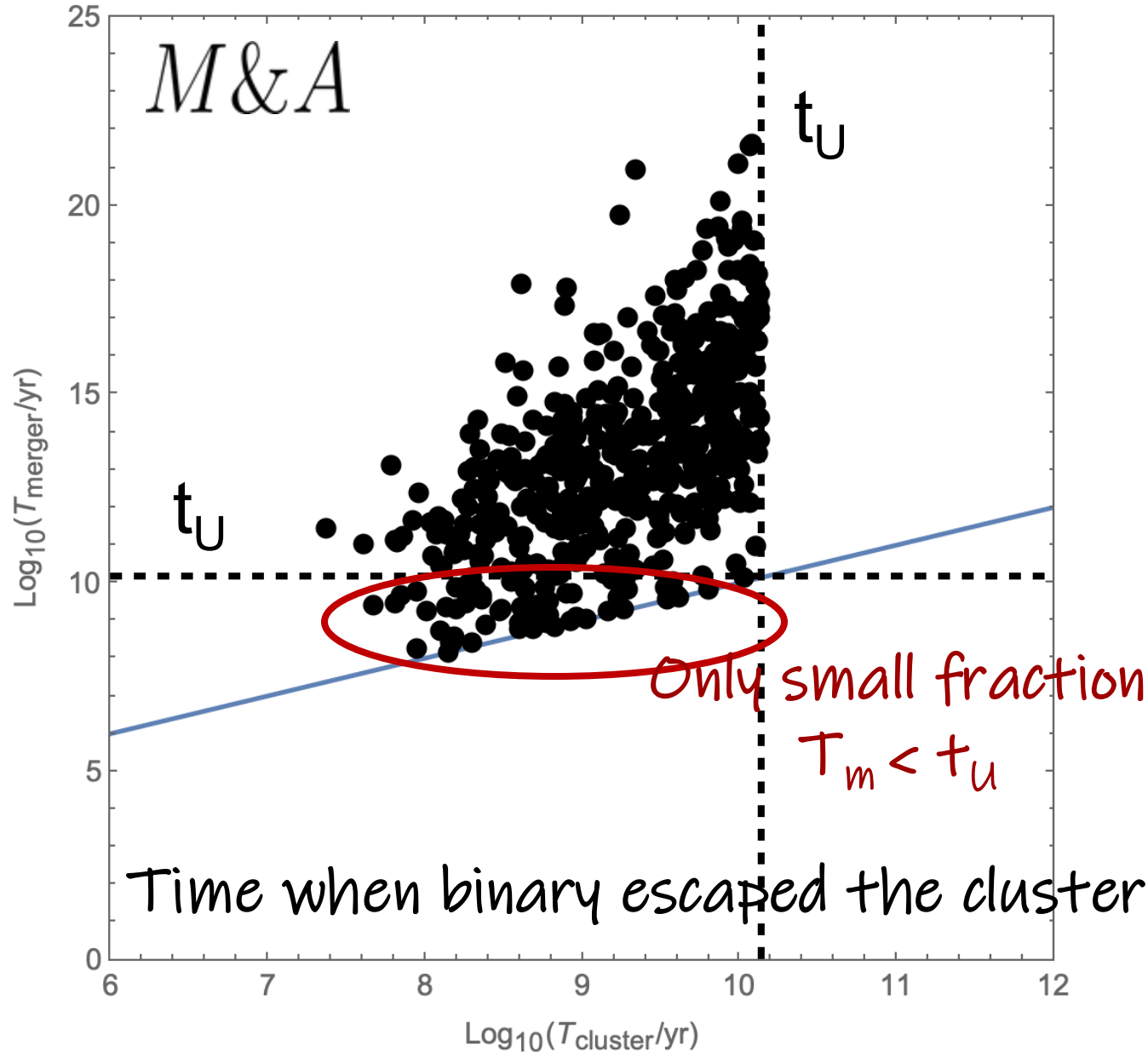
JFN+JGB [2405.06391]



Distribution of merger times for binary escapers using the quasi-circular orbit approximation

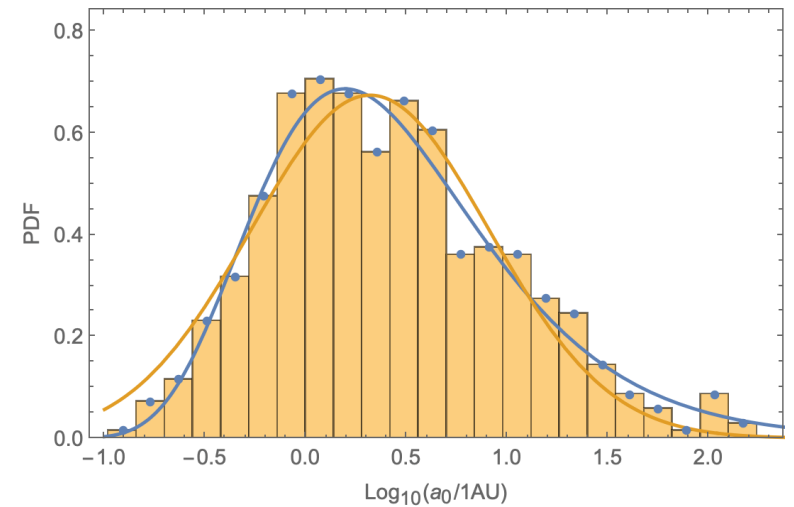
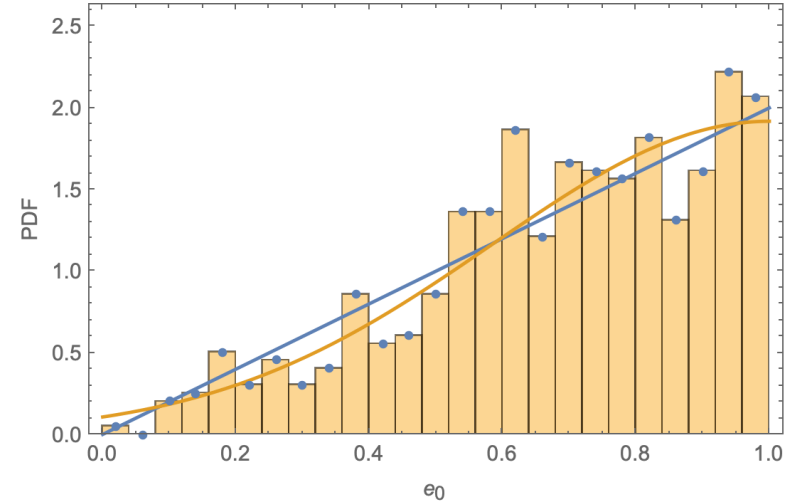
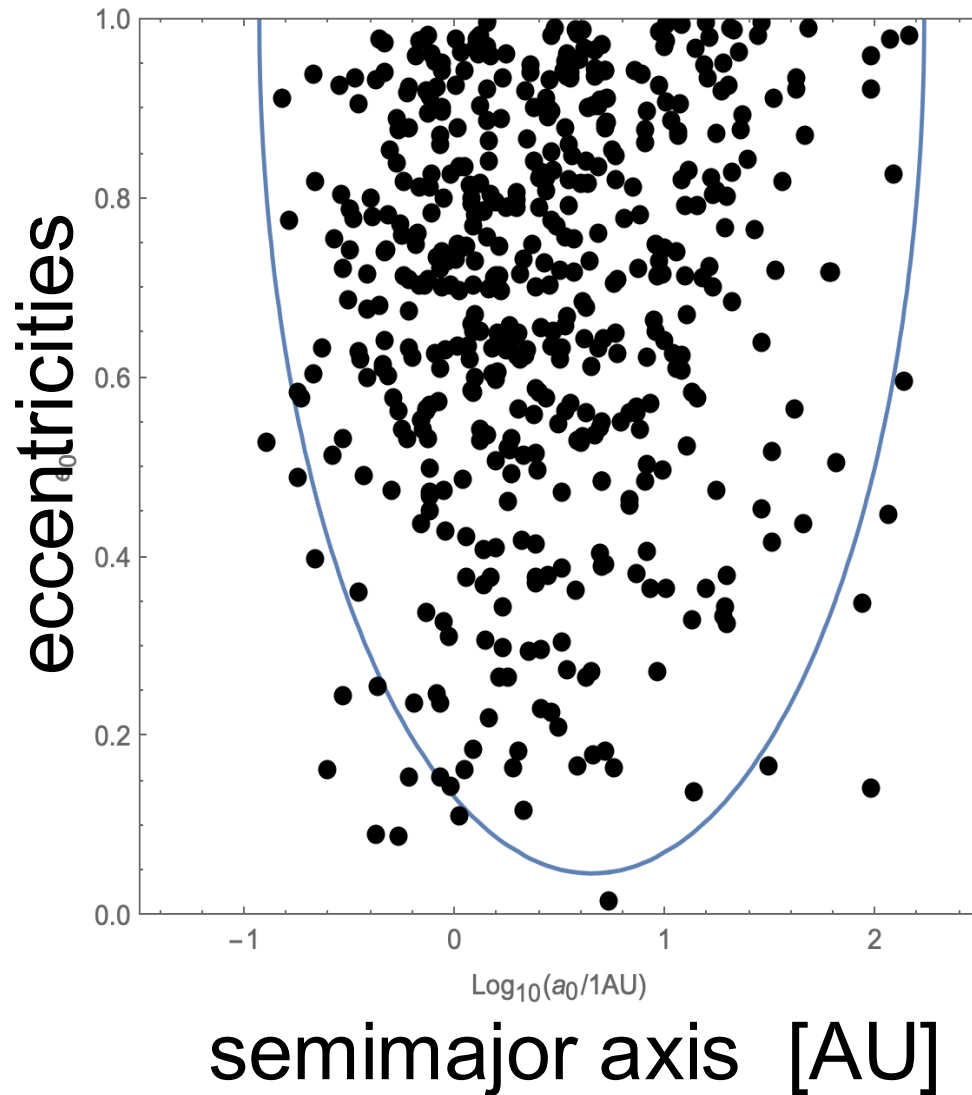
# Binary escapers

Time when escaped binary merged



# Binary escapers

$M\&A$

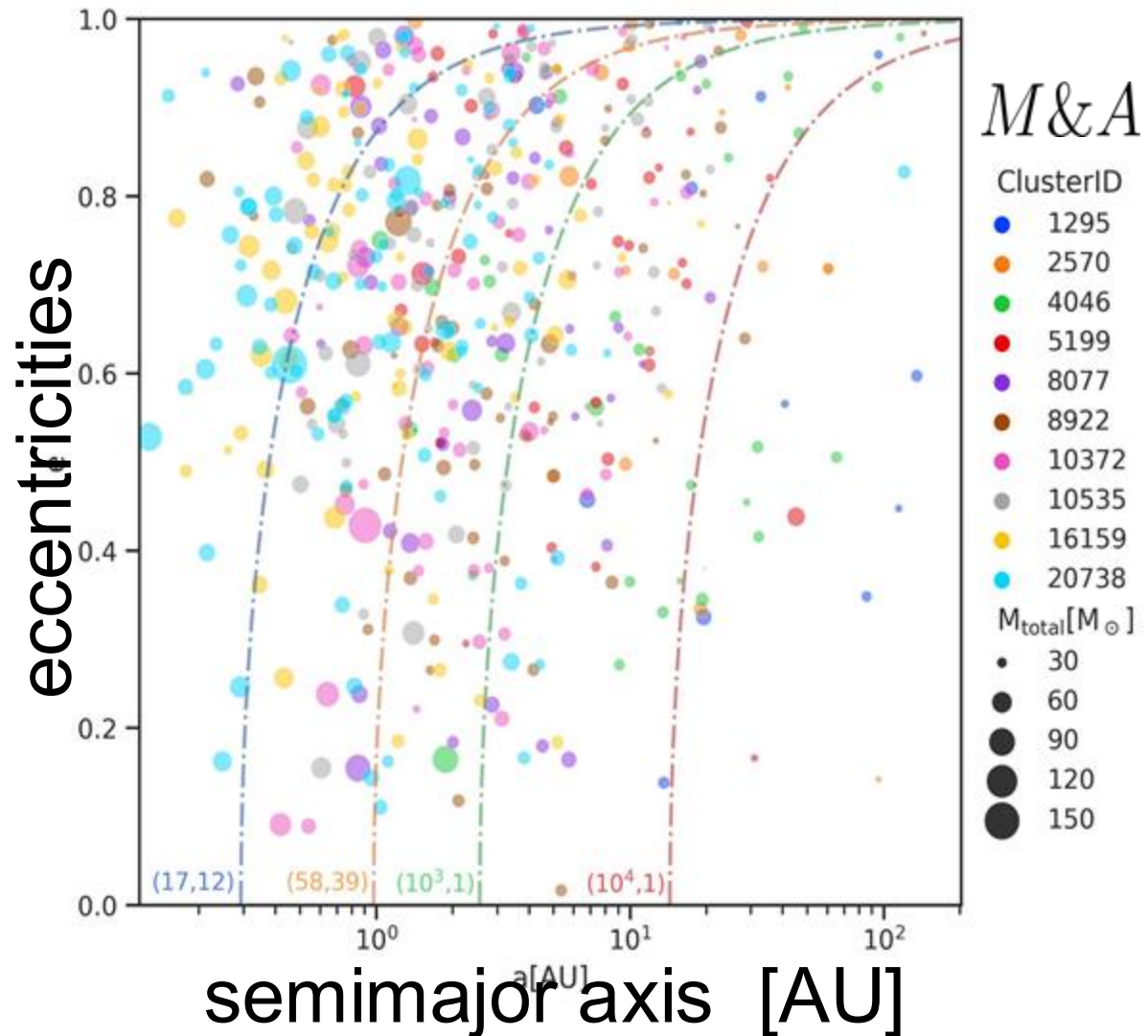


# Binary escapers

Numbers increase with initial density but ratio decreases

The larger the initial  $N$ , the smaller the semimajor axis of the binaries, that is, the harder the binary.

Mainly highly eccentric binaries coalesce in a Hubble time

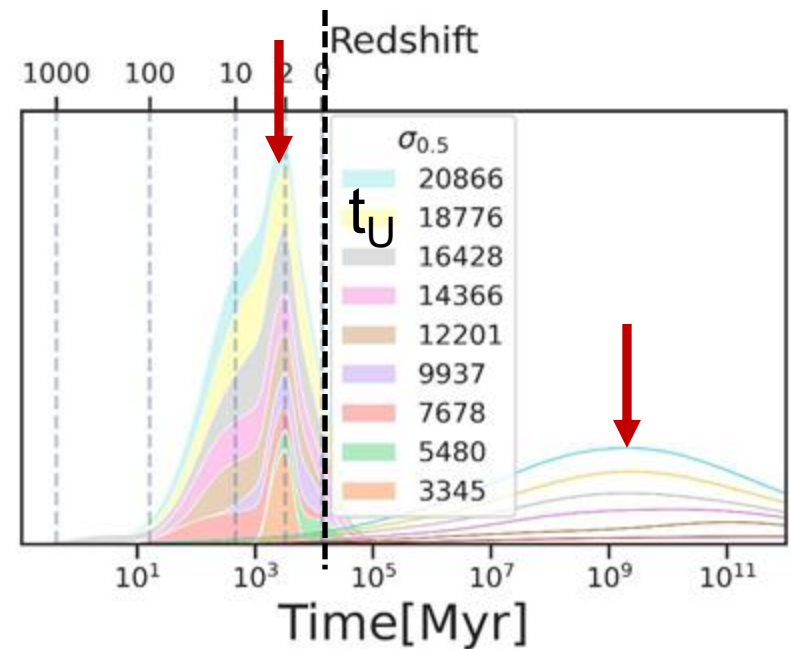
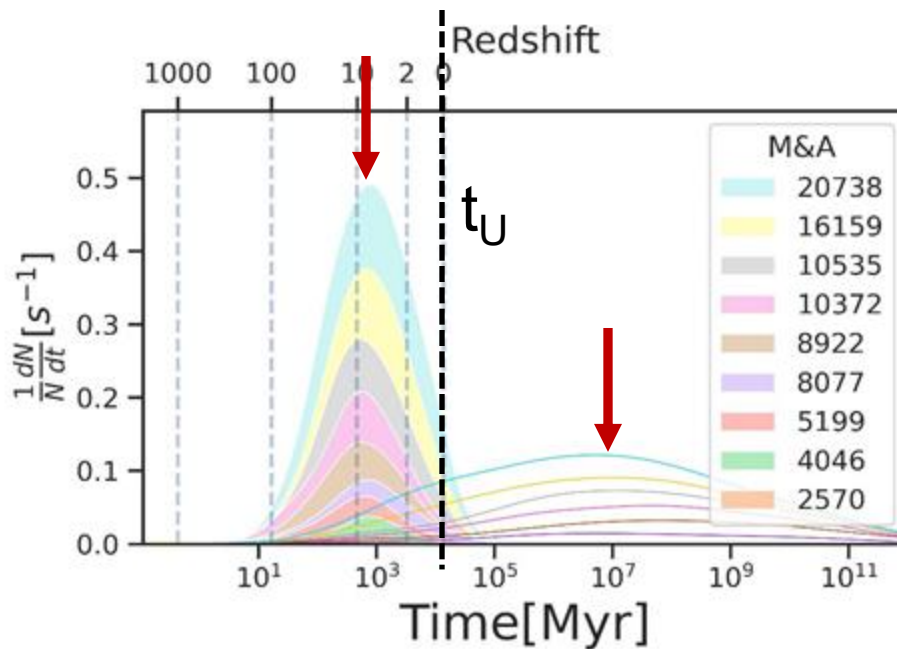


Distribution of eccentricities and semimajor axes of the binary escapers.

# BBH merger rates

In-cluster merger rate  
for  $\sigma_{0.5}$  peaks at  $z \sim 8$   
for M&A peaks at  $z \sim 2$

Escapers merger rate  
 $\sigma_{0.5}$  peaks at  $10^3 t_u$   
M&A peaks at  $10^5 t_u$

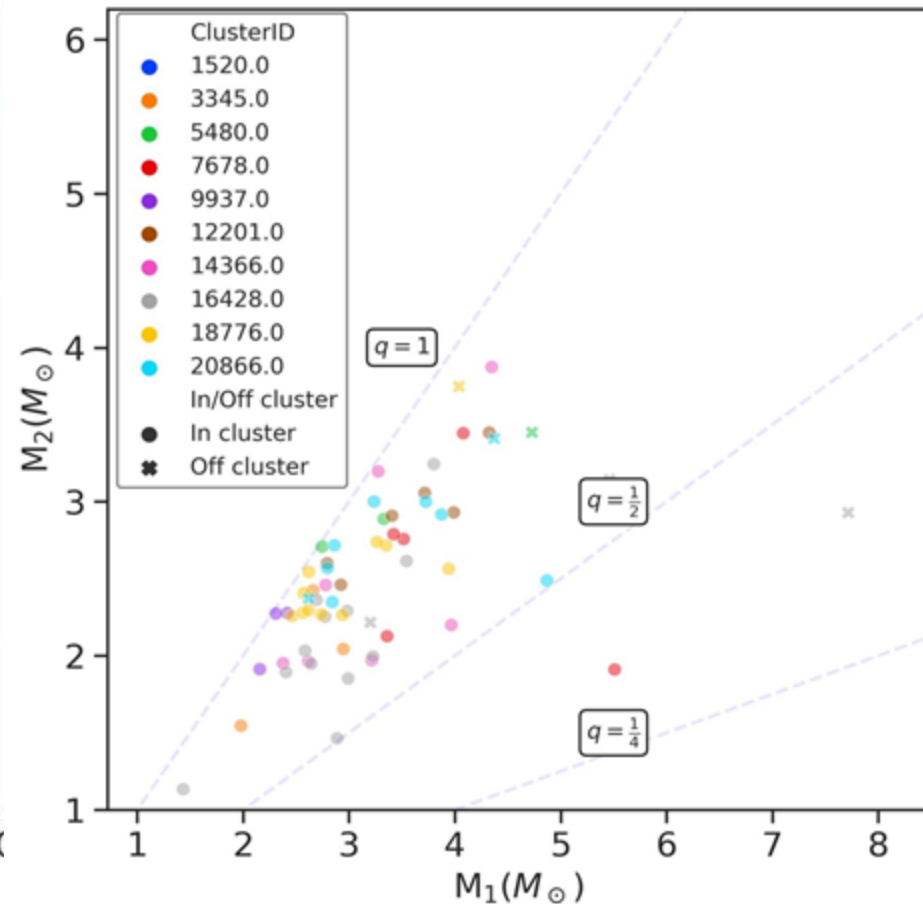
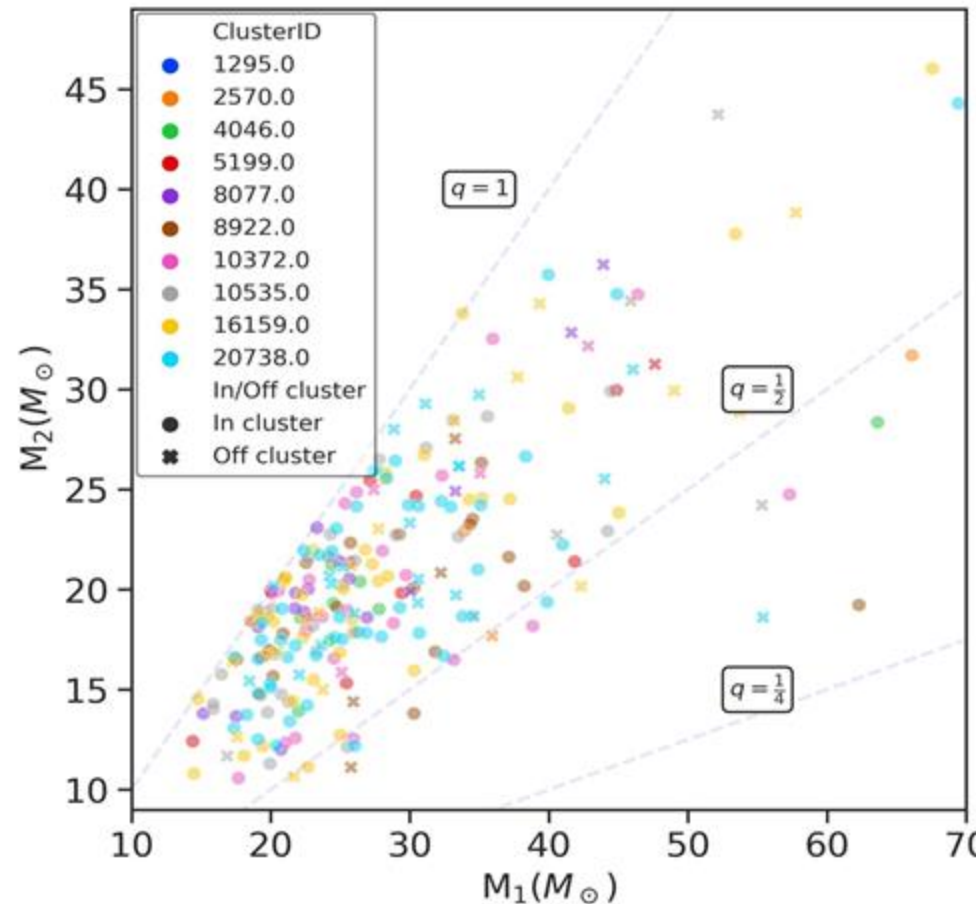


In-cluster and binary escapers merger rate

# BBH merger masses

$M \& A$

$\sigma_{0.5}$



Distribution of the masses ( $m_1$ ,  $m_2$ ) of the BBHs mergers

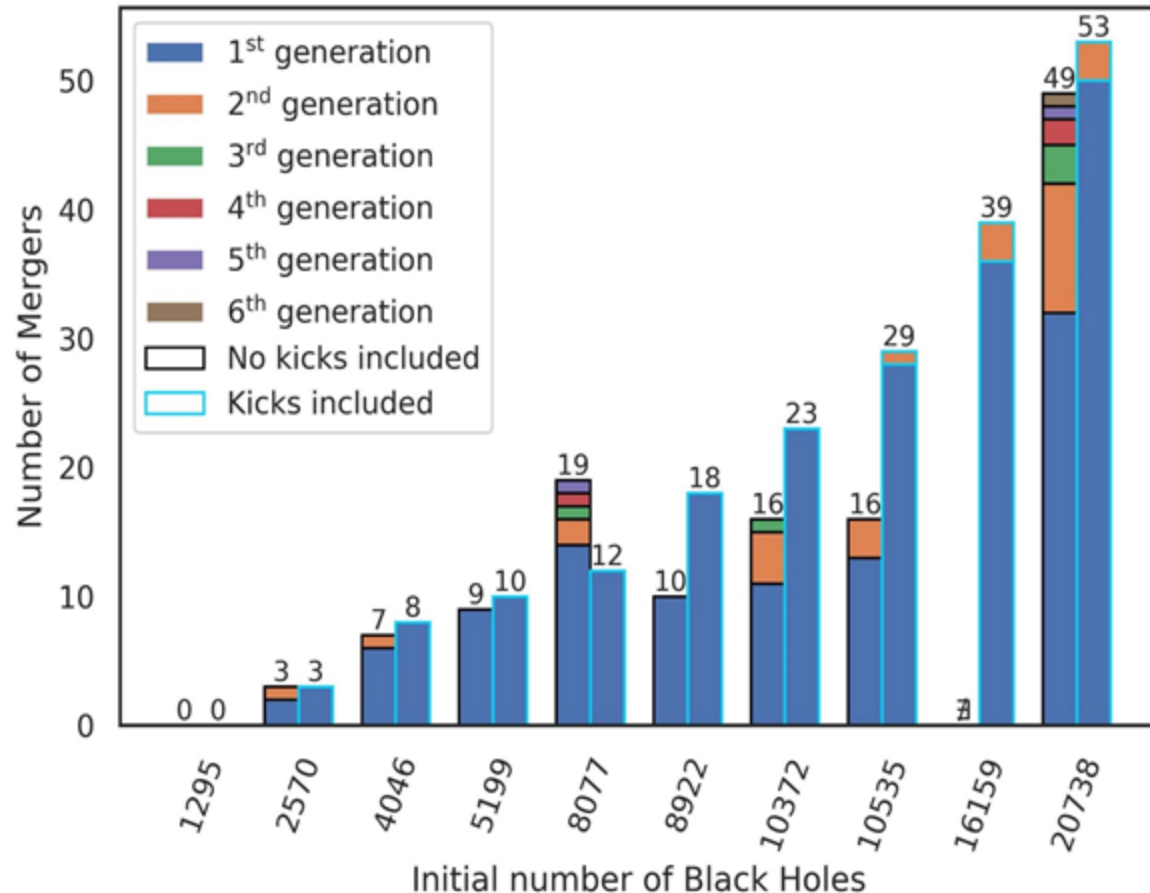
# BBH merger kicks

*M&A*

Best environment to study and understand implications as collisions are numerous

BBH kicks as implemented in **Nbody6++GPU** based on Campanelli et al.

Probability of hierarchical mergers drastically reduced



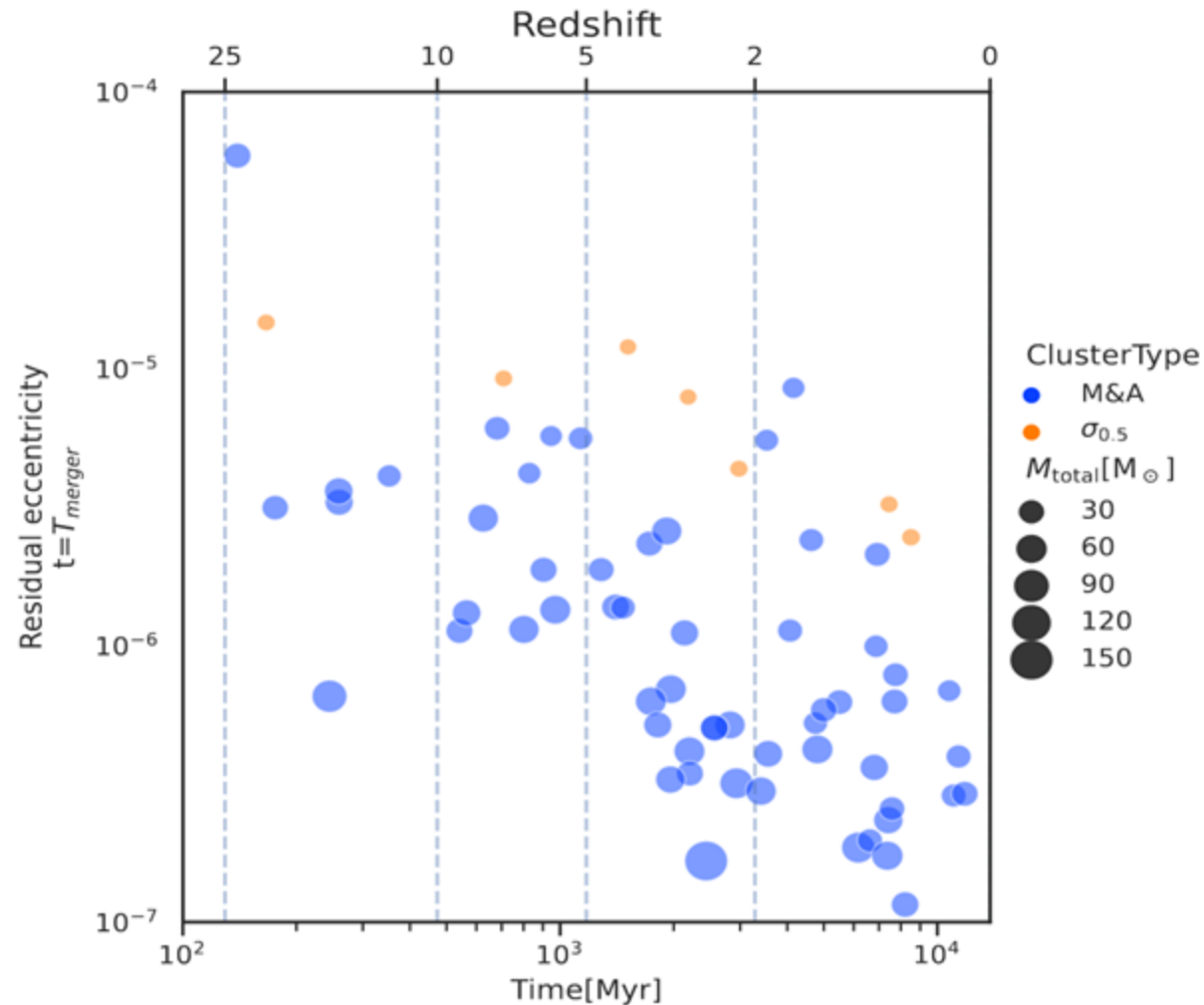
Histogram of the number of in-cluster mergers for the *M&A* type with and without considering BH kicks

# BBH merger eccent.'s

GW searches assume  
quasi-circular approx.  
How good is this  
hypothesis?

Residual eccentricity  
less than  $10^{-4}$  at  
 $f=10\text{Hz}$

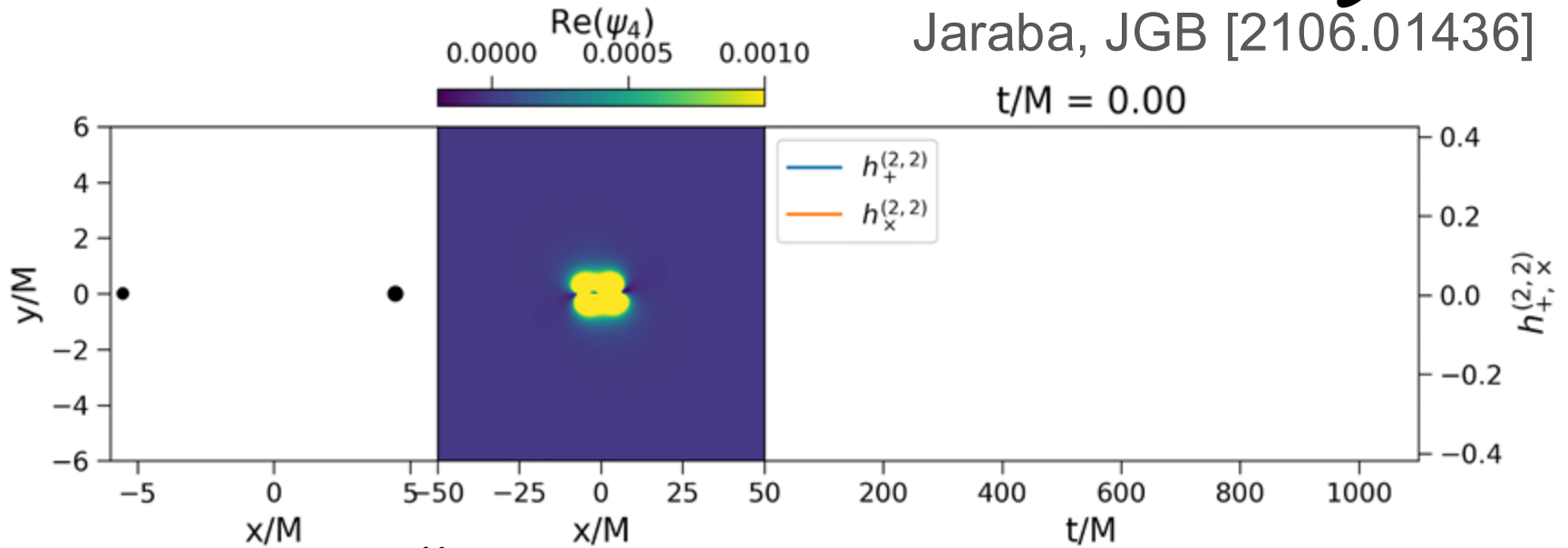
Uncorrelated with  
redshift



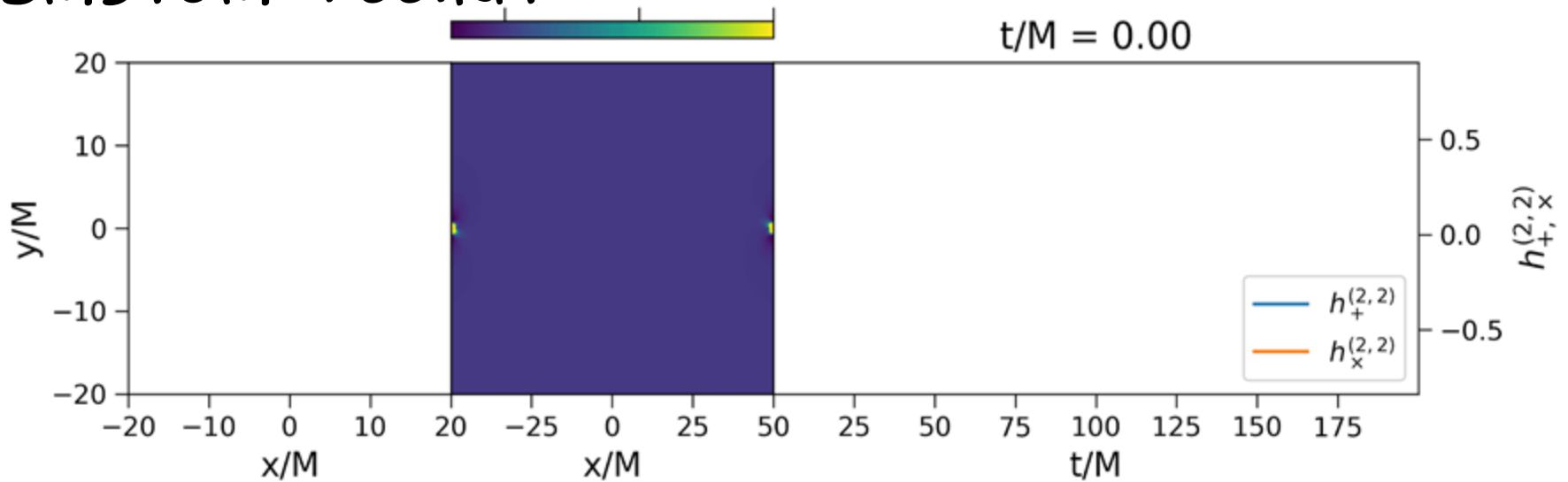
Residual eccentricity of the off-cluster mergers

# Inspirals vs scatterings

Jaraba, JGB [2106.01436]

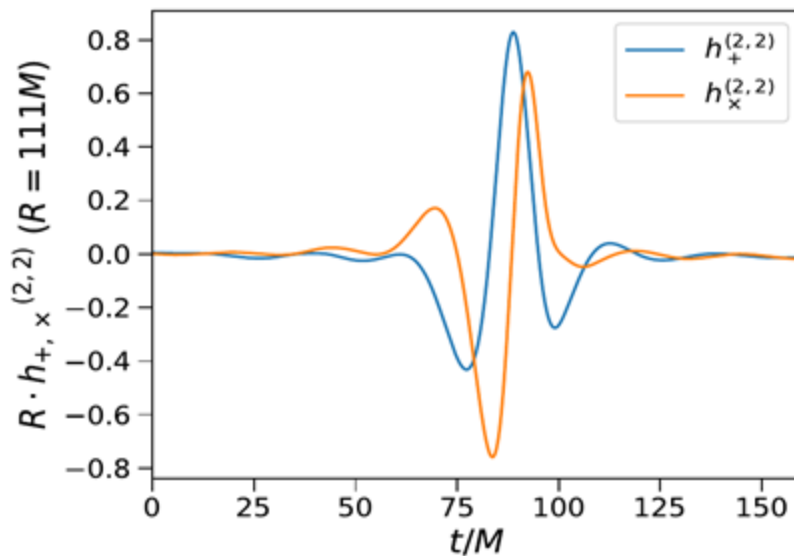
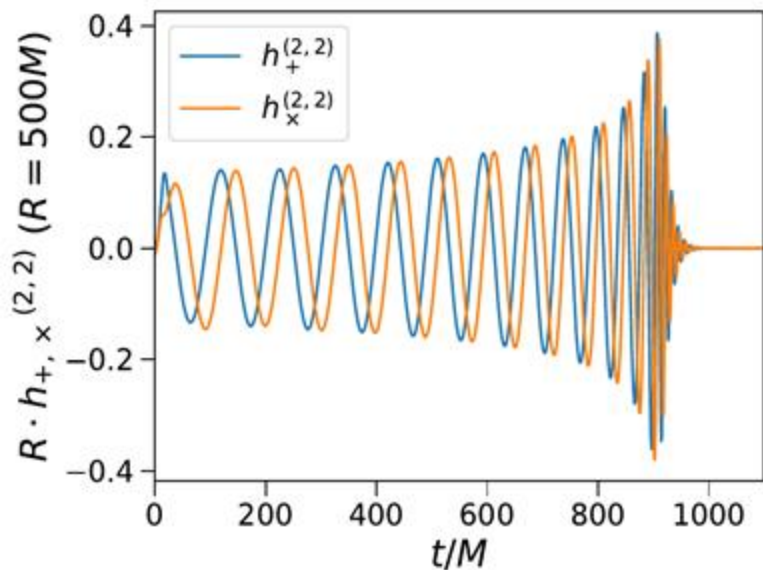


Einstein Toolkit



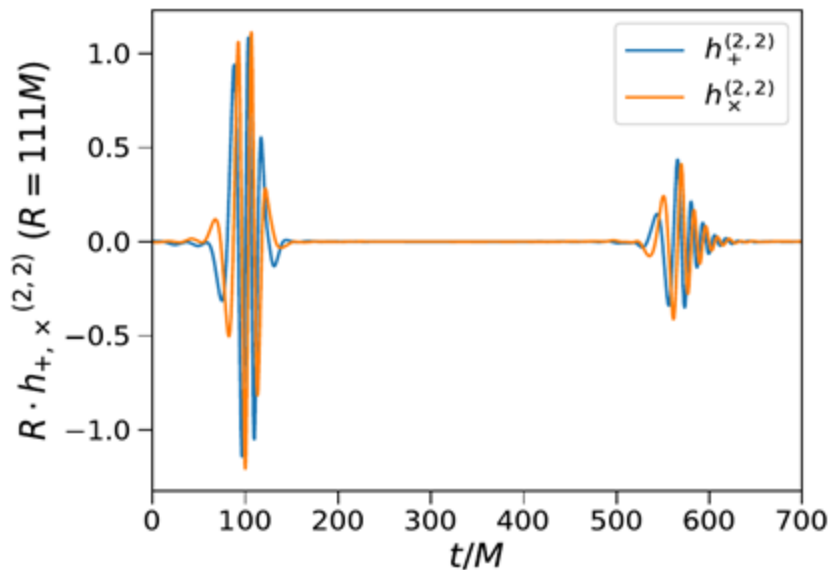
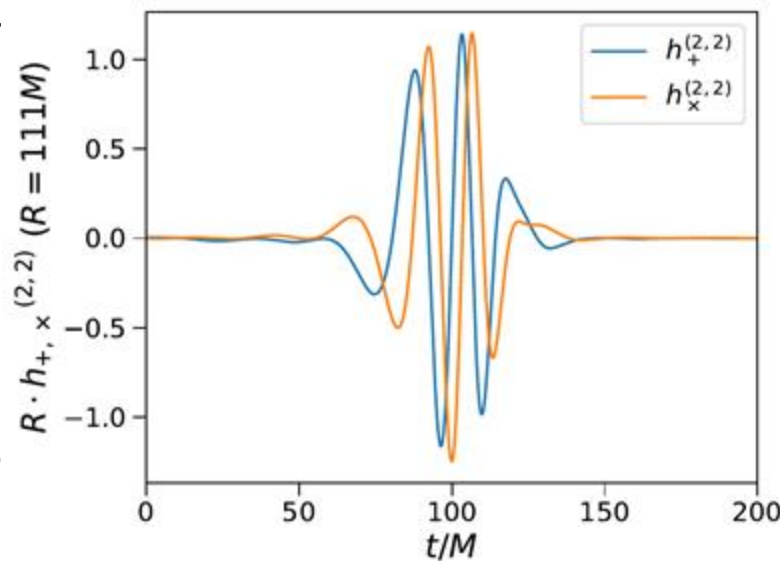
# Inspirals vs scatterings

CBC (GW150914)



CHE ( $d/M=100, q=1$ ,  
 $p/M=0.49, \theta=4.01^\circ$ )

CHE ( $d/M=100, q=1$ ,  
 $p/M=0.49, \theta=3.12^\circ$ )

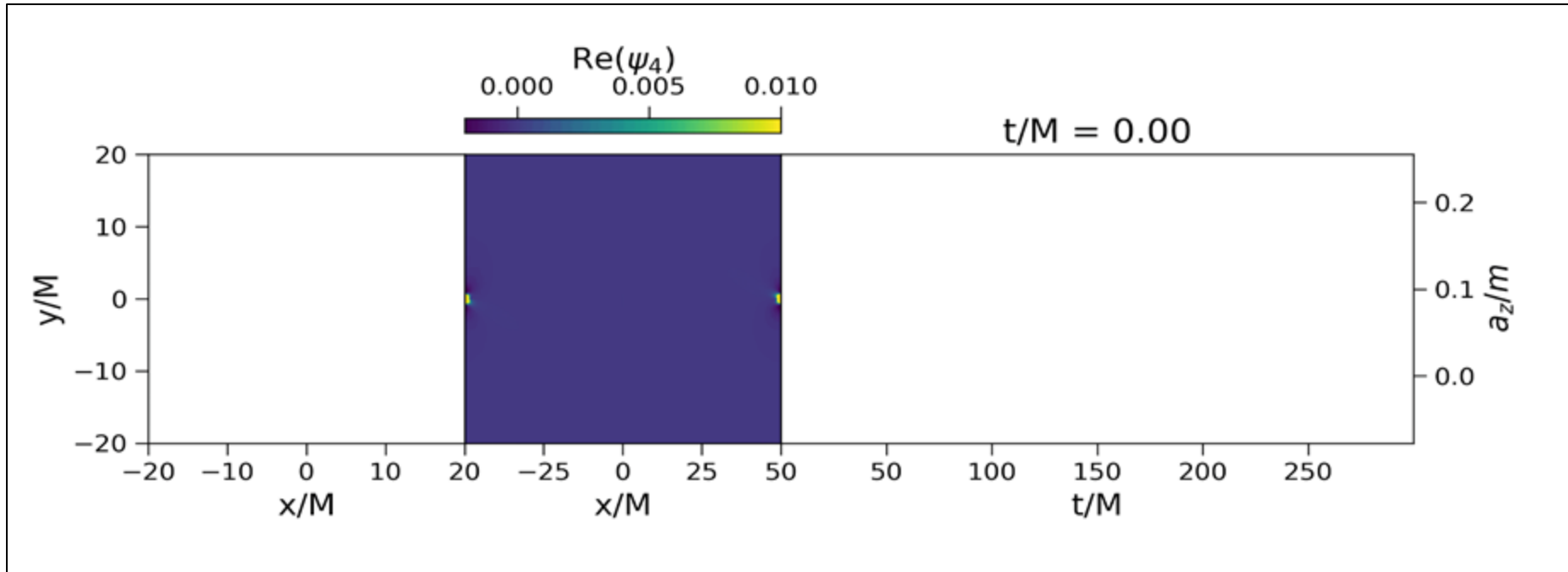
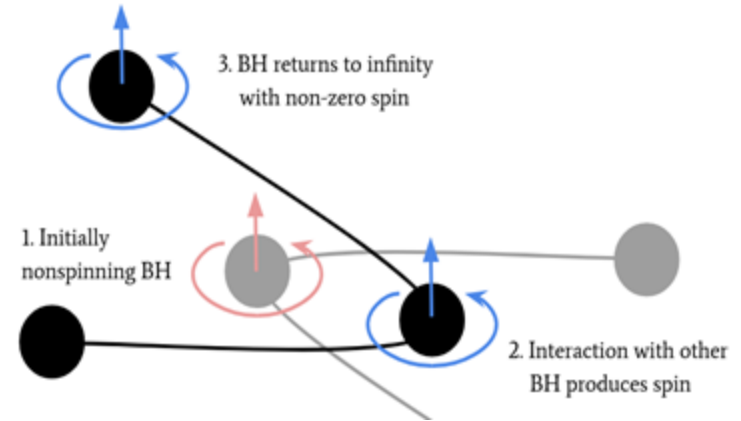


Dynamical capture  
( $d/M=100, q=1, p/M=0.49$ ,  
 $\theta=3.11^\circ$ )

# Spin induction in dense clusters

Spin acquired at periastron, during GW emission.

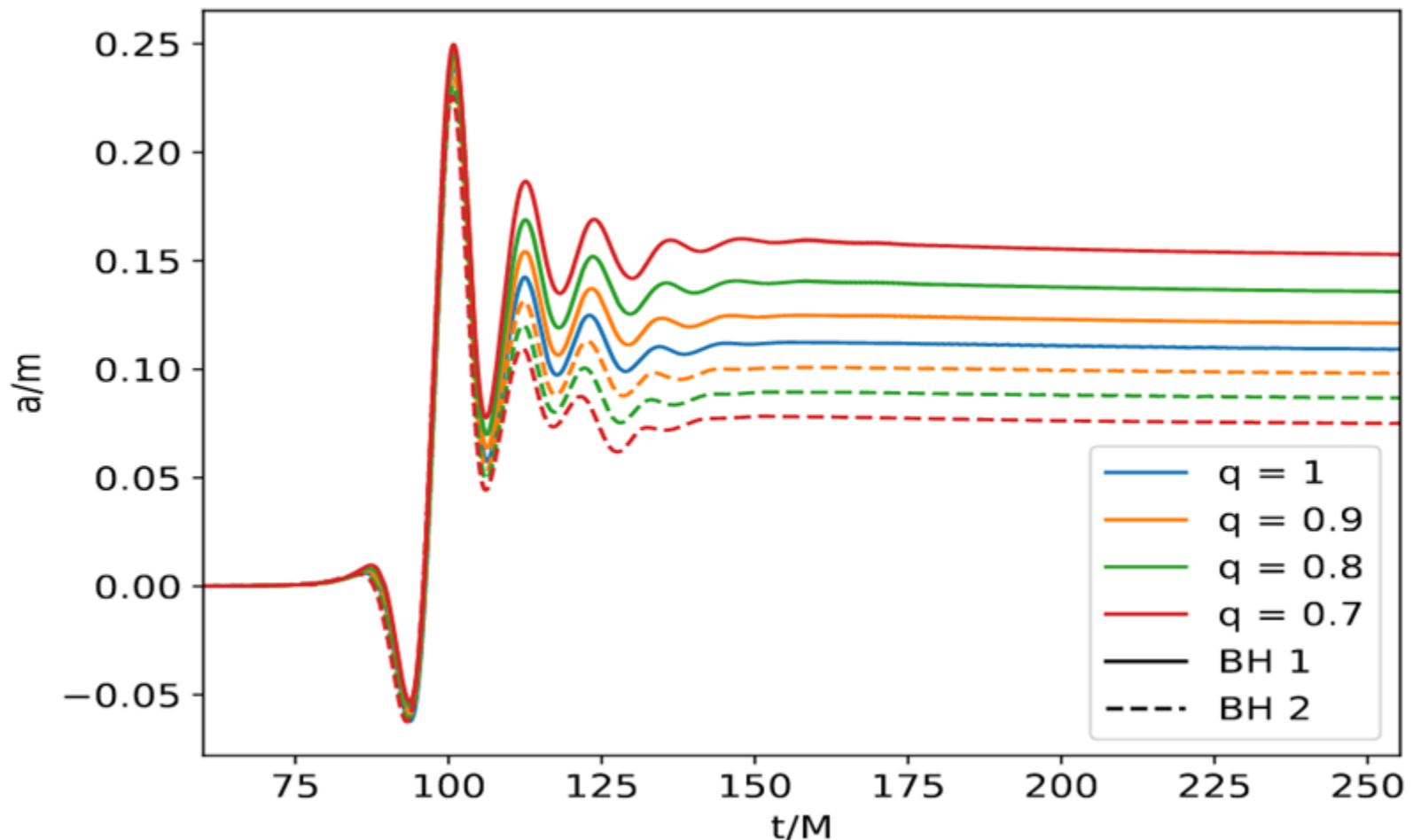
Characterized by Kerr parameter  $a$ .



# Spin induction in dense clusters

Highest spin is induced in most massive black hole.  $q = m_2/m_1 \leq 1$ .

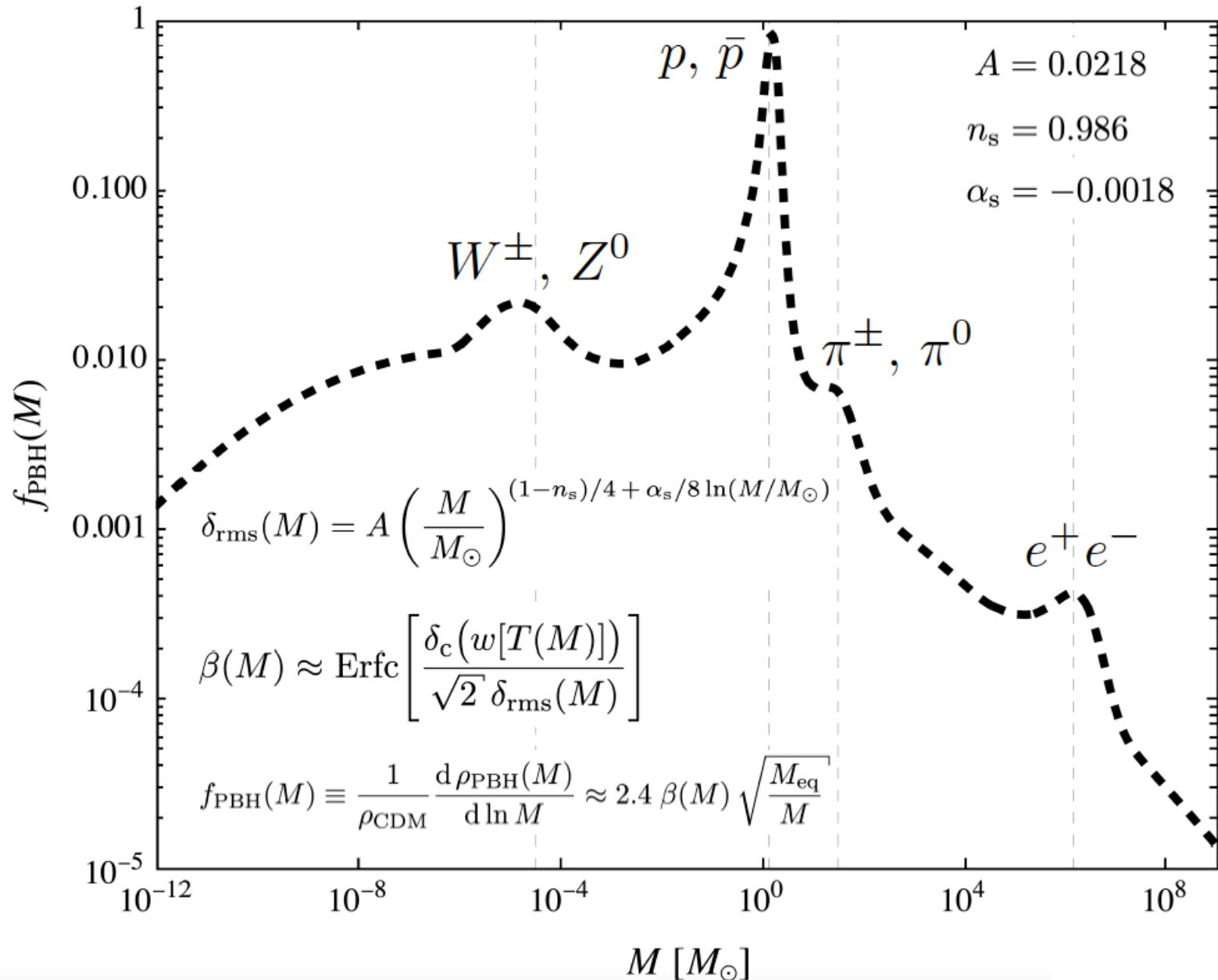
Spin induction is enhanced for the massive black hole when  $q \ll 1$ .



# Observational Evidences

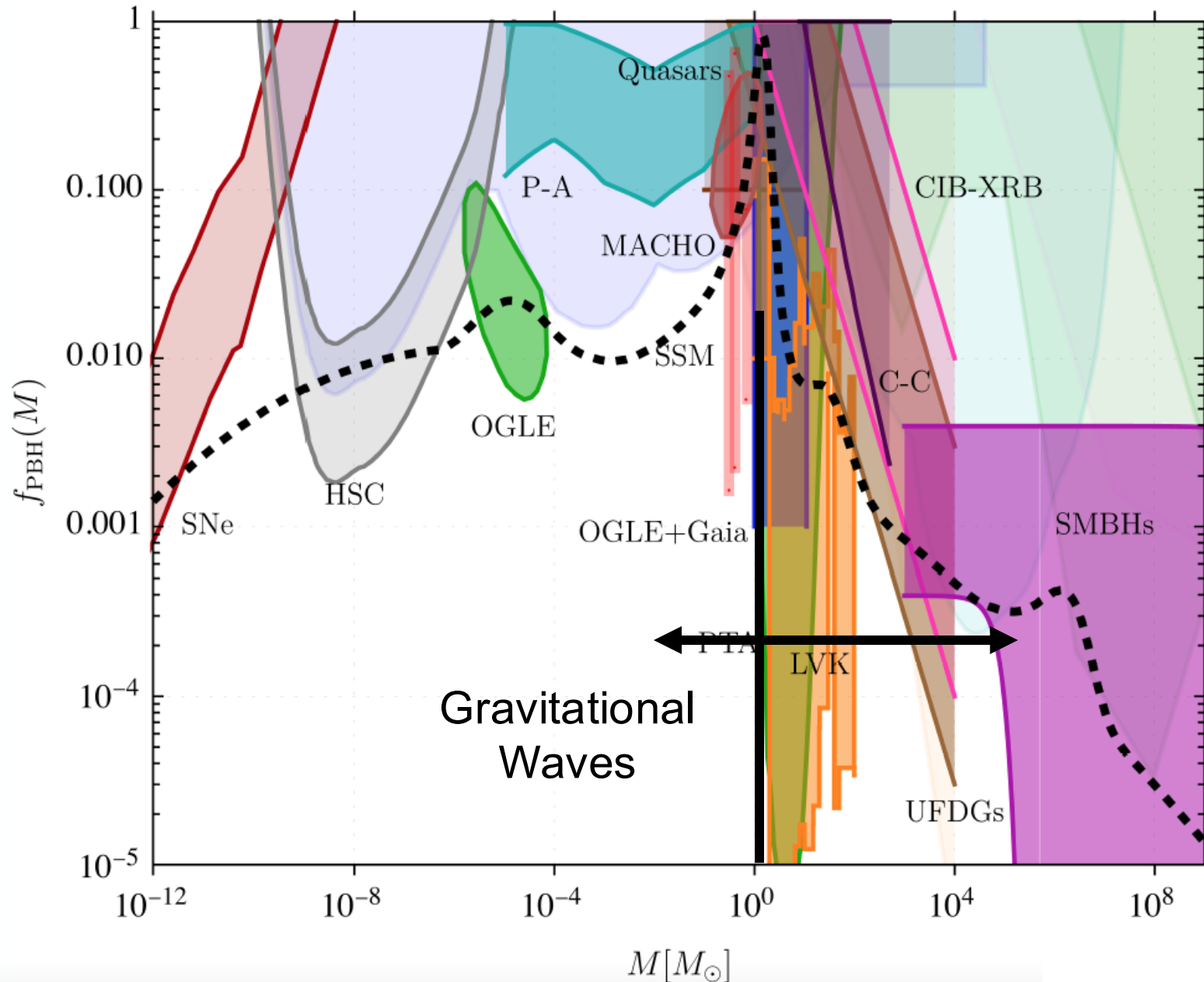
# Observational evidence for primordial black holes

Carr, Clesse, JGB, Hawkins, Kühnel [2306.03903]

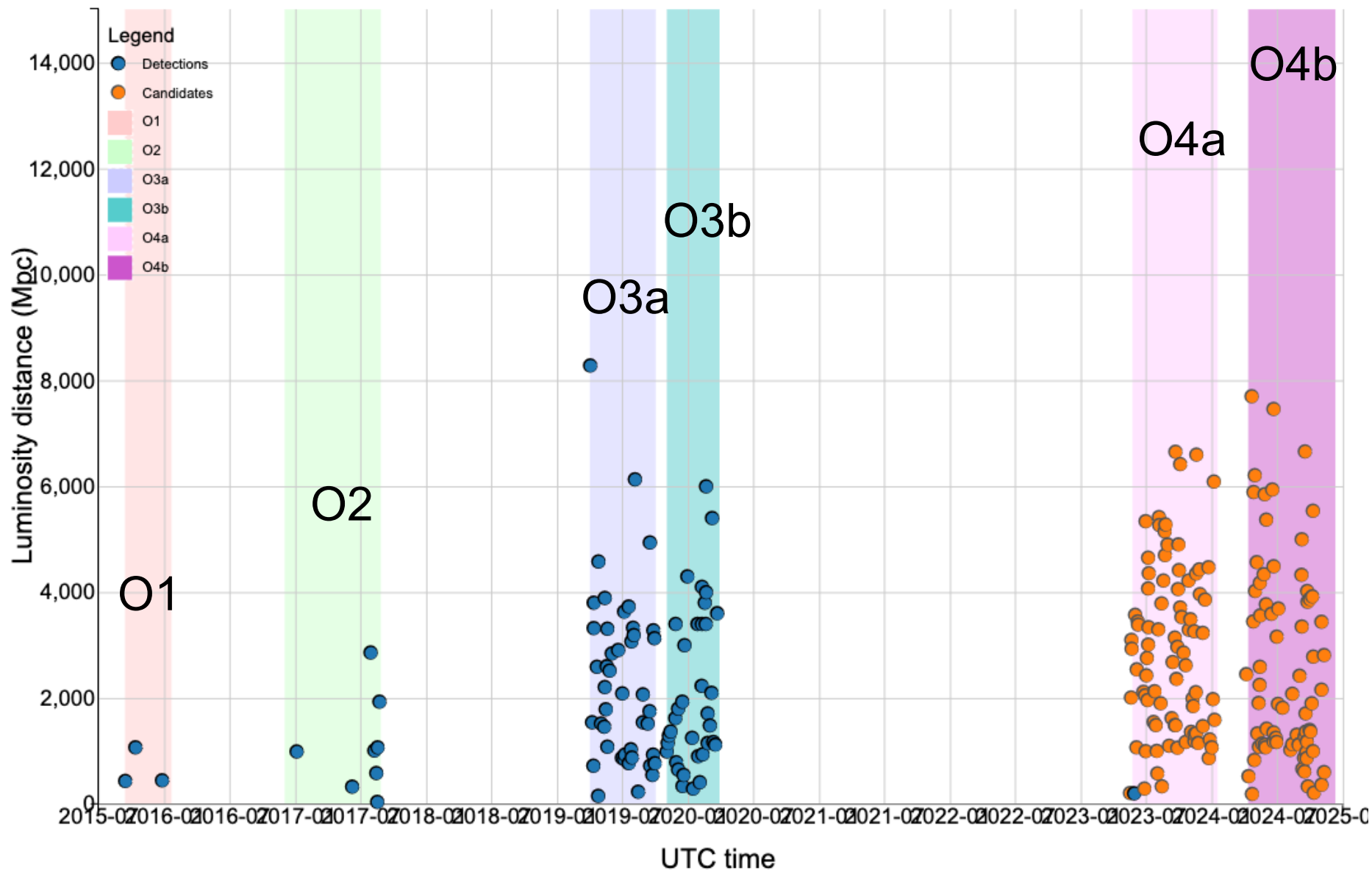


# Observational evidence for primordial black holes

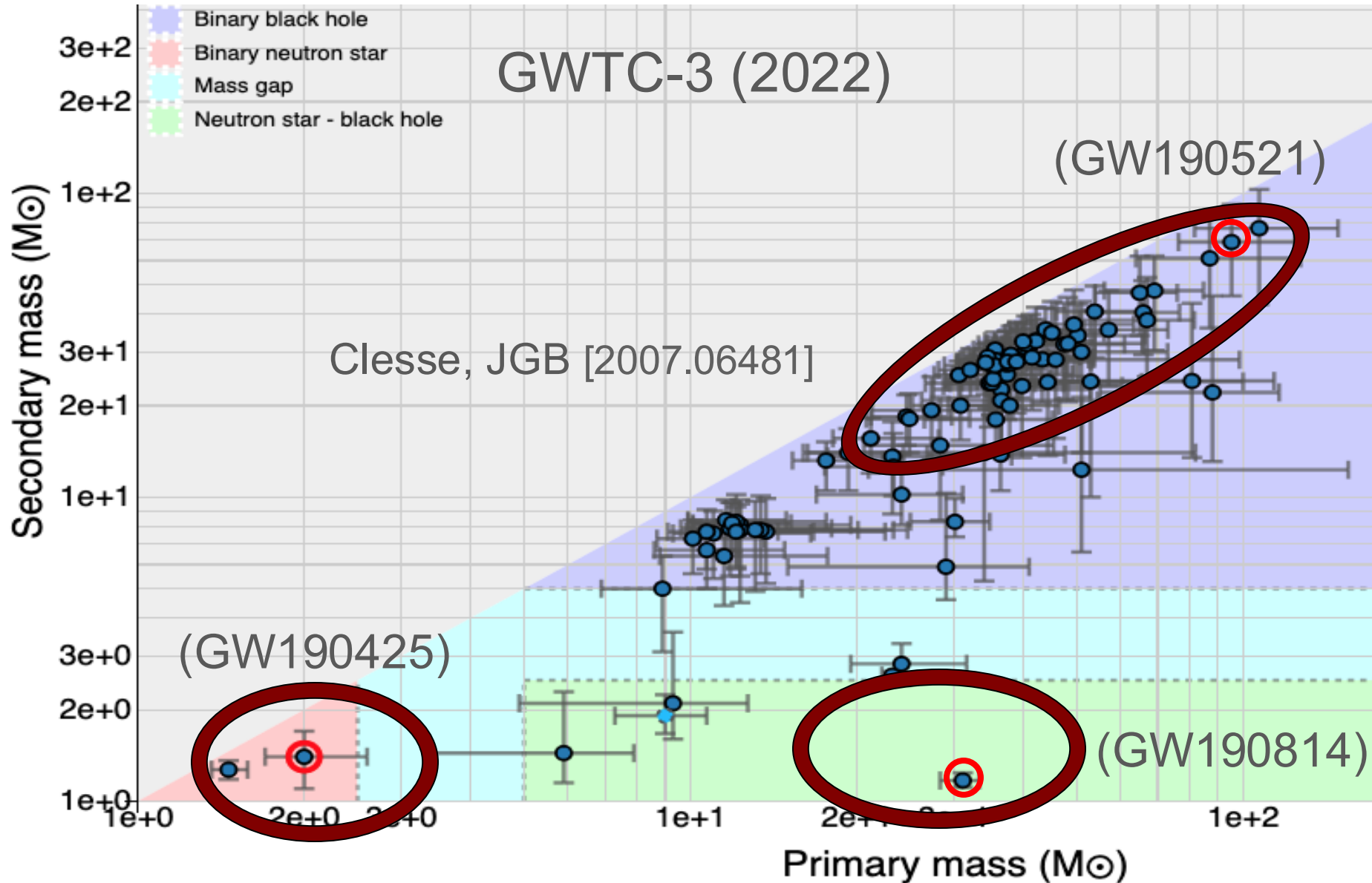
Carr, Clesse, JGB, Hawkins, Kühnel [2306.03903]



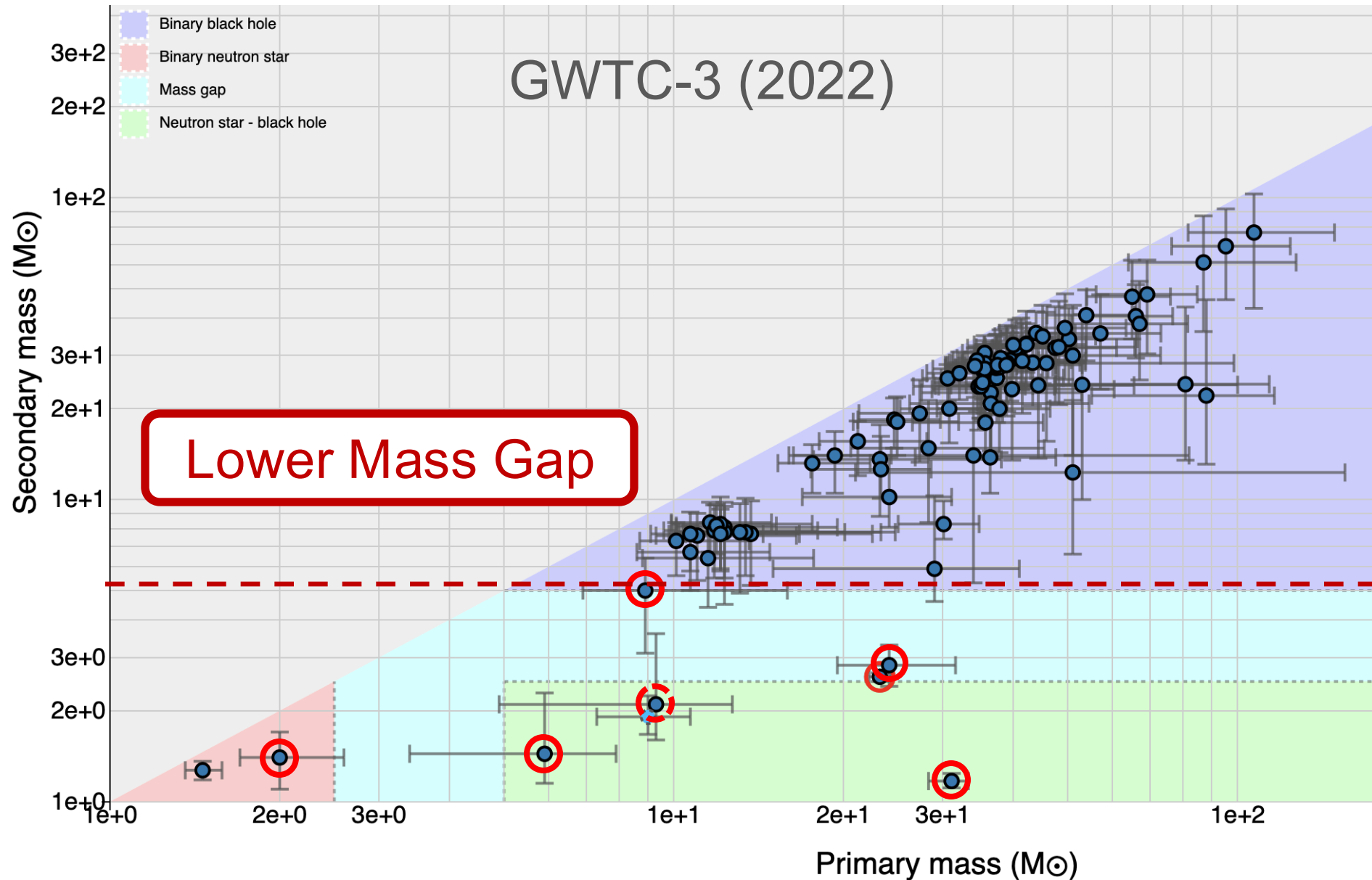
# GWTC-1/4 LVK Coll. (2024)



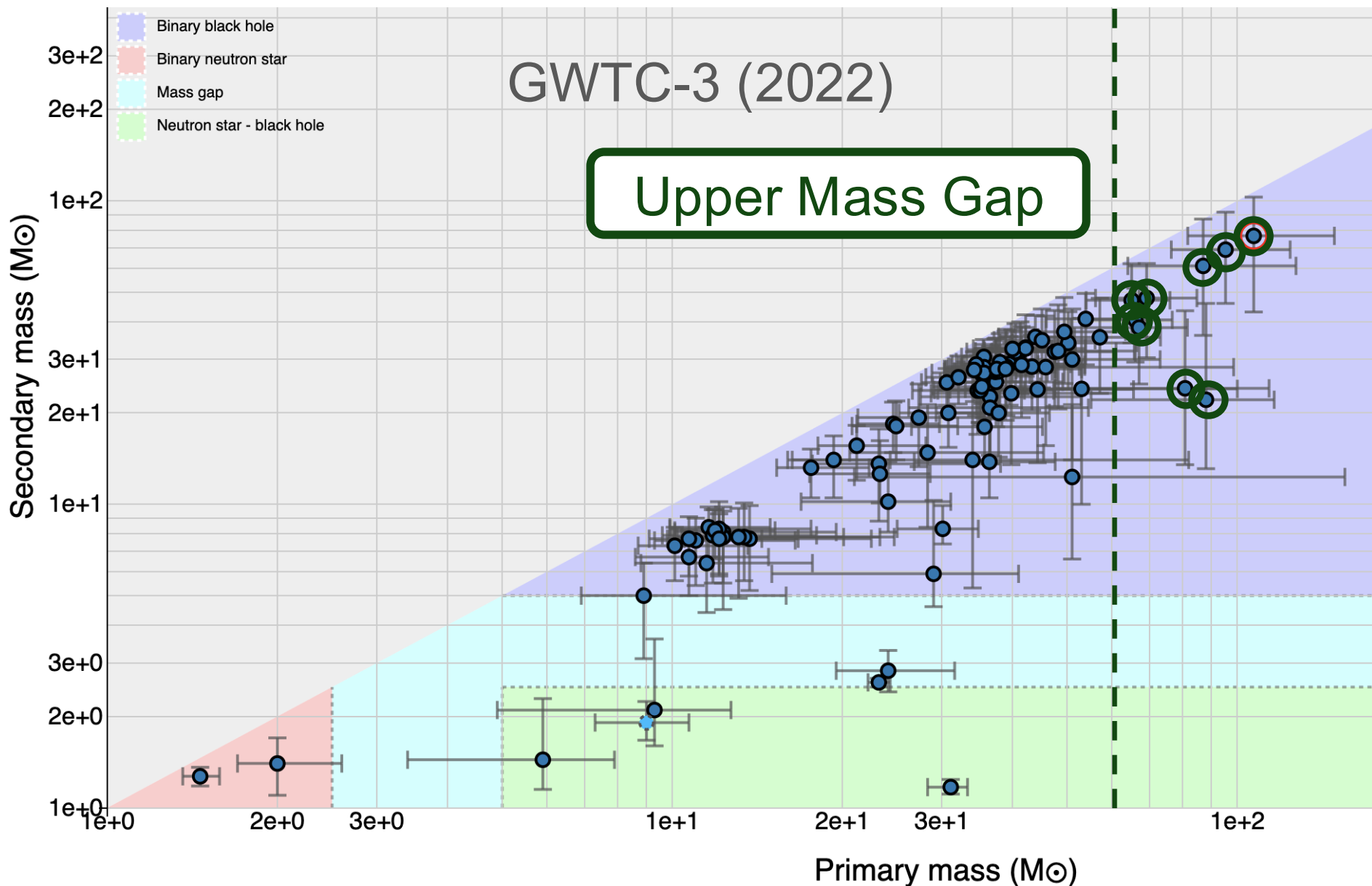
# Primary and secondary masses



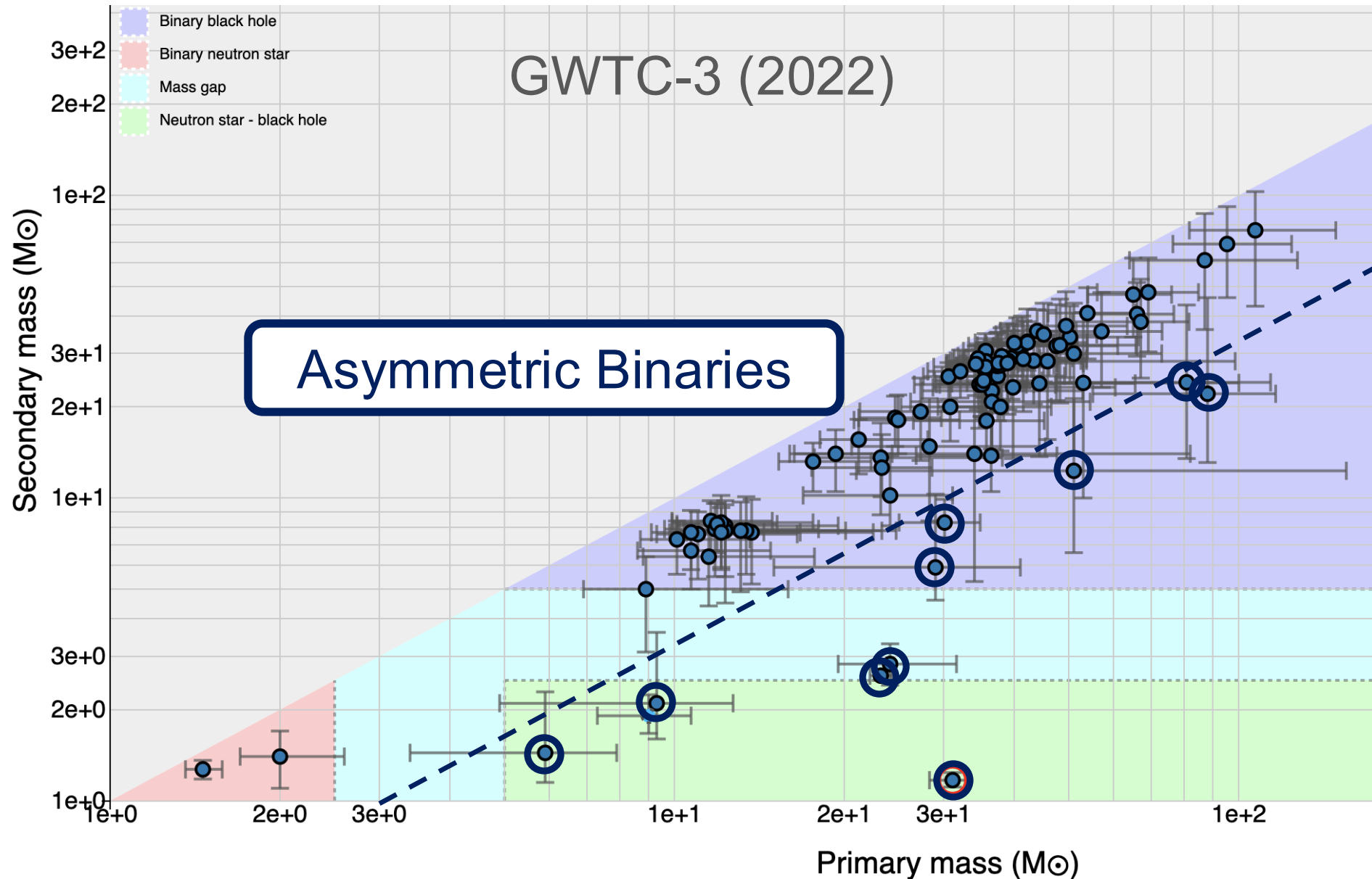
# Are LIGO/Virgo BH Primordial?



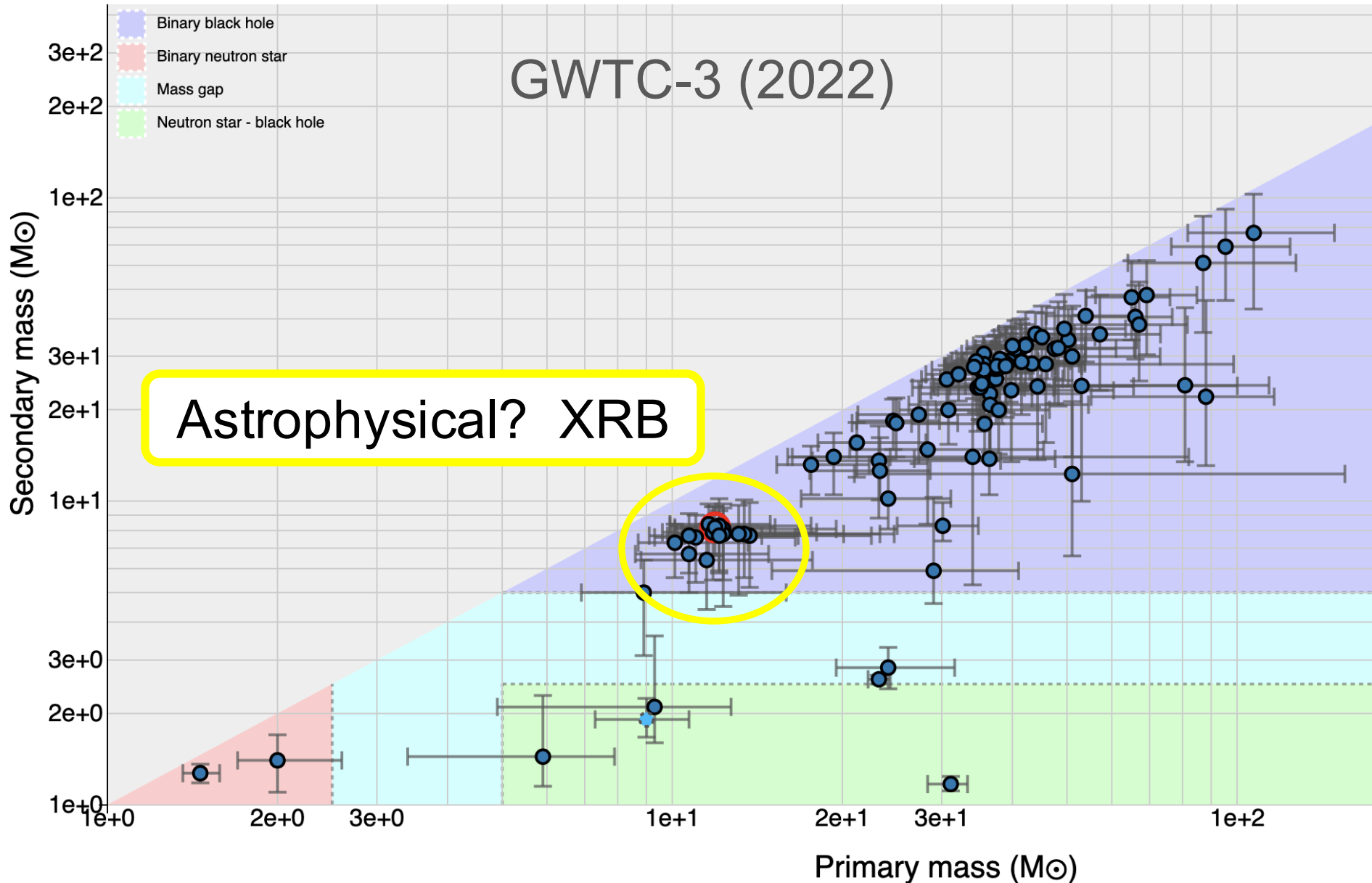
# Are LIGO/Virgo BH Primordial?



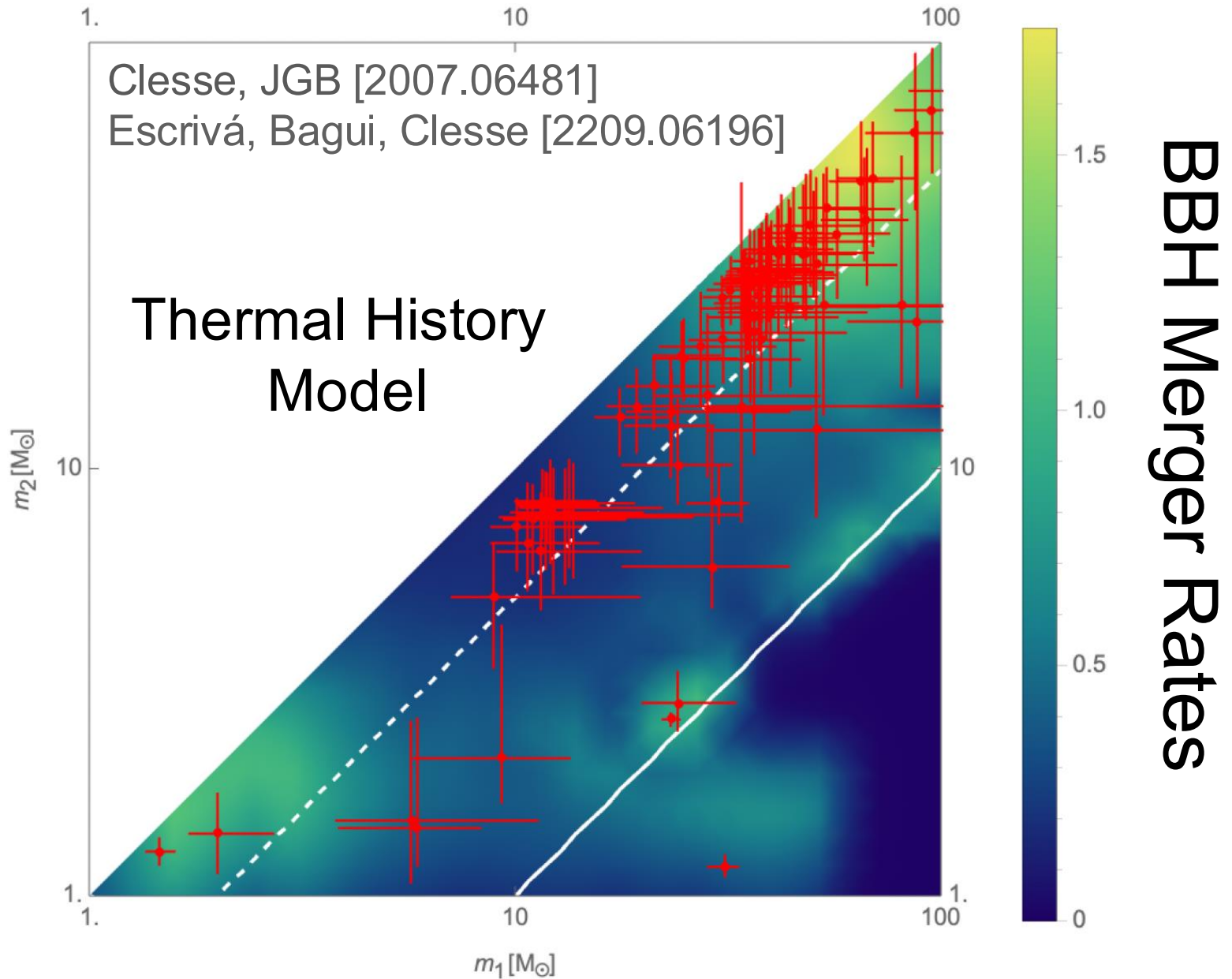
# Are LIGO/Virgo BH Primordial?



# Are LIGO/Virgo BH Primordial?

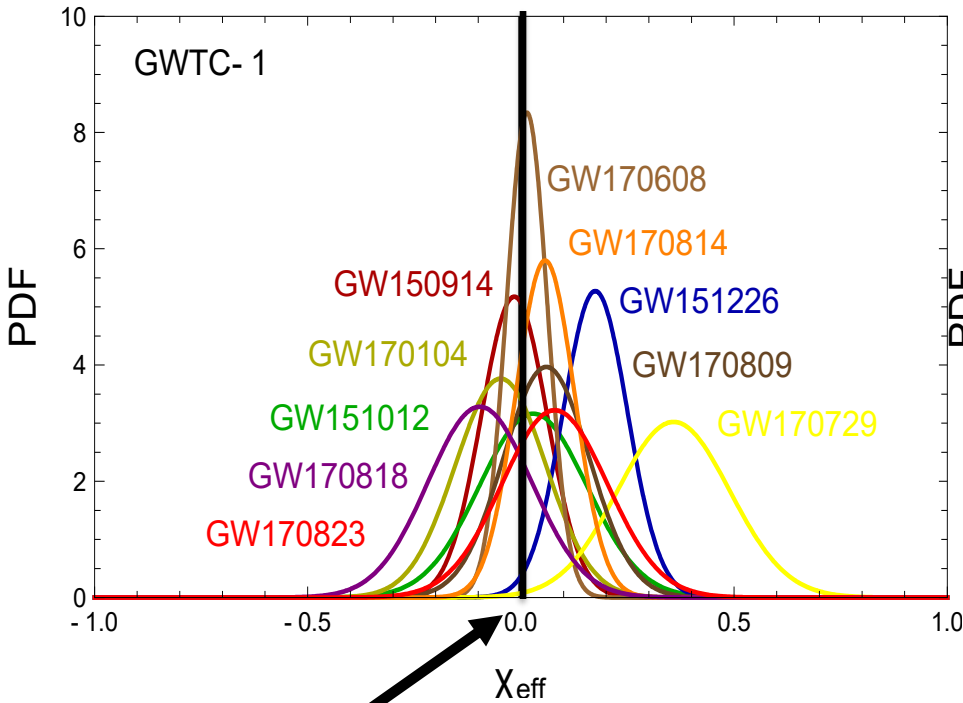


# Are LIGO/Virgo BH Primordial?

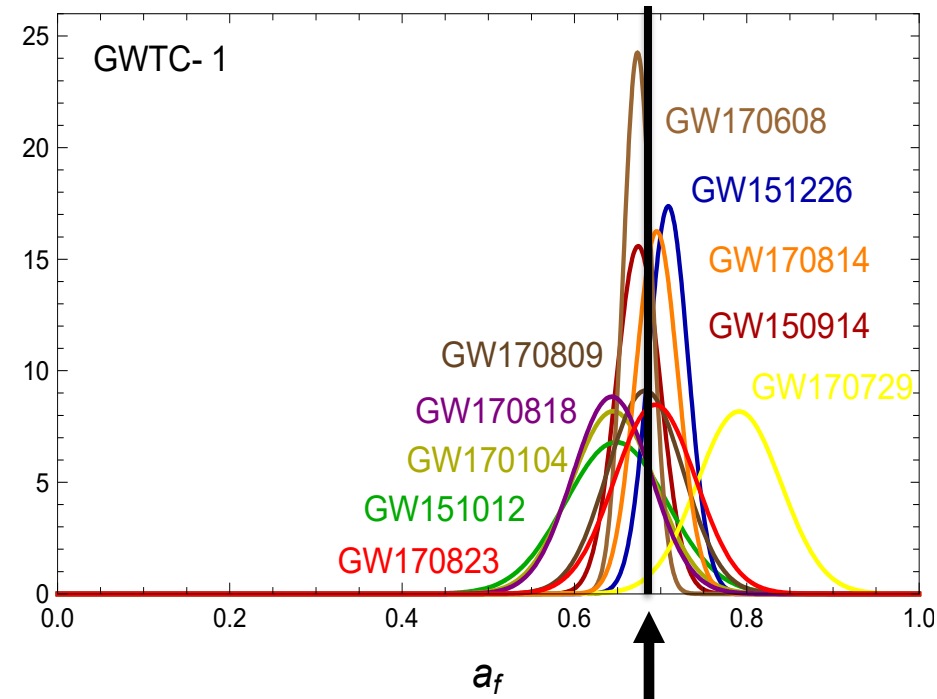


# Effective and Final Spin

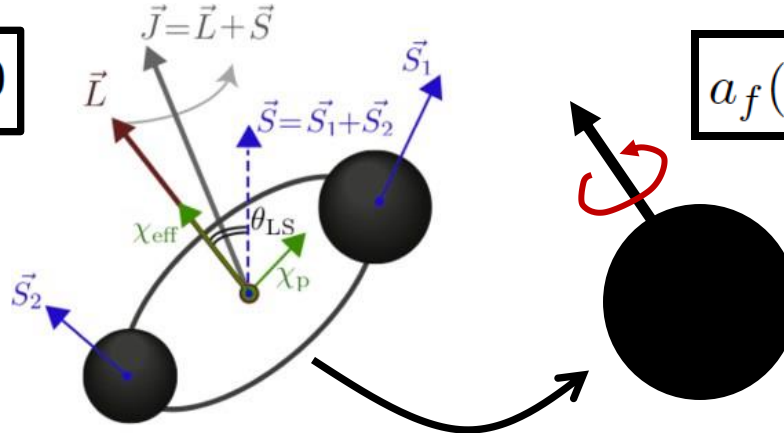
JGB – Phil.Trans.Roy.Soc.A 0091 (2019)



$$\chi_{\text{eff}}(S_1 = S_2 = 0) = 0$$

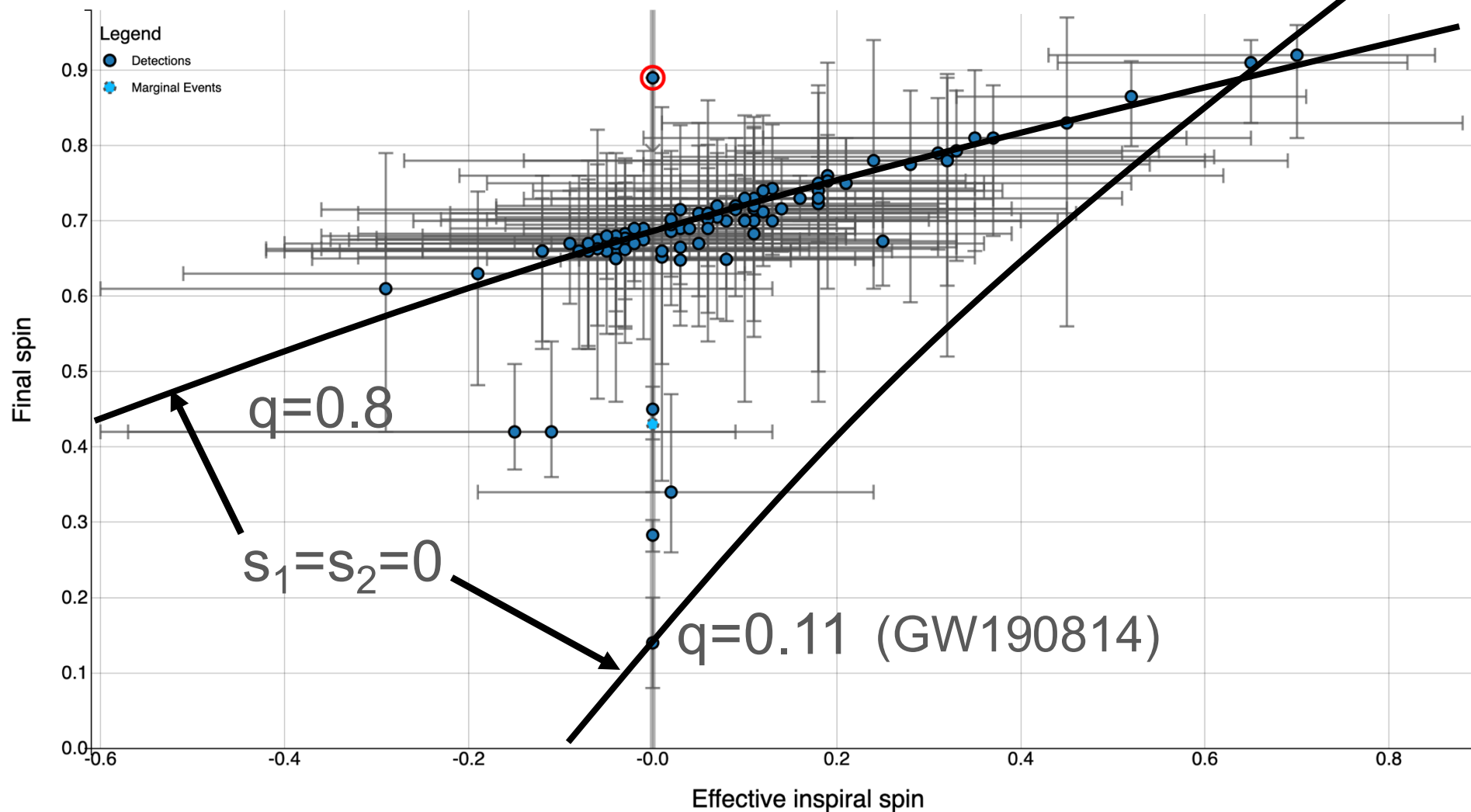


$$a_f(S_1 = S_2 = 0) = 0.686$$



# Effective and Final Spin

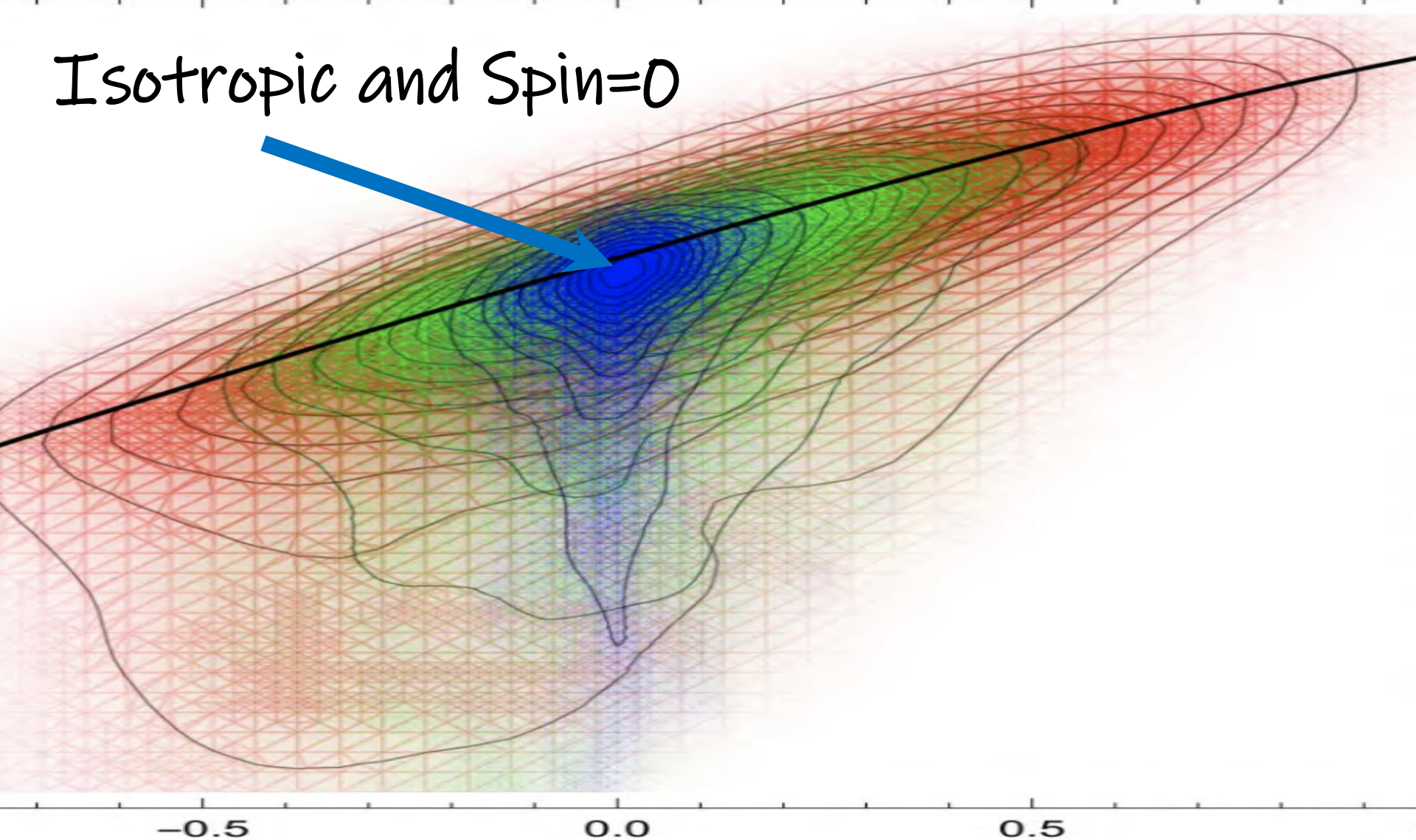
GWTC-3 (2022)



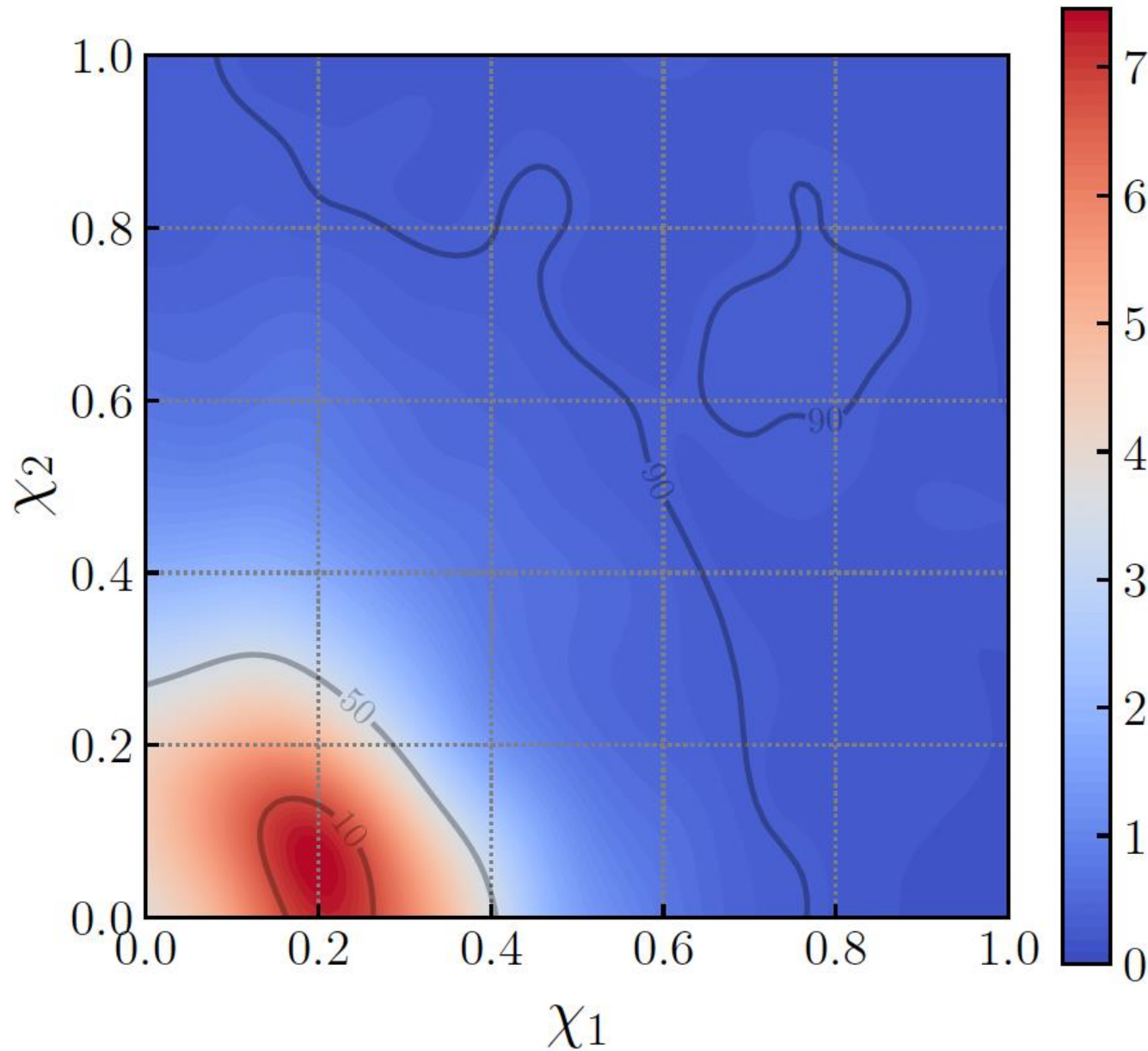
# Effective and Final Spin

JGB, Nuño-Siles, Ruiz Morales [2010.13811].

Isotropic and Spin=0

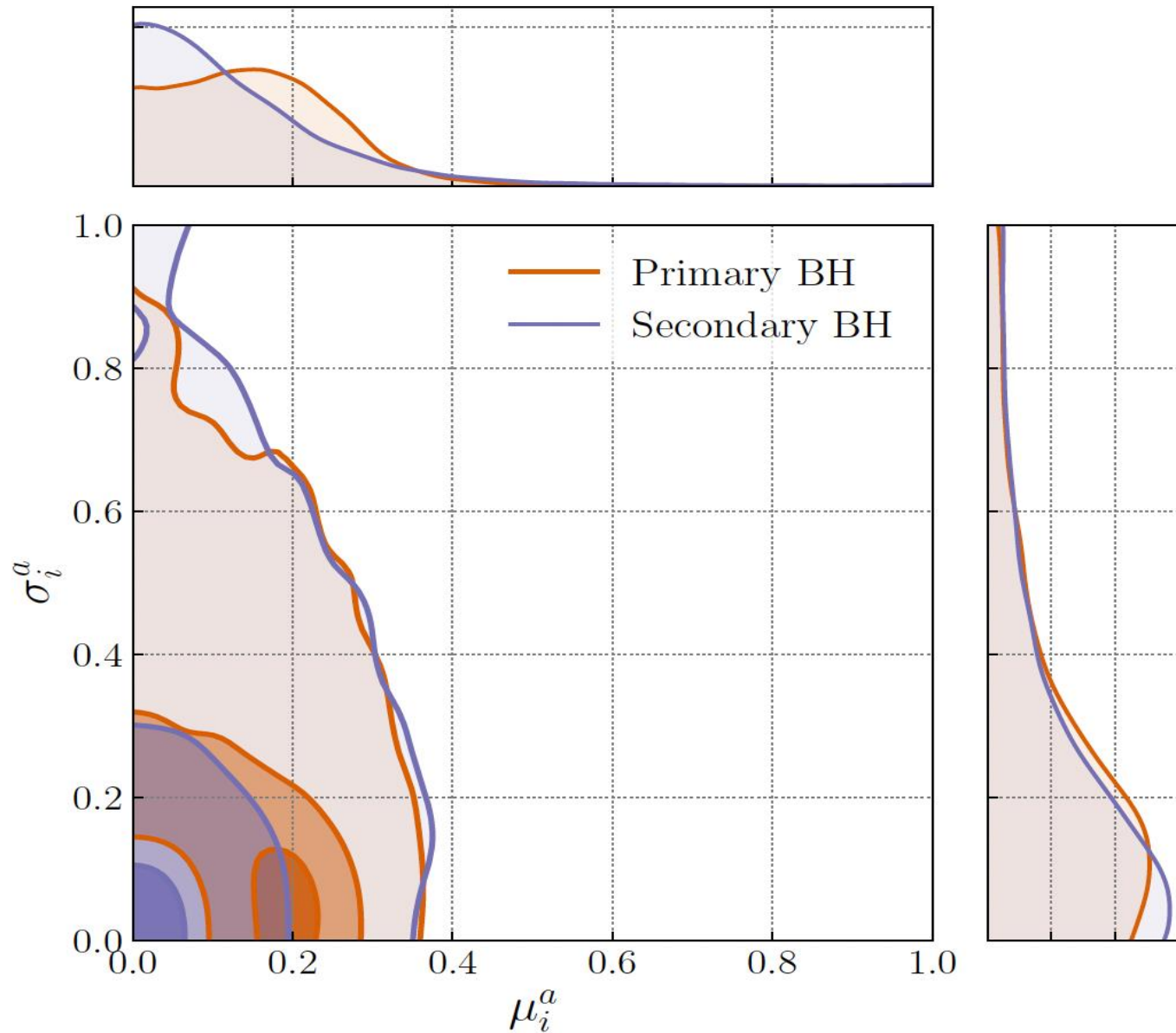


# Spin distributions GWTC-3



Hussain et al. [2411.02252]

# Spin distributions GWTC-3

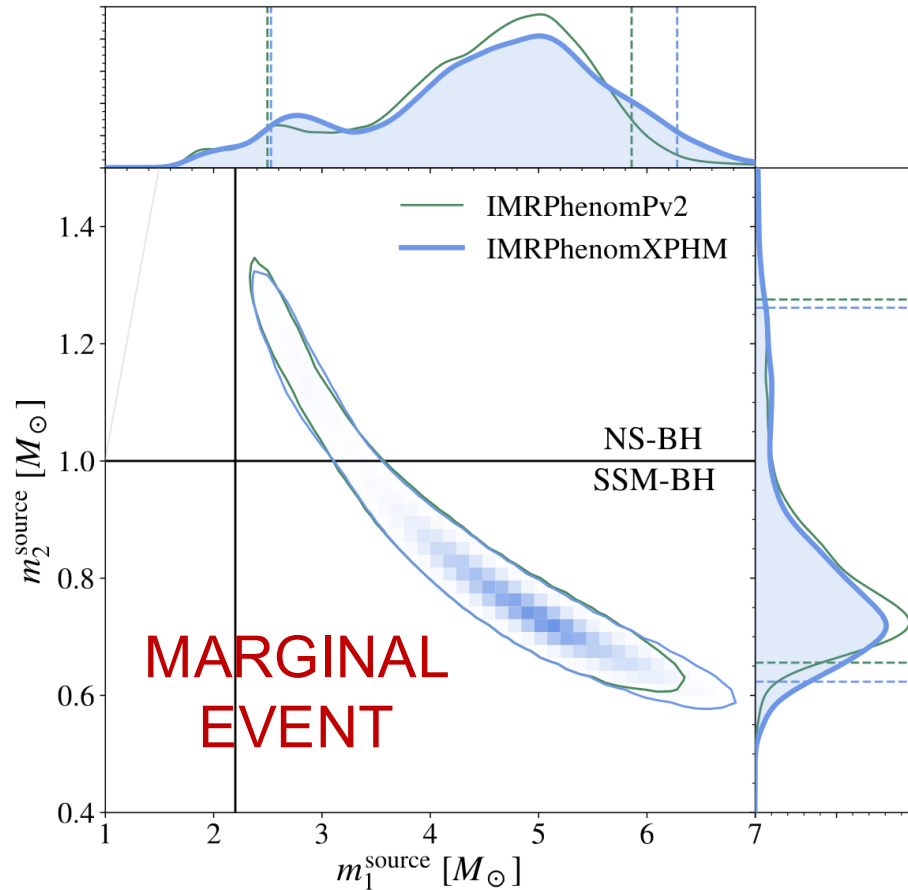


Hussain et al. [2411.02252]

# Are there PBH in LIGO/Virgo?

SSM170401

Morras et al. [2301.11619]

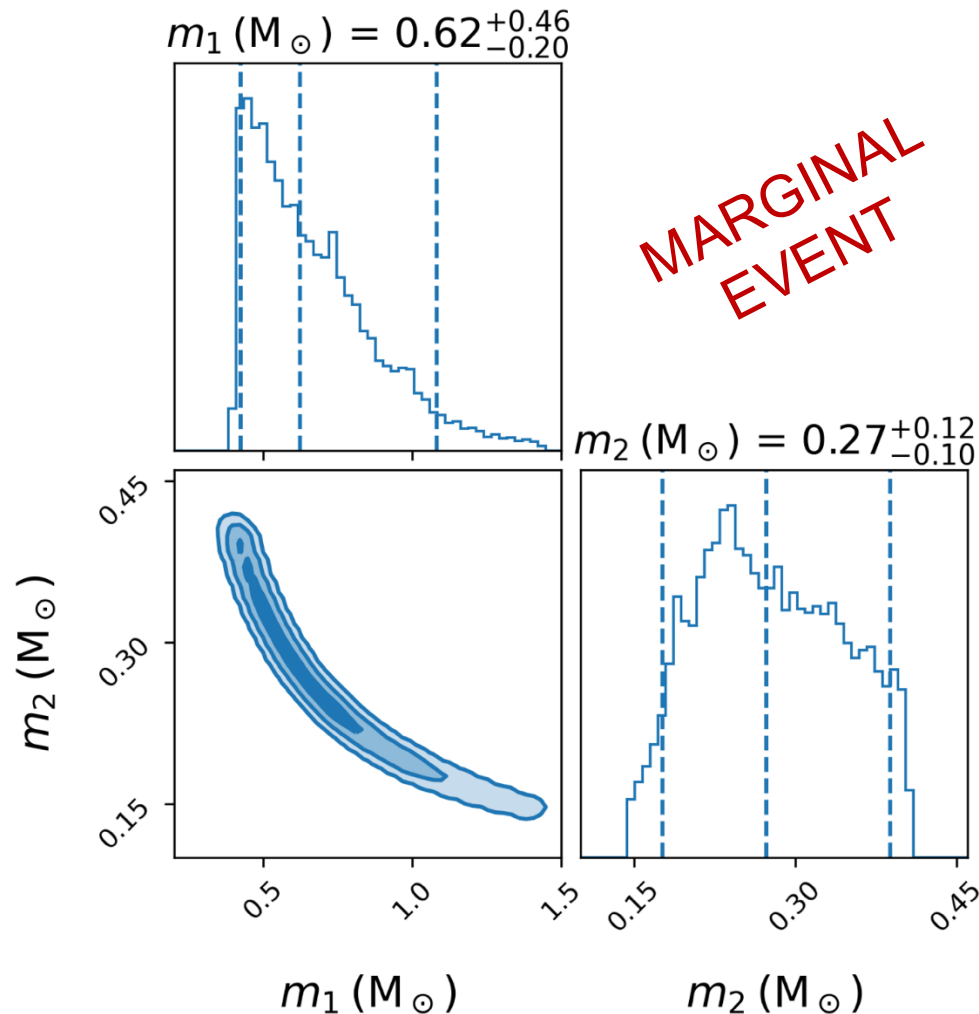


| Parameter                       | IMRPhenomPv2              | IMRPhenomXPHM             |
|---------------------------------|---------------------------|---------------------------|
| Signal to Noise Ratio           | $7.98^{+0.62}_{-1.03}$    | $7.94^{+0.70}_{-1.05}$    |
| Primary mass ( $M_{\odot}$ )    | $4.65^{+1.21}_{-2.15}$    | $4.71^{+1.57}_{-2.18}$    |
| Secondary mass ( $M_{\odot}$ )  | $0.77^{+0.50}_{-0.12}$    | $0.76^{+0.50}_{-0.14}$    |
| Primary spin magnitude          | $0.32^{+0.47}_{-0.26}$    | $0.36^{+0.46}_{-0.30}$    |
| Secondary spin magnitude        | $0.48^{+0.46}_{-0.43}$    | $0.47^{+0.46}_{-0.42}$    |
| Total mass ( $M_{\odot}$ )      | $5.42^{+1.10}_{-1.65}$    | $5.47^{+1.43}_{-1.68}$    |
| Mass ratio ( $m_2/m_1 \leq 1$ ) | $0.17^{+0.34}_{-0.05}$    | $0.16^{+0.34}_{-0.06}$    |
| $\chi_{\text{eff}}$ [51, 52]    | $-0.06^{+0.17}_{-0.32}$   | $-0.05^{+0.22}_{-0.35}$   |
| $\chi_p$ [53]                   | $0.28^{+0.34}_{-0.21}$    | $0.33^{+0.33}_{-0.26}$    |
| Luminosity Distance (Mpc)       | $119^{+82}_{-48}$         | $124^{+82}_{-48}$         |
| Redshift                        | $0.028^{+0.018}_{-0.010}$ | $0.028^{+0.017}_{-0.011}$ |
| Ra ( $^{\circ}$ )               | $-2^{+34}_{-35}$          | $-1^{+34}_{-37}$          |
| Dec ( $^{\circ}$ )              | $47^{+14}_{-26}$          | $46^{+14}_{-29}$          |
| Final mass ( $M_{\odot}$ )      | $5.34^{+1.11}_{-1.70}$    | $5.40^{+1.45}_{-1.73}$    |
| Final spin                      | $0.39^{+0.24}_{-0.07}$    | $0.42^{+0.22}_{-0.10}$    |
| $P(m_2 < 1 M_{\odot})$          | 85%                       | 84%                       |

# Are there PBH in LIGO/Virgo?

SSM200308

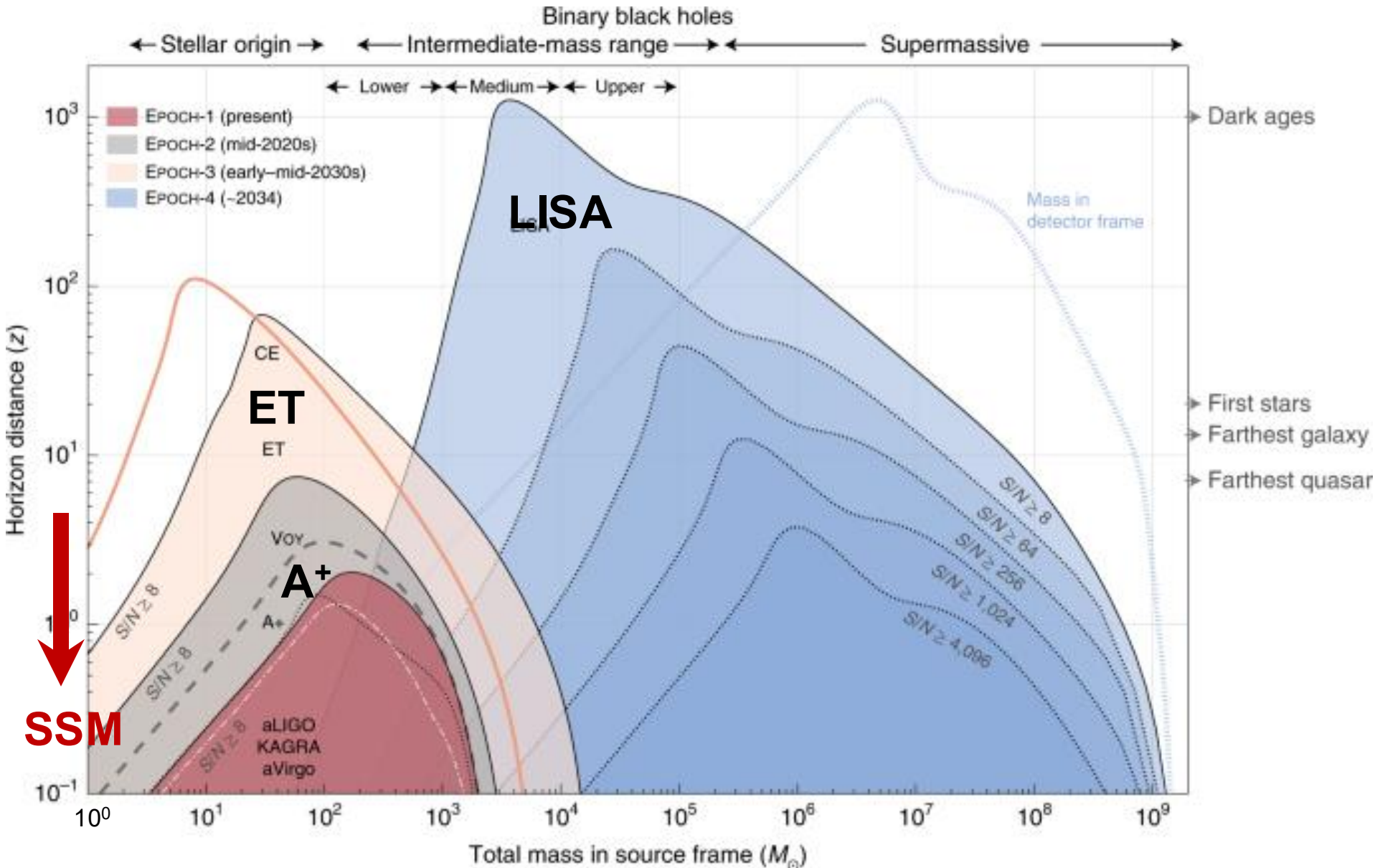
Prunier et al. [2311.16085]



Parameter

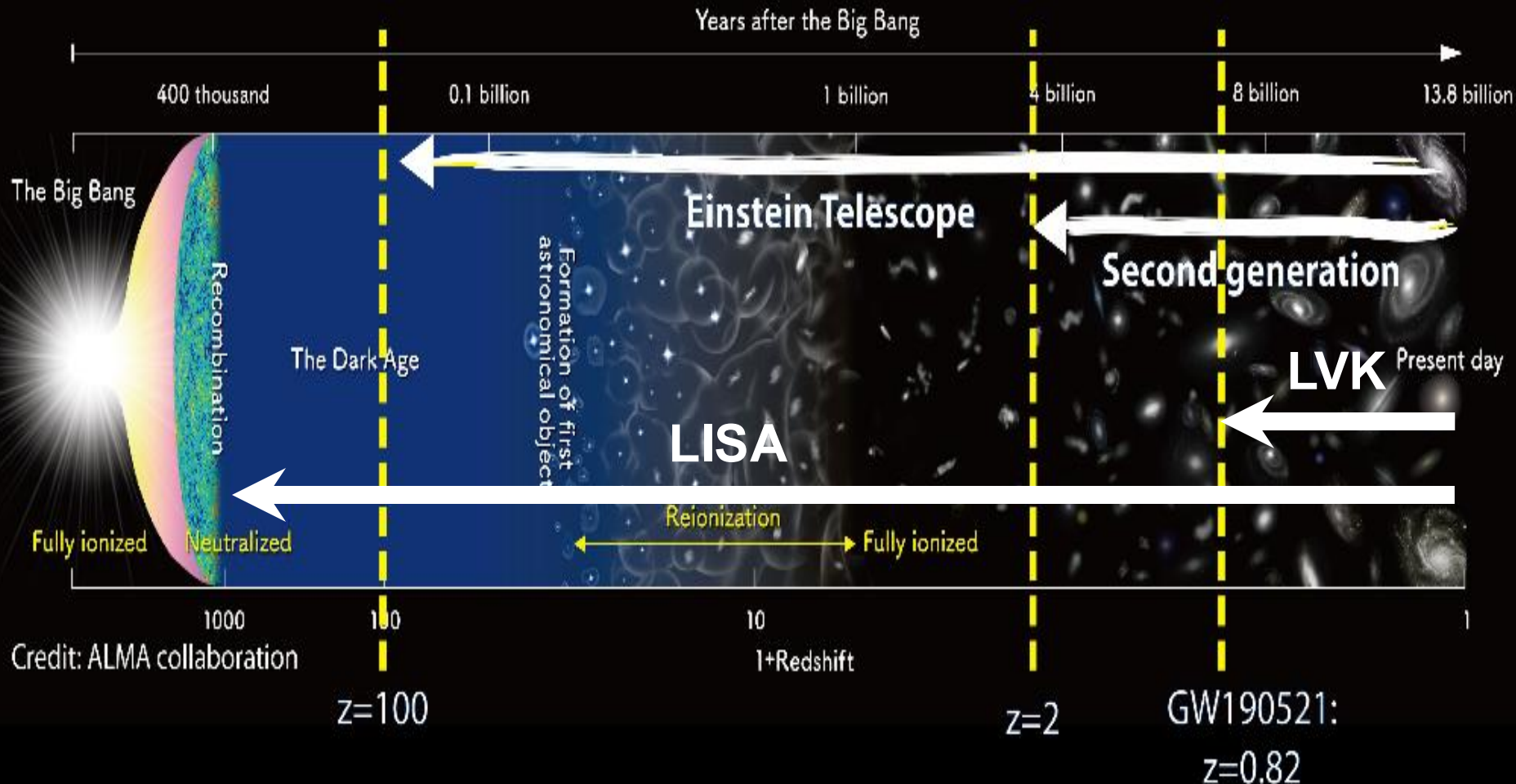
|                                         |                              |
|-----------------------------------------|------------------------------|
| Matched Filter SNR                      | $8.02^{+0.49}_{-0.85}$       |
| Primary mass ( $M_\odot$ )              | $0.62^{+0.46}_{-0.20}$       |
| Secondary mass ( $M_\odot$ )            | $0.27^{+0.12}_{-0.10}$       |
| Primary spin magnitude                  | $0.66^{+0.13}_{-0.25}$       |
| Secondary spin magnitude                | $0.44^{+0.33}_{-0.39}$       |
| Total mass ( $M_\odot$ )                | $0.88^{+0.35}_{-0.08}$       |
| Detector-frame chirp mass ( $M_\odot$ ) | $0.3527^{+0.0003}_{-0.0001}$ |
| Mass ratio ( $m_2/m_1 \leq 1$ )         | $0.44^{+0.48}_{-0.28}$       |
| $\chi_{\text{eff}}$ [27, 28]            | $0.41^{+0.08}_{-0.04}$       |
| $\chi_p$ [29]                           | $0.37^{+0.24}_{-0.24}$       |
| Luminosity Distance (Mpc)               | $90^{+43}_{-39}$             |
| Redshift                                | $0.02^{+0.01}_{-0.01}$       |
| $P(m_1 < 1 M_\odot)$                    | 92%                          |
| $P(m_2 < 1 M_\odot)$                    | 100%                         |

# BBH sensitivity in future G3 GW



# The future of GW (G3)

## Detection horizon for black-hole binaries



# Conclusions

- Quantum diffusion inevitably generates PBH
- Thermal history predicts PBH with multimodal mass distribution  $\sim 10^{-5}, 1, 100, 10^6 M_{\odot}$  ( $10^{-10} M_{\odot}$  also?)
- The predicted PBH spin and mass distribution has been measured by LIGO/Virgo + OGLE/Gaia around  $1-100 M_{\odot}$  (features: peak & plateau)
- Other peaks could be explored with microlensing of stars
- PBH scenario can explain various cosmic conundra (LSS)
- Paradigm shift in Structure Formation of the Universe
- Very rich phenomenology: multi-scale, multi-epoch, multi-probe  $\Rightarrow$  Future G3 detectors (ET, CE, LISA)