



SCALAR BACKREACTION IN SPECTATOR CHROMO NATURAL INFLATION

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THE DAWN OF GRAVITATIONAL WAVE COSMOLOGY – BENASQUE

TO APPEAR SOON ON ARXIV

ALP and Gauge Fields

WHY AXIONS?

- THEORETICALLY WELCOMED IN MANY EXTENSIONS OF THE STANDARD MODEL
- THEY NATURALLY COUPLE TO GAUGE FIELDS

WHY AXIONS DURING INFLATION?

- PREVENTING LOOP CORRECTIONS TO THE INFLATON MASS (SHIFT SYMMETRY)
- NATURAL WAY TO REALIZE THE SLOW-ROLL (IN THE MINIMAL CNI MODEL)
- SUPPORTING RICH PHENOMENOLOGY (CHIRAL GW, NON-GAUSSIANITIES, PBH ...)

Freese et al. : PRL - 65 (1990) 3233 - 3236

The Spectator Chromo Natural Inflation

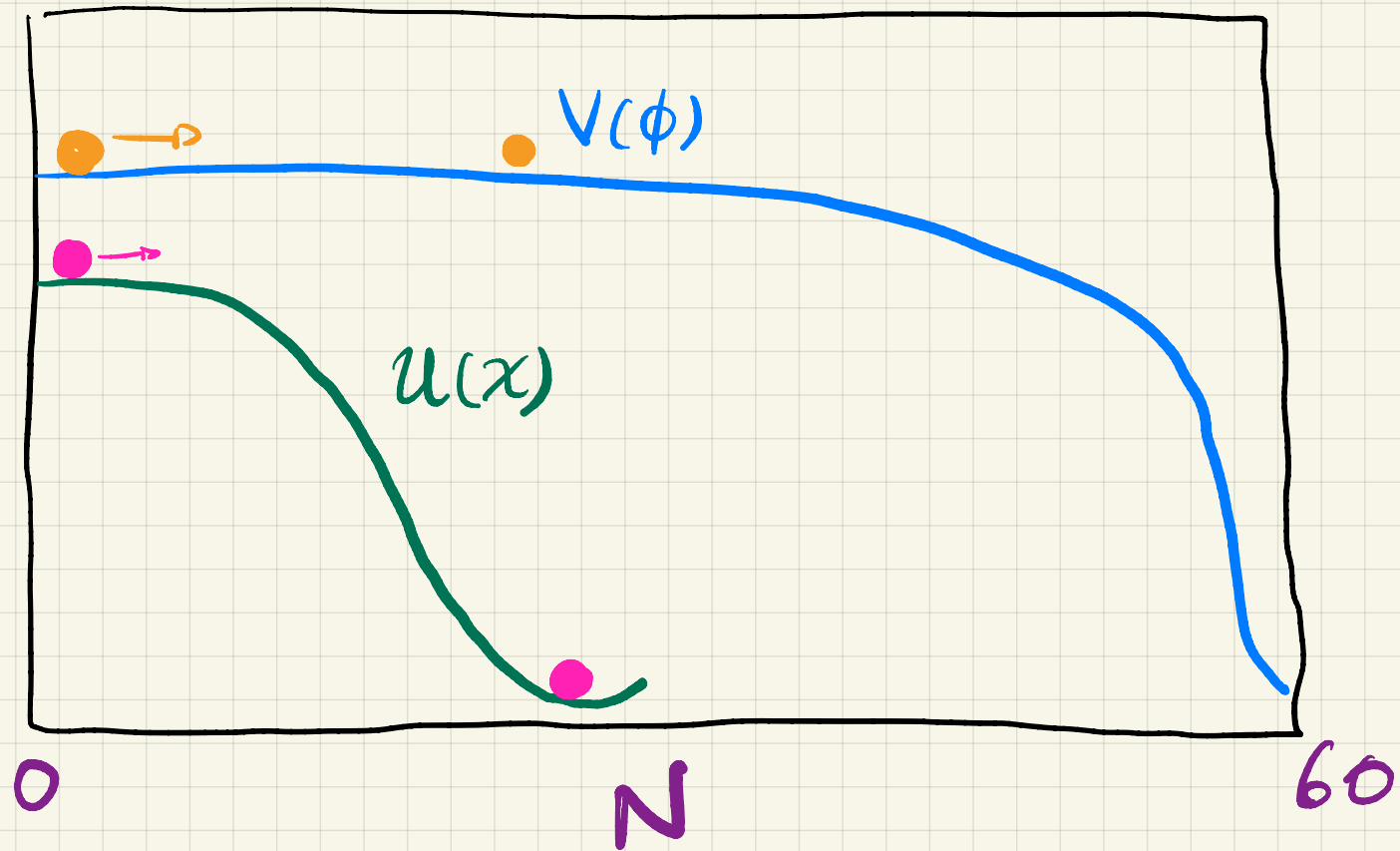
$$\mathcal{S}_{\text{SCNI}} = \int d^4x \left[\frac{M_{\text{Pl}}^2}{2} \mathcal{R} + \mathcal{L}_\phi - \frac{1}{2} (\partial\chi)^2 - U(\chi) + \right. \\ \left. - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + \frac{\lambda \chi}{4f} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \right]$$

Inflation (points to $\mathcal{L}_\phi$)
ALP (points to χ in $(\partial\chi)^2$ and $U(\chi)$)
The Model Parameters (points to f, g, λ)

where:

$$\begin{cases} U(\chi) = \mu^4 \left[1 + \cos\left(\frac{\chi}{f}\right) \right] \\ F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a - g \epsilon^{abc} A_\mu^b A_\nu^c \end{cases}$$

Our Set-up



- The Axion decays well before the end of Inflation
- It Triggers a tachyonic instability inside the horizon

The background Dynamics : No Back reaction YET

The isotropic configuration : $A_0^a = 0$, $A_i^a = \delta_i^a(t) Q(t)$

ALP equation : $\ddot{\chi} + 3H\dot{\chi} + \partial_{\chi} u + \frac{3g\lambda}{f} Q^2 (\dot{Q} + HQ) = 0$

Q evolution : $\ddot{Q} + 3H\dot{Q} + (\dot{H} + 2H^2)Q + gQ^2 \left(2gQ - \frac{\lambda\dot{\chi}}{f} \right) = 0$

Relevant Functions

$$m_Q \equiv 2 \frac{Q}{H}$$

$$\xi = \frac{\lambda\dot{\chi}}{f 2H}$$

$$\Lambda = \frac{\lambda}{f} Q$$

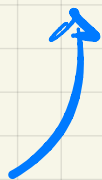
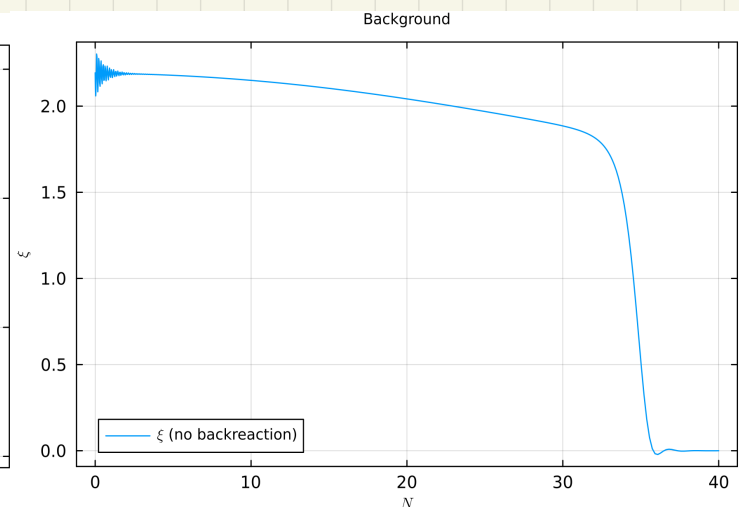
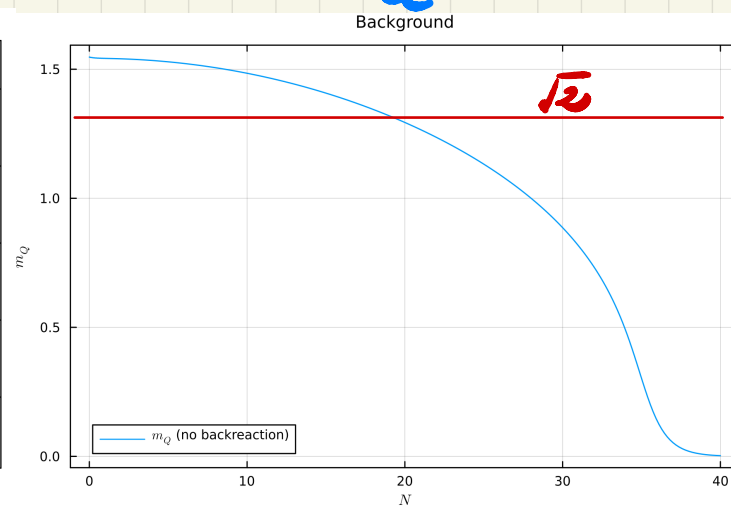
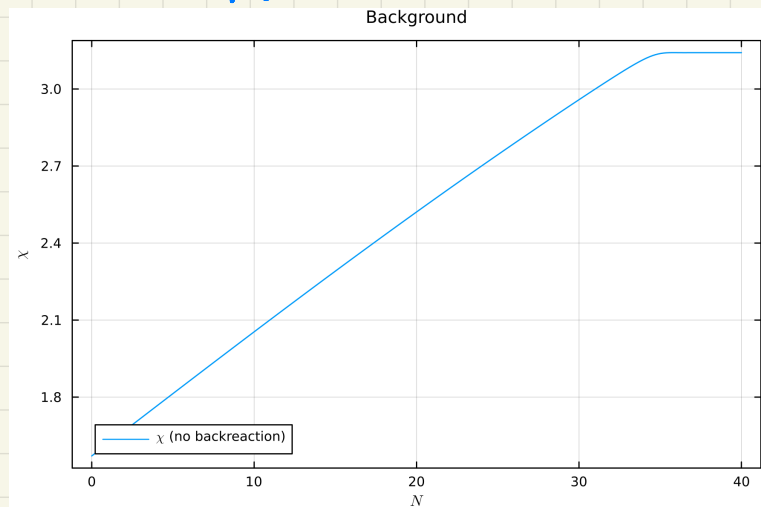
$$\xi \simeq \frac{1}{m_Q} + m_Q$$

Evolution of the Relevant Functions : NO BR YET

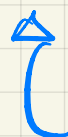
ALP

m_Q

ξ



Reaches the
Minimum of the
Potential and
Stabilize



Typical “Bell”
shape



$m_Q < \sqrt{2} \Rightarrow$ tachyonic instability
for the scalar perturbations



The particle
production
function goes to
zero rapidly

The Perturbations

The Scalars

$$(X, Z, \phi, \Phi)$$

gauge sector perturbations

Inflaton Perturbation

The Tensors

$$(T_{R/L}, \psi_{R/L})$$

gauge tensor modes

Gravitational Waves

Impact of the Perturbations on the Background

$$\ddot{\chi} + 3H\dot{\chi} + 2_{\chi}u + \frac{3g\lambda Q^2}{f}(\dot{Q} + HQ) + \mathcal{B}_{\chi} = 0$$

$$\ddot{Q} + 3H\dot{Q} + (\dot{H} + 2H^2)Q + gQ^2\left(2gQ - \frac{\lambda\dot{\chi}}{f}\right) + \mathcal{B}_Q = 0$$

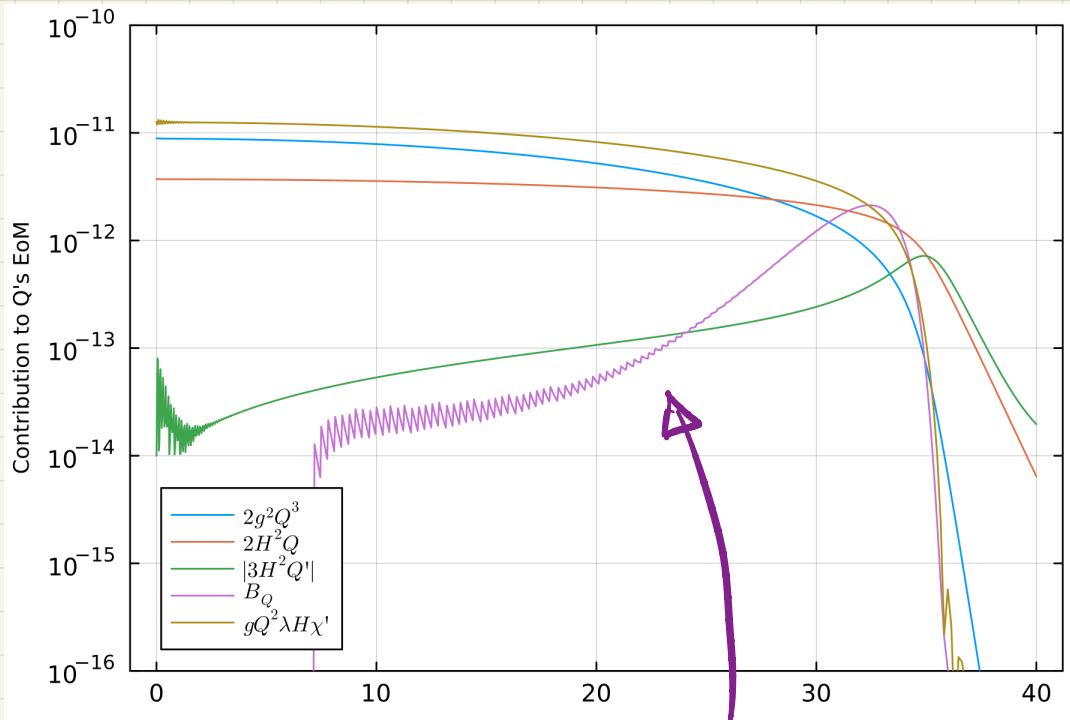
$$\mathcal{B}_{\chi} = \frac{V^{(3)}(\chi)}{2a^2} \int \frac{d^3k}{(2\pi)^3} |\hat{X}(\tau, k)|^2$$

$$\mathcal{B}_Q = \frac{2g\Lambda^3 m_Q}{3a^2} \int \frac{d^3k}{(2\pi)^3} \frac{k^2(k^2 + a^2 H^2 m_Q^2)}{(k^2 + 2a^2 H^2 m_Q^2)^2} |\hat{X}(\tau, k)|^2$$

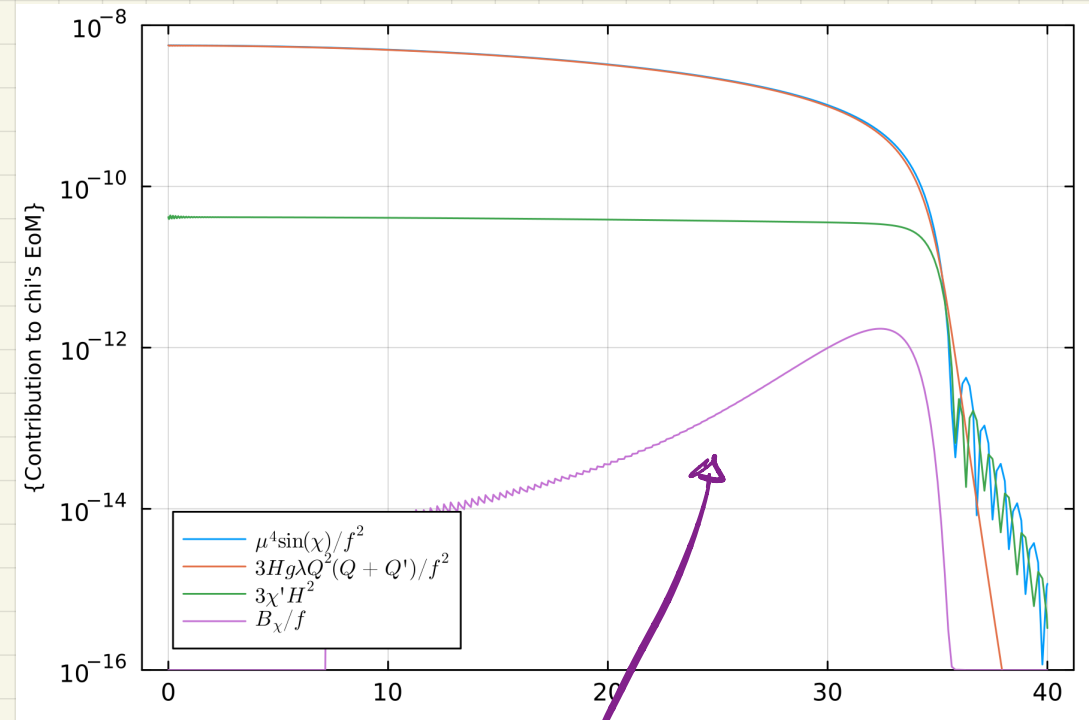
Preliminary evolution of the ~~scalar~~ Backreaction

Q 's EoM

χ 's EoM



$\mathcal{B}_Q$



$\mathcal{B}_\chi$

* In this run we are not including the Backreaction

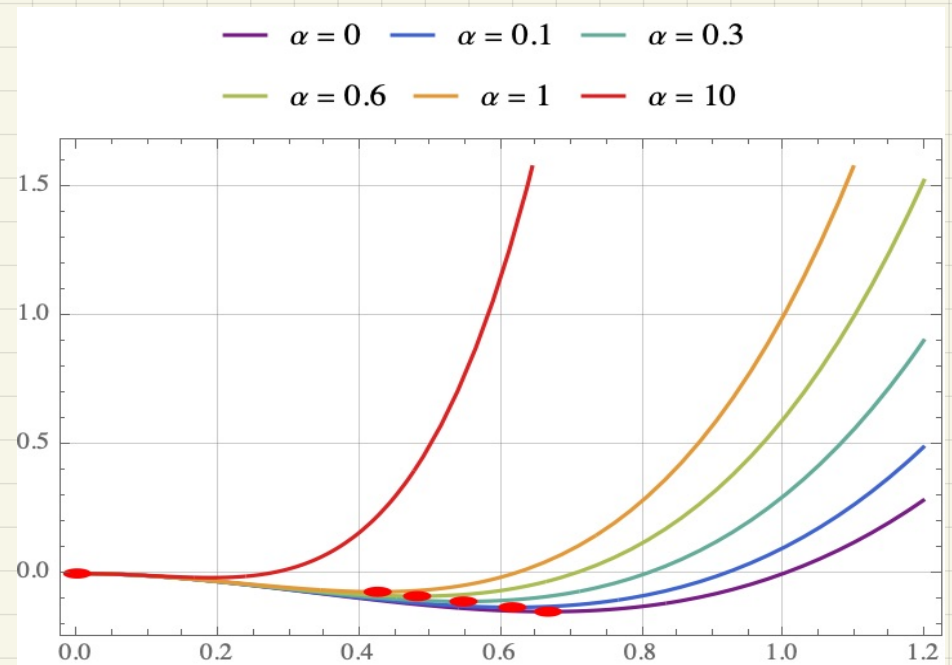
Let's train our intuition on Backreaction

$$Q \text{ equation } \approx \dot{Q} + \frac{\partial V_{\text{eff}}}{\partial Q} = 0$$

$$\mathcal{B}_Q \approx Q^3 \cdot \int \frac{dt}{\alpha(t)}$$

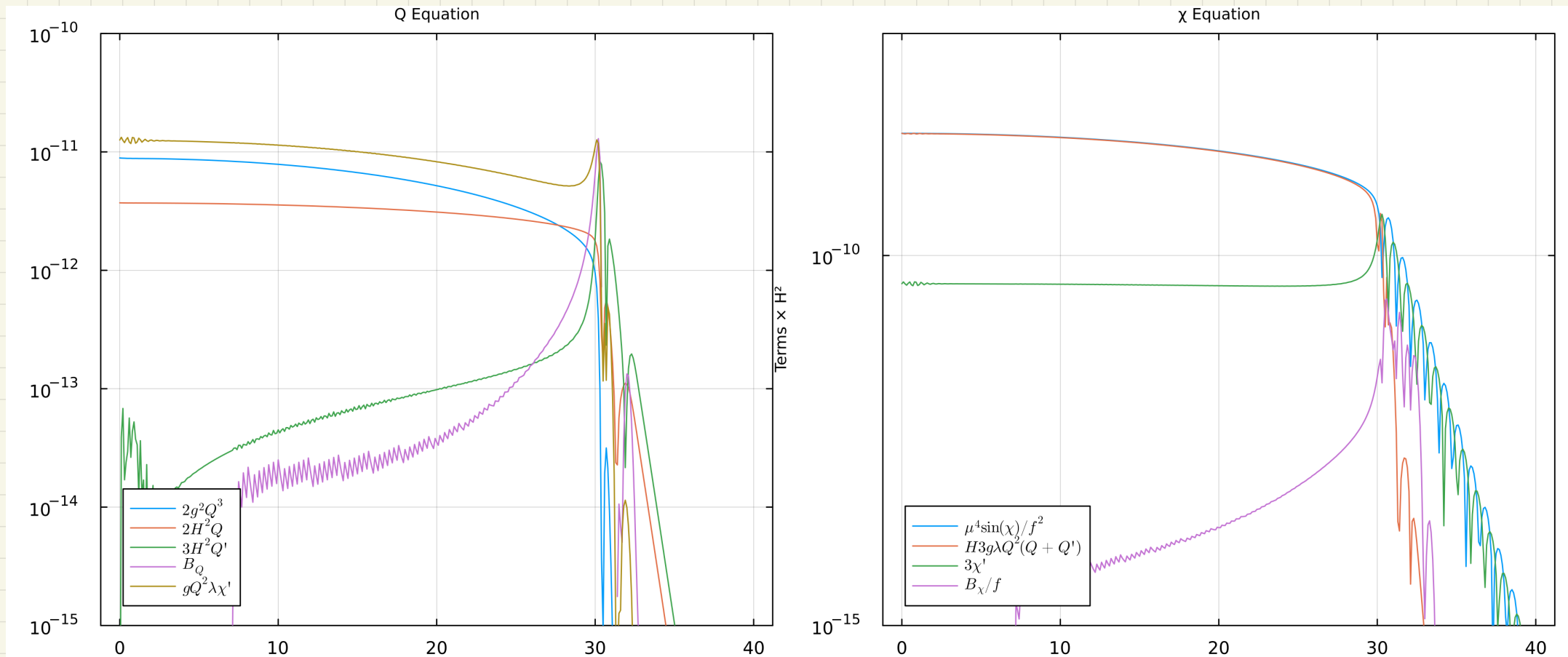
$$V_{\text{eff}} = \# Q^3 - \# Q^2 + (\#_{\text{small}} + \alpha(t)) Q^4$$

When this NEW effective potential dominates, it forces the field Q to the Minimum $Q \rightarrow 0$



Let's switch the Backreaction ON!

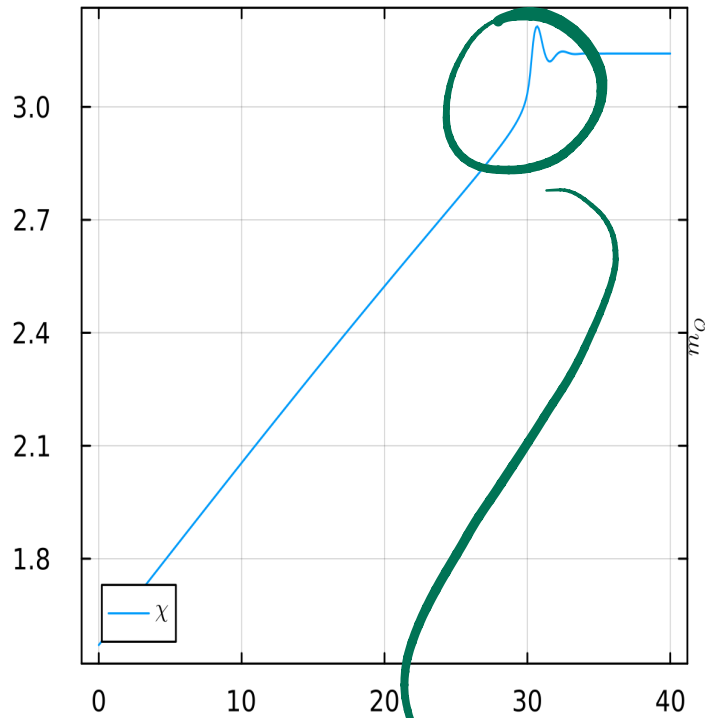
- The FIRST NUMERICAL IMPLEMENTATION -



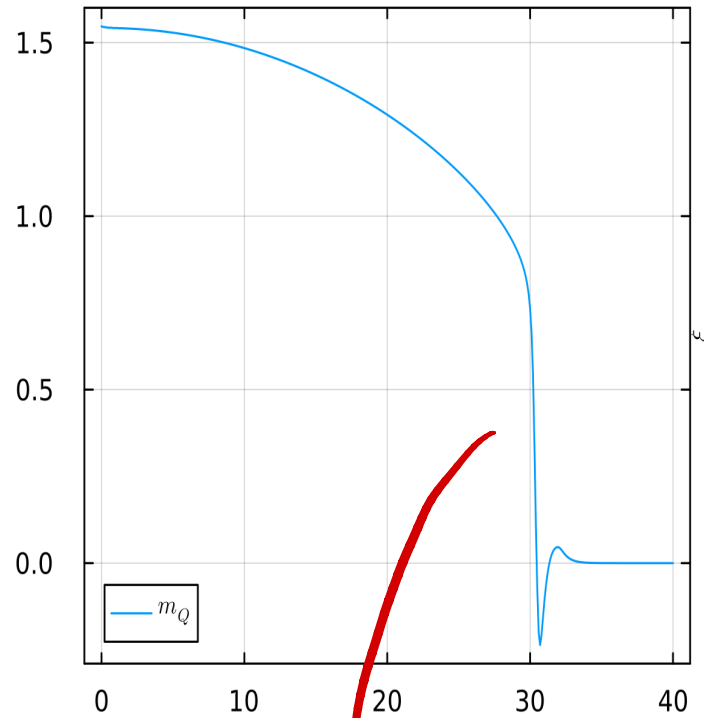
Let's switch the Backreaction ON!

Bump in ξ

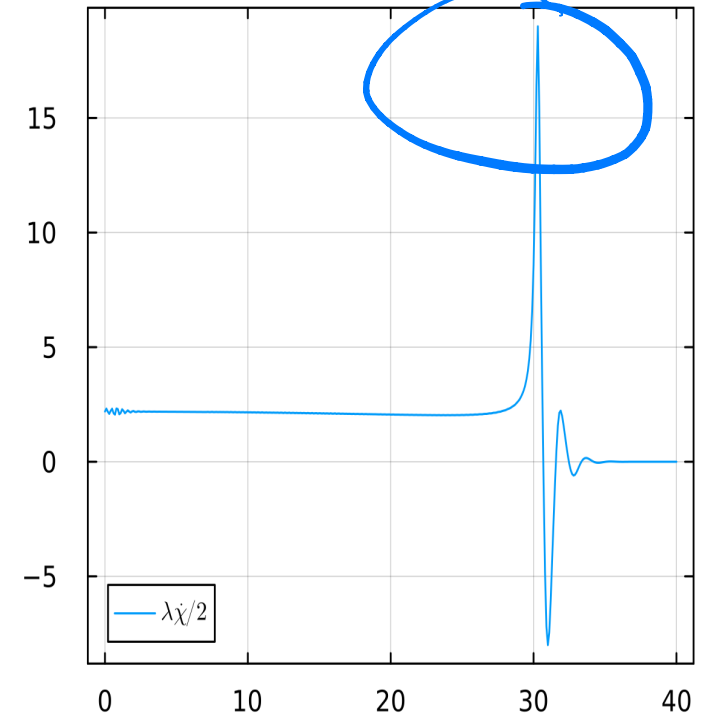
Background - Switching on the Backreaction



Background - Switching on the Backreaction



Background - Switching on the Backreaction



χ rolls nearly frictionless

The term goes to $\rightarrow 0$

Amplification of ξ

Where are the shadows of this mechanism?

GFTM $T_{R,L}'' + \left\{ k^2 + \frac{2}{\gamma^2} [m_Q \xi \pm k\eta (m_Q + \xi)] \right\} T_{R,L} \simeq f(\psi, \varepsilon)$

An amplification of the $T_{R,L}$
sources the GWs

Gravitational Waves: $\psi_{R,L}'' + \left(k^2 - \frac{2}{\gamma^2} \right) \psi_{R,L} \simeq g(T, \varepsilon)$

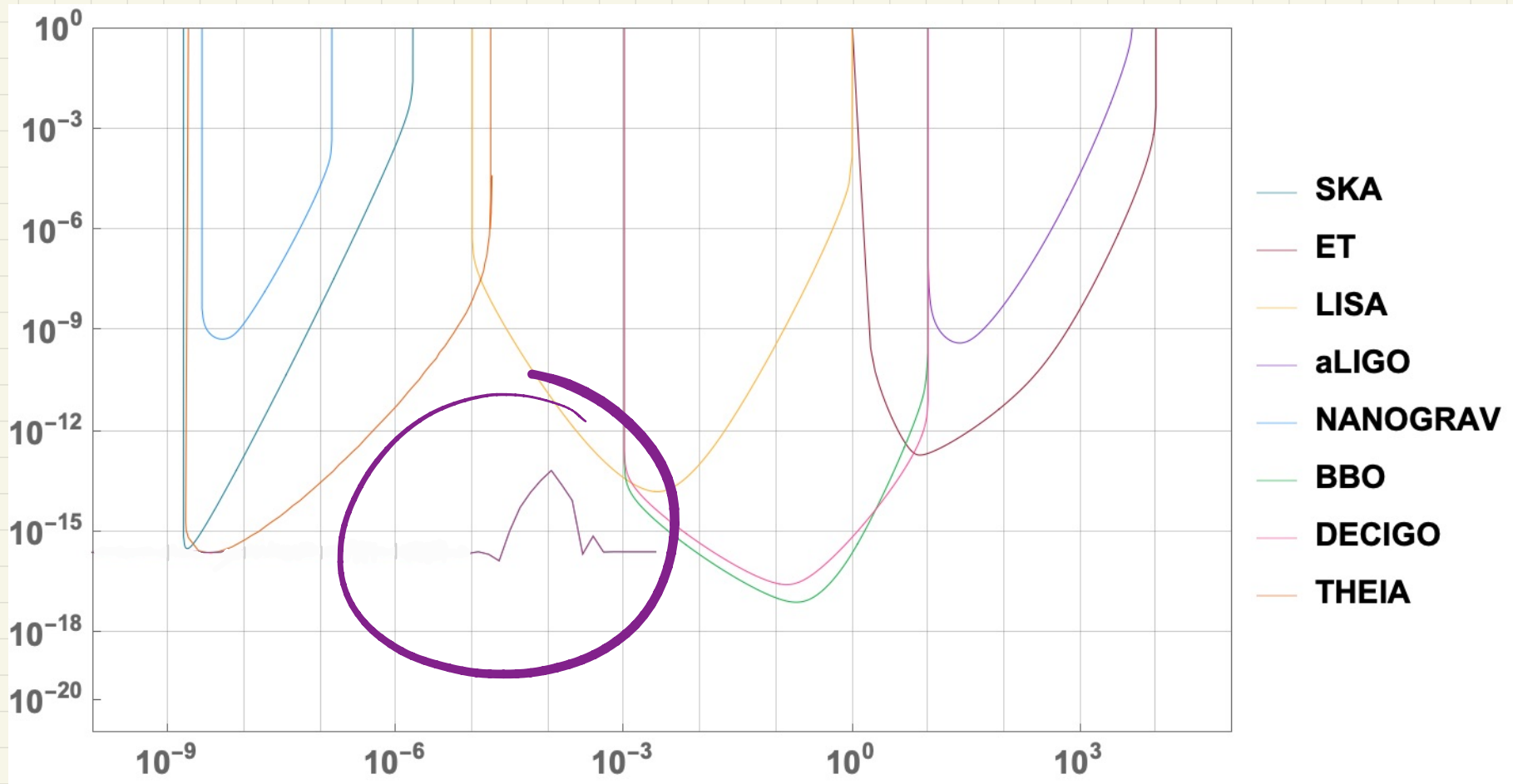
Our Benchmark:

$$f = 3,36 \times 10^{-2} \text{ } \mu\text{pe}$$

$$g = 4 \cdot 10^{-3}$$

$$\lambda = 90$$

Where are the shadows of this mechanism?



We are exploring the phase Space for the parameters...

STAY TUNED

Thank You