Recent advances in RNA secondary structure prediction with machine learning and deep learning

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- Overview of RNA secondary structure prediction
 - Architecture
 - Nussinov algorithm, Nearest neighbor model
 - Inference
 - MFE, MEA
 - Parametrization
 - Machine learning, Deep learning
- Future direction
 - Chemical probing
 - RNA modification
 - Pseudoknots

What is RNA secondary structure prediction?

• Given an RNA sequence, predict its secondary structure

Secondary Structure **RNA** sequence Predict AAACAUGAGGAUUACCCAUGU 20





• Observation 1:

The greater the number of base-pairs, the more energetically stable.

⇒ Nussinov algorithm predicts a secondary structure that maximizes the number of base-pairs.

• Observation 2:

The optimal structure of a given sequence can be constructed from the optimal structures of shorter subsequences.

 \Rightarrow Dynamic programming

Nussinov algorithm

 The optimal structure of a subsequence [i, j] can be computed from a slightly smaller subsequence.



- 1. Add a base-pair (i, j) to the optimal structure of the subsequence [i+1, j-1].
- 2. Add an unpaired base *i* to the optimal structure of the subsequence [i+1, j].
- 3. Add an unpaired base j to the optimal structure of the subsequence [i, j-1].
- 4. Concatenate the two optimal substructures [i, k] and [k+1, j].

• Observation:

The greater the number of base pairs, the more energetically stable.

$$s(i,j) = \max \begin{cases} s(i+1,j-1) + 1 & \text{if the } i\text{-th base and } j\text{-th base are} \\ s(i+1,j) \\ s(i,j-1) \\ \max_k[s(i,k) + s(k+1,j)] \end{cases}$$

• Computational complexity: $O(L^3)$ time, $O(L^2)$ space

The four ingredients of RNA secondary structure prediction



[Rivas 2013]

The four ingredients of RNA secondary structure prediction



- 1. Architecture
 - Nearest neighbor model
 - Context-free grammars



- Nearest neighbor model [Zuker&Stiegler81; Zuker03]
 - The free energy of a secondary structure is the sum of the free energy of its substructures.



overall $\Delta G = -4.6$ kcal/mol

Nearest neighbor model

• Decomposition of RNA secondary structure with the nearest neighbor model



Nearest neighbor model

• Recursive equation for Zuker algorithm [1981]

$$\begin{split} F_{ij} &= \min \left\{ F_{i+1,j}, \min_{i < k \le j} C_{ik} + F_{k+1,j} \right\} \\ C_{ij} &= \min \left\{ \mathcal{H}(i,j), \min_{i < k < l < j} C_{kl} + \mathcal{Y}(i,j;k,l), \min_{i < u < j} M_{i+1,u} + M_{u+1,j-1}^1 + a \right\} \\ M_{ij} &= \min \left\{ \min_{i < u < j} (u - i + 1)c + C_{u+1,j} + b, \min_{i < u < j} M_{iu} + C_{u+1,j} + b, M_{i,j-1} + c \right\} \\ M_{ij}^1 &= \min \left\{ M_{i,j-1}^1 + c, C_{ij} + b \right\} \\ F_{ii} &= 0, \ C_{ii} = M_{ii} = M_{ii}^1 = \infty, \end{split}$$

• Computational complexity: $O(L^3)$ time, $O(L^2)$ space

LinearFold algorithm

- [Huang *et al.*, 2019] developed LinearFold algorithm using:
 - left-to-right incremental dynamic programming, and
 - the beam search approximate to reduce search space.



• Computational complexity: O(L) time, O(L) space

The four ingredients of RNA secondary structure prediction



[Rivas 2013]

4. Inference

- Minimum free energy (MFE)
- Maximum likelihood estimate (MLE)
- Maximum expected accuracy (MEA)

- Inference focuses on which secondary structure is drawn from the probability distribution of RNA secondary structures.
- Predict minimum free energy (MFE) structure
 - Zuker algorithm (Zuker et al., 1981)
 - Software: Mfold / RNAfold
 - Equivalent to maximum likelihood estimate with McCaskill model
- Predict maximum expected accuracy (MEA) structure
 - Prediction by considering "distribution" of secondary structures
 - Software:
 - CONTRAfold (Do et al., 2006)
 - CentroidFold (Hamada et al., 2009, Sato et al. 2009)

MFE structure is not always the best



[Ding et al, 2005]



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Sequence analysis

Prediction of RNA secondary structure using generalized centroid estimators

Michiaki Hamada^{1,2,3,*}, Hisanori Kiryu², Kengo Sato^{2,4}, Toutai Mituyama² and Kiyoshi Asai^{2,5}

Published online 12 May 2009 Nucleic Acids Research, 2009, Vol. 37, Web Server issue W277–W280 doi:10.1093/nar/gkp367

CENTROID FOLD: a web server for RNA secondary structure prediction

Kengo Sato^{1,2,*}, Michiaki Hamada^{2,3}, Kiyoshi Asai^{2,4} and Toutai Mituyama²

Maximizing expected accuracy

• Given a space S(x) of secondary structures of RNA sequence x, predict a structure \hat{y} that maximizes an accuracy metric.

```
y: a reference structure \hat{y}: a predicted structure
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◆Gain function for true prediction $G(y, \hat{y}) = \gamma TP(y, \hat{y}) + TN(y, \hat{y}) \quad (\gamma > 0)$ # of true positives # of true negatives

Predict as many correct base pairs as possible

Maximizing expected accuracy

• Given a probability distribution P(y | x) over a space S(x) of secondary structures, predict a structure \hat{y} that maximizes expected accuracy

Predict as many correct base pairs as possible

• Find \hat{y} that maximizes:

$$\sum_{y \in \mathcal{S}(x)} G(y, \hat{y}) P(y \mid x) = \sum_{i < j} \underbrace{[(\gamma + 1)p_{ij} - 1]\hat{y}_{ij} + C}_{\text{base-pairing probability}}$$

• Nussinov-style dynamic programming

$$s(i,j) = \max \begin{cases} s(i+1,j-1) + [(\gamma+1)p_{ij}-1] \\ s(i+1,j) \\ s(i,j-1) \\ \max_k [s(i,k) + s(k+1,j)] \end{cases}$$

The four ingredients of RNA secondary structure prediction

[Rivas 2013]

- 2. Scoring scheme
 - Weights
 - Probability distribution

The four ingredients of RNA secondary structure prediction

- 3. Parameterization
 - Thermodynamic-based methods
 - Machine learning-based methods
 - discriminative, generative

<u>Thermodynamic-based methods</u>

- Determine free energy parameters by experiments (e.g., Turner1999, Turner2004)
- Experimental errors are not negligible.
- Too simplified models can only be constructed due to the limitations of experimental techniques.

<u>Machine learning-based methods</u>

- Rich-parameterized models can be constructed.
- Potential risk of overfitting due to the inability to provide enough training data.

- Fewer parameters can be determined by experiments for the thermodynamic models.
- There is a possibility of overfitting to the training dataset for machine learningbased models.

Comparison of different methods [Rivas et al., 2012]

#parameters Parameterization Benchma		пагк: F	
		TestSetA	TestSetB
3,500	Thermodynamic	0.510	0.513
12,700	Thermodynamic	0.537	0.543
300	Machine Learning	0.572	0.579
205,000	Machine Learning	0.644	0.490
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i	3,500 12,700 300 205,000 t ch parameters	3,500 Thermodynamic 12,700 Thermodynamic 300 Machine Learning 205,000 Machine Learning	TestSetA3,500Thermodynamic0.51012,700Thermodynamic0.537300Machine Learning0.572205,000Machine Learning0.644Ch parametersHigh accuracy

- Fewer parameters can be determined by experiments for the thermodynamic models.
- There is a possibility of overfitting to the training dataset for machine learningbased models.

Comparison of different methods [Rivas et al., 2012]

Method	#parameters	Parameterization	Benchmark: F	
			TestSetA	TestSetB
UNAfold [Markham et al., 2008]	3,500	Thermodynamic	0.510	0.513
RNAfold [Lorenz et al., 2011]	12,700	Thermodynamic	0.537	0.543
CONTRAfold [Do et al., 2006]	300	Machine Learning	0.572	0.579
ContextFold [Zakov et al., 2011]	205,000	Machine Learning	0.644	0.490
				1
	Rich parameter:	s High a	accuracy	overfitting

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RNA secondary structure prediction using deep learning with thermodynamic integration

Kengo Sato [™], Manato Akiyama¹ & Yasubumi Sakakibara¹

- Develop an algorithm that is robust against the overfitting using...
 - > a scoring model that integrates machine learning and thermodynamic approaches,
 - the max-margin based training algorithm a.k.a. structured support vector machines (SSVM), and
 - thermodynamic regularization that ensures that folding scores and the calculated free energy are as close as possible.

Scoring Model

Scoring Model

• Integrate the thermodynamic approach and the machine learning approach.

x = AAACAUGAGGAUUACCCAUGUy = ...(((((((((())))))))))

Training Algorithm

 To optimize the network parameters λ, we employ a max-margin based training algorithm a.k.a structured support vector machines (SSVM) [Tsochantaridis *et al.,* 2005].

Objective function

$$\mathcal{L}(\lambda) = \sum_{(x,y)\in\mathcal{D}} \left\{ \left(\max_{\hat{y}\in\mathcal{S}(x)} \left[f(x,\hat{y}) + \Delta(y,\hat{y}) \right] - f(x,y) \right\} + C_1 \left[f(x,y) - f_T(x,y) \right]^2 + C_2 ||\lambda||_2 \right\},$$
Loss term
Thermodynamic regularization
$$\Delta(y,\hat{y}) : \text{margin term}, \ f_T(x,y) : \text{the free energy of the structure } y \text{ of the sequence } x$$

 Thermodynamic regularization prevents the folding score of the secondary structure from differing significantly from the free energy of the thermodynamic parameters.

Dataset I

• Assembled by [Rivas *et al.,* 2012]

Comparison with competitive methods

$$PPV = \frac{TP}{TP + FP}, \ SEN = \frac{TP}{TP + FN}$$

Correlation with free energy

- Dataset
 - T-full dataset [Andronescu *et al.*, 2008],
 which contains sequence-structure-energy triplets

	PPV	SEN	F	RMSE	ρ
MXfold2	0.984	0.978	0.980	3.260	0.833
MXfold2 (w/o thermo. reg.)	0.980	0.972	0.973	3.607	0.538
CONTRAfold	0.963	0.639	0.643	5.781	0.736
RNAfold	0.979	0.964	0.963	2.868	0.909

Other DL-based methods

• Multiple binary classifiers for all (i, j) pairs

- SPOT-RNA [Singh et al., 2019], E2Efold [Chen et al., 2020], UFold [Fu et al., 2022]

Strategies for overfitting in other DL-based methods

- SPOT-RNA [Singh et al., 2019]
 - Ensemble of five different DL models
- E2Efold [Chen *et al.,* 2020]
 - None
- UFold [Fu et al., 2022]
 - Data augmentation using test data mutated

Dataset II

Assembled by [Sato et al., 2021]

Comparison with other DL-based methods

 $PPV = \frac{TP}{TP + FP}, SEN = \frac{TP}{TP + FN}, F = \frac{2 \times PPV \times SEN}{PPV + SEN}$

Comparison with other DL-based methods on another study

UFold's data augmentation is not likely to be helpful.

Values are taken from [de Lajarte et al., 2024]

But not perfect

• Family-wise cross validation on Archive II dataset [Szikszai et al., 2022]

Family	F ₁					
	RNAstructure	MXfold2	UFold			
5S rRNA	0.63	0.54	0.53			
SRP RNA	0.64	0.50	0.26			
tRNA	0.80	0.64	0.26			
tmRNA	0.43	0.46	0.40			
RNase P RNA	0.55	0.51	0.41			
Group I intron	0.53	0.45	0.45			
16 S rRNA	0.58	0.55	0.41			
Telomerase RNA	0.50	0.34	0.80			
23S rRNA	0.73	0.64	0.45			
Mean	0.60	0.51				

Structural bioinformatics

Deep learning models for RNA secondary structure prediction (probably) do not generalize across families

Marcell Szikszai ()^{1,*}, Michael Wise^{1,2}, Amitava Datta¹, Max Ward^{1,3} and David H. Mathews⁴

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The number of known structures of proteins and RNA

• The number of known RNA structures is 100 times less than that of proteins.

SHAPE-directed folding

• RNAstructure [Deigan et al. PNAS. 2009]

adds pseudo-energy for *i*-th base for base-pairing:

 $\Delta G_{\text{SHAPE}}(i) = m \ln[\text{SHAPE reactivity}(i) + 1] + b$

shows significant improvement in prediction accuracy

		No constra	aints	SHAPE	
RNA	Nucleotides	Sensitivity	PPV	Sensitivity	PPV
Yeast tRNA ^{Asp}	75	95.2	95.2	100.0	100.0
HCV IRES domain II	95	56.5	59.1	95.7	100.0
P546 domain, group l intron	155	42.9	44.4	96.4	98.2

• We implemented SHAPE-directed folding in MXfold2 following this same approach.

Training from chemical probing data

- EternaFold [Wayment-Steele et al. Nat. Methods. 2022]
 - Multi-task learning based on the CONTRAfold model

 We implemented SHAPE-directed "training" in MXfold2 while avoiding the computation of the partition function.

Training from chemical probing data

- Key idea:
 - SHAPE-directed folding make a perfect prediction, so use it as the reference structure.
- Update the model parameter θ for a sequence x with chemical probing data
 - 1. predict secondary structure y of x using SHAPE-directed folding with parameter θ
 - 2. predict secondary structure \hat{y} of x using normal folding with parameter θ
 - 3. update parameter: $\theta \leftarrow \theta \eta \nabla_{\theta} loss(y, \hat{y})$

Training from chemical probing data

[Sato et al., in prep]

Distribution of SHAPE reactivity

• [Wu et al. *NAR*. 2015]

Large scale training dataset including chemical probing

• Performance will be improved by significantly scaling up both the quality and quantity of training data.

<u>Current</u>

- 4,270 sequences with complete SS
 - TrainSetA+B, TestSetA+B
 [Rivas et al., 2012]

<u>New</u>

- 19,266 sequences with complete SS
 - TrainSetA+B, TestSetA+B
 [Rivas et al., 2012]
 - bpRNA-1m [Danaee et al., 2018]
 - bpRNAnew [Sato et al., 2021]
- 48,614 sequences with chemical reactivity
 - 1,456 human mRNA 3' end,
 1,098 human pri-miRNA
 [de Lajarte et al., 2024]
 - 46,060 Ribonanza data [He et al., 2024]

Large scale training dataset including chemical probing

Values are taken from [de Lajarte et al., 2024] [Sato et al., in prep]

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- play important roles in biological processes such as gene regulation [Camper et al., 1984],
- are known to exist >170 types [Nombela et al., 2021], and

Inosine (I)

N6-methyladenosine (m⁶A)

• alter RNA secondary structures [Alseth et al., 2014].

However, few methods are available for predicting RNA secondary structures that consider RNA modifications.

Methods: Representation for RNA modifications

One-hot encoding

- Takes characters (RNAs) as inputs, and
- Identifies input characters by a set bit.

Fingerprint encoding ECFP (Extended-Connectivity Fingerprint)

- Takes chemical structures as inputs, and
- Represents the presence or absence of substructures in 1024 bits.

	# of	Modif	ied bas	es (%)		
	seqs.	I	ψ	m ⁶ A		
TrainSetA ^{%1}	3166	0.0	0.0	0.0	RNA seqs without modifications	Pre-training
mod_data ^{%2}	218	0.16	8.8	0.26	tRNA seqs with modifications	Fine-tuning
no_mod_data ^{%2}	218	0.0	0.0	0.0	same seqs as mod_data, but no mods	Fine-tuning
pdb_data ^{涨3}	11	1.7	18.0	0.0	tRNA seqs with modifications	Evaluation

^{**1} Rivas *et al*, 2012, ^{**2} Boccaletto *et al.*, 2018, ^{**3} Lorenz *et al.*, 2017, Helm *et al.*, 2006, Guy *et al.*, 2014, Bilbille *et al.*, 2011, Swinehart *et al.*, 2020, Keller *et al.*, 1999, Jank *et al.*, 1977, Kulinska *et al.*, 1974, Hayase *et al.*, 1974, Tinse *et al.*, 2000

Results

• Pre-train with TrainSetA, evaluate positions at modified bases on pdb_data

• Fingerprint encoding tends to be more accurate for modified bases than one-hot encoding.

• The fingerprint encoding can share the results of the training for common bits.

How to prepare sequence data with structures including modified bases?

- Few sequence data are available that contain modified bases with complete secondary structures.
- Chemical probing data with modified bases has also never been available.

Check for updates

We plan to combine experimental data in different experiments as in:

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Secondary structure prediction for RNA sequences including N⁶-methyladenosine

Elzbieta Kierzek ¹^M, Xiaoju Zhang², Richard M. Watson², Scott D. Kennedy ², Marta Szabat¹, Ryszard Kierzek¹ & David H. Mathews ^{2⊠}

> **Transcriptome-wide predictions with m⁶A**. To further test our m⁶A nearest neighbor parameters and software, we predicted structures for 18,026 mRNAs that were identified as having $N^{6}A$ methylation by whole transcriptome sequencing⁶¹ and for which PARS structure mapping data are available⁶². We used the nearest neighbor parameters and RNAstructure package to estimate the

Human embryonic kidney 293T cells

Human lymphoblastoid cell lines

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RNA pseudoknotted secondary structure

- Pseudoknots play several roles in RNA functions
 Regulation of translation & splicing, etc.
- Pseudoknots assist the overall 3D folding
- → Pseudoknots should be considered for structural analysis

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IPknot: fast and accurate prediction of RNA secondary structures with pseudoknots using integer programming

Kengo Sato^{1,*,†}, Yuki Kato^{2,*,†}, Michiaki Hamada¹, Tatsuya Akutsu³ and Kiyoshi Asai^{1,4}

Briefings in Bioinformatics, 23(1), 2022, 1–9

https://doi.org/10.1093/bib/bbab395 Problem Solving Protocol

Prediction of RNA secondary structure including pseudoknots for long sequences

Kengo Sato and Yuki Kato

IPknot: Integer Programming-based prediction of RNA pseudoKNOTs

Approximate a probability distribution over pseudoknotted structures by its factorization

$$P(y \mid x) \simeq \prod_{1 \le p \le m} P'(y^{(p)} \mid x)$$

Objective function (expected accuracy)

maximize
$$\sum_{1 \le p \le m} \alpha^{(p)} \sum_{i < j} \left[(\gamma^{(p)} + 1) p_{ij} - 1 \right] \hat{y}_{ij}^{(p)} + C \quad (*)$$
To be positive
$$Predicted base pair$$

Consider only base pairs whose pairing probabilities are larger than thresholds

→Threshold cut

Find $y = (y^{(1)}, ..., y^{(m)})$ that maximizes (*)

• $y_{ij}^{(1)}$ such that $p_{ij} > \theta^{(1)} = 1/(\gamma^{(1)} + 1)$: • $y_{ij}^{(m)}$ such that $p_{ij} > \theta^{(m)} = 1/(\gamma^{(m)} + 1)$ Thresholds

Constraints

• The following hold for all levels $p (1 \le p \le m)$ and $q (\le p)$

one base pair at the lower

level q

Prediction accuracy for pseudoknotted structures

Test data was compiled from bpRNA-1m and Rfam 14.5.

- IPknot approximates a probability distribution over pseudoknotted structures by its factorization of pseudoknot-free structures:
 - (2011 version) CONTRAfold model, ViennaRNA model, NUPACK model
 - (2022 version) LinearFold-C model, LinearFold-V model
- We implemented new IPknot that integrates MXfold2 as a probability distribution over pseudoknot-free structures.

IPknot integrated with MXfold2

 We are participating in CASP16 as RNA_Dojo team with a workflow based on the new IPknot with MXfold2, FARFAR2, and RNA-BRiQ.

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- IPknot, CentroidFold
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 - Kiyoshi Asai (U Tokyo)
 - Tatsuya Akutsu (Kyoto U)
 - Michiaki Hamada (Waseda U)
 - Hisanori Kiryu (U Tokyo)
 - Toutai Mituyama (AIST)
- MXfold2
 - Yasubumi Sakakibara (Keio U)
 - Manato Akiyama (Keio U)

- RNA Dojo in CASP16
 - Junichi Iwakiri (U Tokyo)
 - Takumi Otagaki (U Tokyo)
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