

Observing GW Memory (with LISA)

Silvia Gasparotto (IFAE)

Based on Phys.Rev.D 107 (2023) 12 and 2406.09228



UAB
Universitat
Autònoma
de Barcelona



Generalitat de Catalunya
**Departament de Recerca
i Universitats**

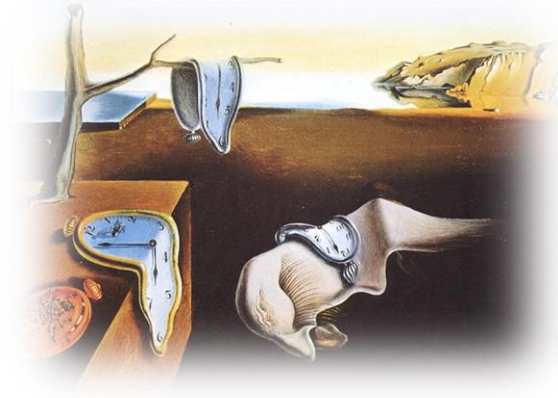
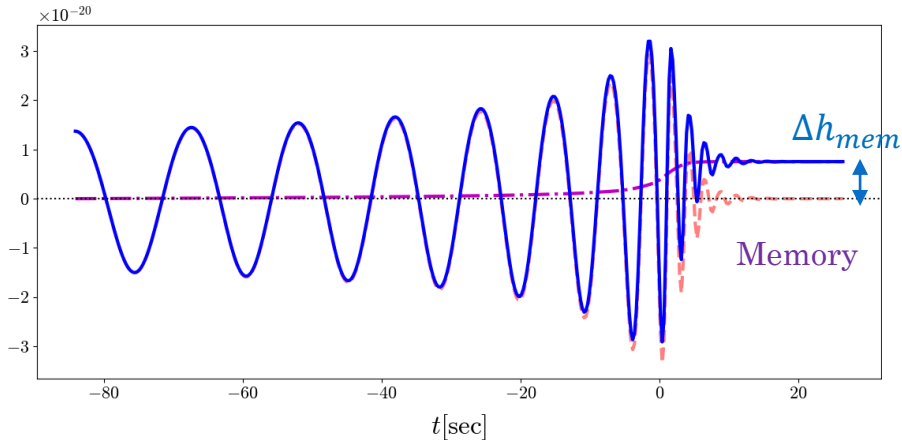
New Frontiers in Strong
Gravity,
Benasque 2024

IFAE
Institut de Física
d'Altes Energies

a
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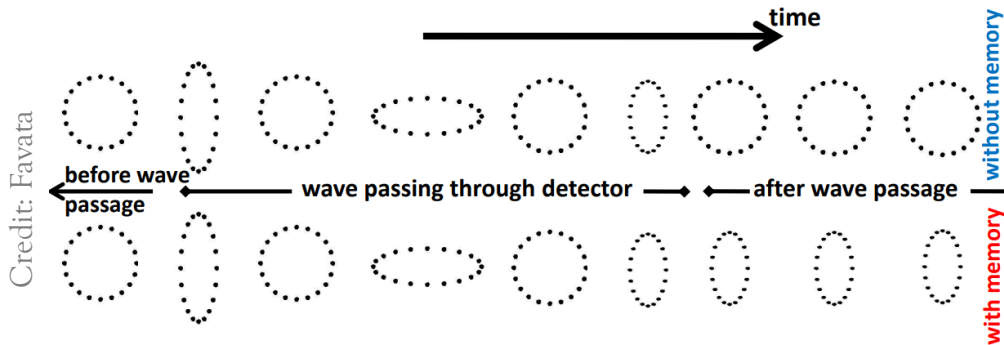
Gravitational Wave Memory



“The Persistence of Memory”
(also known as “The Soft Watches”)
Salvador Dalí, 1931

Persistent off-set of the
GW strain

The effect is a net displacement
between two comoving
observers



Credit: Favata

Linear and Non-linear Memory

- **Linear memory** (Zeldovich & Polnarev '74, Brangisky & Grischchuk '85, Brangisky & Thorne '87)

Related to the motion of unbound objects or radiation to infinity
(ex: neutrino emission in SN, hyperbolic objects etc)

- **Non-linear memory** (Christodoulou '91, Blanchet & Damour '92, Wiseman & Will '91...)

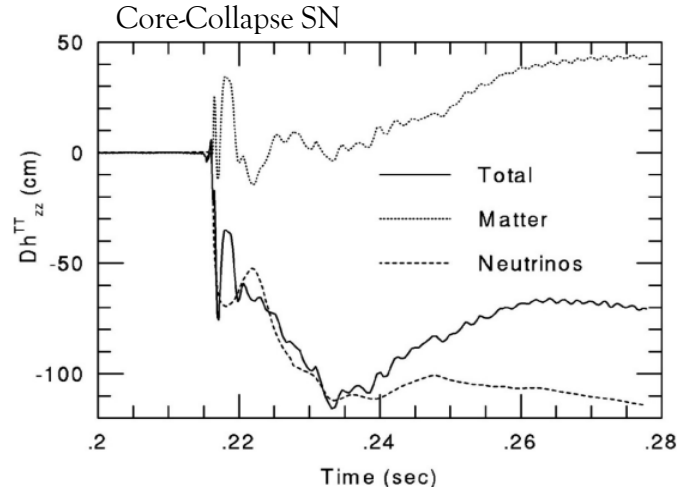
The GW itself sources GWs!

$$\partial^\mu \partial_\mu \bar{h}^{j,k} = 16\pi \left(T_{matter}^{jk} + T_{GW}^{jk} \right)$$

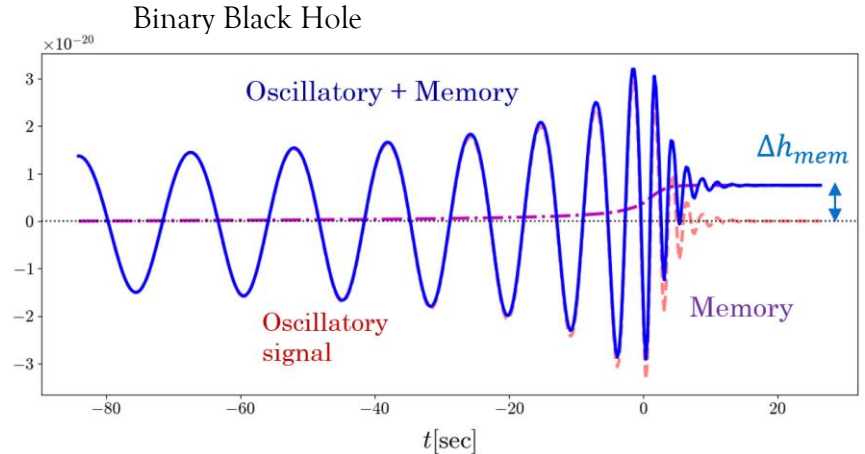
$$T_{GW}^{jk} = \frac{1}{R^2} \frac{dE_{GW}}{dt d\Omega} n_j n_k \sim \mathcal{O}(h^2)$$

Thorne Formula:

$$\delta \bar{h}_{ij}^{TT}(T_R) = \frac{4}{R} \int_{-\infty}^{T_R} dt' \left[\int \frac{dE_{GW}}{dt' d\Omega'} \frac{n'_j n'_k}{|1 - n' \cdot N|} d\Omega' \right]^{TT}$$



Credit: Burrows & Hayes '96



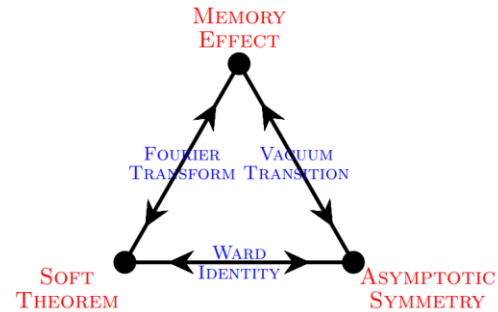
Non-linear GW memory

Why do we care?

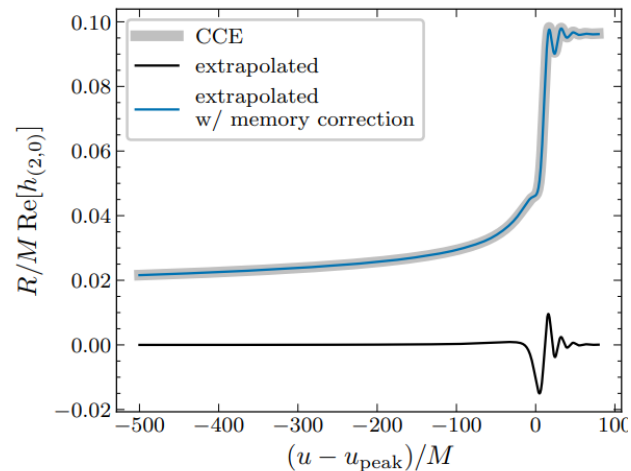
- Non-linear prediction of GR, still undetected
- Relation with the [BMS symmetries](#) and the [Soft theorem](#) (Strominger and A. Zhiboedov 2016)
- Related to the super-translation symmetry, renamed “[Displacement memory](#)”, but new (subdominant) memories from other symmetries

How do we compute it?

- Traditional waveforms don't present the memory → [difficulties in extracting from NR simulations](#)
- Memory can be [computed from the energy flux of GW](#) (GWMemory, BMS flux balance laws); the main (2,0)-mode
- First Surrogate model with the memory (J. Yoo et al. 2306.03148), with new Cauchy Characteristics Extraction (CCE) scheme [NRHybSur3dq8_CCE](#)



See Alexander Grant talk



Detecting GW memory

Earth-based interferometers

- **Ligo-Kagra-Virgo:** no detection so far.
Estimated $O(2000)$ sources to claim detection
(1911.12496, 2105.02879, 2210.16266, 2404.11919)
- **Einstein Telescope & Cosmic Explorer:** $O(1) \text{ yr}^{-1}$ (2210.16266)

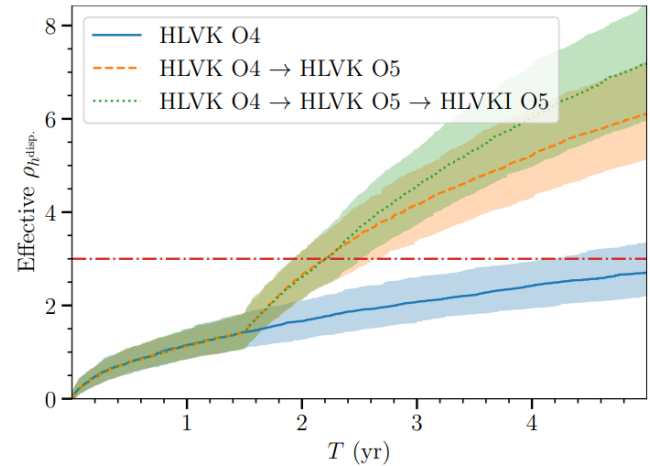
Space-based interferometers

- **LISA:** previous prospects 1906.11936, updates H. Inchauspé & S. Gasparotto et al. 2406.09228
- **TianQin:** 2207.13009, 2401.11416

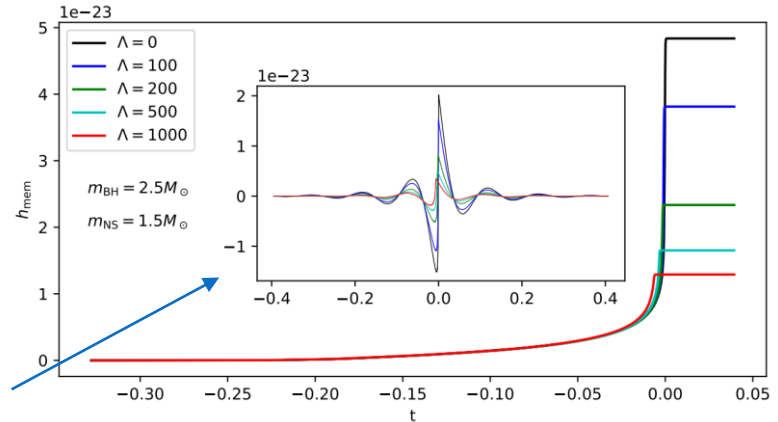
PTA: Search for burst-like signal with memory as mergers of SMBH
 $M \sim 10^8 M_{\odot}$ (0909.0954, 2307.13797)

Others???

In ground-based interferometers, we don't observe the persistent off-set, high-passed signal



Credit: A. M. Grant & D.A. Nichols



“Leveraging gw memory to distinguish NS-BH binaries from BH binaries” 2110.1117

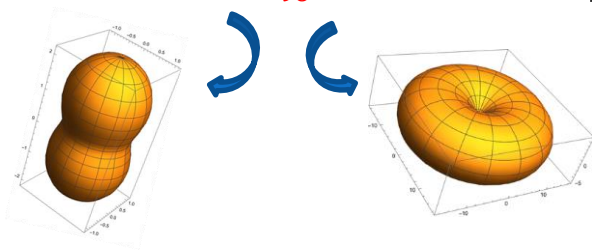


Enhancing parameter estimation with the memory

- Importance of adding the (2,0)-mode to the waveform

$$h_{+,0PN} = \left[-(1 + \cos^2 i) \cos 2\Phi(t) + \frac{1}{96} \sin^2 i (17 + \cos^2 i) \right] \frac{2\eta M (M\omega(t))^{2/3}}{R}$$

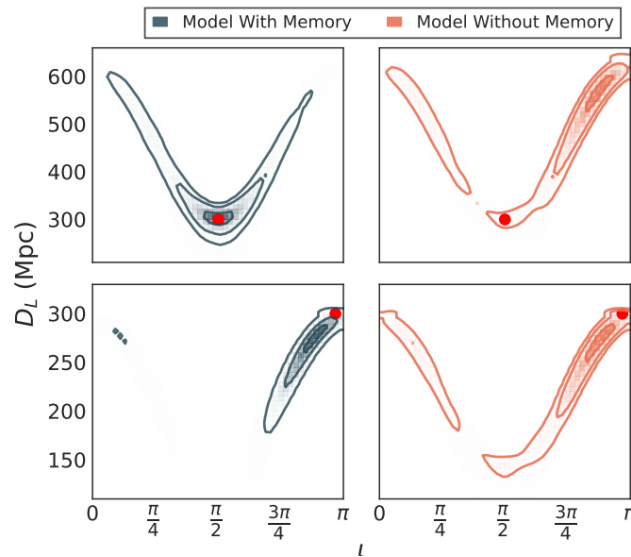
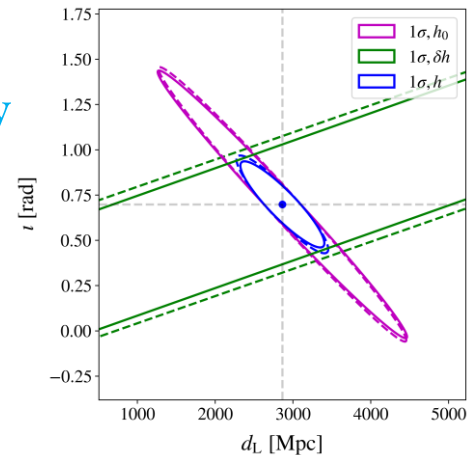
Can the memory break the luminosity distance-inclination degeneracy?



- Results for LISA: Gasparotto et al. 2301.13228 (Fisher matrix)
- Results for (Advanced) LIGO: 2403.00441 (Bayesian)

Common outcome:

- Memory extends the signal at a lower frequency, which helps for short inspiral and almost out-of-band sources



Credit: Yumeng Xu et al. 2403.00441

Measuring GW memory with LISA

Based on 2406.09228 with H. Inchauspé, D. Blas, L. Heisenberg, J. Zosso and S. Tiwari.

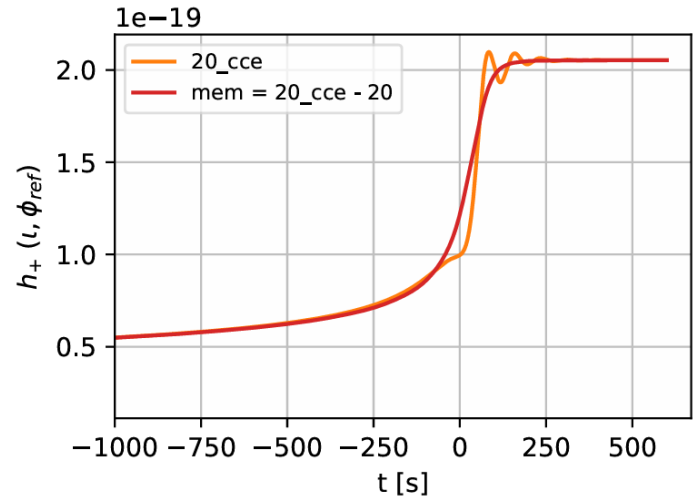
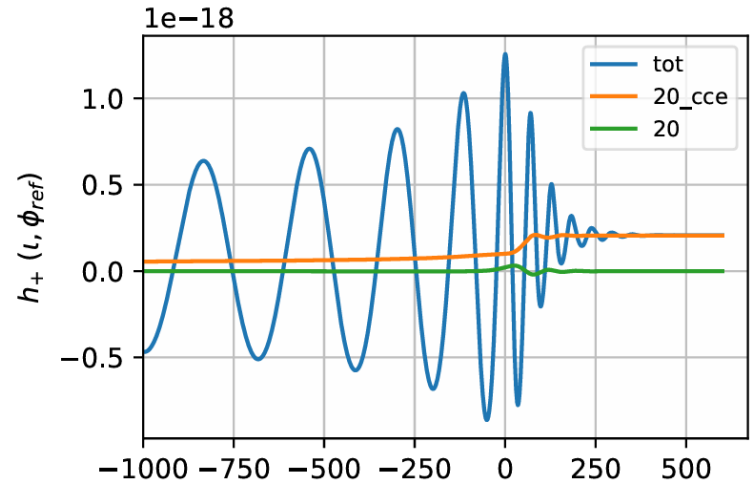
Part of the *Ringdown* collaborative projects of the LISA FPWG.

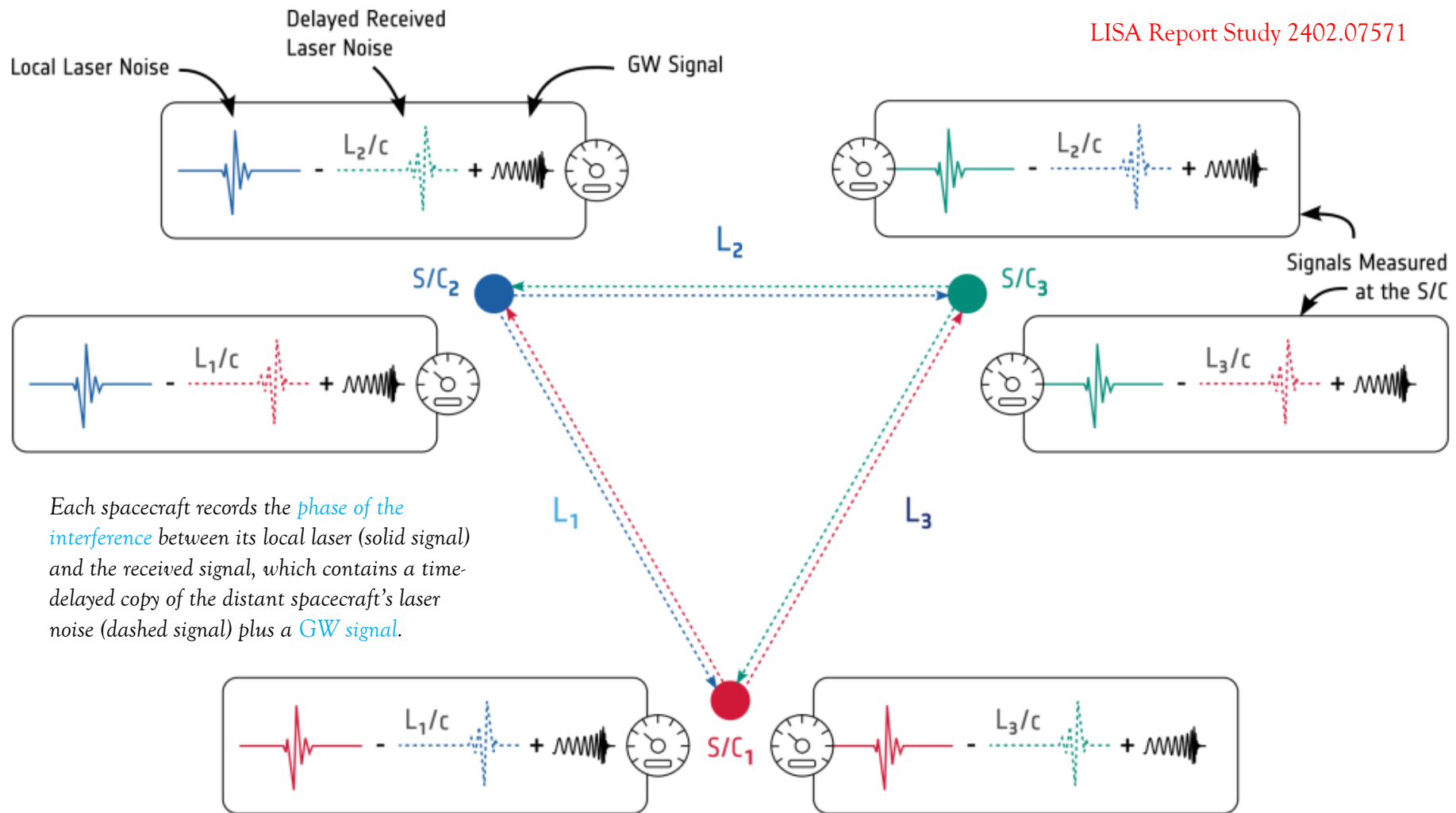
How is the imprint of the GW memory left in the LISA detector?

How do we separate the memory from the non-memory signal?

What is the scientific reach of LISA for the GW memory?

We simulate the full time-domain response of the detector down to the **TDI** (Time-delay-Interferometry) data streams → a combination of the data stream at different edges of LISA







TDI imprint of GW memory

$$\begin{aligned}
X_2 = & X_{1.5} + \mathbf{D}_{13121}y_{12} + \mathbf{D}_{131212}y_{21} + \mathbf{D}_{1312121}y_{13} \\
& + \mathbf{D}_{13121213}y_{31} - [\mathbf{D}_{12131}y_{13} + \mathbf{D}_{121313}y_{31} \\
& + \mathbf{D}_{1213131}y_{12} + \mathbf{D}_{12131312}y_{21}],
\end{aligned}$$

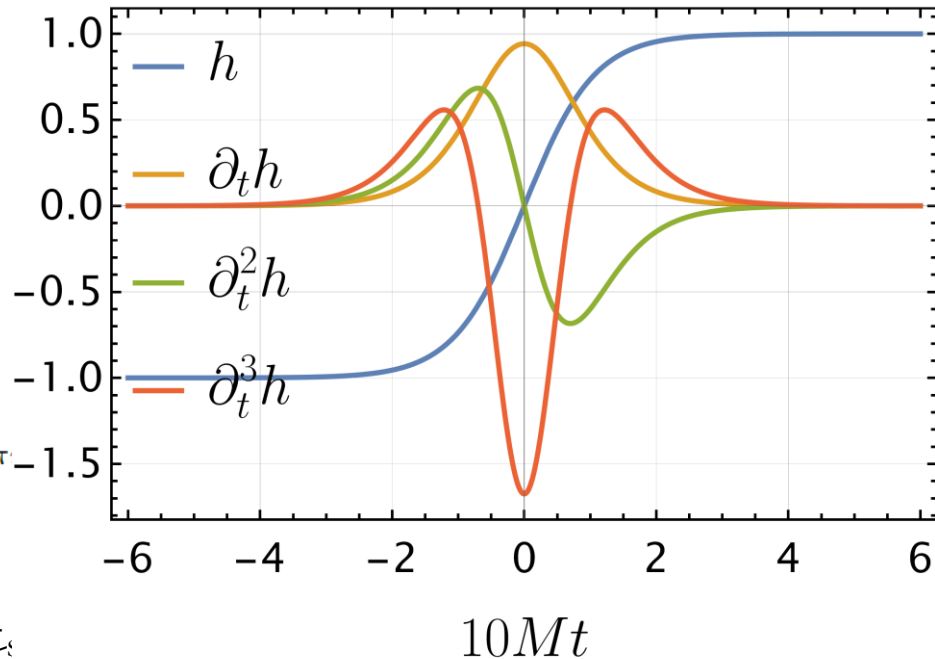
with

$$\begin{aligned}
X_{1.5} = & y_{13} + \mathbf{D}_{13}y_{31} + \mathbf{D}_{131}y_{12} + \mathbf{D}_{1312}y_{21} \\
& - (y_{12} + \mathbf{D}_{12}y_{21} + \mathbf{D}_{121}y_{13} + \mathbf{D}_{1213}y_{31}).
\end{aligned}$$

$$\mathbf{D}_{ij}x(t) = x(t - L_{ij}(t)) \xrightarrow{FT} \tilde{\mathbf{D}}_{ij}\tilde{x}(f) = \tilde{x}(f) e^{-2\pi i f L_{ij}(f)}$$

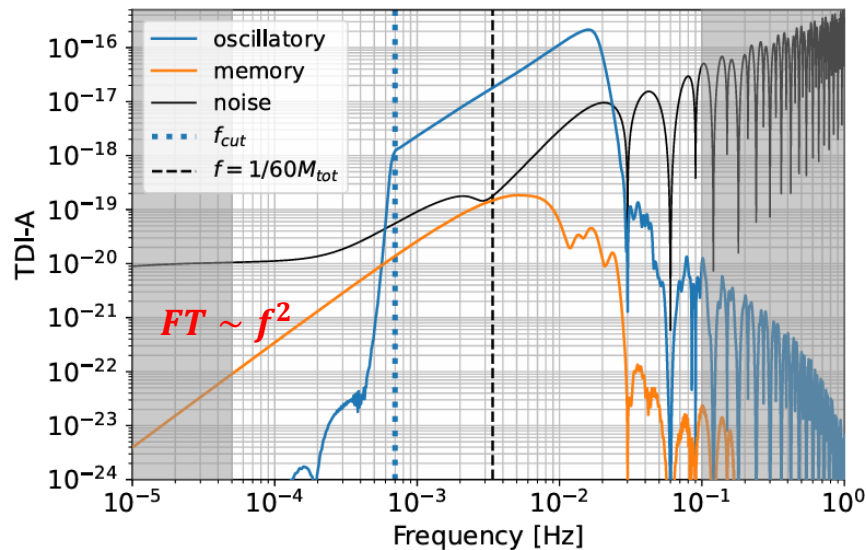
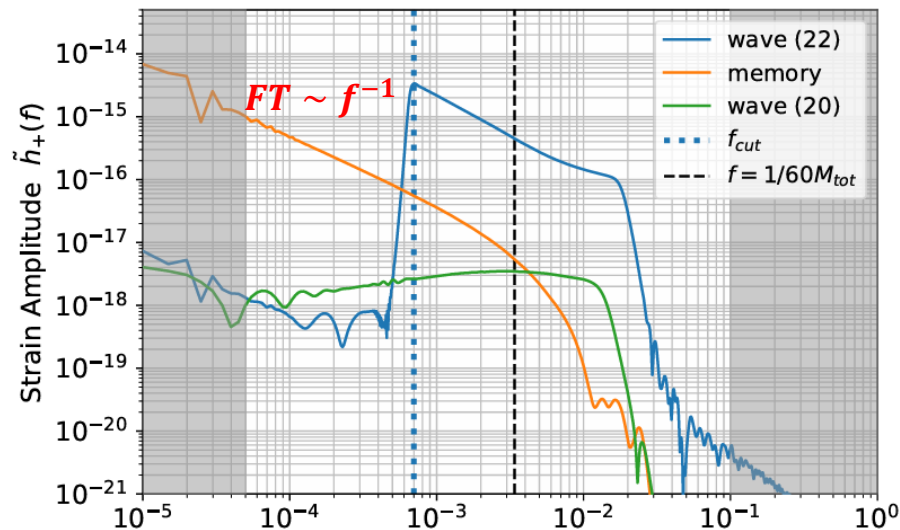
Delay operator

Burst-like signal: We don't observe the persistent offset of the memory, but just its time-variation $X \propto \partial^3 h$



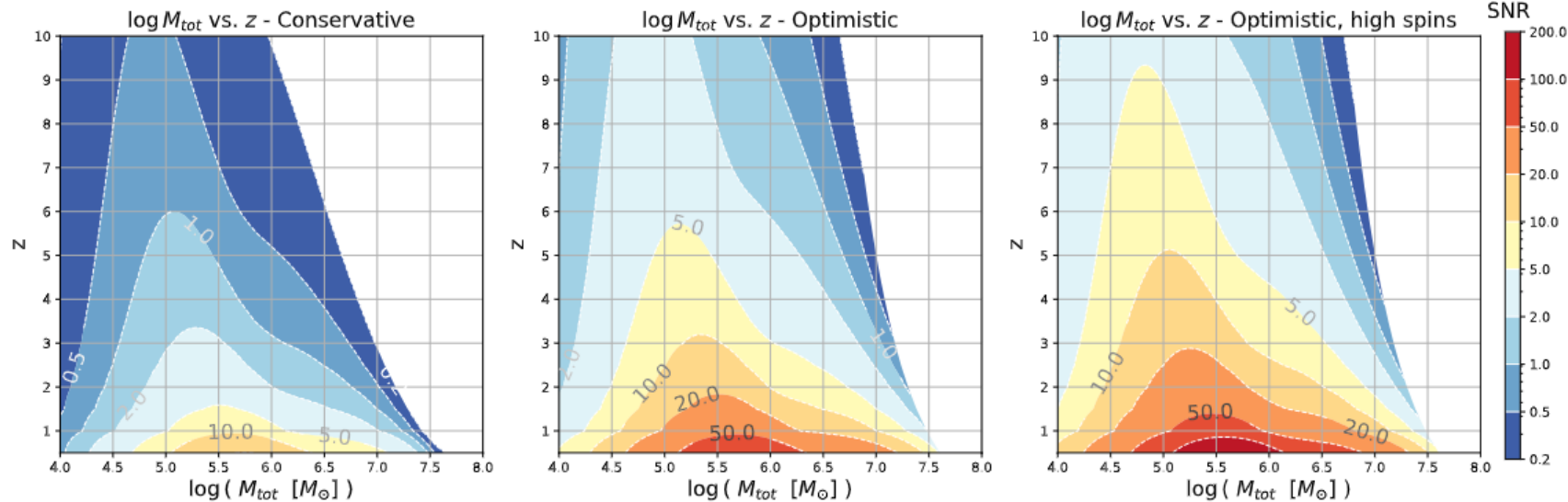
Time domain vs Frequency domain

Fourier Transform of a step like function $\sim f^{-1} \rightarrow$ Extends the signal at lower frequencies





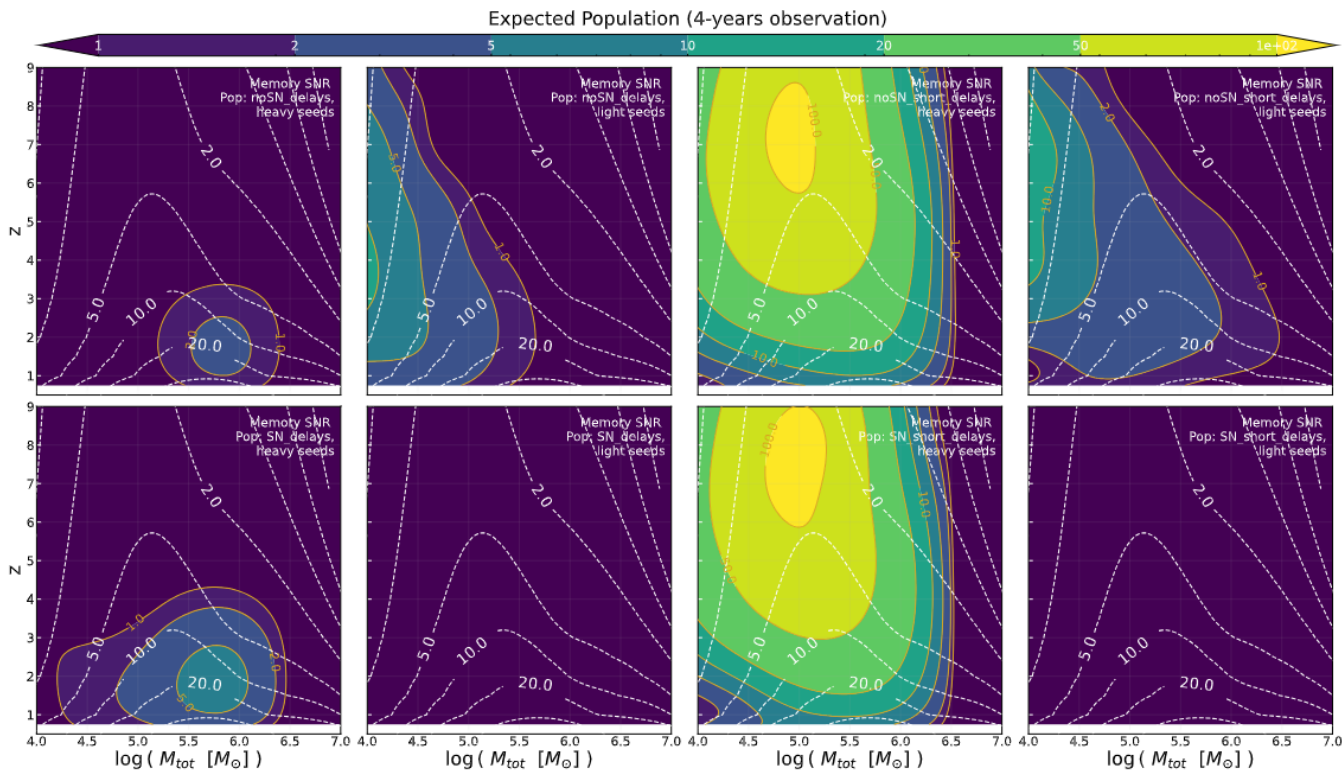
Scientific Reach of LISA: Memory Waterfall Plots



Baseline	q	χ	inclination ι [rad]	lat. β [rad]	long. λ [rad]	pixel p
1. Conservative	2.5	0.0	1.047	0.62	0.20	145
2. Optimistic	1.0	0.0	1.571	0.52	3.24	192
3. Opt. & Spin.	1.0	0.8	1.571	0.52	3.24	192

Astrophysical population models

Population from Barausse et al. 2020



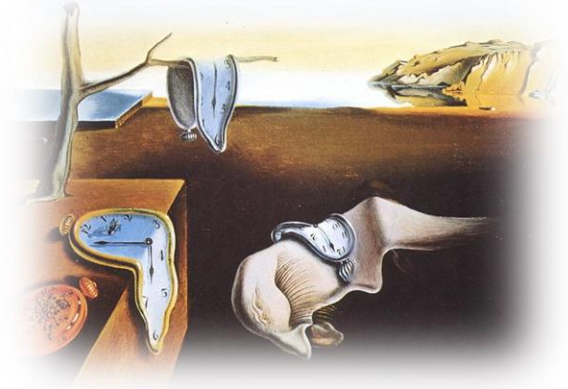
Discussion and Future Directions

- GW memory as a powerful tool for testing GR in a strong regime
 - Which kind of modifications do we expect?
 - Can we probe additional channels of radiation?
 - Can we use GW memory to guide us in understanding the underlying theory of gravity and its asymptotic symmetries?
- Consequences on the posteriors of the GW signal
- New ideas to look for the GW memory (stochastic background?)

$$\delta h_H^{lm}(u, r) = \frac{1}{r} \sqrt{\frac{(l-2)!}{(l+2)!}} \int_{S^2} d^2\Omega' \bar{Y}^{lm}(\Omega') \times \int_{-\infty}^u du' r'^2 \left\langle |\dot{\hat{h}}_+|^2 + |\dot{\hat{h}}_\times|^2 + \sum_{\lambda=1}^N |\dot{\hat{\psi}}_\lambda|^2 \right\rangle$$

L.Heisenberg et al 2303.02021

Thank you for your attention!



Time-Frequency representation

Oscillatory and memory signals have very separate time-frequency representation.
Can we use this to separate the two?

Look at the different scales!

