

A bit of context…

HEP is moving towards new technologies, in particular hardware accelerators

Moving from general purpose devices \Rightarrow application specific

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Monte Carlo simulation and data analysis are intensive and requires lots of computing power.

Quantum computing for HEP experiments

QC4HEP WG [arXiv: [2307.03236\]](https://arxiv.org/abs/2307.03236)

Many experimental and theoretical HEP applications are deemed to benefit from quantum computation.

Recap

- required to develop algorithms \blacksquare
- complete introspection \blacksquare
- require noise modeling \blacksquare

- limited (in many senses) \Box
- requires calibration \blacksquare
- final validation \Box

Discrete gates primer

Goal: Construct a generic $U(2^n)$ operation based on building blocks

The Hilbert space on which the unitaries act is a strutured as a \bigotimes tensor product of n qubits

$$
|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \hspace{1cm} |1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}
$$

the generic qubit state is:

$$
\ket{\psi} = \alpha \ket{0} + \beta \ket{1} \qquad \text{with} \ \ \vert \alpha \vert^2 + \vert \beta \vert^2 = 1
$$

and it can be visualized as a point on the Bloch sphere

$$
\alpha = \cos \theta/2 \qquad \beta = e^{-i\phi} \sin \theta/2
$$

Example gates: Pauli

X gate

The X gate acts like the classical NOT gate, it is *represented by the* σ_x *matrix,*

$$
\sigma_x=\begin{pmatrix}0&1\\1&0\end{pmatrix}
$$

therefore

$$
\begin{array}{c} |0\rangle \longrightarrow |1\rangle \\ |1\rangle \longrightarrow |0\rangle \end{array}
$$

The Z gate flips the sign of $\ket{1}$, it is represented by the σ_z matrix,

$$
\sigma_z=\begin{pmatrix}1&0\\0&-1\end{pmatrix}
$$

therefore

 $|0\rangle \longrightarrow |0\rangle$ $|1\rangle \longrightarrow -|1\rangle$

P possibly **redundant**, since it may be efficient to execute

 \circledS

nultiple implementations, related to diverse hardware

Gates could be variously parametrized, so there exists universal sets made beyond

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 \circled{c}

 \blacksquare

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 $\circ \circ \circ \circ \circ \circ$

Circuit

Unitary - but measurements.

Circuit are a way to compose gates to build unitaries, *sequentially*

$$
|\psi\rangle - Y - X - = -X \cdot Y - XY |\psi\rangle
$$

or in *parallel*

$$
\begin{array}{ccc}\n\ket{\psi} & -\boxed{Y} - Y \ket{\psi} & & \ket{\psi} \\
\ket{\phi} & -\boxed{X} - X \ket{\phi} & & \ket{\phi} - \boxed{Y \otimes X} \\
\end{array}\n\begin{array}{ccc}\n\ket{\psi} & - & \boxed{Y \otimes X} \\
\ket{\phi} & - & \boxed{Y \otimes X}\n\end{array}\n\begin{array}{ccc}\n\end{array}\n\begin{array}{ccc}\n\ket{Y \otimes X} & \ket{\psi} \otimes \phi\n\end{array}
$$

Parametrized gate

Other parameters are possible: GPI and $GPI2$ parametrize the position of the axis, multi-qubit gates can paramterize complex interactions, …

Having parameters, it opens the door to optimization $\mathcal{D} \rightarrow$ i.e. quantum machine learning (QML)

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The atoms of interaction

Controlled gates (conditionals)

The controlled-\$NOT\$ (\$CNOT\$) gate is a conditional gate defined as

$$
CNOT \equiv \begin{pmatrix} 1 & 0 \\ 0 & \sigma_x \end{pmatrix}
$$

control target

$$
|00\rangle \rightarrow |00\rangle \qquad |01\rangle \rightarrow |01\rangle
$$

$$
|10\rangle \rightarrow |11\rangle \qquad |11\rangle \rightarrow |10\rangle
$$

We define a control qubit which, if at $\ket{1}$, applies X to a target qubit.

Multi-qubit gates allow entangling states

Measurement

The non-unitary gate *that you have*

Measurements are special gates, in two ways:

- 1. it is the only operation that allows to extract information
- 2. it is the only non-unitary gate

Noise and channels

Non-unitary operations model

Instead of acting over a state vector, the state will be tracked by a density matrix

 $|\psi\rangle \longrightarrow \rho \quad (\sim |\psi\rangle\,\overline{\langle\psi|})'$

This makes possible to track phenomena like decoherence, which has not a unitary action on the state.

Another option is to exploit measurement nonunitarity, and represent the noise through *repeated execution*.

Kraus **TI**

$$
\Phi(\rho)=\sum_i B_i \rho B_i^*
$$

Stinespring \Box

$$
U_0=\sum_\alpha K_\alpha \otimes \ket{\alpha}\bra{v_0}
$$

Choi

- $\Lambda = \vert U \rangle \rangle \langle \langle U \vert$
- Liouville, Quantum networks, … \blacksquare

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Applications

credits M. Robbiati

credits M. Robbiati

QML - remarks

A classical function being clasically optimized.

$$
\bar{y}_{est}(\bar{\theta}) = \bra{0} U(\bar{\theta}) \ket{0} \quad : \quad \mathbb{R}^n \to \mathbb{R}^m
$$

If a first-order optimization \mathcal{D} method used, gradient calculation may be "quantum-aware" (PSR). \rightarrow

The advantage is mainly in the inference time, and possibly ansatz expressivity.

Quantum computation is naturally based on continuous variables. But in practice they are generated through digital control electronics with noisy calibrated pulses

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qPDF [arXiv: [2011.13934\]](https://arxiv.org/abs/2011.13934)

 \bigcircled{C} Parametrize *Parton Distribution Functions (PDF)* with multi-qubit variational quantum circuits

\triangle

1. Define a quantum circuit: $\mathcal{U}(\theta,x)\ket{0}^{\otimes n} = \ket{\psi(\theta,x)}$ 2 . $\mathcal{U}_w(\alpha, x) = R_z(\alpha_3 \log(x) + \alpha_4) R_z(\alpha_1 \log(x) + \alpha_2).$ 3. Using $z_i(\theta, x) = \bra{\psi(\theta, x)} Z_i \ket{\psi(\theta, x)}$

$$
\mathrm{qPDF}_i(x,Q_0,\theta) = \frac{1-z_i(\theta,x)}{1+z_i(\theta,x)}
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Algorithm's summary:

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Density estimation with adiabatic QML [arXiv: [2303.11346\]](https://arxiv.org/abs/2303.11346)

Determining *Probability Density Functions (PDF)*

by fitting the corresponding Cumulative Density Function (CDF) using an adiabatic QML ansatz.

\Leftrightarrow

 (\cancel{C})

- 1. Optimize the parameters $\bar{\theta}$ using adiabatic evolution: $H_{ad}(\tau; \bar{\theta}) = 0$ $[1 - s(\tau; \bar{\theta})] \hat{X} + s(\tau; \bar{\theta}) \hat{Z}$ in order to approximate some target CDF values
- 2. Derivate from H_{ad} a circuit $\mathcal{C}(\tau; \bar{\theta})$ whose action on the ground state of \hat{X} returns $\ket{\psi(\tau)}$
- 3. The circuit at step 2 can be used to calculate the CDF
- 4. Compute the PDF by derivating ${\cal C}$ with respect to τ using the Parameter Shift Rule

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Quantum hardware

Quantum computation

Various models are proposed and explored

- 1. discrete gate-based
- 2. continuous variable (a.k.a. bosonic)
- 3. quantum annealing

The potential use cases partially overlap, and it is possible to emulate each other (at least approximately).

They are particularly related to the hardware realizing them...
Technologies

Many technologies simultaneously investigated [arXiv: [2304.14360\]](https://arxiv.org/abs/2304.14360)

Pros and cons for each, investigated by different groups, including diverse private companies.

Some optimal for specific applications, others for further usage, e.g. quantum memories [arXiv: [1511.04018\]](https://arxiv.org/abs/1511.04018).

Superconducting

One of the platforms with most resonance

«IBM» and *«Google»* are definitely two prominent players, but superconducting hardware is being investigated by a plethora of labs.

Within the scope of this technology, many variations are also possible (flux-tunable qubits, couplers, crossresonance schemes), so it is a macro-category.

Neutral atoms

«Atom computing» have been the first to claim >1000 qubits LarXiv: [2401.16177\]](https://arxiv.org/abs/2401.16177)

Control

Qibo

- Your quantum workhorse -

The ecosystem

Contributors (March 2024)

Execution

Backends mechanism

Plug the framework.

Structure the integration of the various libraries.

Common operations are implemented once and reused (when possible).

Results [[arXiv: [2203.08826](https://arxiv.org/abs/2203.08826)]

Automatic differentiation

for quantum machine learning → *Qiboml*

Autodiff simulation is fundamental to support QML investigation.

A dedicated differentiable backend in simulation can considerably help algorithms development.

Moving towards a single interface, encompassing both simulation and quantum hardware implementations.

Framework portability: implement in one, export derivatives.

Clifford

Specialized execution.

 $|\psi\rangle = U |\psi\rangle$

 $\bf{Theorem~1}$ $\bf{Given~an~}$ \bf{n} -qubit state $|\psi\rangle$, the *following are equivalent:*

(i) $\ket{\psi}$ can be obtained from $\ket{0} \otimes n$ by CNOT, Hadamard, *and phase gates only.* (ii) $\ket{\psi}$ can be obtained from $\ket{0}\otimes n$ by CNOT, Hadamard, *phase, and measurement gates only.* (iii) *is stabilized by exactly 2n Pauli operators.* ∣*ψ*⟩ (iv) $|\psi\rangle$ *is uniquely determined by* $S(|\psi\rangle) = 0$ $Stab(\ket{\psi}) \cap P_n$ <u>or the group of Pauli operators that</u> *stabilize* ∣*ψ*⟩

Instead of operating on the whole state vector, the state is represented by a much more compressed *tableau*.

It still requires vectorized operations on the boolean entries, that can be optimized in a similar fashion to the general state vector approach.

Clifford

Benchmarks

Clifford

Benchmarks

Optimized for observables.

Optimized for observables.

Optimized for observables.

Optimized for observables.

beyond opt_einsum

Approximation

Based on singular value decomposition (SVD).

A very frequent matrix product state (MPS).

But also other ansatzes are used.

Workload distribution

for q in range(nq): c.apply_gate('H', q)

```
for q in range(\emptyset, nq, 2):
    c.apply_gate('CNOT', q, q + 1)
```
c.apply_gate('CNOT', 4, 7) c.apply_gate('CNOT', 4, 1) c.apply_gate('CNOT', 4, 0)

beyond opt_einsum

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```
QiboTN

QiboTN

Transpilation

-- the bridge to hardware

Qibolab [[arXiv: [2308.06313\]](https://arxiv.org/abs/2308.06313)

Quantum control

Execution flow

Qibolab - Interface

The **input** for a computation could be very standard, at the level of a **circuit**. That kind of interface is already defined by $Qibo$ itself.

However, at a lower level, **pulses** are still a standard-enough way to interact with hardware, and these are defined by **Qibolab**.

def create():

instrument = DummyInstrument("myinstr", "0.0.0.0:0")

```
channels = ChannelMap()
channels \models Channel"readout",
    port=instrument.ports("o1")
```
return Platform("myplatform", qubits={ $qubit.name: qubit$ }, instruments={instrument.name: instrument}, .

Qibolab - Drivers

Qibosoq - Server on QICK [arXiv: [2310.05851\]](https://arxiv.org/abs/2310.05851)

Qibolab handles the whole connection, and takes care of fetching the single or multiple results.

For the single open source platform *FPGA firmware* currently in Qibolab, there has been a dedicate effort to define a suitable server, to optimize the communication with the board.

 \rightarrow Qibosoq

[Platform dashboard](http://login.qrccluster.com:10000/)

 $15:00$

 0 2.39 K 103

 $\frac{1}{15:30}$

avg current

Qibocal [arXiv: [2303.10397\]](https://arxiv.org/abs/2303.10397)

A due mention

- \Box characterize the hardware
- calibrate control
- validate performances

Pulses' calibration

Scan spectrum to identify the coupled resonator frequency.

Tune the amplitude (duration) of the drive pulse, in order to excite the qubit from the ground state up to state $|1\rangle$.

Protocols report

QPU control implementation

$CHSH \rightarrow$

Randomized benchmarking ↓

They are two of the routines available in Qibocal, allowing to validate the QPU performances.

Protocols report

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Uploaded Reports

Please select a report from the table below:

Qibocal Reports

Calibrated data

\geq Not a one-man show...

Thanks