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Model wavefunctions for an interface between lattice Laughlin and Moore-Read states

Blazej Jaworowski
Model wavefunctions for interfaces between lattice Laughlin and Moore-Read states

Błażej Jaworowski, Anne E.B. Nielsen

**Motivation:** What happens at non-Abelian FQH interfaces?

- Interfaces can have topological structure which can generate nontrivial phenomena (e.g. additional topological degeneracy).
- Few microscopic works – ED is hard. Model wavefunctions can help.
- Almost all of them describe continuum systems
- Anyons are important, but we are not aware of any microscopic studies.

**Method:** Model wavefunctions from CFT correlator of two types of vertex operators,

\[ \psi(n) = \langle 0| \prod_{i=1}^{N_L} V_{i,\text{MR}}(z_i, n_i) \prod_{i=N_L+1}^{N} V_{i,\text{Laughlin}}(z_i, n_i) |0 \rangle, \]

and Monte Carlo study of their properties (GS+quasiholes+quasielectrons).
**Ground state:** particle density, correlation function, entanglement entropy

---

**Anyons:** charge and statistics of anyons before and after crossing the interface.

**Multiple islands:** topological degeneracy.
A random unitary circuit model for black hole evaporation

Christoph Sunderhauf
A random unitary circuit model for black hole evaporation

Lorenzo Piroli*, Christoph Sünderhauf*, Xiao-Liang Qi (* contributed equally)


Coupling to environment

$W_{l,m}$  SWAP

Instrinsic dynamics

$U_{i,j}$  Haar-random
(w/ & w/o charge conservation)
A random unitary circuit model for black hole evaporation

Lorenzo Piroli*, Christoph Sünderhauf*, Xiao-Liang Qi (* contributed equally)

AKLT-states as ZX-diagrams: diagrammatic reasoning for quantum states

Richard D.P.East
AKLT-states as ZX-diagrams: diagrammatic reasoning for quantum states


- Tensor networks have found numerous applications.
- They are an excellent graphical representation of states.

But

- Diagrammatic representations of tensor networks are an excellent aid, but not a calculation tool.

Our solution

- The ZX calculus is a diagrammatic language for qubit tensor networks.
- We can perform calculations by only altering the diagrams.

(a) Singlet

\[ \frac{1}{\sqrt{2}} (|01\rangle - |10\rangle) \propto \]

(b) Projector

\[ |+\rangle \langle 11| + |0\rangle \frac{\langle 10| + \langle 01|}{\sqrt{2}} + |\rangle \langle 00| \]

(c) AKLT state

\[ j_n \]

(d) Spin-1

\[ \alpha_1 \]

(e) MPS equivalence

\[ \propto M^{[n]+1} \quad \propto M^{[n]0} \quad \propto M^{[n]-1} \]
Things you can do

- In the 1D AKLT state we identify the edge states, retrieve the MPS representation, and prove the existence of a string order diagrammatically.

- In 2D we simplify the proof that the 2D AKLT state is a universal resource.

\[
\begin{align*}
\frac{1}{2} & = \frac{1}{2\sqrt{2}} \\
\frac{1}{2} & = \frac{1}{2\sqrt{2}} \\
\frac{1}{2} & = \frac{1}{2\sqrt{2}}
\end{align*}
\]

\[
 offending \\
(\text{f})
\]

\[
\begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} = \frac{1}{\sqrt{6}} M^{[n]+1}
\]

Example of a diagrammatic calculation.
Anderson complexes: Bound states of atoms due to Anderson localization

Krzysztof Giergiel
Cold atomic system driven by time periodic external force can give rise to *time crystals*.

Disordered time periodic driving gives rise to *Anderson localization in time domain*.

Cold atoms by *Feshbach* resonance give control over interaction strength (even sign).

It is natural to investigate *periodic driving* of internal *interaction strength* instead of external force.

If this interaction strength varies in disordered fashion in time what will we see?
What?
Anderson Complexes - Bound states of atoms due to Anderson localization

\[ H = \frac{p_{12}^2}{m^*} + V(r_{12}), \]

\( V(r_{12}) \) is a random function with infinite support.

In localized regime one expect exponential localization in relative distance:

![Interaction potential and Probability density plots](image-url)
Continuous matrix product operator approach to finite temperature quantum states

Wei Tang
CONTINUOUS MATRIX PRODUCT OPERATOR APPROACH
TO FINITE TEMPERATURE QUANTUM STATES

Wei Tang @ PKU

\[ L = \infty \]

\[ \beta \]

\[ \langle l | \quad T \quad | r \rangle \]
Correlation-enhanced Neural Networks as Interpretable Variational Quantum States

Agnes Valenti
Correlation-enhanced Neural Networks as Variational Quantum States

RBMs with correlators

Topological phases

Excited states without symmetries

In preparation:
A Valenti (ETH Zürich), E Greplova, NH Lindner and SD Huber
Effcient MPS methods for extracting spectral information on rings and cylinders

Maarten Van Damme
Efficient MPS methods for extracting spectral information on rings and cylinders

Quasiparticle ansatz

\[
\sum_i \begin{array}{c}
A_i^l \\
\vdots \\
B_i \\
\vdots \\
A_N^r
\end{array}
\]

(1)

Applied to

- finite mps
- cylinder infinite mps
Efficient MPS methods for extracting spectral information on rings and cylinders

(a) spin 1 heisenberg, OBC

(b) critical ising, PBC

(c) cylinder ising, $p_y = 0$

(d) Magnon hubbard, different $p_y$
Generating Function for Tensor Network Diagrammatic Summation

Wei-Lin Tu
GENERATING FUNCTION FOR TENSOR NETWORK
DIAGRAMMATIC SUMMATION

Wei-Lin Tu

Institute for Solid State Physics (ISSP), University of Tokyo


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Tensor Networks:

One-particle excitation:

\[ S^{\alpha,\beta}(k) = \frac{1}{N} \sum_{j,j'=1}^{N} e^{ik \cdot (r_j - r_{j'})} \left\langle \hat{O}_{j}^{\alpha} \hat{O}_{j'}^{\beta} \right\rangle \]

Static structural factor:

\[ S_{\alpha,\beta}^{\alpha,\beta}(k) = \frac{1}{N} \sum_{j,j'=1}^{N} e^{ik \cdot (r_j - r_{j'})} \left\langle \hat{O}_{j}^{\alpha} \hat{O}_{j'}^{\beta} \right\rangle \]

Generating function

\[ |G_\Phi(\lambda)\rangle = \begin{array}{c} \text{MPS} \\ \text{PEPS} \end{array} \]

\[ MPS_j(\lambda) = A + \lambda e^{-ikr_j}B \]

\[ \hat{G}_{\text{SF}}(\lambda) = \begin{array}{c} \text{MPS} \\ \text{PEPS} \end{array} \]

\[ \hat{G}_{\Phi}(\lambda) = \begin{array}{c} \text{MPS} \\ \text{PEPS} \end{array} \]

\[ \hat{O}_{j}^{\beta}(\lambda) = I + \lambda e^{-ikr_j}\hat{O}_{j}^{\beta} \]

With the help of desired generating functions, the number of tensors under consideration can be largely reduced!
Homogeneous Floquet time crystal from weak ergodicity breaking

Hadi Yarloo
Horizon bound in QFT

Ivan Kukuljan
Horizon bound in QFT

- Prepare a QFT in a short range correlated initial state \( \langle O(x)O(y) \rangle_C \propto e^{-|x-y|/\xi} \)
- Quench \( H_0 \rightarrow H \)
- Correlations spread within a horizon
  \[ |\langle O(t,x)O(t,y) \rangle_C| < \kappa e^{-\max\{(|x-y|-2ct)/\xi_h,0\}} \]
- Proven in CFT, demonstrated analytically and numerically in many systems, observed experimentally
  \( \rightarrow \) Believed to be a general property of quantum systems
Horizon violation

- Oscillating infinite range correlations of currents
  \[ C_\mu(t, x, y) = \langle J^\mu(t, x) J^\mu(t, y) \rangle \]
  - Found in the sine–Gordon model (using bosonisation and truncated Hamiltonian methods)
    *IK, Sotiriadis, Takács, JHEP 2020, 224*
  
- Recently found in gauge theory – 1+1D quantum electrodynamics (using THM)
  *IK, arXiv:2101.07807 [hep-th]*

- Related to nontrivial field topology
Investigation of the Néel phase of the frustrated Heisenberg antiferromagnet by differentiable symmetric tensor networks

Juraj Hasik
Investigation of the Néel phase of the frustrated Heisenberg antiferromagnet by differentiable symmetric tensor networks, SciPost Phys. 10, 012 (2021)
Measurement-induced transition in random quantum circuits: from stroboscopic to continuous

M. Szyniszewski
Measurement-induced transition in random quantum circuits: from stroboscopic to continuous

BY M. SZYNISZEWSKI, A. ROMITO, H. SCHOMERUS

Quantum circuit

- Random unitary evolution (U) and weak measurements (M)

- What is the stationary state entanglement?

\( \lambda \) favours volume law.
\( M \) (if strong) favours area law.

Stroboscopic measurements: phase diagram

\[ \text{var}(S_\infty) \]

\( 0.03 \quad 0.09 \quad 0.15 \quad 0.21 \quad 0.27 \quad 0.33 \quad 0.39 \)

\[ \text{Measurement frequency } p \]

Area law
Volume law
Continuous measurements: phase transition

- Phase transition still present when continuous measurement is used

Universality of the phase transition

Discrete and continuous regimes seem to be smoothly connected and exhibit similar critical exponents. Universality between the two regimes?
Non-separable time-crystal structures on the Mobius strip

Arkadiusz Kuros
Non-separable time-crystal structures on the Möbius strip

Krzysztof Giergiel¹
Arkadiusz Kuros³
Arkadiusz Kosior²
Krzysztof Sacha¹

¹Institute of Theoretical Physics, Jagiellonian University in Kraków, Poland
²Max-Planck-Institut für Physik Komplexer Systeme, Dresden, Germany

Abstract

Periodically driven many-body quantum systems provide a comfortable platform for modelling crystalline structure in the time dimension which opens a path to realize temporal condensed matter physics and explore novel phenomena. It has been already shown that the time domain can host Anderson localization, Mott insulator phase [1], topological phases [2], dynamical phase transitions [3], quasi-crystals [4] and fractional time crystals [5]. Here, we present a simple implementation of non-separable two-dimensional lattices with a non-trivial topology in the time domain that can be created for a Bose-Einstein condensate bouncing resonantly between two oscillating mirrors. As an example, we consider a three-band Lieb lattice [6] on the Möbius strip with a middle flat band. The dynamics of the flat band is governed solely by interactions, which can be easily tuned by periodic changes of scattering length using Feshbach resonance mechanism. This allows us to engineer exotic long-range interactions [7] and offers a new perspective for studying many-body dynamics.

Single-particle bouncing between two oscillating mirrors

- Hamiltonian in the frame oscillating with the mirrors

\[ H = \frac{p_x^2 + p_y^2}{2} + V(x, y) + (x + y) f_{xy} + y f_{xy}(0) \quad y \geq x \geq 0 \]

- The mirrors are located around \( x = 0 \) and \( x = y = 0 \) and form a wedge with the angle \( 45° \)

- The effective time-independent Hamiltonian that describes the motion of a particle close to a resonant orbit

\[ H(t) = H(t + T) \quad T = \frac{\pi}{2} \]

- \( f_{xy}(t), f_{xy}(t) \) - periodic functions correspond to the mirror oscillations

The static wedge for \( f_{xy}(t) = f_{xy}(t + T) = 0 \)

- \( \theta \)


Box

- the system is integrable \( \rightarrow \) action-angle variables

\[ H_{ij}(L_x, L_y) = \frac{n x^2 + 2}{2} L_x^2 + L_y^2 \]

- for \( k_i \Omega \Theta \) \( k_i \partial \Omega \partial \)

- all trajectories are periodic

- third independent integral of motion \( I_3 = (L_3 \partial L_3 - L_3 \partial L_3) (\mod 2x) \)

- periodic orbit can be described by a single frequency only

- canonical transformation from \( (I_x, I_y, \theta_x, \theta_y) \) to new variables \( (I_x, I_y, \theta_x, \theta_y) \)

\[ I_3 = \text{const.} \quad \theta_3 = \text{const.} \quad \theta_3 = 0 + \theta_3 \]

Periodically oscillating mirrors

- resonant driving of a particle \( \omega \approx \delta \Omega (I_x', I_y') \)

- classical secular approximation

- canonical transformation to the frame moving along a resonant orbit

- Cartesian coordinates \( (I_x, \theta_x) \) and \( y \) \( (I_y, \theta_y) \) can be expanded in the Fourier series

- all dynamical variables evolve slowly if we choose initial conditions close to the resonant orbits

- averaging over the fast time variable

- effective time-independent Hamiltonian that describes the motion of a particle close to a resonant orbit

\[ H_{ij} = \frac{p_{ij}^2}{2m_{ij}} + V_{ij}(\theta_i, \theta_j, f_{ij}, f_{ij}) \]

By different shaking protocols of two mirrors \( f_{ij}(t) \) and \( f_{ij}(t) \), it is feasible to construct many lattice geometries, just like in optical lattice engineering.

Lattice structures

- effective Hamiltonian

\[ H_{i,j} = \frac{p_{ij}^2}{2m_{ij}} + \frac{\lambda_1}{2} \cos(2\theta_i \phi) \cos(2\theta_j \phi) + \frac{\lambda_2}{2} \cos(\theta_i \phi) \cos(\theta_j \phi) + \frac{\lambda_3}{2} \cos(2\theta_i \phi) + \phi \]

- with \( \phi = \theta_i - \theta_i \theta_j \)

- for \( f_{ij}(t) = \lambda_2 \cos(\theta_i \phi) + \lambda_3 \sin(\theta_i \phi) \) and \( f_{ij}(t) = -\lambda_1 \cos(\theta_i \phi) + \phi \)

- \( H_{ij} \) describes a particle moving on the Möbius strip in the presence of a non-separable lattice potential

Tightly bounded particle in the asymmetric Lieb lattice

- quantum description in resonant Hilbert subspace

\[ H_{ij} = -J_{ij} \sum_i \frac{\partial \hat{a}_i}{\partial \hat{a}} \bar{j} - \sum_i \bar{j} \frac{\partial \hat{a}_i}{\partial \hat{a}} \bar{i} \]

- for \( J_{ij} \ll 1 \), eigenvalues of \( H_{ij} \) form well separated three bands where the central band is flat

Ultra-cold bosonic atoms in the flat band

- \( N \) bosons interact via Dirac-delta potential \( g \psi(x) \)

- many-body Floquet Hamiltonian restricted to the flat band subspace

\[ H = \frac{1}{T} \int_0^T dt \int d\Psi(x, y) \left[ \frac{H_{ij} - g}{2} \frac{\partial \hat{a}_i}{\partial \hat{a}} \bar{j} + \text{constant} \right] \]

- \( \theta = \sum_{i=1}^{\omega+1} n_\omega \) with the bosonic operators \( \hat{j}, \hat{j}^\dagger \)

- control of the contact interactions by changes of scattering length using Feshbach resonance mechanism

- Wannier states corresponding to the flat band \( w_i(x, y, t) = \hat{w}_i(x, y, t) \)

Pair tunnelling processes

- hard-core bosonic Floquet Hamiltonian

\[ H_F = -J \sum_i \Delta_i \hat{a}^\dagger_i \hat{a}^\dagger_i \]

- simultaneous tunneling of two particles between four distinct lattice sites \( J = \delta \frac{n^2}{4} \delta \psi(\gamma \epsilon) \)

- nearest neighbour repulsion \( U = \delta \frac{n^2}{4} \delta \psi(\gamma \epsilon) \)

References

Resonating valence bond realization of spin-1 non-Abelian chiral spin liquid on the torus

Hua-Chen Zhang
Resonating valence bond realization of spin-1 non-Abelian chiral spin liquid on the torus

Hua-Chen Zhang @
IOP CAS & TU Dresden
23 Feb 2021, Benasque SCS
We propose resonating valence bond (RVB) wave functions for a spin-1 lattice system on the torus that realize a non-Abelian chiral spin liquid.

These wave functions are shown to be equivalent to chiral correlation functions in a certain conformal field theory (CFT) and identified to be a lattice analogue of the bosonic Moore-Read state at unit filling.

The topological order of this system is revealed by explicit construction of the topologically degenerate ground states and analytical computation of their modular matrices.
Simulation of three-dimensional quantum systems with projected entangled-pair states

Patrick Vlaar
Simulation of three-dimensional quantum systems with projected entangled-pair states

Patrick Vlaar & Philippe Corboz
arXiv:2102.06715
Simulation of three-dimensional quantum systems with projected entangled-pair states

• Tensor network techniques very successful in 1D and 2D, however applications in 3D are limited

• We present two techniques
  • Cluster contraction
  • Full contraction

• We expect this work to be an important step towards making iPEPS a promising tool to study open problems in 3D
Solving frustrated Ising models using tensor networks

Bram Vanhecke
Solving frustrated Ising models using tensor networks

Bram Vanhecke, Jeanne Colbois, Laurens Vanderstrectaten, Frank Verstraete, Frédéric Mila

Phys. Rev. Research 3, 013041 – Published 13 January 2021

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<th>AF-Ising on kagome</th>
<th>AF-Ising on triangular</th>
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<td>MPS</td>
<td>0.5018331646 (D = 10)</td>
<td>0.3230659407 (D = 250)</td>
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<tr>
<td>exact</td>
<td>0.5018331646</td>
<td>0.3230659669</td>
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Spurious cluster configurations
Convex sets, and linear programming: $A \hat{x} \leq \bar{B}$
String order parameters for symmetry fractionalization in an enriched toric code

Mohsin Iqbal
String order parameters for symmetry fractionalization in an enriched toric code

José Garre-Rubio, Mohsin Iqbal, David T. Stephen


SCS Benasque-2021
**Goal**

Construct SOP for characterizing the symmetry fractionalization pattern of the anyons: detect the SET phase

We start from TC on edges decoupled from ferromagnet on vertices

\[ \tilde{H}_{TC} = H_{TC} - \sum_{v \in V} X_v \]

The charge fractionalizes TRS, BC inversion and the on-site symmetry $\mathbb{Z}_2 \times \mathbb{Z}_2$

We generalize the SOP of [1] beyond PEPS and RGFP to measure the SF class of the charge.

\[ \mathcal{O}^{[a,b]} = \frac{\langle \Lambda^{[a,b]} \rangle}{\langle \Lambda^{[0,0]} \rangle} \]

Results

Test the SOP in the Hamiltonian interpolation

\[ \lambda \tilde{H}_{TC} + (1 - \lambda) H_{SET} \]

Phase diagram under magnetic fields

\[ H_{SET} - h^X_e \sum_e Z_e - h^Z_e \sum_e X_e \]

We observe SSB because of the condensation of the anyon that fractionalizes the symmetry (charge vs flux)

The phase diagram changes from the one of the TC: infinite line between trivial (topological) phases!
The SYK model from strained honeycomb irradiates: A case study

Mikael Fremling
The SYK model from strained honeycomb iridates

Sachdev-Ye-Kitaev

Strained
Kitaev Honecomb

The dream

SYK

Mikael Fremling
Utrecht University

H$_3$LiIr$_2$O$_6$ Iridates

Entanglement in Strongly Correlated Systems - Benasque - February 2021
Random hopping elements in a flat band

\[
H_{\text{SYK}} = \sum_{i,j,k,l} J_{i,j,k,l} \gamma_i \gamma_j \gamma_j \gamma_k
\]

\[
H_{\text{Strain}} = \sum_{n_1,n_2;m_3,m_4} J_{n_1,n_2;m_3,m_4} \gamma^{A}_{n_1} \gamma^{A}_{n_2} \gamma^{B}_{m_3} \gamma^{B}_{m_4}
\]
Variational wave functions for spin-phonon models

F. Ferrari