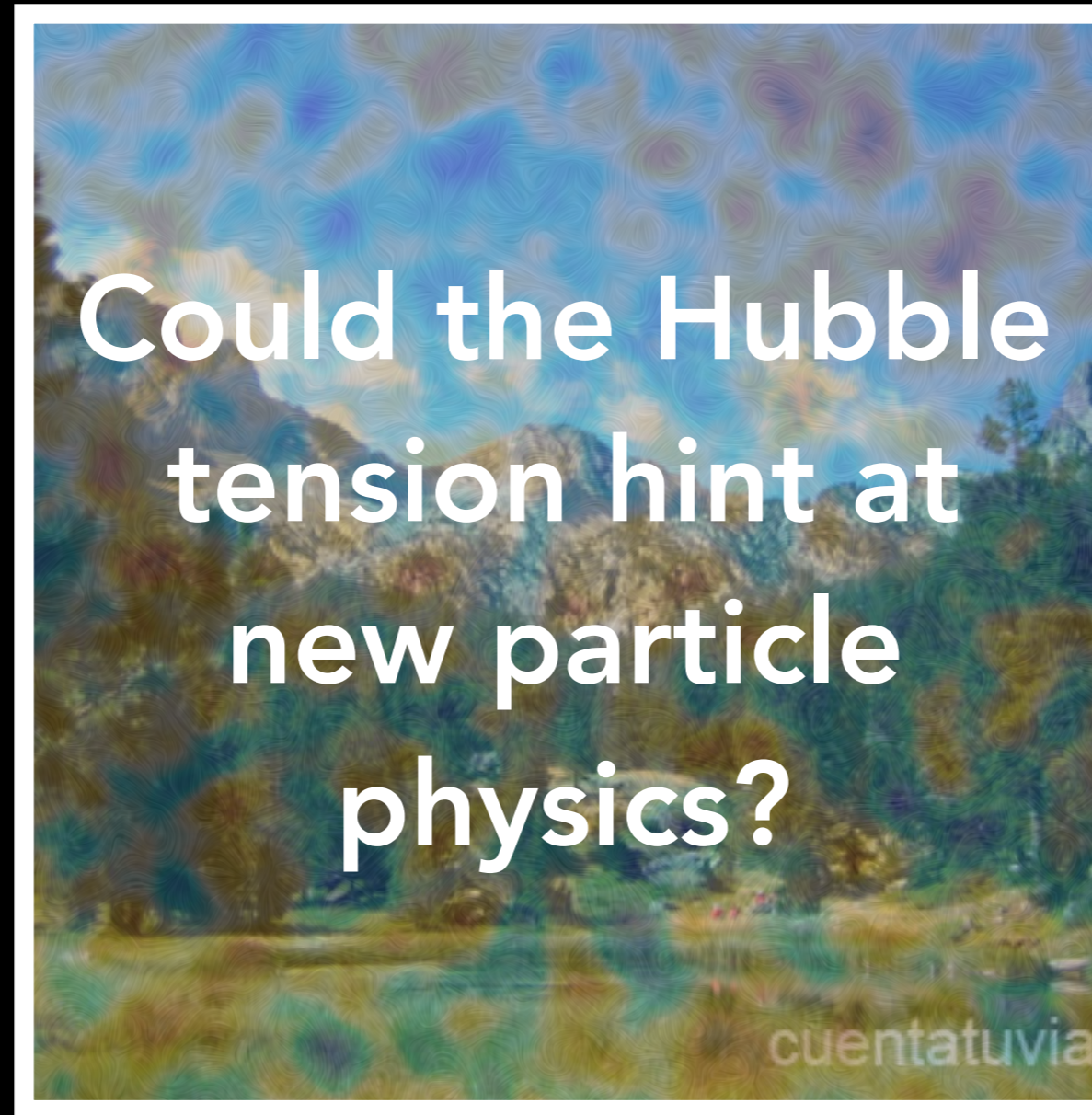


Benasque, 7.08.2019

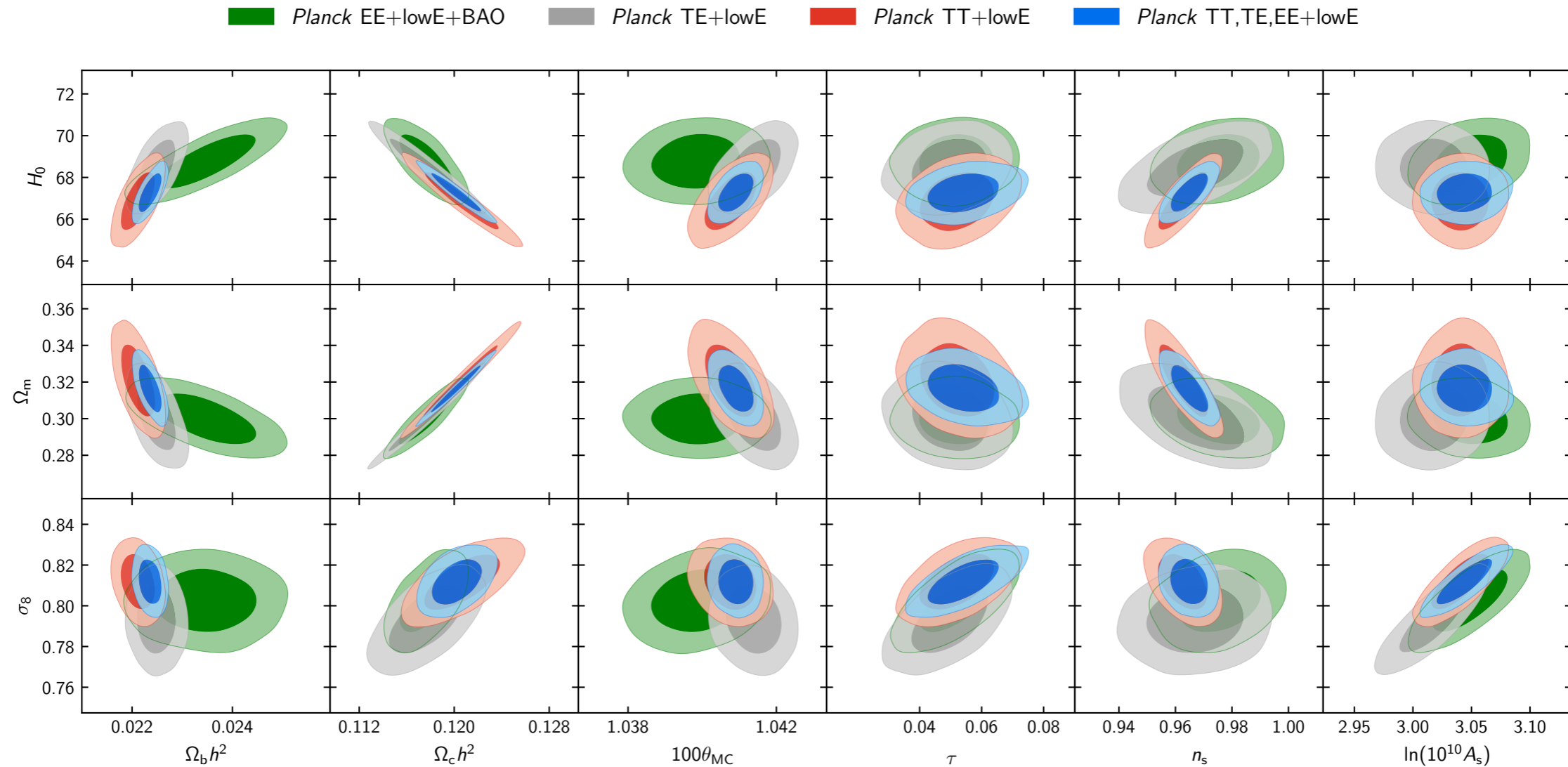


J. Lesgourgues

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Robustness of Λ CDM

- Internal consistency of Λ CDM fit to CMB observables [Planck col. 1807.06209]

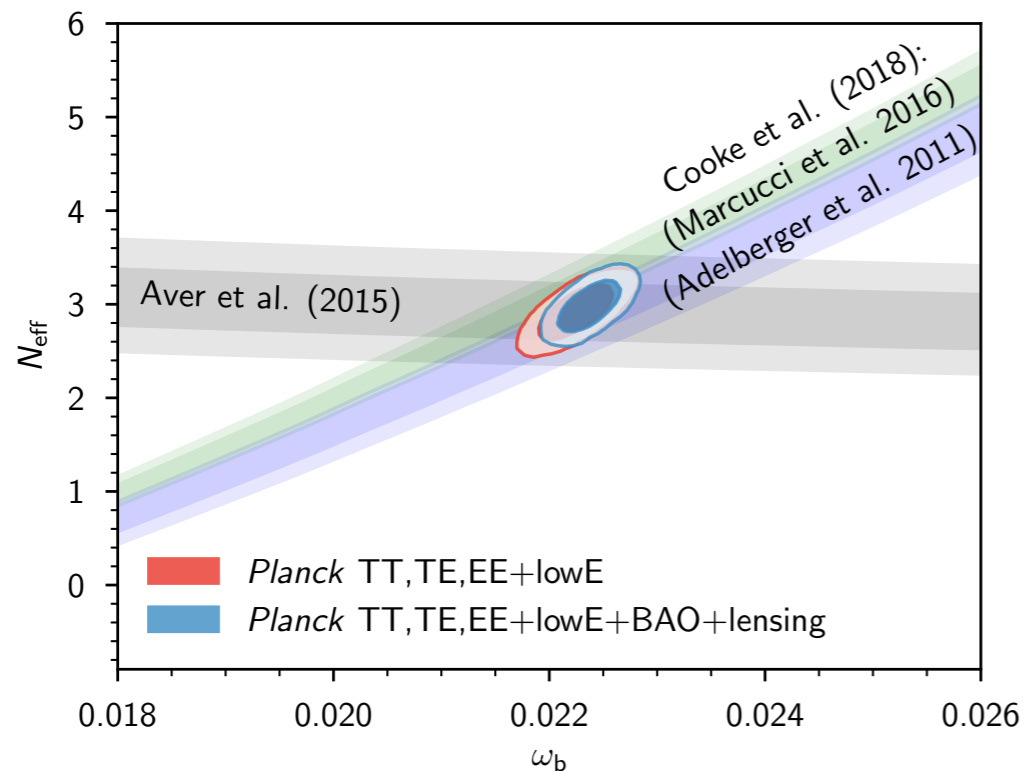


- Still: CMB data probes the universe mainly at $10^3 < z < 10^5$, with some sensitivity to lower redshift through: angular distance, CMB lensing, (late ISW). H_0 and σ_8 extrapolated from data+model.

Robustness of Λ CDM and Hubble tension

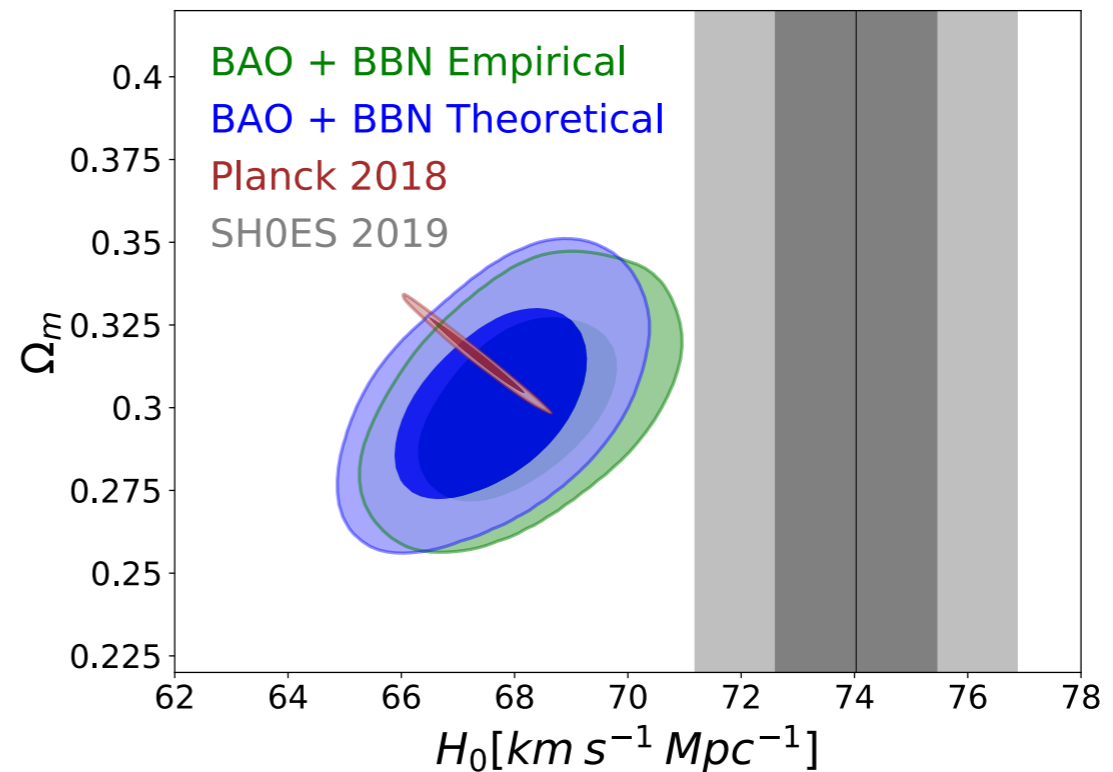
- Consistency of Λ CDM fit across multiple probes: CMB, BAO, BBN, distant SNIa...

He, D $\rightarrow \omega_b, N_{\text{eff}}$



[Planck col. 1807.06209]

BAO $\rightarrow H_0, \Omega_m, \omega_b$; BBN $\rightarrow \omega_b$



[Cuceu et al. 1906.11628]

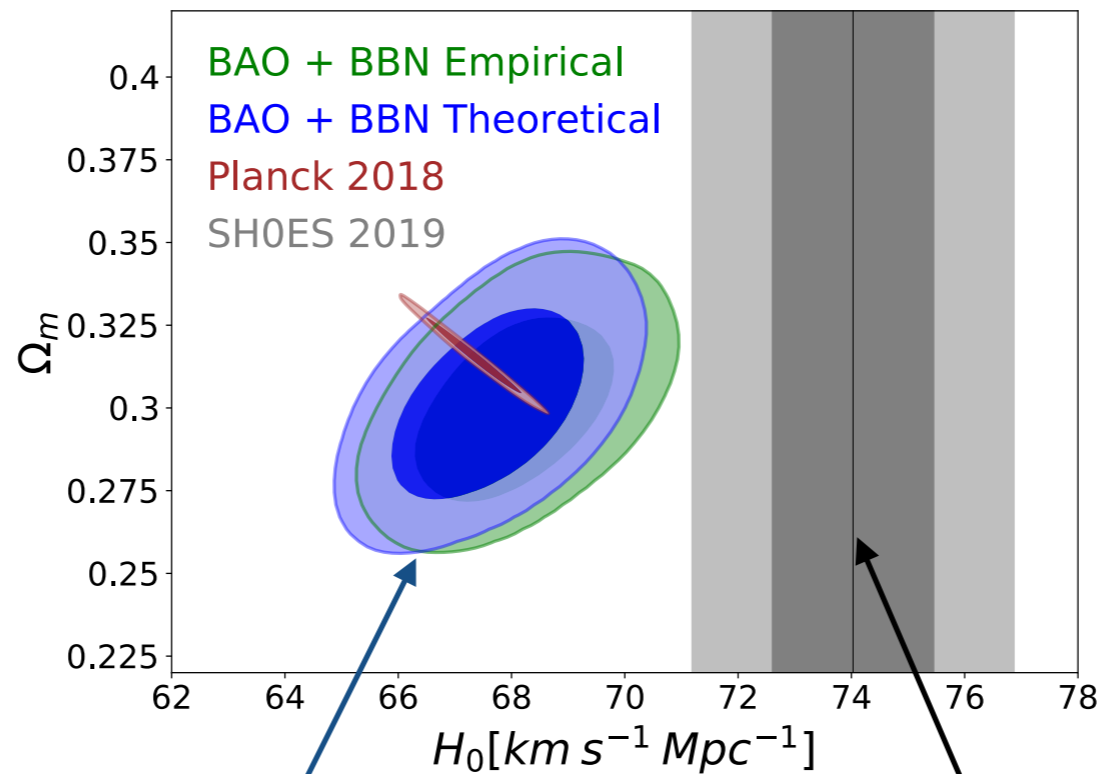
- Inconsistency with high H_0 measured with SNIa calibrated with cepheids (HST, SHOES). 4σ with Riess et al. 1903.07603. Quasar time-delay also prefer high H_0 and combination gives 5σ tension.

Violating the Etherington relation, or something simpler?

- BAO+BBN versus SH0ES: if all basic assumptions are correct:

standard expression for BAO scale
deuterium measurement and BBN calculations

cepheid calibration method for SNs



Very well tested
see however Rigault et al.
[1412.6501, 1806.03849]

[Cuceu et al. 1906.11628]

Standard rulers

Standard candles

Etherington reciprocity relation (1933) : $d_L(z) = (1+z)^2 d_A(z)$ for general metric theories of gravity
(see exceptions in Bassett & Kunz astro-ph/0312443)

Deuterium measurement and BBN calculations

- Deuterium = most robust primordial abundance measurements (> Helium > Lithium), because D not produced by stars. Converging observations:

$$10^5 n_D / n_H = 2.527 \pm 0.030 \text{ (68 \% CL), } \text{Cooke et al. (2018)}$$

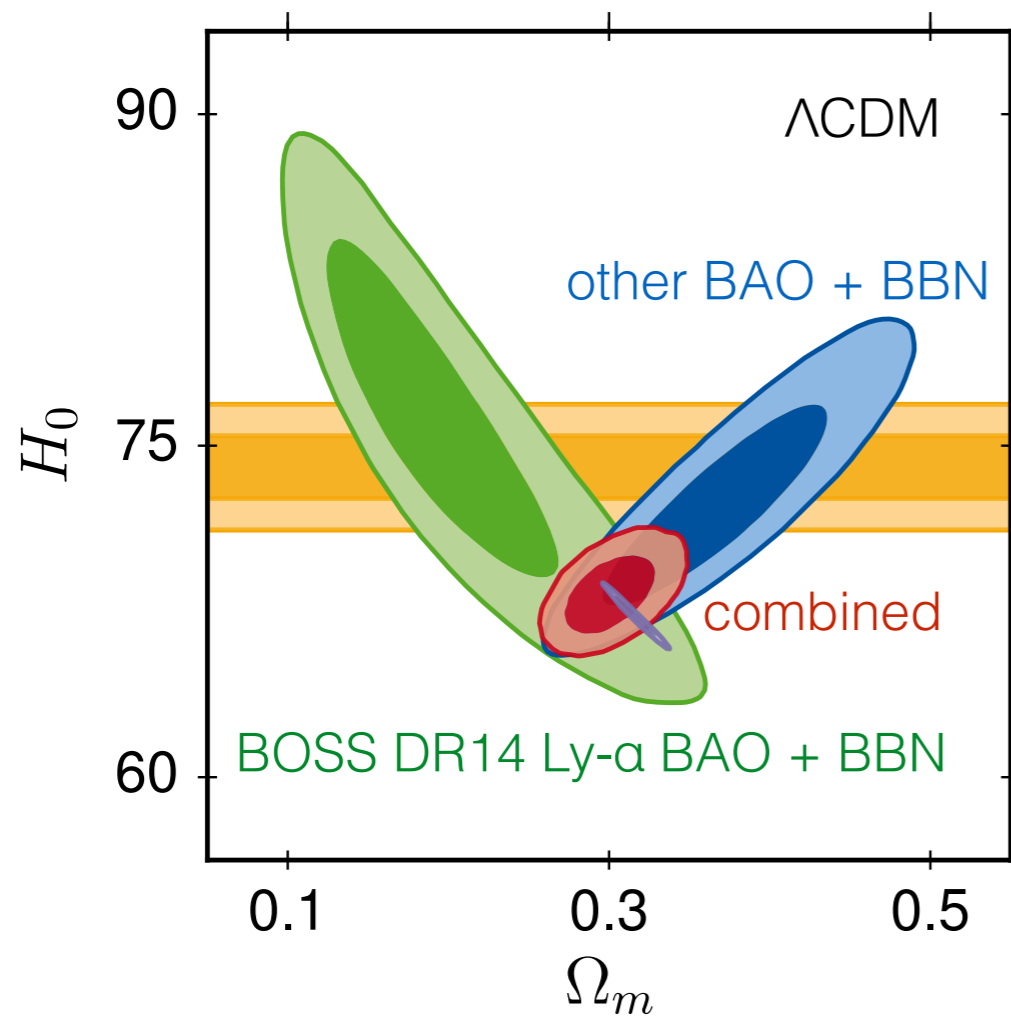
- $\omega_b \rightarrow$ BBN code $\rightarrow n_D/n_H$:

uncertainties on nuclear rates: proton fusion $d(p,\gamma)^3\text{He}$, deuterium fusion $d(d, n)^3\text{He}$, $d(d, p)^3\text{H}$

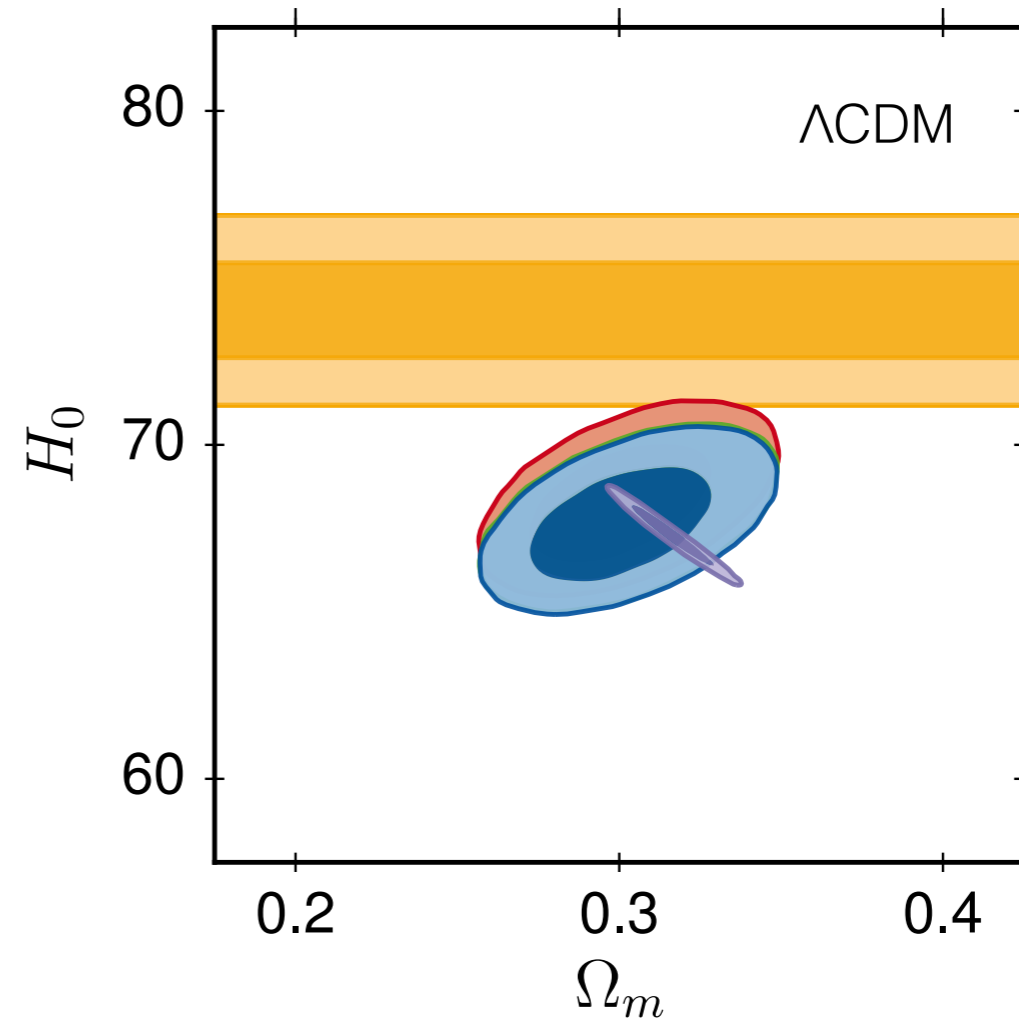
Authors	Code	$d(p,\gamma)^3\text{He}$	Δy_{DP}	$100 \omega_b$
Cooke et al. (2018)	Nollett et al.	theo.	0.02	$2.166 \pm 0.015 \pm 0.011$
Planck 2018 case (a)	PArthENoPE	obs.	0.06	$2.270 \pm 0.017 \pm 0.034$
Planck 2018 case (b)	PArthENoPE	theo.	0.03	$2.197 \pm 0.016 \pm 0.016$
Planck 2018 case (c)	PRIMAT	mixed	0.03	$2.188 \pm 0.016 \pm 0.017$

Deuterium measurement and BBN calculations

- BAO+BBN predictions for Λ CDM in [Schöneberg et al. \[1907.11594\]](#)



case (a): 3.2σ BAO+BBN — SH0ES tension
(3.6σ in Cuceu et al.)



cases (a), (b), (c) give the same results

Solving Hubble tension with extended cosmological model

- self-interacting active neutrinos plus Dark Radiation

Lancaster et al. [1704.06657], Oldengott et al. [1706.02123], Di Valentino et al. [1710.02559],
Kreisch et al. [1902.00534], Park et al. [1904.02625]

- light sterile neutrino interacting with a scalar field Archidiacono et al. [1606.07673]

- Interacting Dark Matter — Dark Radiation

Lesgourgues et al. [1507.04351], Buen-Abad et al. [1708.09406], Archidiacono et al. [1907.01496]

- Dark Matter converting into Dark Radiation

Poulin et al. [1606.02073], Binder et al. [1712.01246], Bringmann et al. [1803.03644]

- Dark Radiation from PBH Hooper et al. [1905.01301]

- Early Dark Energy Poulin et al. [1811.04083], Argrawal et al. [1904.01016], Lin et al. [1905.12618]

- fifth force effects on cepheids and supernovae physics Desmond et al. [1907.03778]

- Dark Matter interacting with Dark Energy Pan et al. [1907.07540], ...

- etc. (non-exhaustive)

some models also solve σ_8 tension

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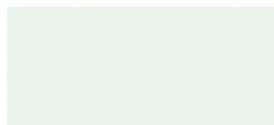
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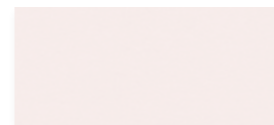
- Dark Matter interacting with Dark Energy ($\Rightarrow w < -1$) Pan et al. [1907.07540], ...

- etc. (non-exhaustive)

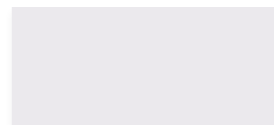
change BAO scale
(but not angle)



change $d_A(z), d_L(z)$
only at very small z



change standard
candle physics



Solving Hubble tension with extended cosmological model

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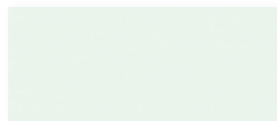
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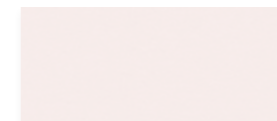
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$N_{\text{eff}} > 3$

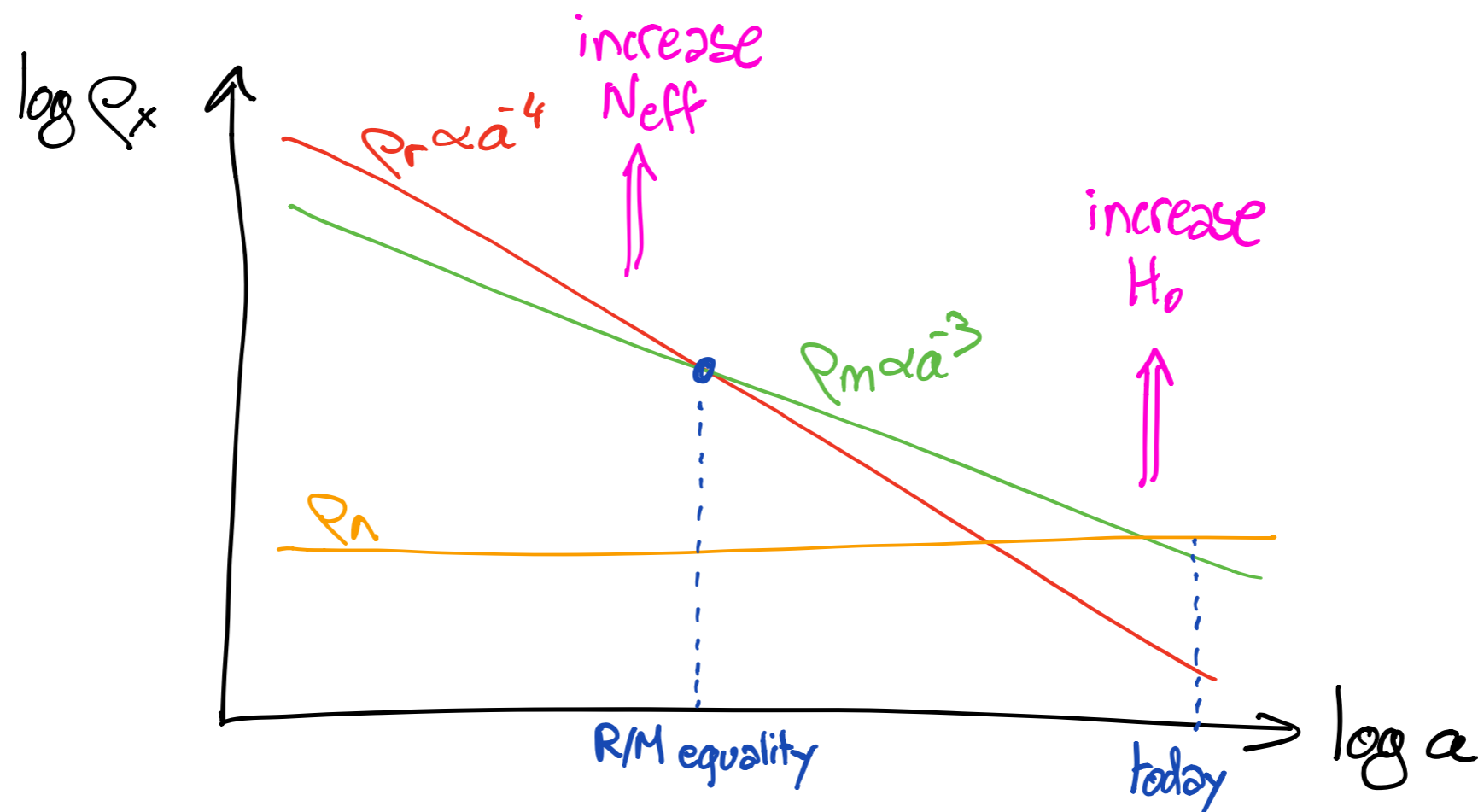


other form of energy excess around equality



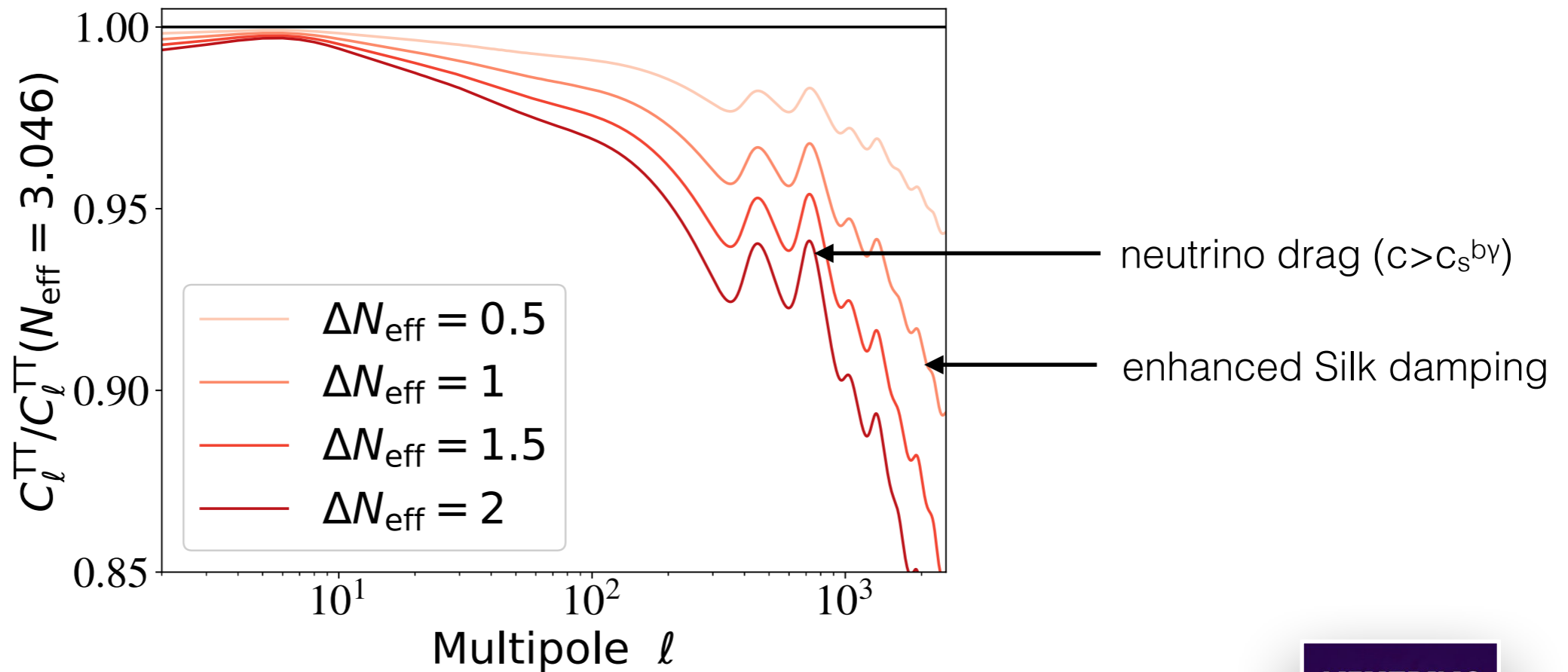
The $H_0 - N_{\text{eff}}$ (partial) degeneracy

- Observations (CMB, BAO, LSS...) mainly sensitive to ratios:
 - $\rho_m / \rho_r \Rightarrow \omega_m / \omega_r = \Omega_m / \Omega_r \Rightarrow z_{\text{eq}}$
 - $\rho_\Lambda / \rho_m \Rightarrow \Omega_m = 1 - \Omega_\Lambda \Rightarrow z_\Lambda$
- Fixed Ω_m : H_0 governs absolute matter and Λ density today, $\rho_m \sim \Omega_m H_0^2$, $\rho_\Lambda \sim \Omega_\Lambda H_0^2$
- May increase (H_0, N_{eff}) last same time with fixed z_{eq}



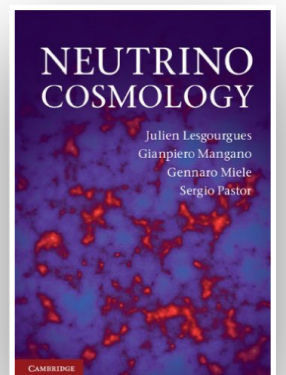
The $H_0 - N_{\text{eff}}$ (partial) degeneracy

- So, high H_0 , $N_{\text{eff}} \sim 4$ (e.g. light sterile neutrino), and that's it?
- **NO!** Increasing (H_0, N_{eff}) has other (bad) effects: CMB damping tail, neutrino drag on CMB peaks,



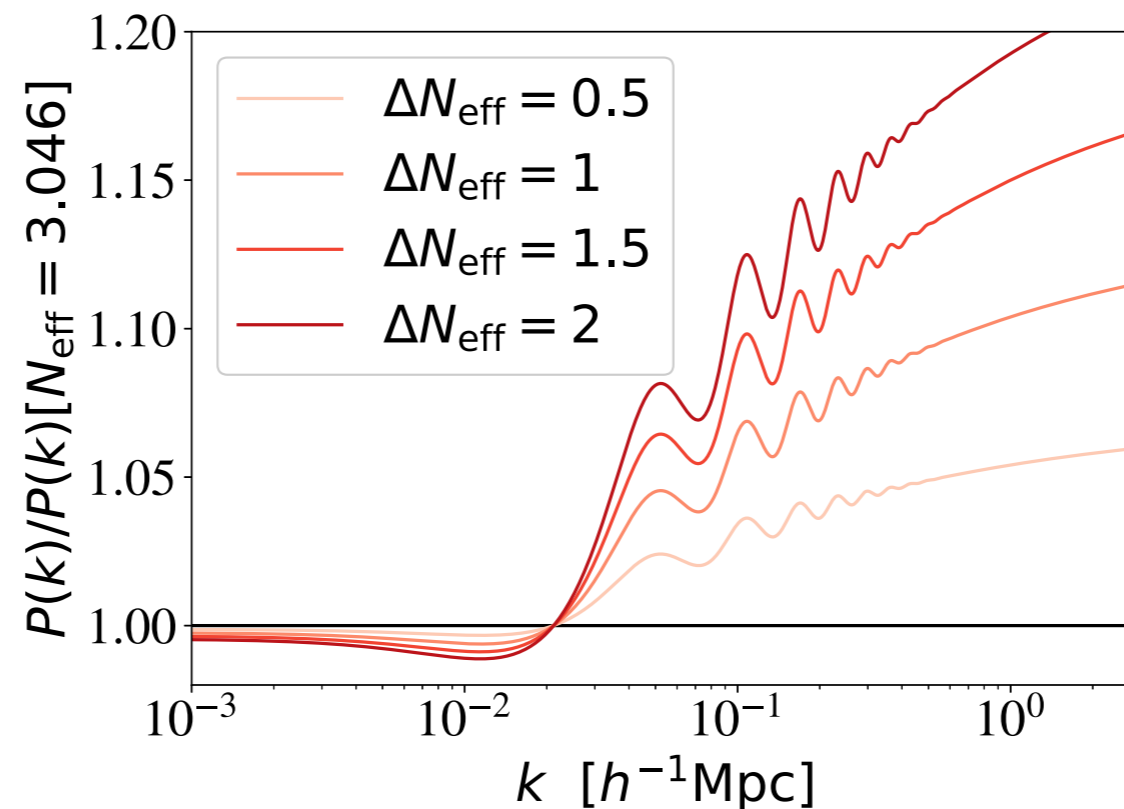
[PDG review on Neutrinos in Cosmology, J.L. & L.Verde]

also Bashinsky & Seljak 03, Hou et al. 11, Neutrino Cosmology (2013) JL et al.



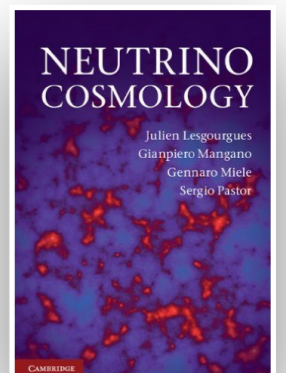
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- $\Omega_m h^2 = \Omega_b h^2 + \Omega_{\text{cdm}} h^2$. CMB also fixes $\Omega_b h^2$ so $\Omega_b / \Omega_{\text{cdm}}$ changes. Small-scale matter power spectrum enhanced.



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The $H_0 - N_{\text{eff}}$ (partial) degeneracy

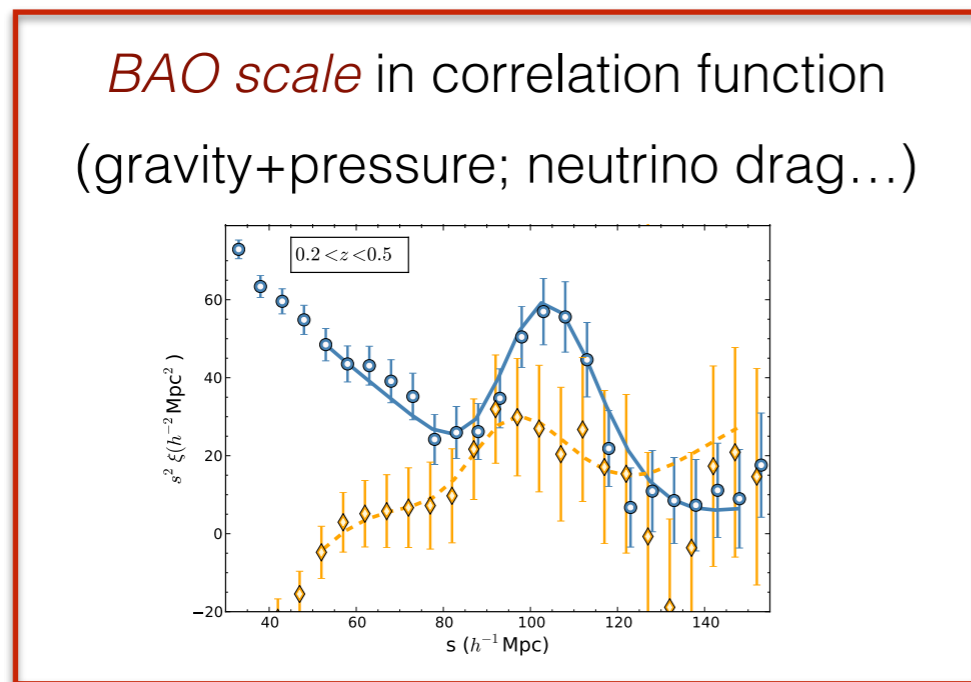
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- “bad effects” can be reduced by exotic physics:
 - extra radiation is self-interacting -> no neutrino drag;
 - radiation remains more clustered during RD -> less Silk damping;
 - Matter clusters less during MD -> no power spectrum enhancement...

Constraints on background cosmology with enhanced Neff

- Can test *only the background evolution* in these models?
 —> independently of perturbations, scattering, self-interactions...
 —> N_{eff} from free-streaming ($v=c$) or self-coupled ($c_s^2=1/3$) relativistic species...

- BAO data test the background evolution : $\theta(z) = \frac{r_s(z_D)}{r_A(z)}$

- not so obvious... [Thepsuryia & Lewis 1409.5066; Schöneberg et al. 1907.11594 Appendix A]



sound horizon
(pressure only)

$$r_s(z_D) = \int_0^{\tau_D} c_s(\tau) d\tau = \int_0^{t_D} \frac{dt}{3a(t)\sqrt{1+R(t)}}$$

$$R = \frac{3\rho_b}{4\rho_\gamma}$$

Ratio of the two could depend on cosmology (e.g. on N_{eff} of free-streaming species)

$N_{\text{eff}} 3 \rightarrow 4$: ratio increases by 0.1%; BAO errors: 0.9% ; so sound horizon OK as a proxy!

Constraints on background cosmology with enhanced Neff

- Can we find test background evolution in these models?
 - > independently of perturbations, scattering, self-interactions...
 - > N_{eff} from free-streaming ($v=c$) or self-coupled ($c_s^2=1/3$) relativistic species...
- BAO data test the background evolution
- BAO —> H_0, Ω_m, ω_b ; no H_0 constraint without ω_b prior
 - BAO + ω_b from CMB? No, ω_b degenerate with perturbation-related ingredients
 - BAO + ω_b from BBN? Yes!
- *The BAO+BBN take on the Hubble tension* [1907.11594]



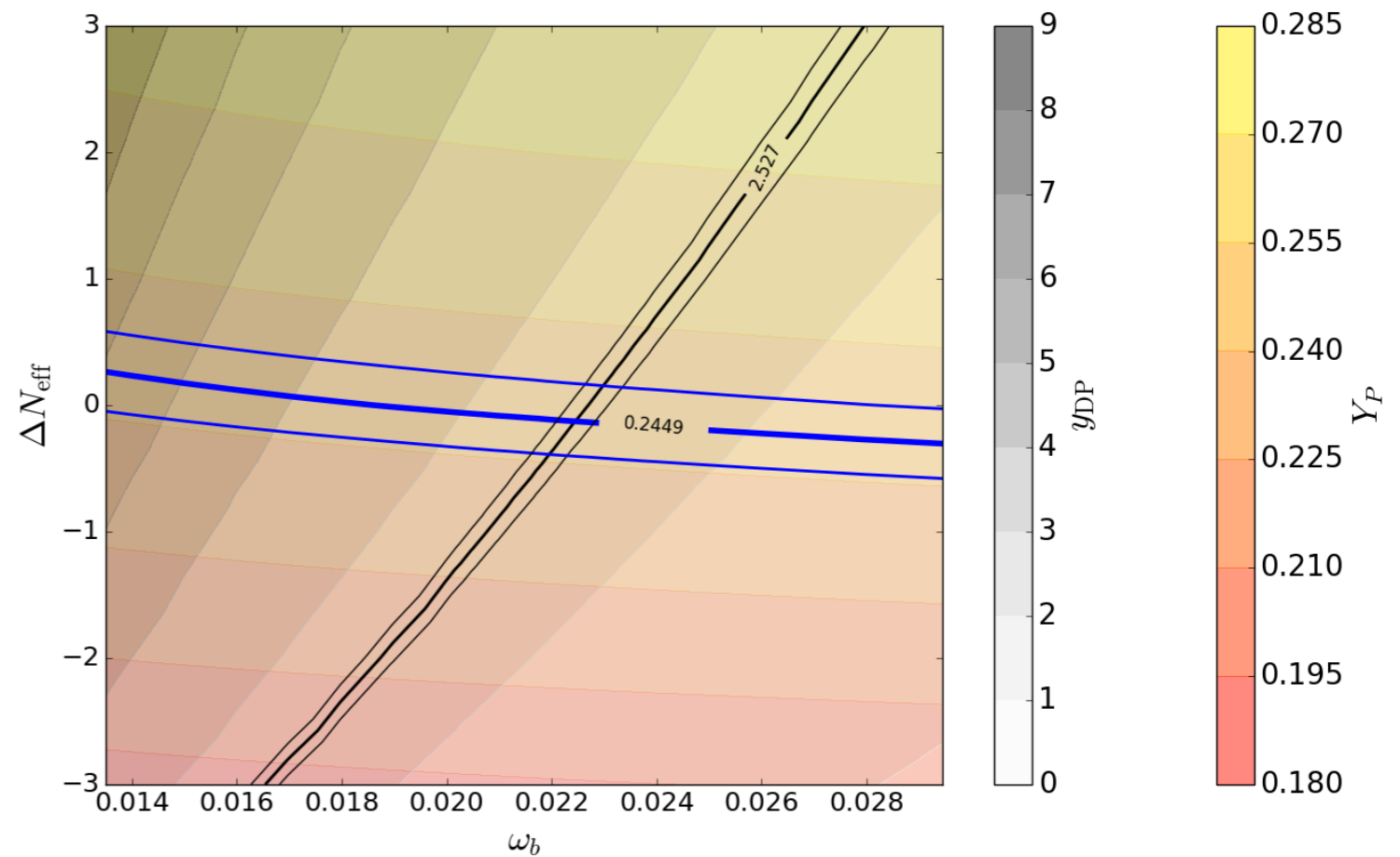
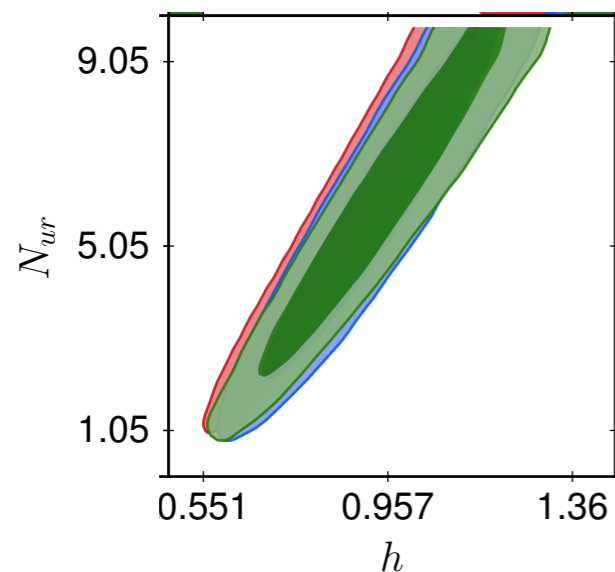
with Nils Schöneberg Deanna Hooper

Constraints on background cosmology with enhanced Neff

- Deuterium only : allows arbitrary variations in H_0 , N_{eff}

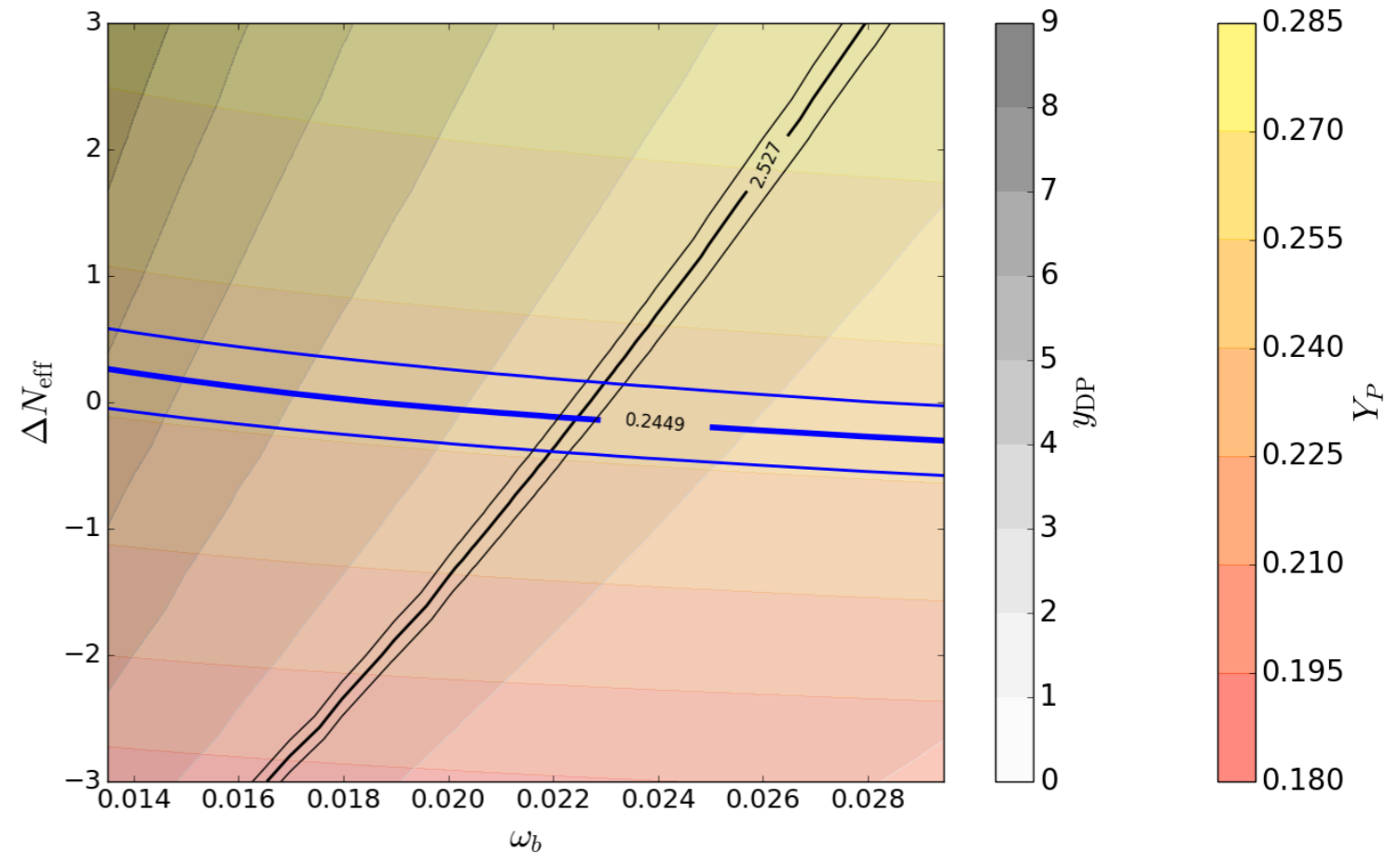
$$\theta(z) = \frac{r_s(z_D)}{r_A(z)} \simeq \frac{\int_{z_D}^{\infty} c_s(\omega_b, \tilde{z}) [\Omega_r/\Omega_m(1+\tilde{z})^4 + (1+\tilde{z})^3]^{-1/2} d\tilde{z}}{\int_0^z [1/\Omega_m - 1 + (1+\tilde{z})^3]^{-1/2} d\tilde{z}}$$

N_{eff} increases $\rightarrow \omega_b$ increases,
but small and can be adjusted



Constraints on background cosmology with enhanced N_{eff}

- Adding Helium constraints?

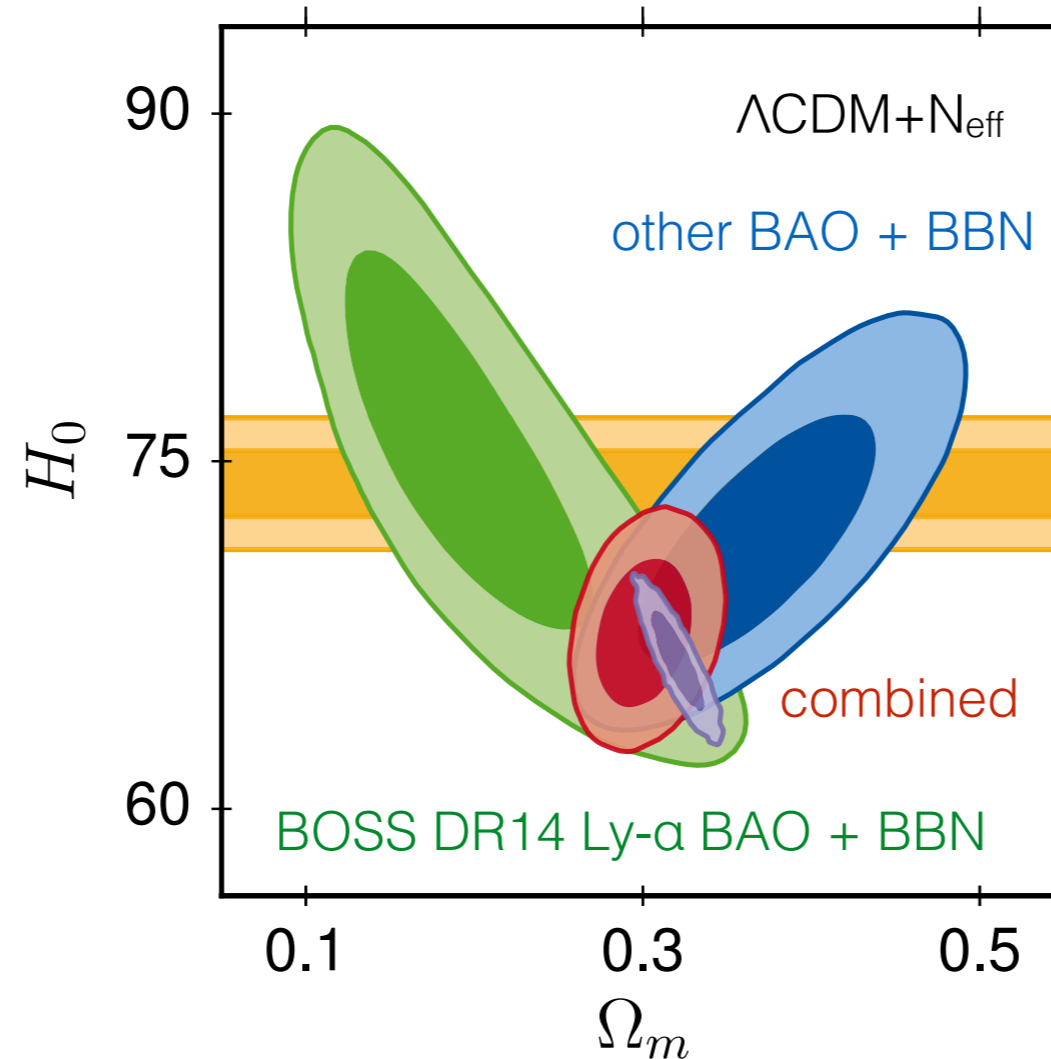


- If $N_{\text{eff}} \approx 3$ at BBN and ΔN_{eff} generated between BBN and equality: still no constraint (e.g. DM annihilating into DR, [1712.01246](#), [1803.03644](#))

- If N_{eff} is constant between BBN and CMB:

Helium $\xrightarrow{\text{BBN}}$ N_{eff} bounds $\xrightarrow{\text{BAO}}$ H_0 bounds (independent of perturbations)

Constraints on background cosmology with enhanced N_{eff}



[Schöneberg et al.1907.11594]

- Tension BAO+BBN \longleftrightarrow SH0ES reduces from 3.2σ to 2.6σ level only!
- $H_0 = 67.7^{+2.0}_{-2.2}$ km/s/Mpc (68% CL)
- Could be enough if $H_0 \searrow$ (star formation bias),
otherwise: N_{eff} produced late or radically different mechanism...

Solving Hubble tension with extended cosmological model

- self-interacting active neutrinos plus Dark Radiation

Lancaster et al. [1704.06657], Oldengott et al. [1706.02123], Di Valentino et al. [1710.02559],
Kreisch et al. [1902.00534], Park et al. [1904.02625]

- light sterile neutrino interacting with a scalar field

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- Interacting Dark Matter — Dark Radiation

Lesgourgues et al. [1507.04351], Buen-Abad et al. [1708.09406], Archidiacono et al. [1907.01496]

- Dark Matter converting into Dark Radiation **Slightly better than Λ CDM+N_{eff} by tuning annihilation history**

Poulin et al. [1606.02073], Binder et al. [1712.01246], Bringmann et al. [1803.03644]

- Dark Radiation from PBH

No better than Λ CDM+N_{eff}

Hooper et al. [1905.01301]

- Early Dark Energy

Poulin et al. [1811.04083], Argrawal et al. [1904.01016], Lin et al. [1905.12618]

- fifth force effects

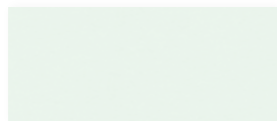
Desmond et al. [1907.03778]

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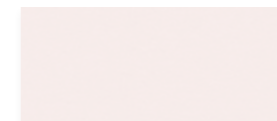
Pan et al. [1907.07540], ...

- etc. (non-exhaustive)

N_{eff}>3



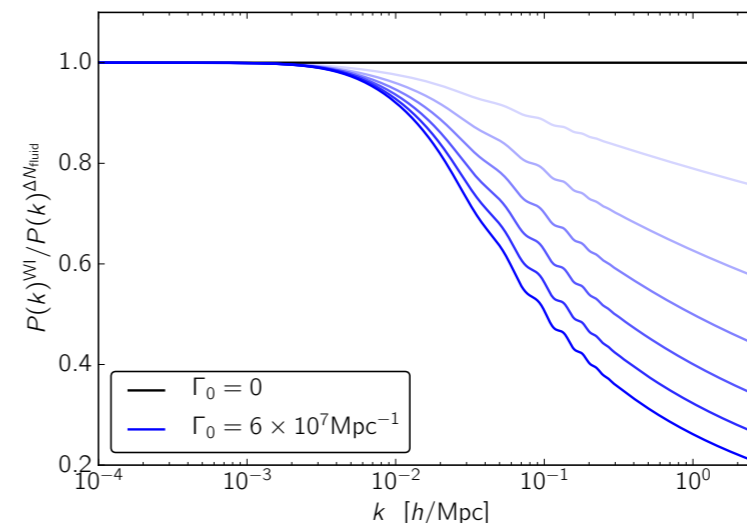
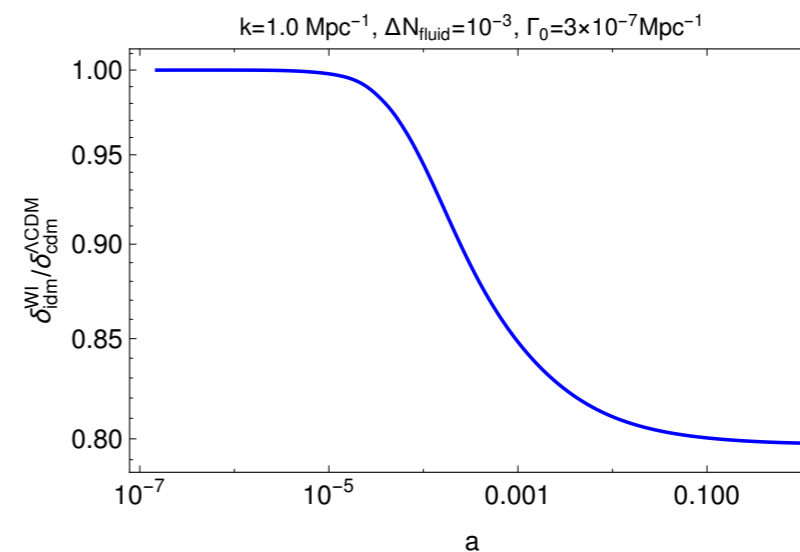
other form of energy excess around equality



Interacting Dark Sector

Particle physics: Buen-Abad, Marques-Tavares, Schmaltz, 1505.03542; ← LHC-motivated
 Cosmo: Lesgourgues et al. 1507.04351; Buen-Abad et al. 1708.09406; Archidiacono et al. 1907.01496

- DM and DR = relics from a Dark Sector (dark symmetry, massive fermions, dark photons or dark gluons), DR = self-coupled fluid enhancing N_{eff}
- DM-DR momentum exchange rate $\sim T^2$, $\Gamma/H = \text{constant}$ during radiation era, constant small dragging of DR over DM, DR growth rate enhanced, DM growth rate reduced
- “bad effects” of high N_{eff} on CMB cured by DR sound speed and perturbations / on $P(k)$ cured by DR drag on DM, even σ_8 reduction!



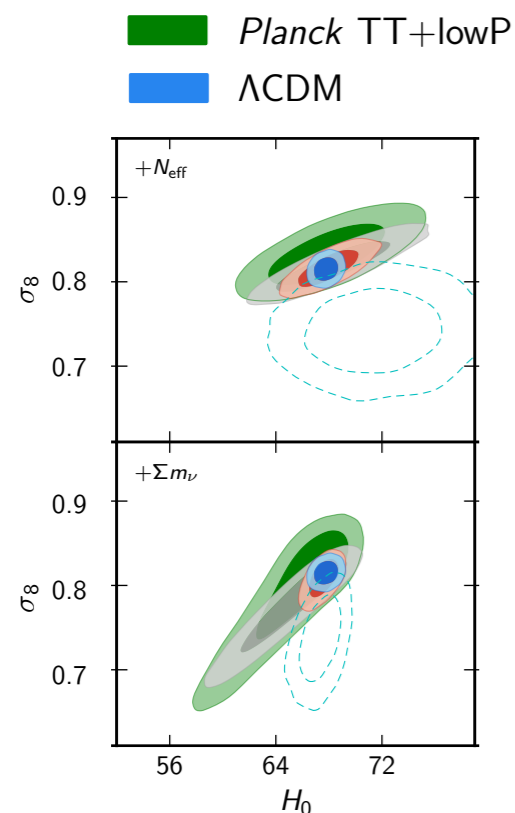
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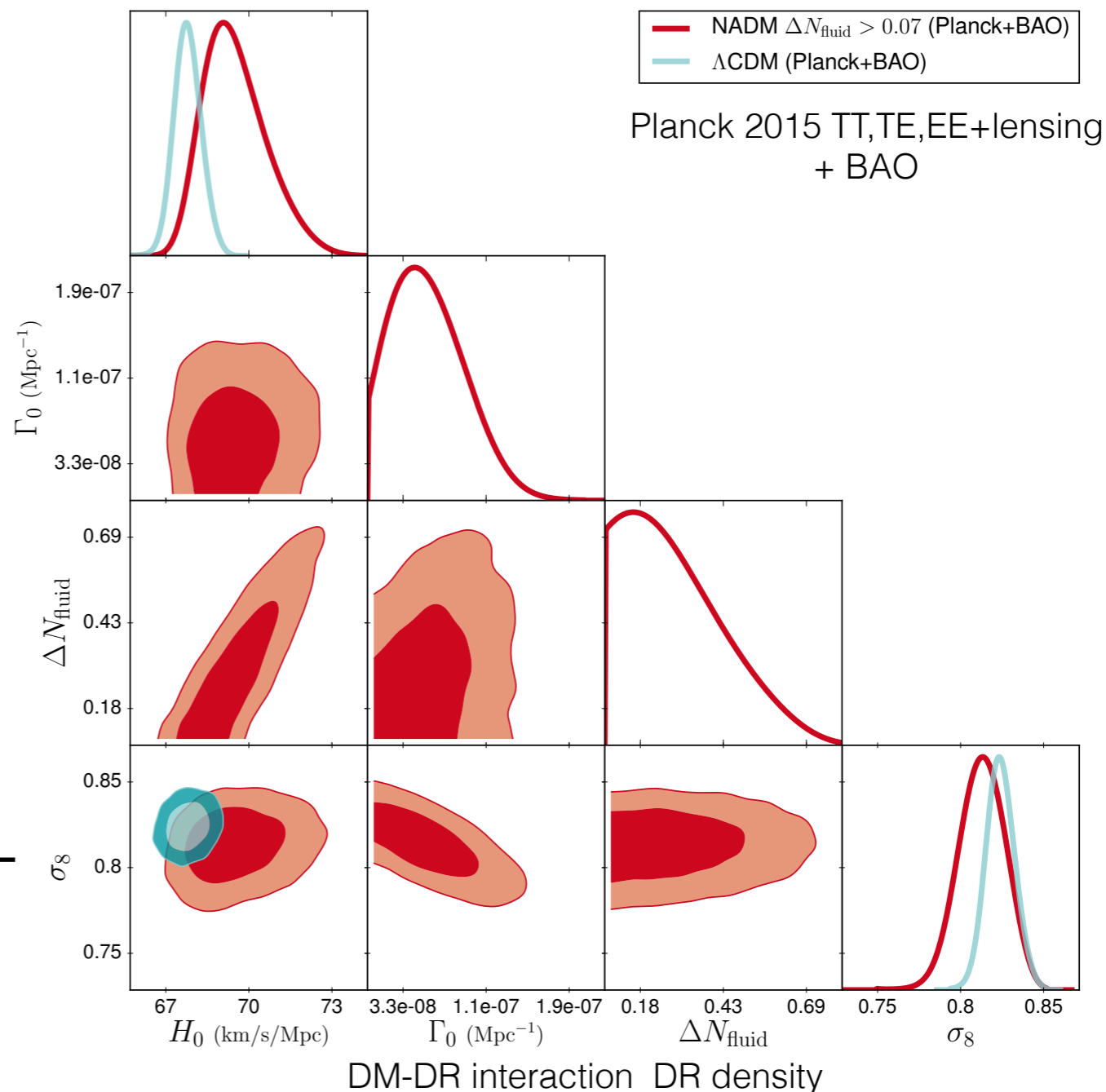
Cosmo: Lesgourgues et al. 1507.04351; Buen-Abad et al. 1708.09406; Archidiacono et al. 1907.01496

Large values of ΔN_{fluid}

ease both Hubble and σ_8 tensions :



← compare with



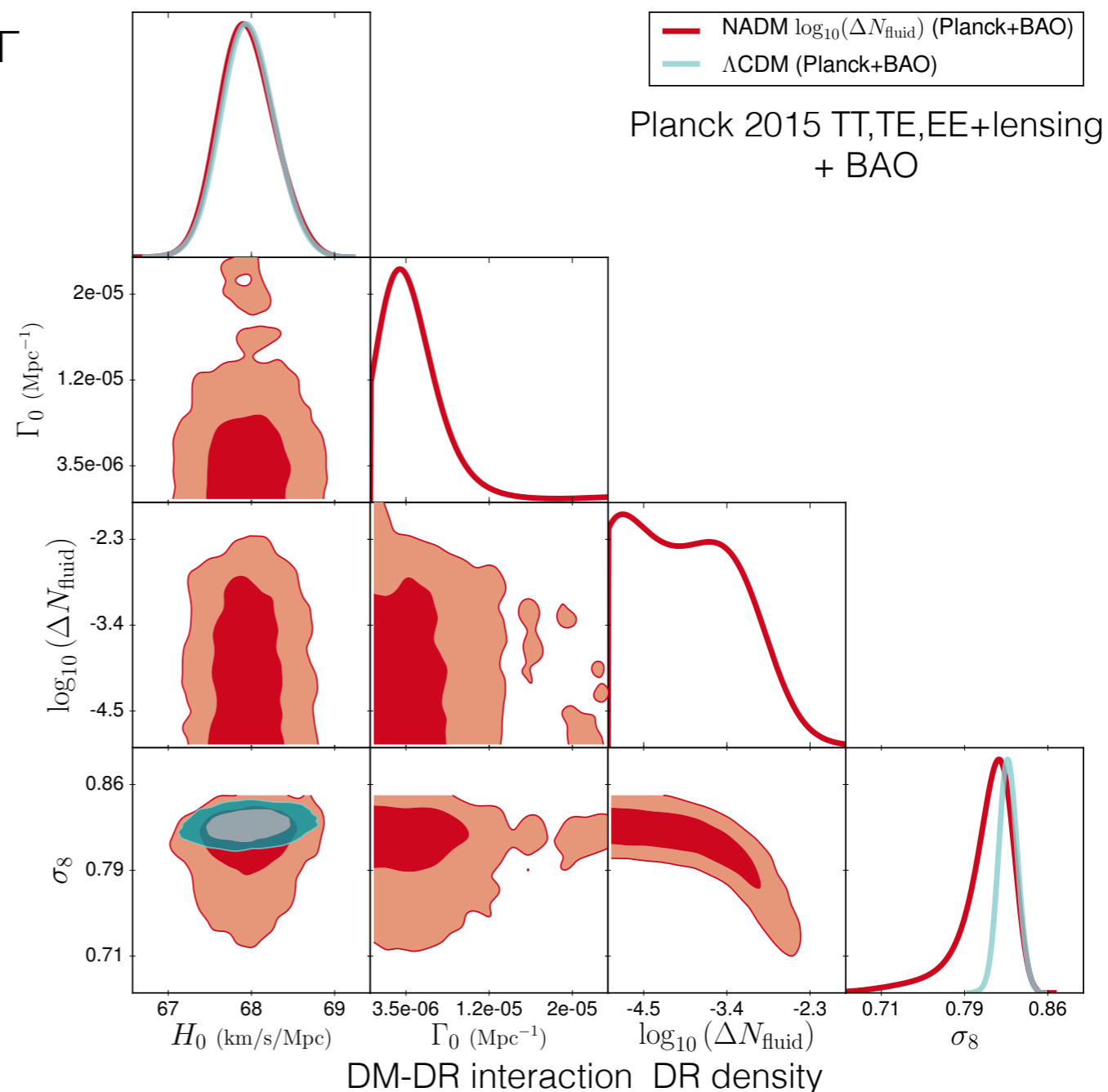
[Planck 2015 parameters]

Interacting Dark Sector

Particle physics: Buen-Abad, Marques-Tavares, Schmaltz, 1505.03542;

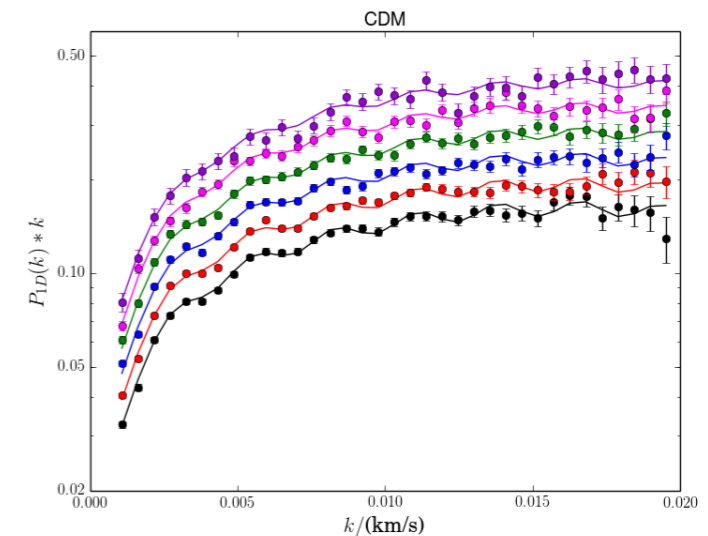
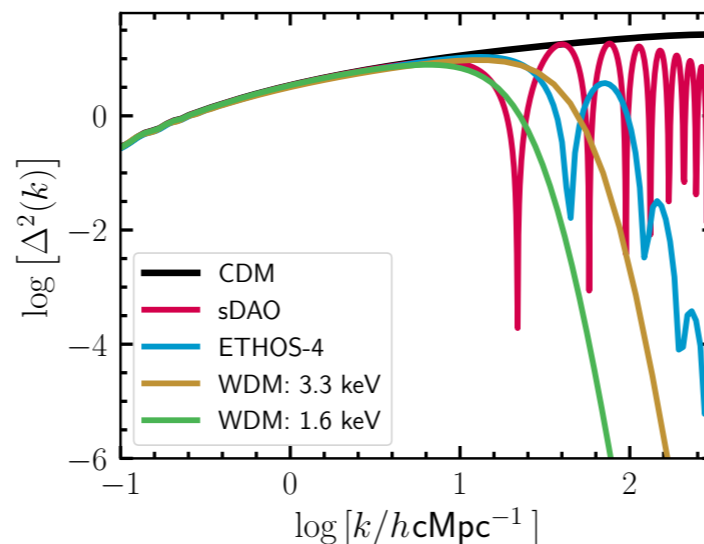
Cosmo: Lesgourgues et al. 1507.04351; Buen-Abad et al. 1708.09406; Archidiacono et al. 1907.01496

Tiny values of ΔN_{fluid} compatible with large Γ
and very low σ_8 :



Interacting Dark Sector and Lyman- α

- This model : $n=0$ case of the ETHOS parametrisation of any Lagrangian-based DM-DR interaction [Cyr-Racine et al. 1512.05344]
- $n = 2, 4$ cases: exponential suppression of small-scale power spectrum + Dark Acoustic Oscillation: candidate for small-scale CDM crisis



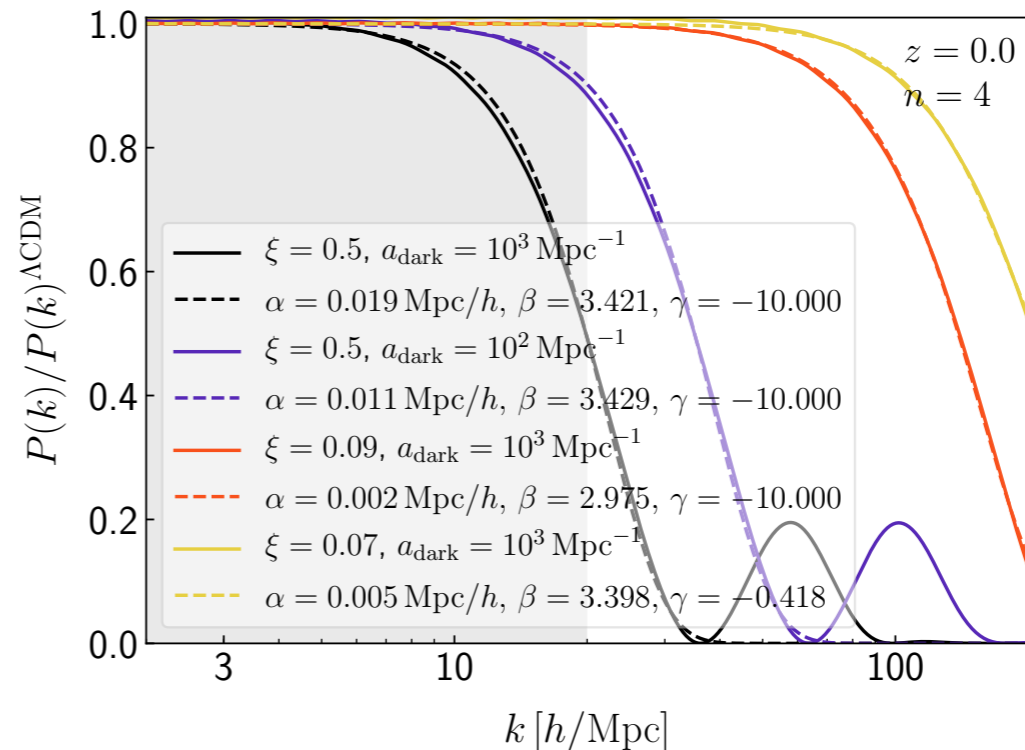
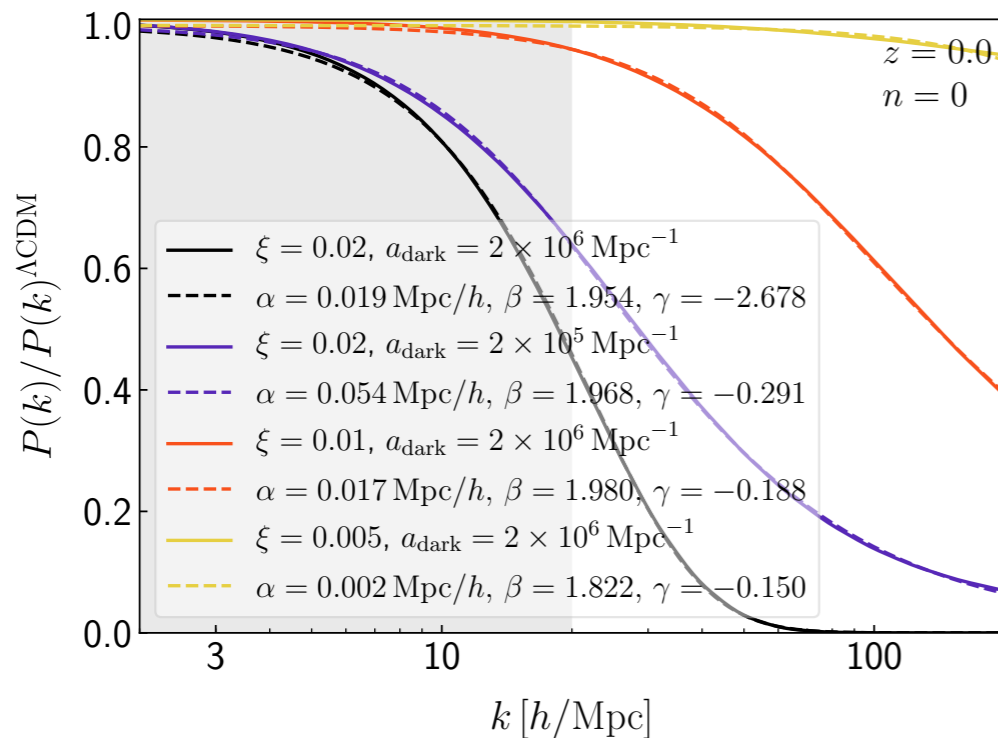
- Test with Lyman- α 1D flux?
 - Krall et al [1705.08894]: constraints on $n=0$ with SDSS-II Ly- α : McDonald et al.'s (σ_8 , N_{eff}): σ_8 larger than for Λ CDM, $n=0$ model disfavoured
 - Garny et al. [1805.12203]: constraints on $n=0$ with BOSS Ly- α : analytical modelling of 1D flux power spectrum, $n=0$ model unconstrained by Lyman- α
 - Bose et al. [1811.10630]: show how to compute 1D flux for $n=4$ with simulations; DAO washed out

Non-standard neutrino self-interactions (+extra relics)

Archidiacono, Hooper, Murgia, Bohr, Lesgourgues, Viel et al. 1907.01496



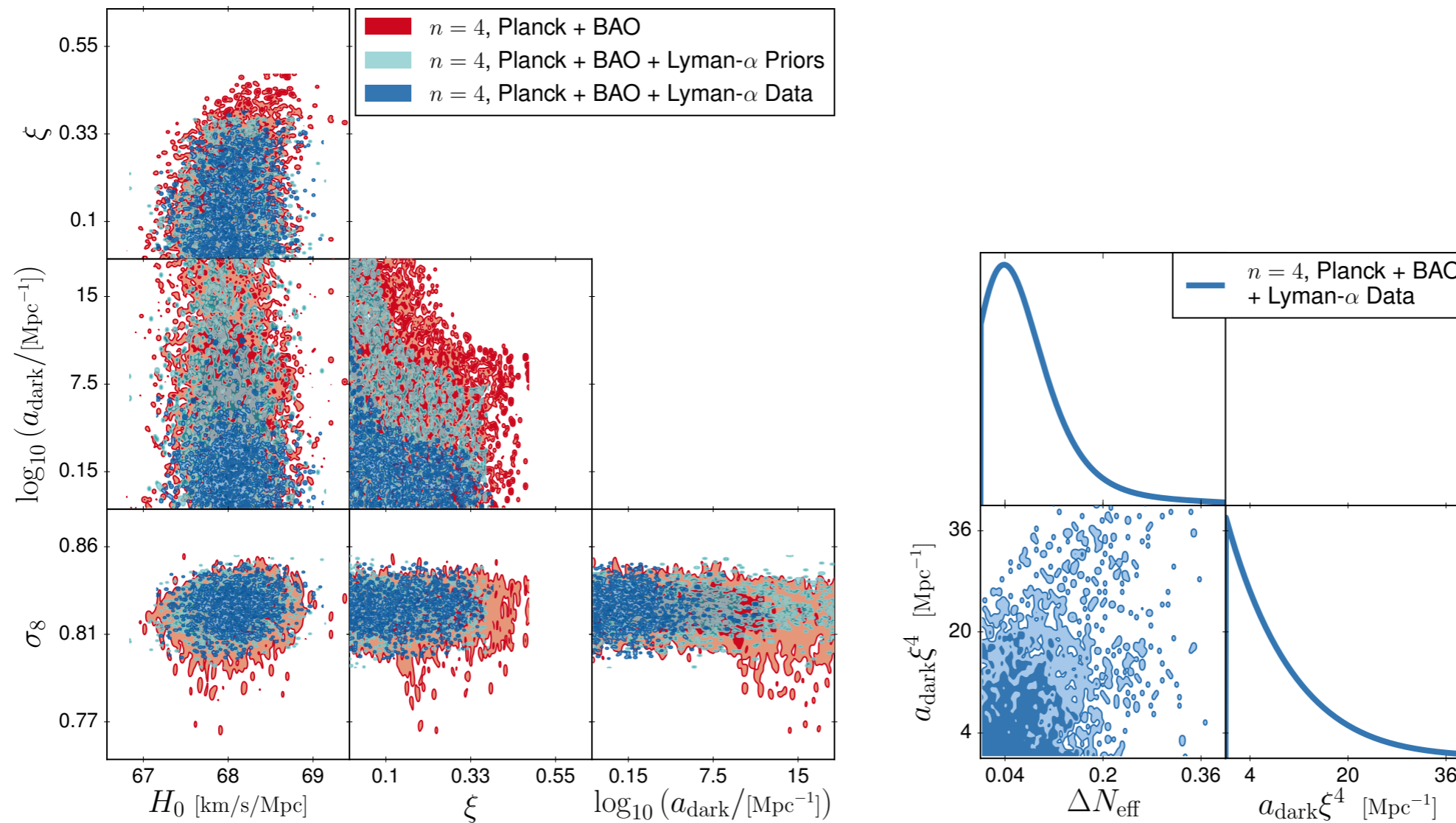
- high-resolution HIRES/MIKE Ly- α : with simulations for (α, β, γ) parametrisation $T(k) = [1 + (\alpha k)^\beta]^\gamma$
- Likelihood in MontePython finds “equivalent Λ CDM model”, take linear $P(k)$ ratio, fits (α, β, γ) , get $P_{F^{1D}}(k, z; \alpha, \beta, \gamma)$ by interpolation, fits data to get $\chi^2(\alpha, \beta, \gamma)$ like in [Murgia et al. 1704.07838](#)



Non-standard neutrino self-interactions (+extra relics)

Archidiacono, Hooper, Murgia, Bohr, Lesgourgues, Viel et al. 1907.01496

- Case $n=4$: Ly- α pushes down constraint on coupling by 6 orders of magnitude

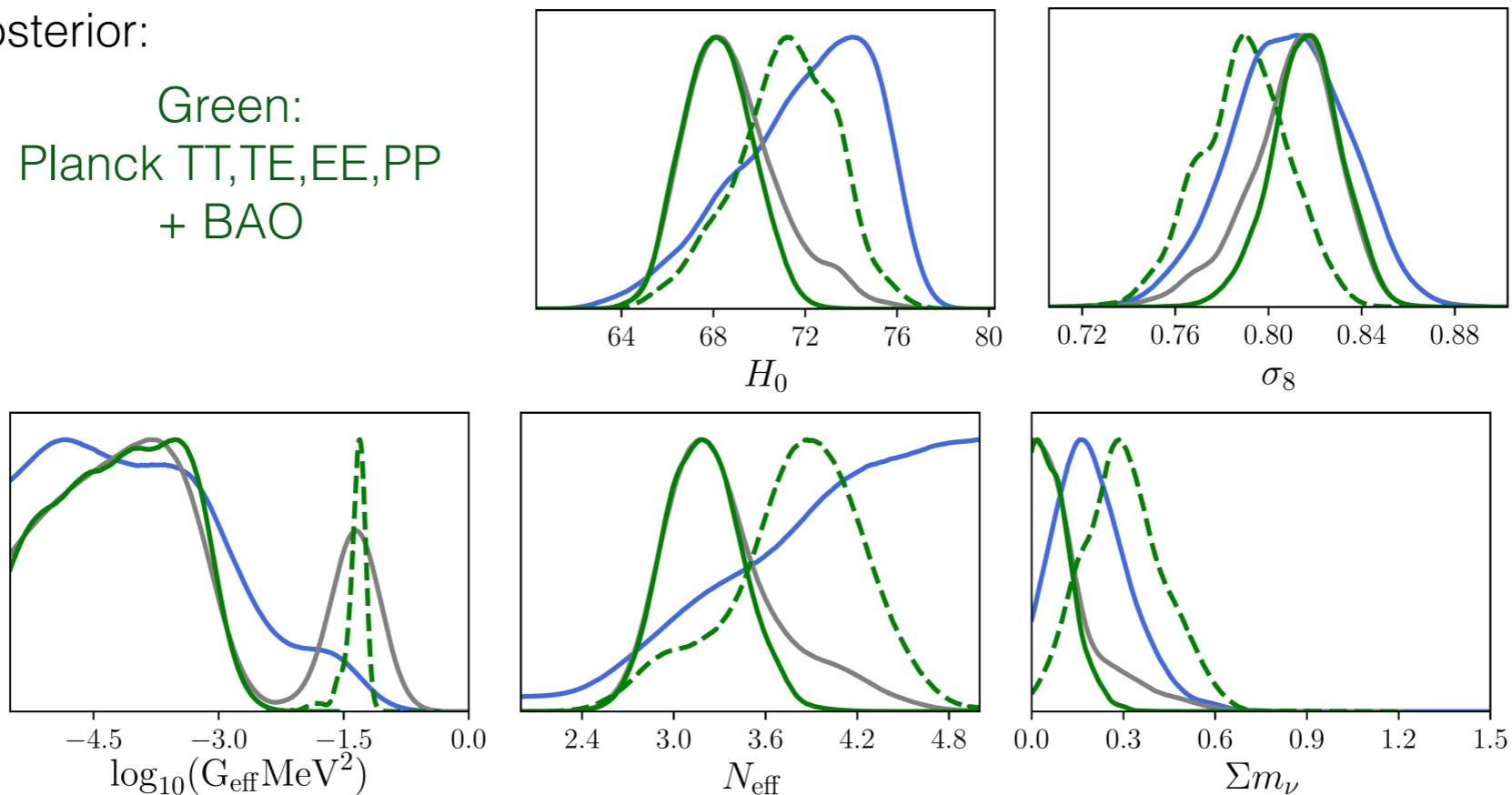


- Case $n=2$: similar behaviour
- Case $n=0$: Ly- α less constraining than CMB! (model affects larger scales)

Non-standard neutrino self-interactions (+extra relics)

Lancaster et al. [1704.06657], Oldengott et al. [1706.02123], Di Valentino et al. [1710.02559],
 Kreisch et al. [1902.00534], [Park et al. \[1904.02625\]](#)

- Neutrinos **cluster more** than free-streaming ones: reduced the “bad effects” of increasing N_{eff} (e.g. neutrino drag) and of increasing M_ν .
- Bimodal posterior:



- High-interaction case accommodates $N_{\text{eff}} \sim 2.8-4.5$ and $M_\nu \sim 0.05-0.55$ eV (95%CL)! M_ν bounds released by factor 4.5
- **Could be discriminated** with more LSS data and better CMB temperature and polarisation data (Simons observatory, CMB Stage 4...)

Non-standard neutrino self-interactions (+extra relics)

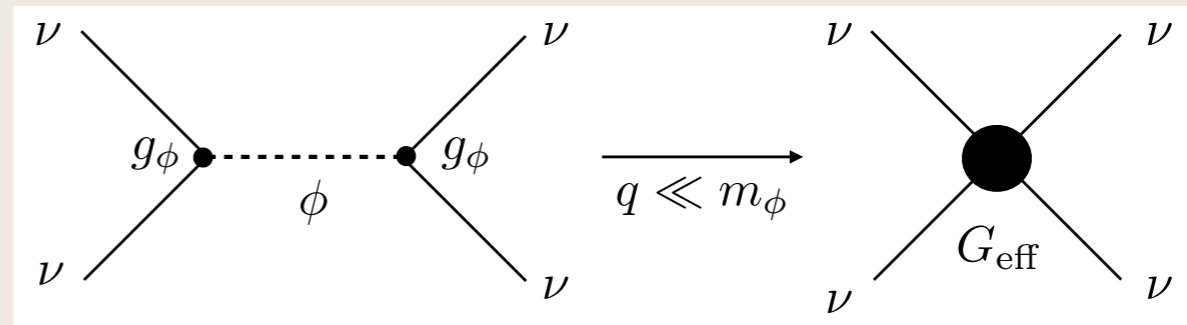
Lancaster et al. [1704.06657], Oldengott et al. [1706.02123], Di Valentino et al. [1710.02559],
 Kreisch et al. [1902.00534], [Park et al. \[1904.02625\]](#)

- Neu
- (e.g
- Bim

Several problems at particle physics level

Blinov et al. [1905.02727]

$$\mathcal{L}_{\text{eff}} = G_{\text{eff}}(\bar{\nu}\nu)(\bar{\nu}\nu) \text{ from}$$

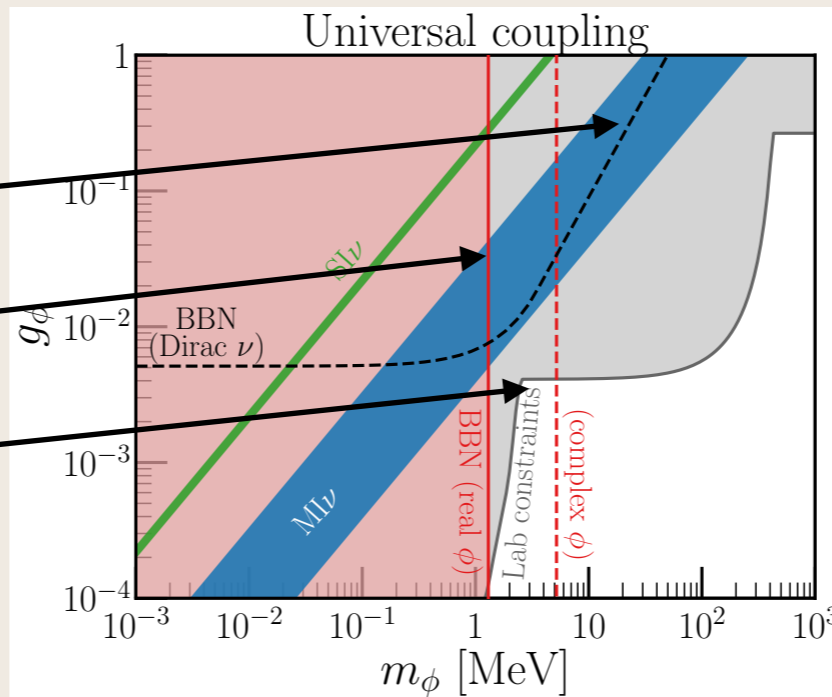


Mediator: scalar field, too light; $G_{\text{eff}} \gg G_{\text{Fermi}}$

BBN: too much $RH\nu$

BBN: too much ϕ

$\beta\beta$ and meson decay



problems to generate ν mass (no seesaw)

requires medium interactions with ν_τ only

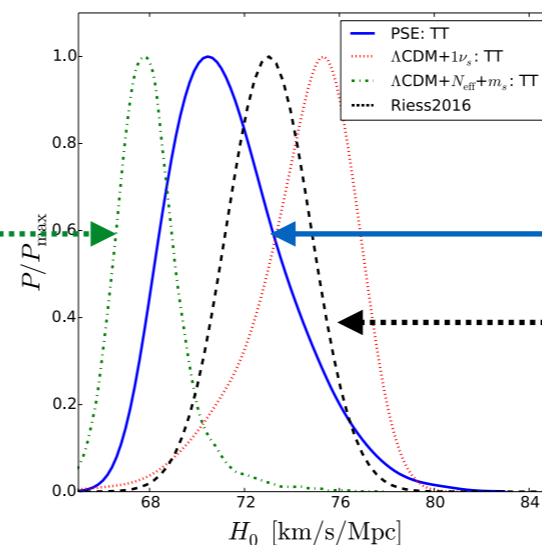
- High rele
- Cou
- (Sim

Light sterile neutrino interacting with pseudo-scalar

Hannestad et al. 2013; Saviano et al. 2014; Archidiacono et al. 2016

- $\mathcal{L} \sim g_s \phi \bar{\nu}_4 \gamma_5 \nu_4$ motivated by LSND + MiniBoone oscillation anomalies, high H_0 by surprise
- Would not work with vector; pseudo-scalar (odd under parity) to avoid 5th force bounds;
- Late thermal equilibrium of ϕ : N_{eff} enhanced by ~ 0.5 after BBN by both pseudo-scalar and sterile neutrino.
- Light sterile + massless pseudo-scalar play the role of **interacting radiation** over some range of time,
- **late decay of sterile ν into massless pseudo-scalar** removes eV-mass effects on matter power spectrum. LSS data compatible with $m_s \sim \text{eV}$.

“simple” non-thermalised sterile



this model

SHOES

Solving Hubble tension with extended cosmological model

- self-interacting active neutrinos plus Dark Radiation

Lancaster et al. [1704.06457], Oldengott et al. [1706.02123], Di Valentino et al. [1710.02559],

- light sterile neutrinos

Beyond Standard Model
particle physics must be rich,

- Interacting Dark Matter

Lesgourgues

Should have cosmological
consequences,

- Dark Matter conversion

- Dark Radiation from

Hubble tension comes from not
having identified these effects?

- Early Dark Energy

- fifth force effects

- Dark Matter interacting with Dark Energy

- etc. (non-exhaustive)

Price to pay too high,

Models too fine-tuned,

SH0ES driven by systematics,

Tension will disappear?

Pan et al. [1907.07540], ...

some models also solve σ_8 tension

On-going progress on front of Einstein-Boltzmann solvers

1. `input.c`

2. `background.c`

3. `thermodynamics.c`

4. `perturbations.c` →

5. `primordial.c`

6. `nonlinear.c`

7. `transfer.c` →

8. `spectra.c`

9. `lensing.c`

10. `output.c`

Bottleneck 1. Integral over perturbation equations.

- Not highly parallelisable/vectorisable (just k loop)
- Replace by neural network

[Albers, Fidler, JL, Schöneberg, Torrado \[1907.05764\]](#)

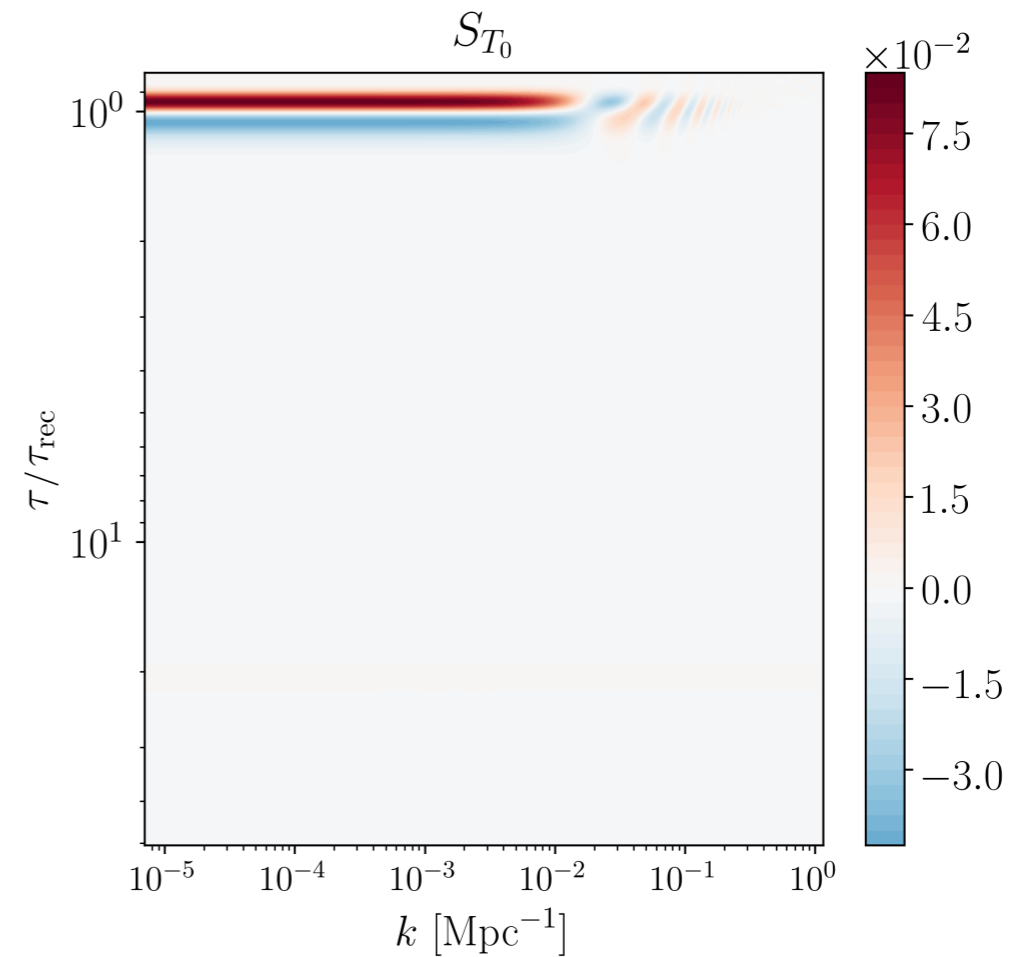
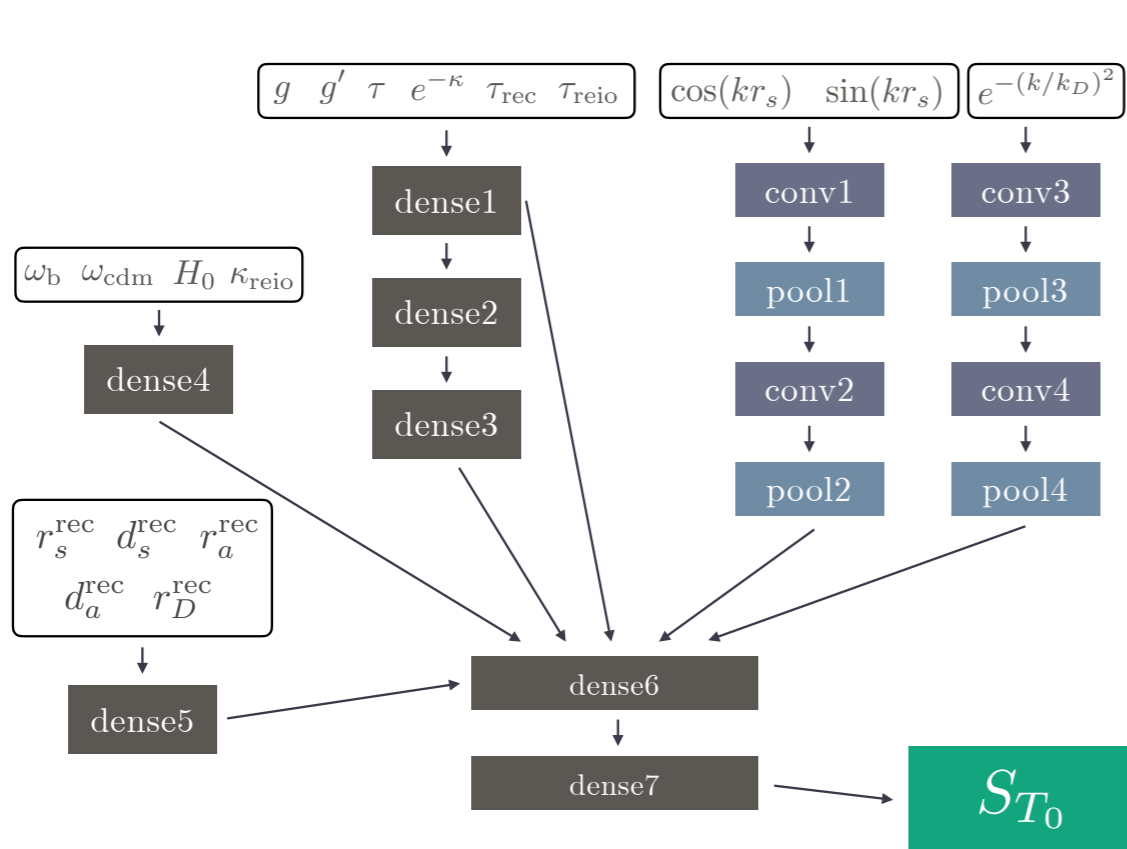
- Provide analytic approximations: accurate and fast-to-(re)train
- Only depends on few (background) cosmo parameters

Bottleneck 2. Loop over line-of-sight integrals.

- Highly parallelisable/vectorisable
- Alternative integral formulations

e.g. [Schöneberg, JL, Simonovic, Zaldarriaga \[1807.09540\]](#)

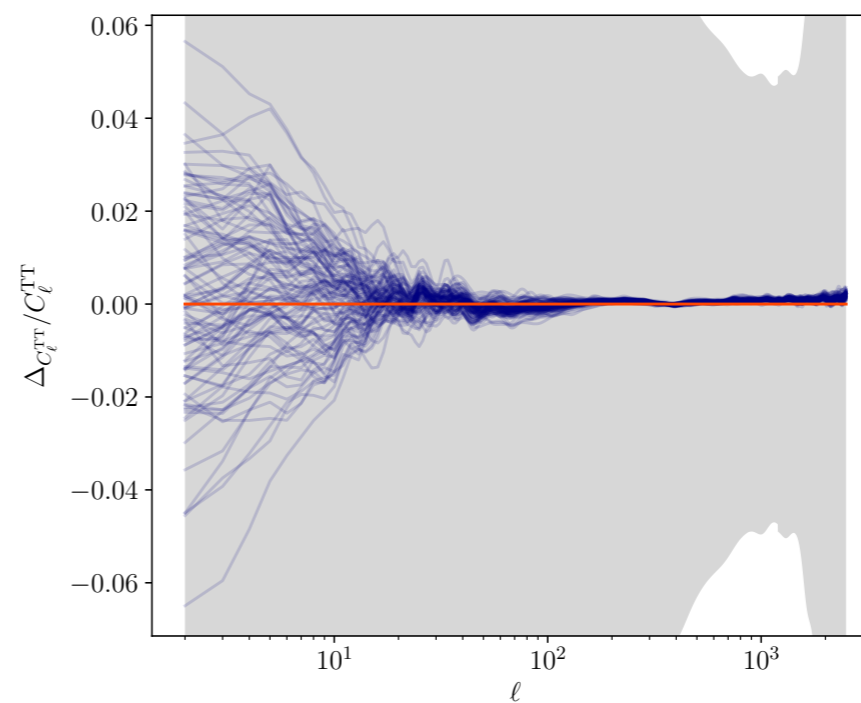
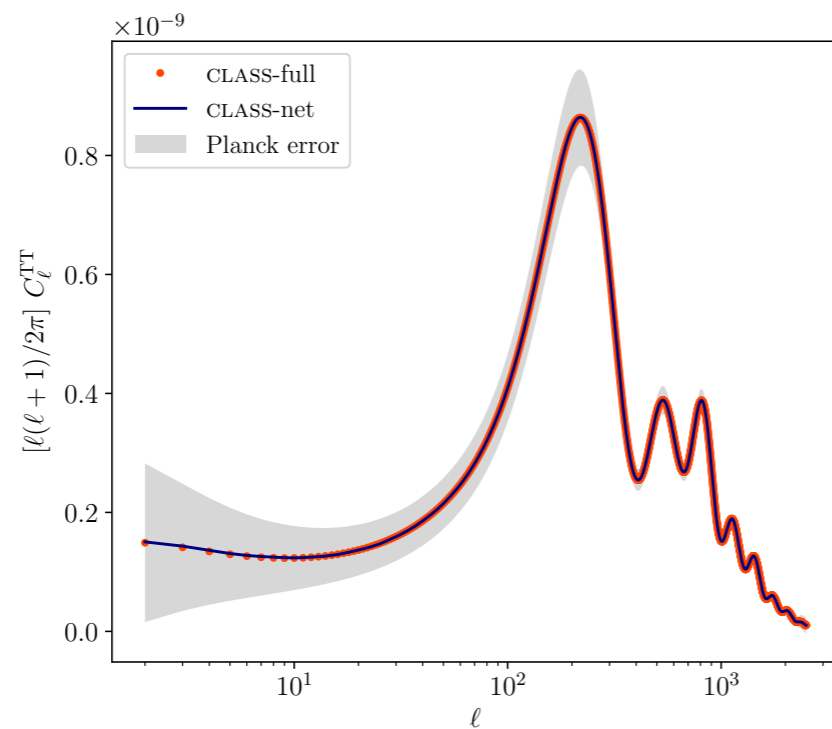
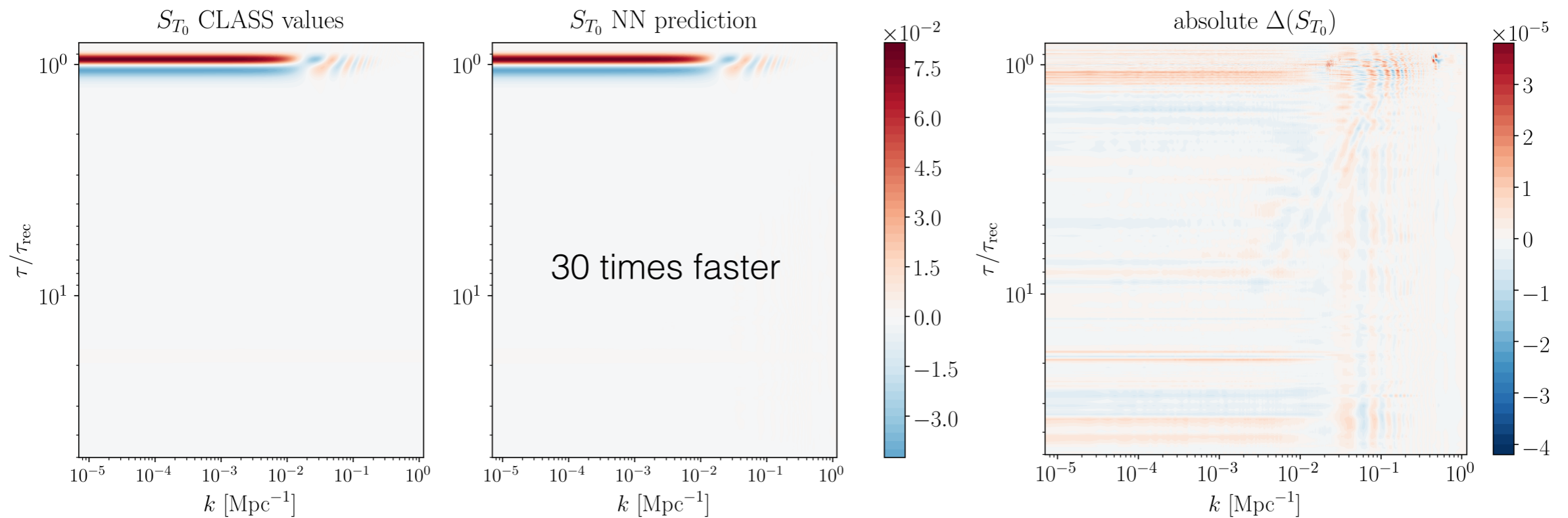
On-going progress on front of Einstein-Boltzmann solvers



Half-a-day of training on one laptop

Loss function guarantees given precision level on observables

On-going progress on front of Einstein-Boltzmann solvers



On-going progress on front of Einstein-Boltzmann solvers

