

Axions

-

Motivated by the Strong Interactions, Perfect for Cosmology

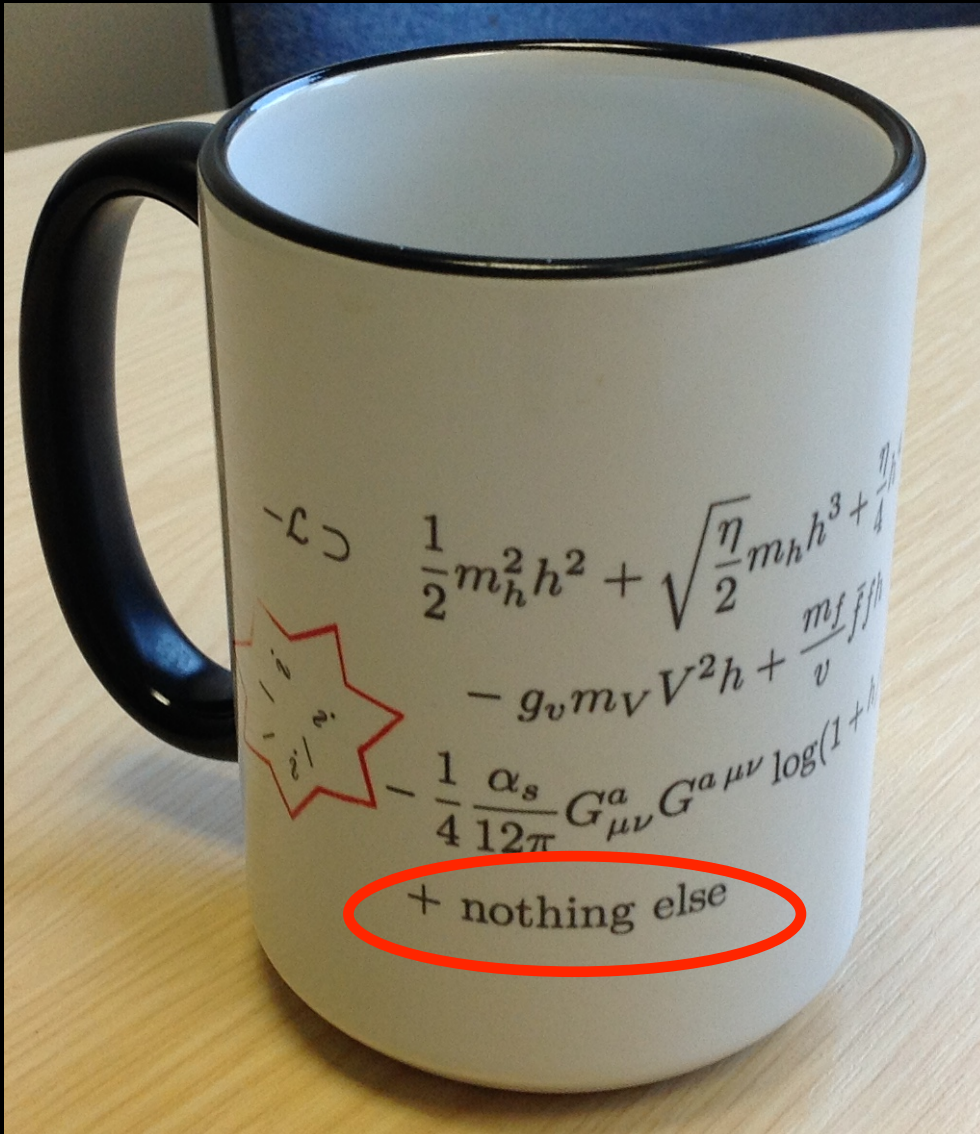
J. Jaeckel^{**}

S. Abel[†], G. Alonso^{**}, J. Berges^{**}, B. Doebrich^z, L. Gastaldo^{**},
M. Goodsell^{xx}, H. Gies⁰, F. Kahlhoefer^{*x}, S. Knirck^{**},
V. Khoze[†], A. Lobanov^y, J. Redondo^x,
A. Ringwald^{*}, U. Schmidt^{**}, K. Schmidt-Hoberg^{*}
and The FUNK Collaboration

^{**}ITP Heidelberg, ^zCERN, [†]IPPP Durham, ^{*}DESY, ^yMPIfR Bonn,
^xU. Zaragoza, ^{xx}Paris LPTHE, ⁰ITP Jena, ^{*x}RWTH Aachen

We need...

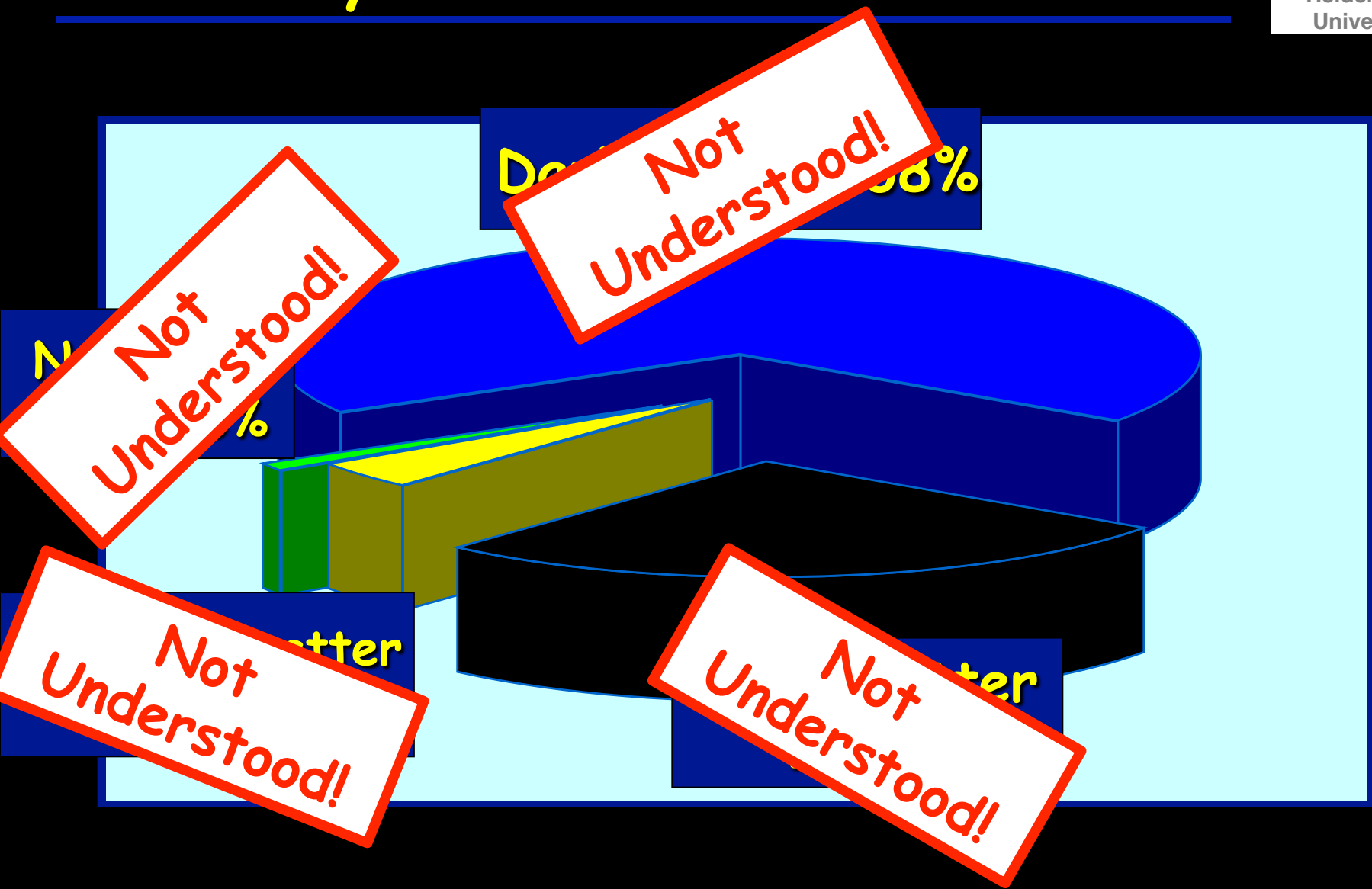
**Physics beyond the
Standard Model**



$$-\mathcal{L} \supset \frac{1}{2} m_h^2 h^2 + \sqrt{\frac{\eta}{2}} m_h h^3 + \frac{\eta}{4} h^4$$
$$- g_v m_V V^2 h + \frac{m_f \bar{f} f}{v}$$
$$- \frac{1}{4} \frac{\alpha_s}{12\pi} G_{\mu\nu}^a G^{a\mu\nu} \log(1 + \frac{h}{v})$$

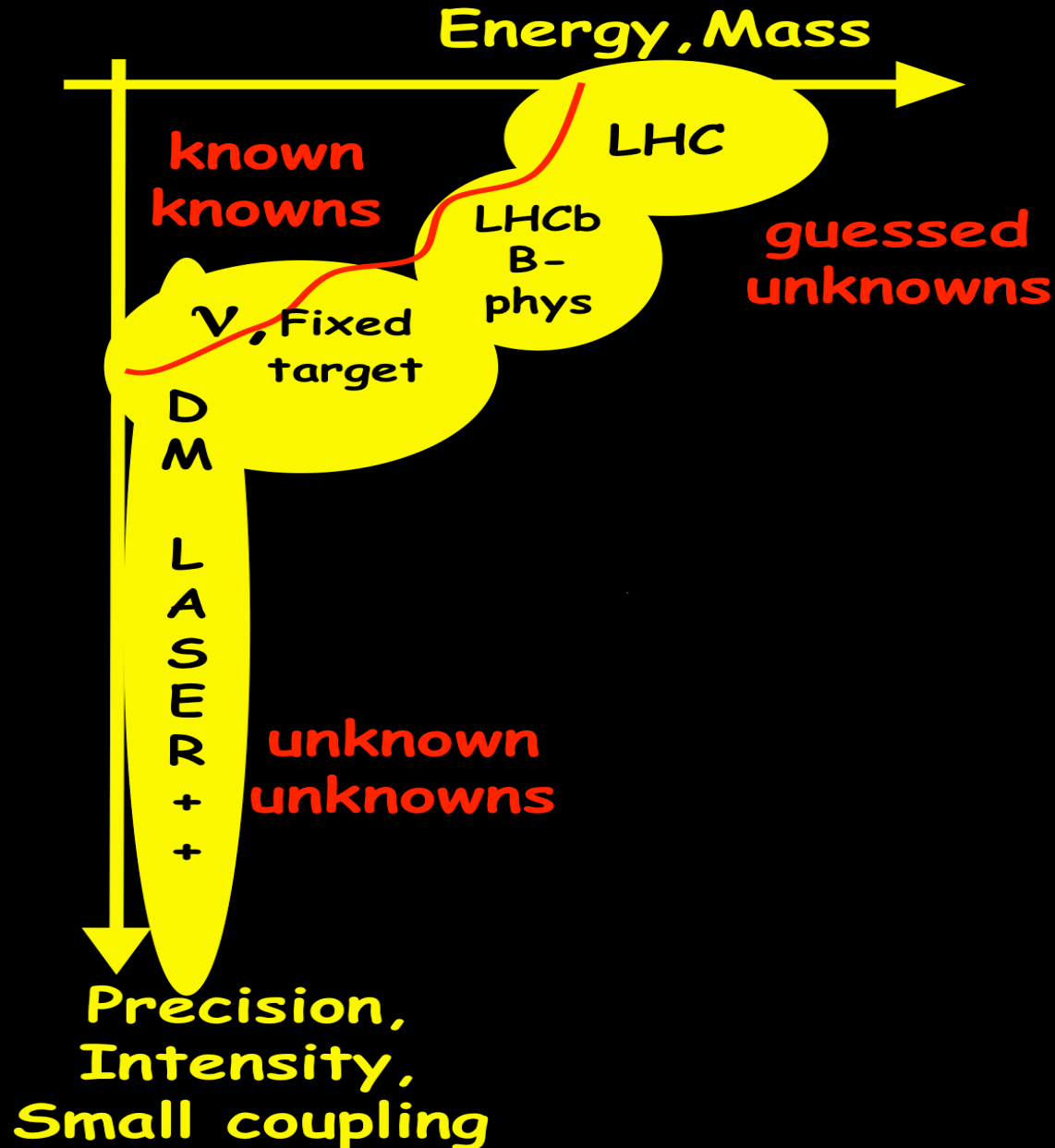
+ nothing else

Inventory of the Universe

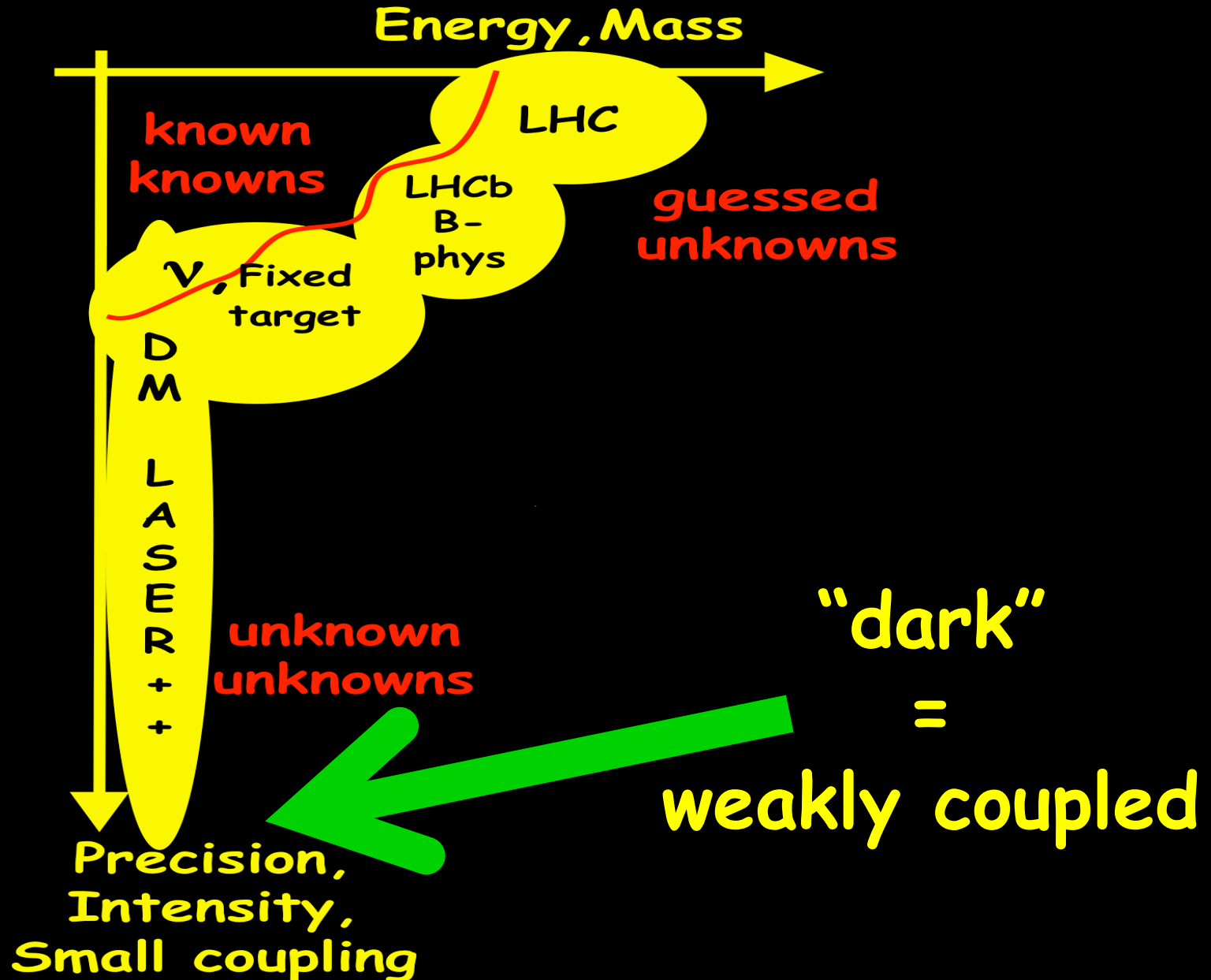


Where does it hide?

Exploring is (at least) 2 dimensional



Exploring is (at least) 2 dimensional



What are Axioms?
And why do we need them?

A „visible“ Hint
for new Physics

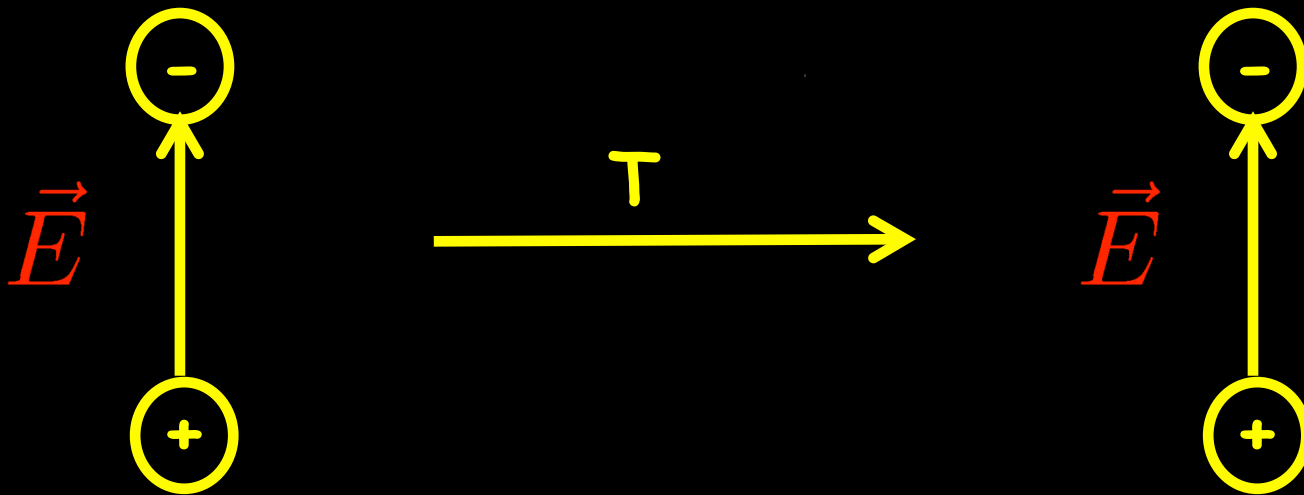
The strong CP Problem

A dirty little secret...

$$S = \int d^4x \left[-\frac{1}{4} G^{\mu\nu} G_{\mu\nu} - \frac{\theta}{4} G^{\mu\nu} \tilde{G}_{\mu\nu} + i\bar{\psi} D_\mu \gamma^\mu \psi + \bar{\psi} M \psi \right]$$

” $\sim \theta \vec{E} \cdot \vec{B}$ ”

- The θ -term violates time reversal (T=CP)!

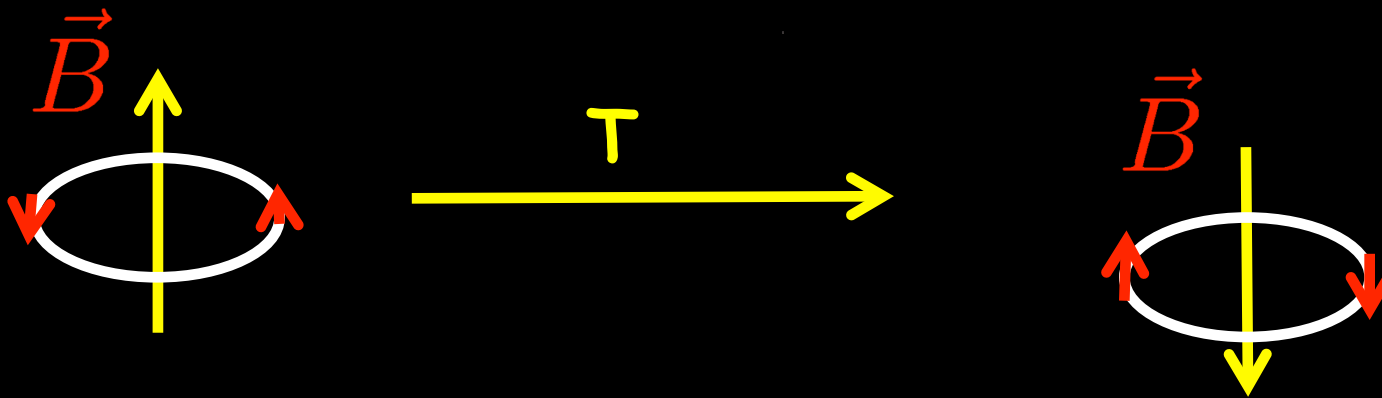


A dirty little secret...

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” $\sim \theta \vec{E} \cdot \vec{B}$ ”

- The θ -term violates time reversal (T=CP)!

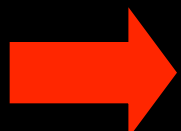
$$\begin{array}{ccc} & \text{T=CP} & \\ \vec{E} & \longrightarrow & \vec{E} \\ \vec{B} & \longrightarrow & -\vec{B} \\ \vec{E} \cdot \vec{B} & \longrightarrow & -\vec{E} \cdot \vec{B} \end{array}$$

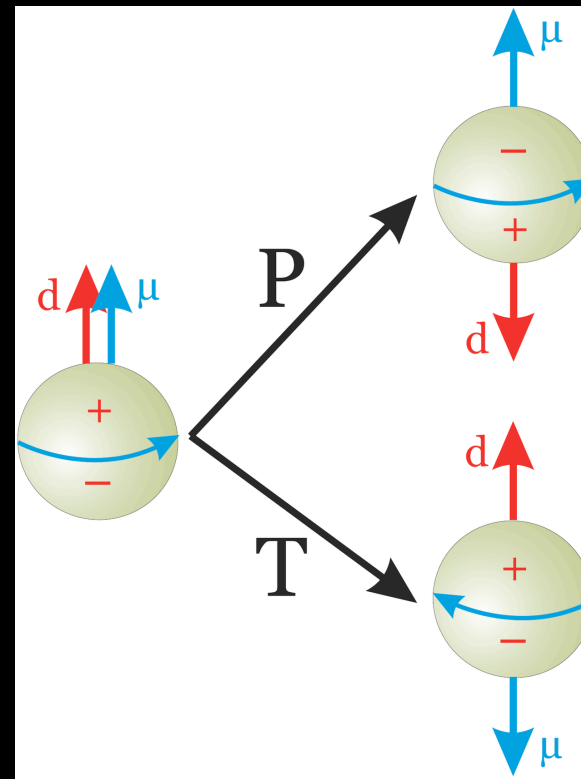
A dirty little secret...

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” $\sim \theta \vec{E} \cdot \vec{B}$ ”

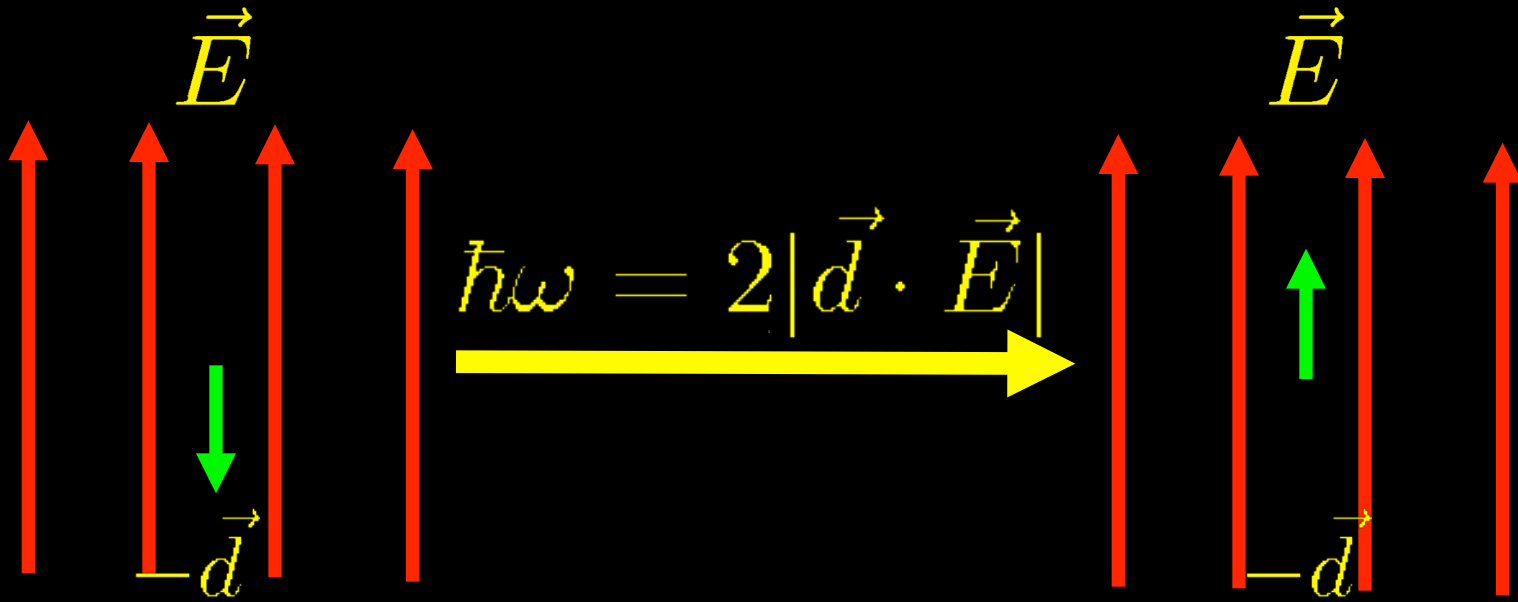
- The θ -term violates time reversal ($T=CP$)!
- Connected to strong interactions!

 **Electric
dipole moment
of the neutron!**



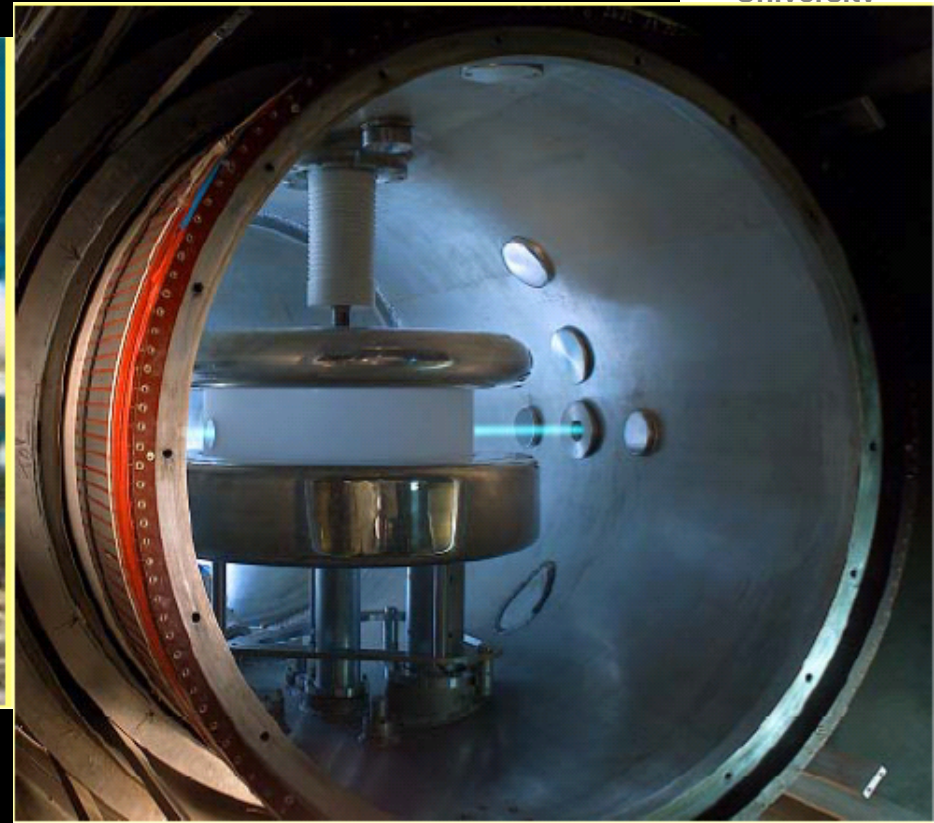
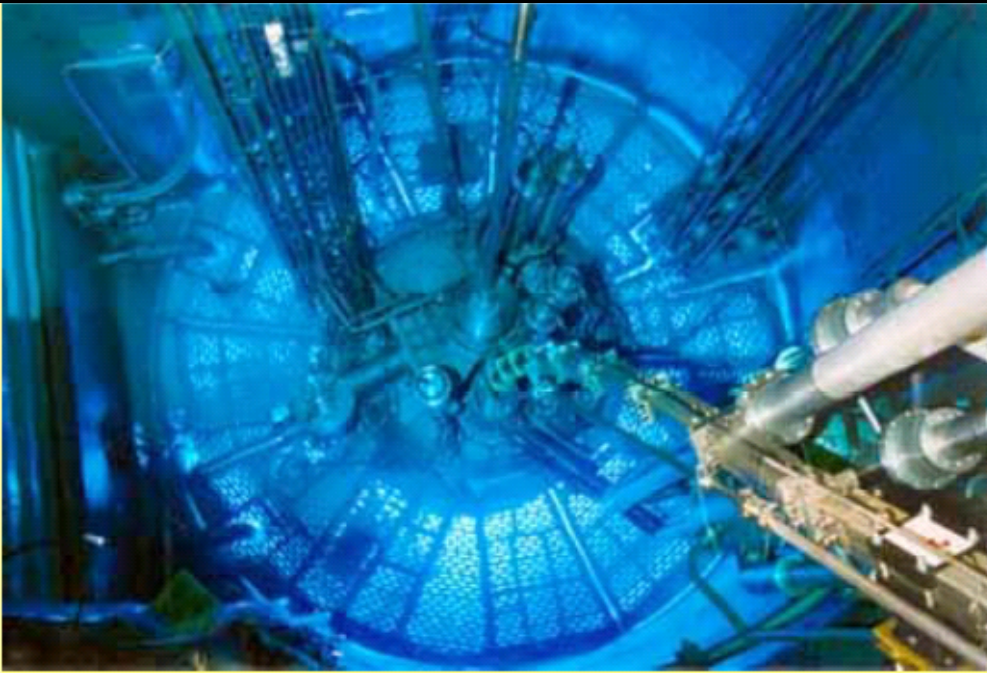
Measure neutron electric dipole moment

- θ would cause neutron EDM \longrightarrow Experiment



\longrightarrow Measure transition frequency.

No neutron electric dipole moment...



RAL-Sussex-ILL EDM collaboration

$$|\vec{d}| < 3 \cdot 10^{-26} \text{ e cm} \\ = 3 \cdot 10^{-13} \text{ e fm}$$

What do we expect?

- Two mass scales in the game:

$$m_q \sim 1 - 10 \text{ MeV}$$

$$\Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$

$$d_n \sim e \times \text{length} \times \theta \sim e \times \frac{m_q}{\Lambda_{\text{QCD}}^2} \times \theta$$

$$\sim (1 - 10) \times 10^{-16} e \text{ cm } \theta$$

"Argument" EDM Blackboard

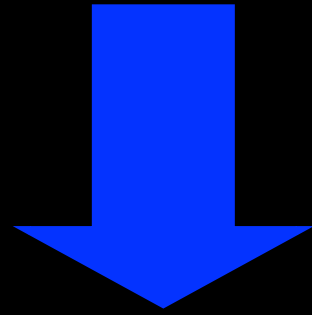
Implications

- Detailed calculation gives

$$|\vec{d}| \sim 1 - 10 \times 10^{-16} e \text{ cm } \theta$$

 $|\theta| < 3 \cdot 10^{-9}$

 **Extremely unnatural!**



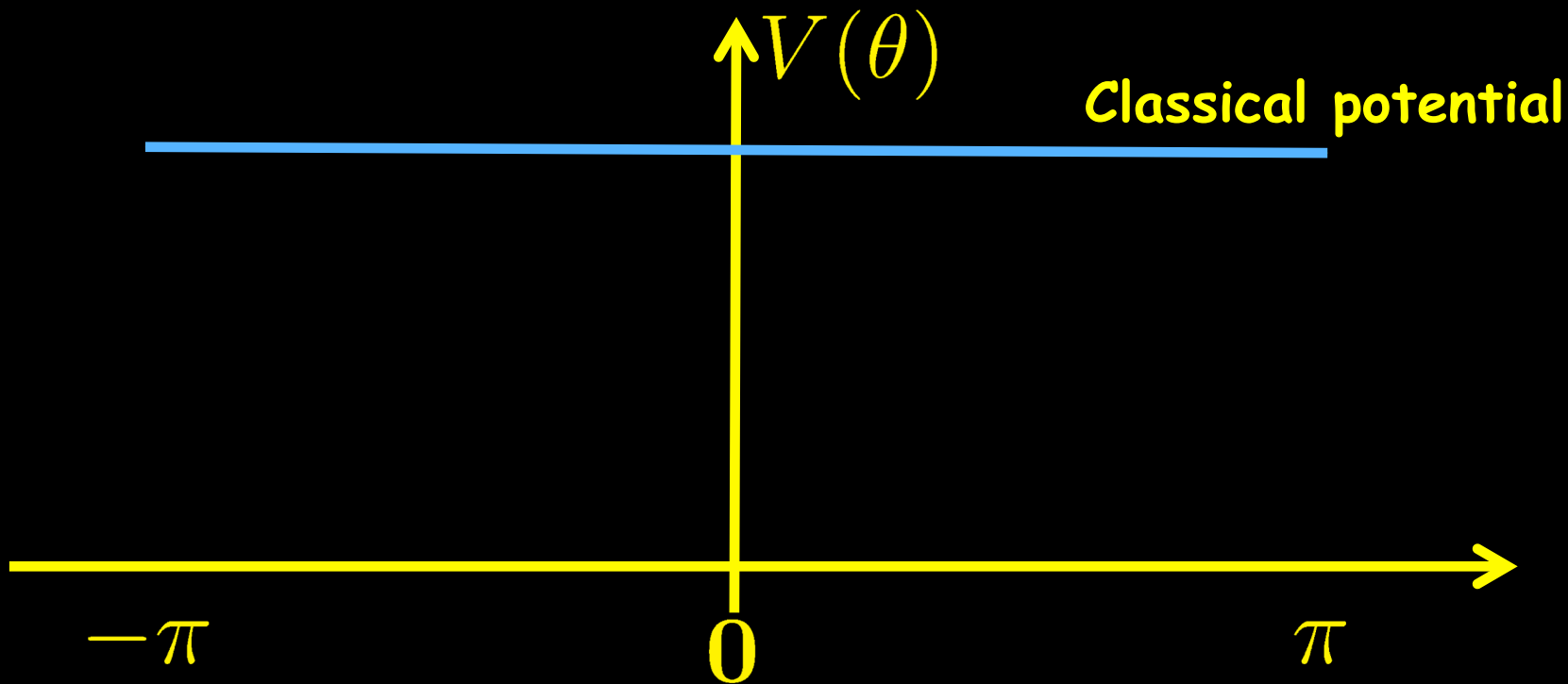
Strong CP Problem

The axion solution
to the strong CP problem

In pictures...

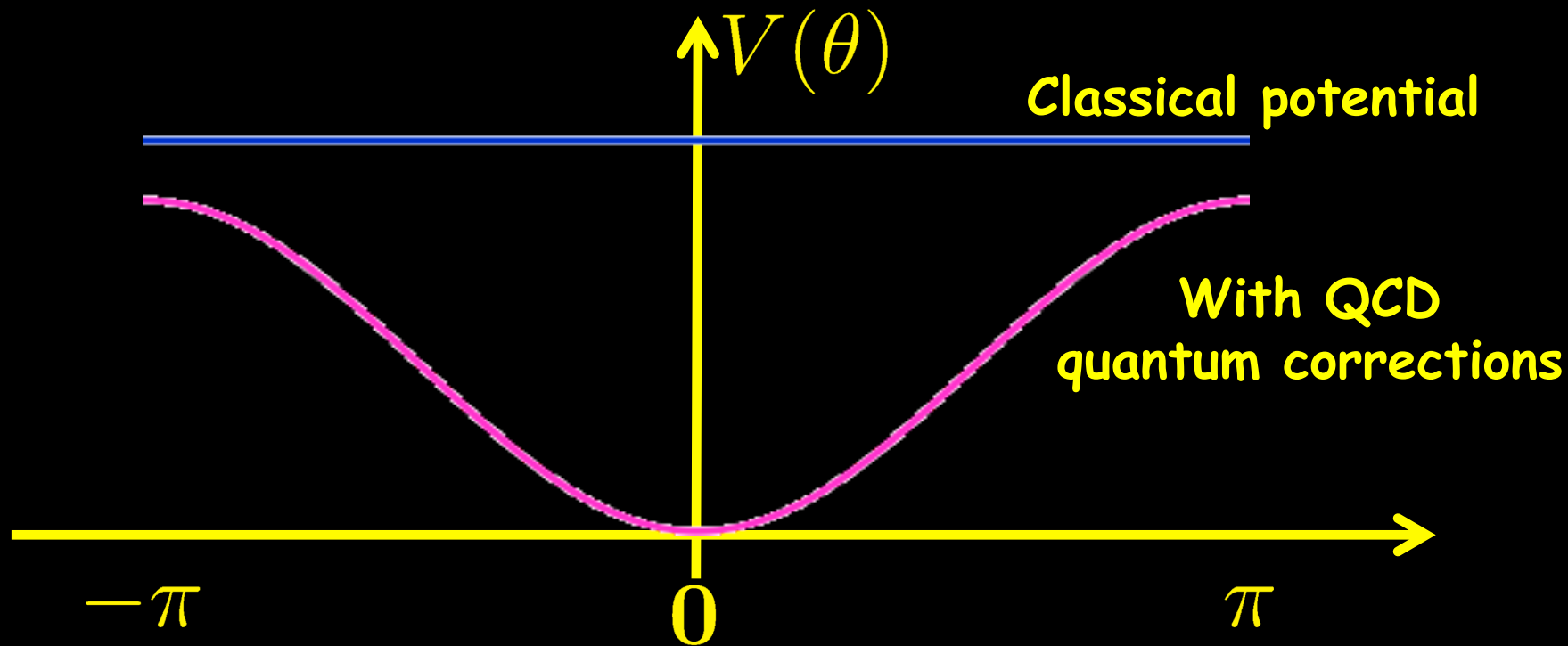
The axion solution to the strong CP problem

- Make θ dynamical \rightarrow it can change its value



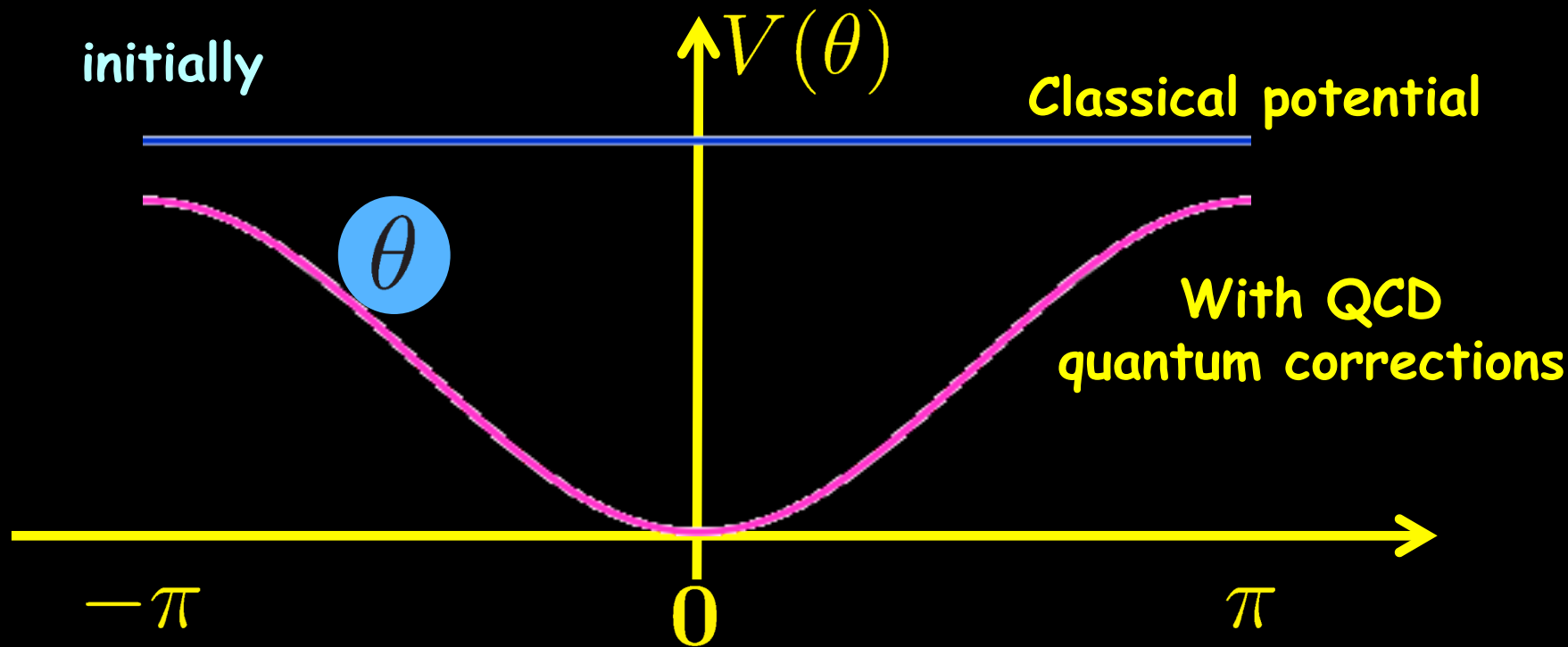
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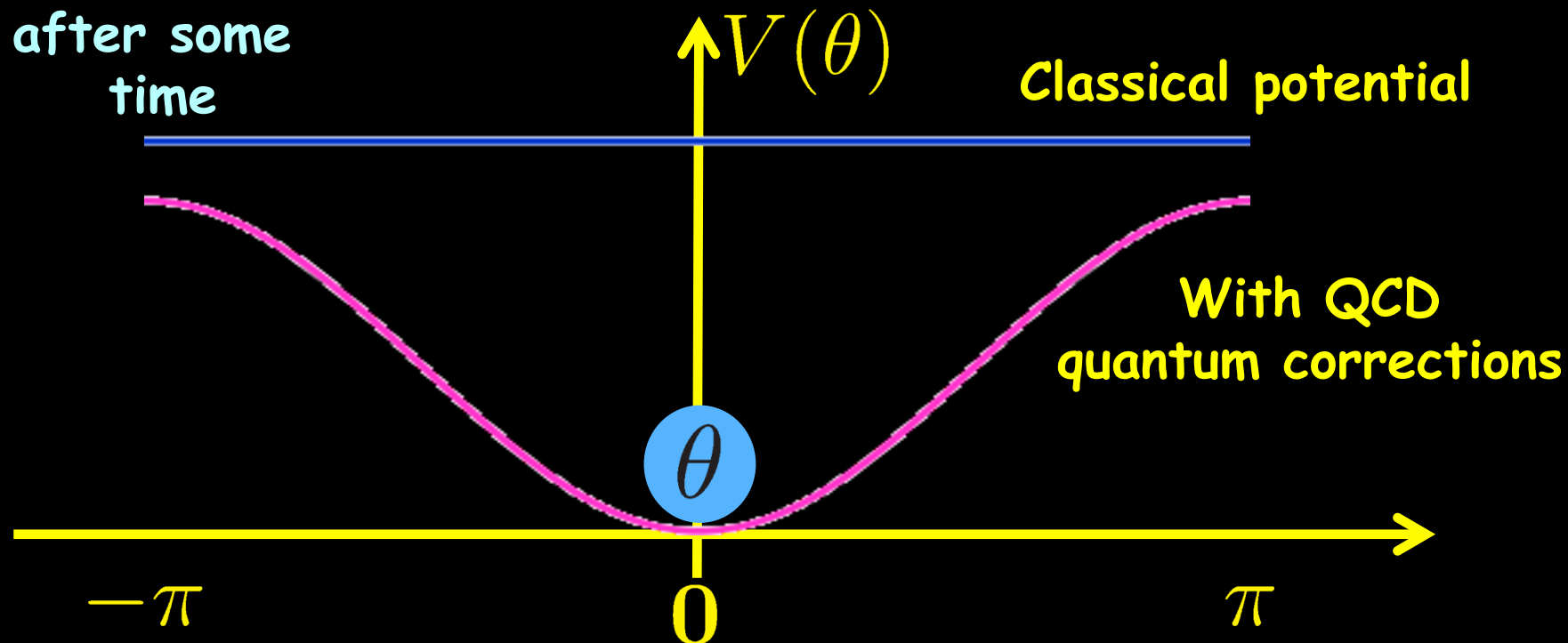
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The axion solution to the strong CP problem

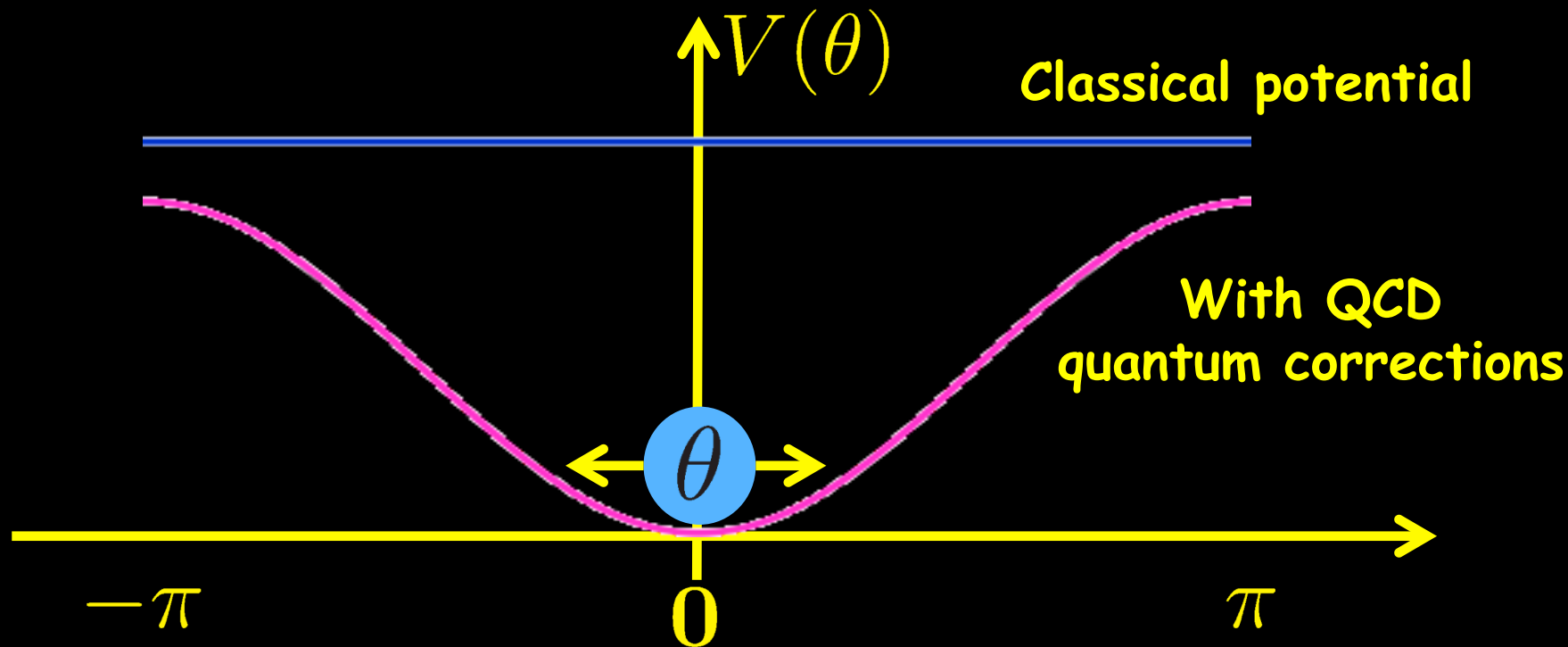
- Make θ dynamical \rightarrow it can change its value



\rightarrow QCD likes to be CP conserving (if we allow it)

The axion solution to the strong CP problem

- Make θ dynamical \rightarrow it can change its value



\rightarrow Can still move

\rightarrow new particle = axion

- Classical flatness from symmetry
- Quantum corrections are small
- New **light** particle: **The Axion**
(it's a **Weakly Interacting Sub-eV Particle**)



In Equations...

A Dynamical θ

- **Idea:**
 - Make θ a dynamical degree of freedom
 - Let θ have no tree level potential
 - Let θ have only derivative couplings
- **Then:**

$$\begin{aligned}\exp\left(-\int_x V(\theta)\right) &= \left| \int \mathcal{D}A_\mu \exp(-S_{eff}[\phi, A^\mu]) \exp\left(-i\theta \frac{g^2}{32\pi^2} \int_x G^{\mu\nu} \tilde{G}_{\mu\nu}\right) \right| \\ &\leq \int \mathcal{D}A_\mu \left| \exp(-S_{eff}[\phi, A^\mu]) \exp\left(-i\theta \frac{g^2}{32\pi^2} \int_x G^{\mu\nu} \tilde{G}_{\mu\nu}\right) \right| \\ &\leq \int \mathcal{D}A_\mu \exp(-S_{eff}[\phi, A^\mu]) \\ &\leq \exp\left(-\int_x V[0]\right)\end{aligned}$$

A Dynamical θ

- **Idea:**
 - Make θ a dynamical degree of freedom a .
 - Let θ have no tree level potential
 - Let θ have only derivative couplings
- **Canonically normalize $\theta = a/f_a$**

→ $V[a/f_a = \theta = 0] \leq V[\theta] \quad \forall \theta$

→ $\theta = a/f_a$ will evolve to $a = \theta = 0$

→ **CP is conserved**

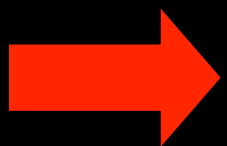
What is a?

- Properties:

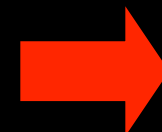
- Let a be a dynamical degree of freedom.
- Let a have no tree level potential
- Let a have only derivative couplings

- $a/f_a \in [0, 2\pi]$ since

$$\frac{g^2}{32\pi^2} \int d^4x G_{\mu\nu} \tilde{G}^{\mu\nu} = n \in \mathbb{Z}$$



a is Goldstone boson
of a $U(1)$ symmetry



Axion!

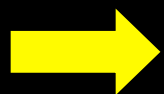
Peccei-Quinn Symmetry

- Toy model:

$$\mathcal{L} = -\frac{1}{4}F^2 + i\bar{\psi}D_\mu\gamma^\mu\psi - |\partial_\mu\phi|^2 - \mu^2|\phi|^2 - \lambda|\phi|^4 \\ + \bar{\psi}\left(Y\phi\frac{1+\gamma_5}{2} + Y^*\phi^*\frac{1-\gamma_5}{2}\right)\psi$$

- **U(1):** $\phi \rightarrow \exp(i\beta)\phi$
 $\psi \rightarrow \exp\left(-i\frac{\beta}{2}\gamma_5\right)\psi$

- If $\mu^2 < 0$ we have SSB



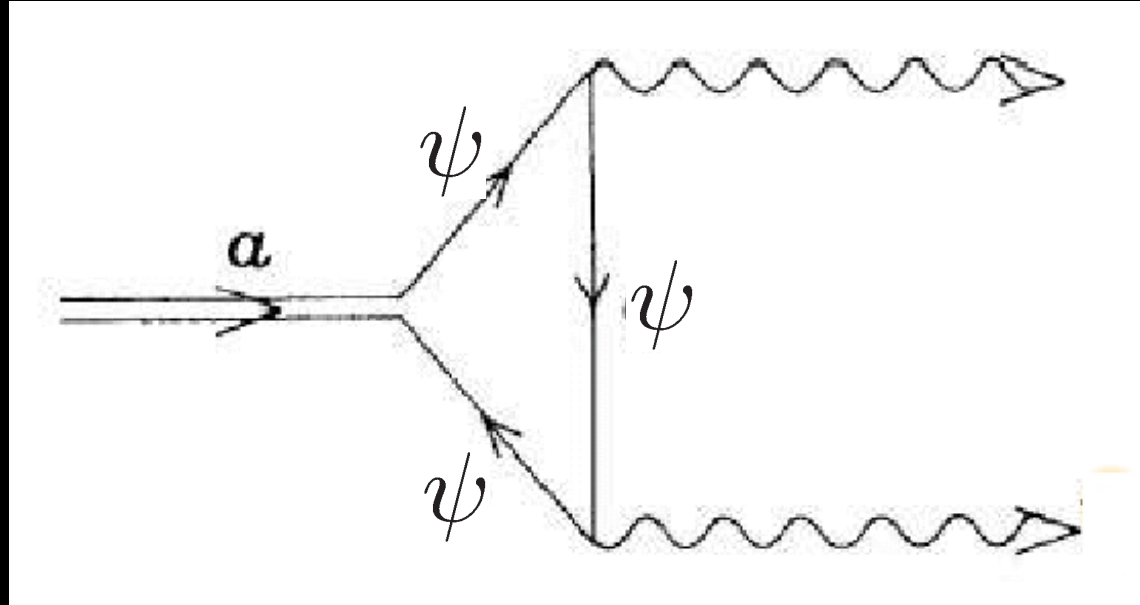
Phase is Goldstone



Use it as Axion

The Coupling to $F\tilde{F}$ ($G\tilde{G}$ analog)

- A diagram



- And a dimensional argument:

$$g \sim \frac{1}{\text{mass}} \sim \frac{1}{f_a}$$

The Coupling to $F \tilde{F}$

- Adler-Bell-Jackiw anomaly

$$\partial_\mu j^\mu = \frac{g^2}{16\pi^2} F^{\mu\nu} \tilde{F}_{\mu\nu}$$

- Chiral rotations not a good symmetry: it is anomalous

$$d\mu' = \mathcal{D}\psi' \mathcal{D}\bar{\psi}' = d\mu \exp \left(-\frac{i}{4} \int_x \frac{\beta}{2} \frac{e^2}{8\pi^2} \text{Tr} F^{\mu\nu} \tilde{F}_{\mu\nu} \right)$$

$$\psi' = \exp \left(-i \frac{\beta}{2} \gamma_5 \right) \psi = \frac{a}{f_a}$$


The Coupling to $F \tilde{F}$

- Adler-Bell-Jackiw anomaly

$$\partial_\mu j^\mu = \frac{g^2}{16\pi^2} F^{\mu\nu} \tilde{F}_{\mu\nu}$$

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$$\mathcal{L} \supset -\frac{1}{4} \frac{\alpha}{4\pi f_a} a F^{\mu\nu} \tilde{F}_{\mu\nu}$$

The mass of the Axion

- $U(1)_{PQ}$ is not exact. It's anomalous!

➡ Goldstone ➡ Pseudogoldstone

- Dimensional considerations

- SSB scale

$$\sim f_a$$

- Quark masses

$$\sim m_q$$

- QCD scale

$$\sim \Lambda_{\text{QCD}} \sim f_\pi$$

➡ PseudoGoldstone mass

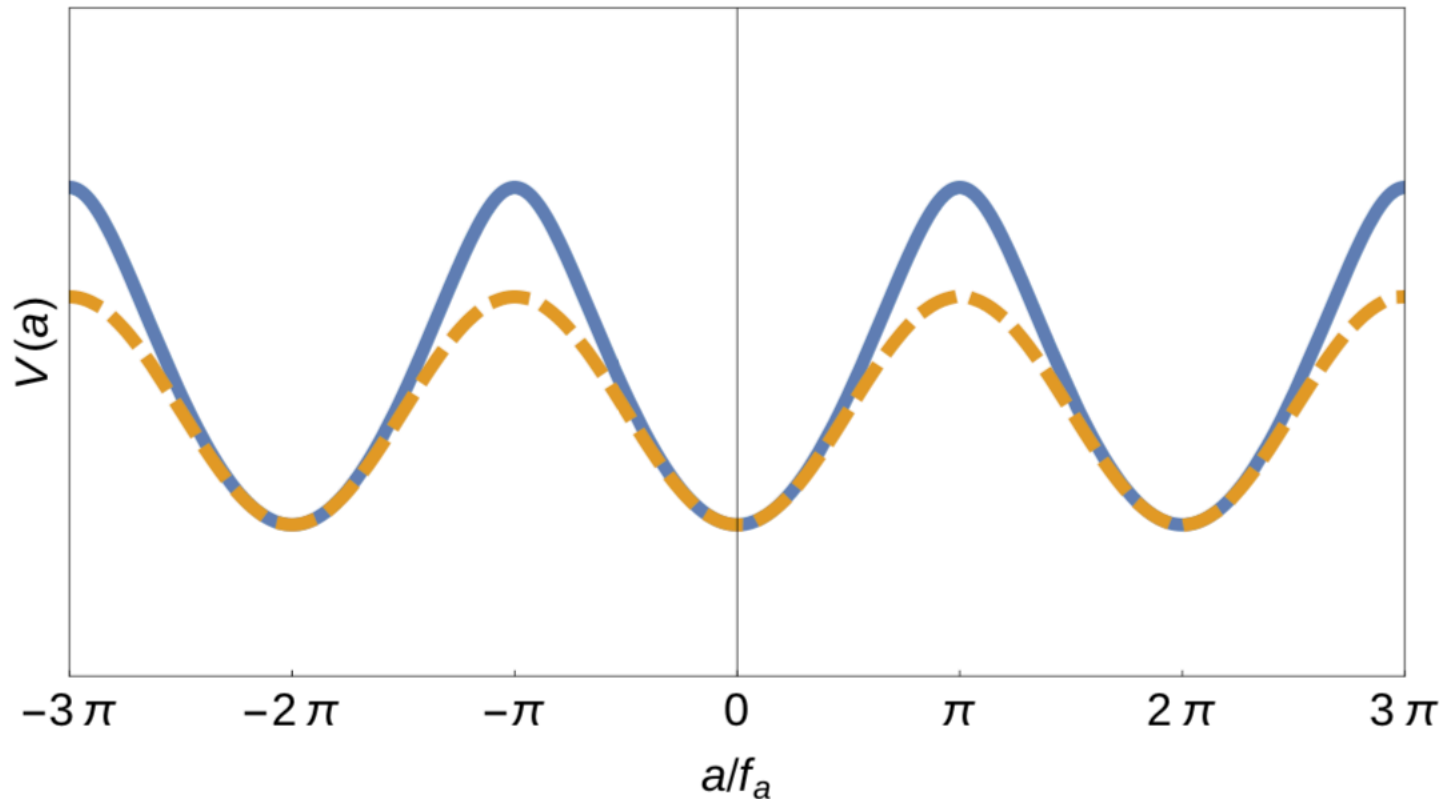
$$m_a^2 = \frac{m_u m_d}{(m_u + m_d)^2} \frac{m_\pi^2 f_\pi^2}{f_a^2}$$

One can actually calculate the potential

$$V(a) = -m_\pi^2 f_\pi^2 \sqrt{1 - \frac{4m_u m_d}{(m_u + m_d)^2} \sin^2 \left(\frac{a}{2f_a} \right)}$$

The QCD axion, precisely

Giovanni Grilli di Cortona^a, Edward Hardy^b,
Javier Pardo Vega^{a,b} and Giovanni Villadoro^b



"Argument"
Topological Suszeptibility

The ``topological'' axion mass

$$\begin{aligned}\frac{d^2}{d\theta^2} \exp\left(-\int_x V(\theta)\right) &= \frac{d^2}{d\theta^2} \exp(-V(\theta)\mathcal{V}) \\ &= (-V''(\theta)\mathcal{V} + (V'(\theta)\mathcal{V})^2) \exp(-V(\theta)\mathcal{V})\end{aligned}$$

→ Evaluate at $\theta=0$ (minimum)
normalize $V(0)=0$

$$\begin{aligned}&= -V''(\theta)\mathcal{V} \\ &= -m_a^2 f_a^2 \mathcal{V}\end{aligned}$$

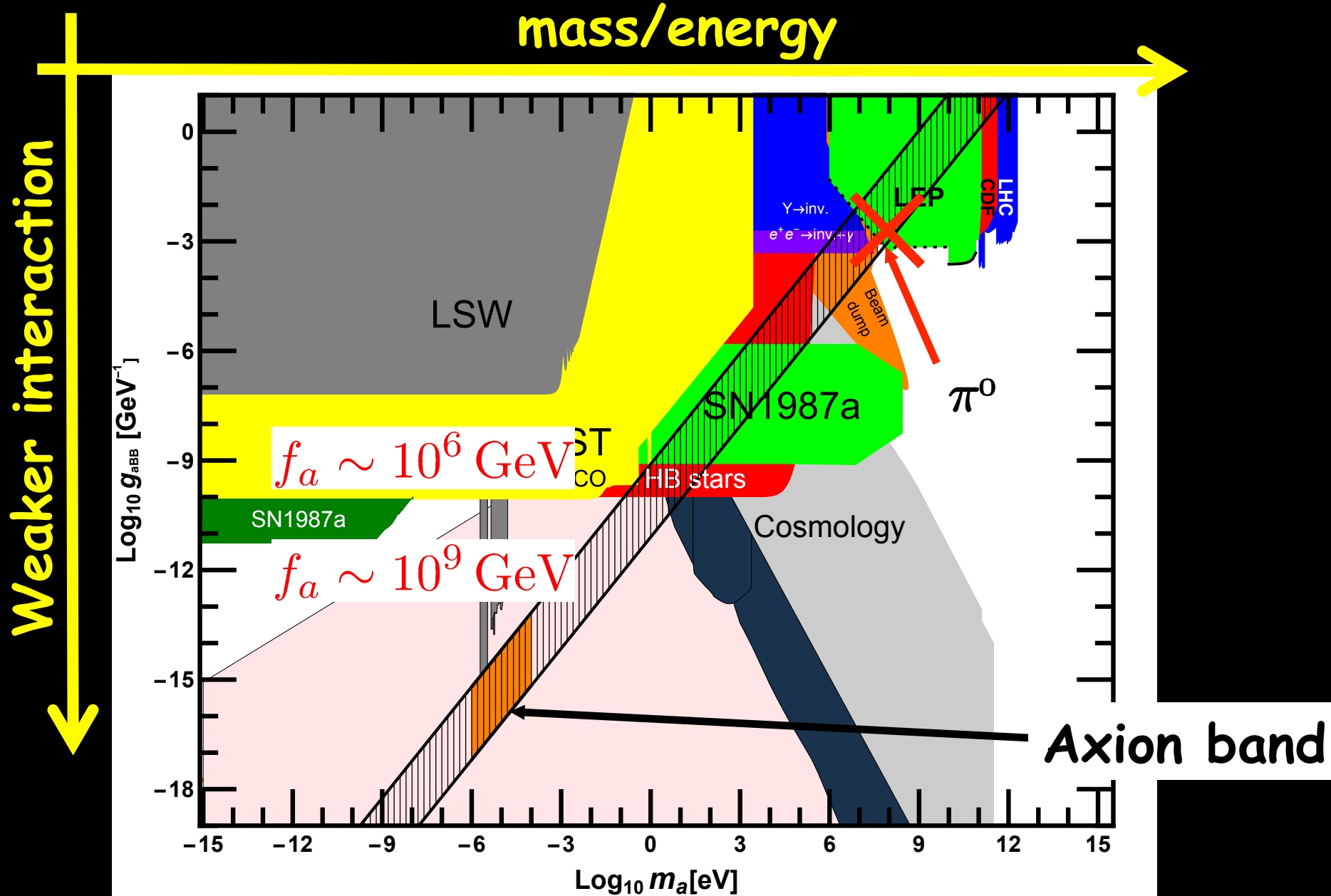
The axion mass

$$\begin{aligned}\exp\left(-\int_x V(\theta)\right) &= \int \mathcal{D}A_\mu \exp(-S_{eff}[\phi, A^\mu]) \exp\left(-i\theta \frac{g^2}{32\pi^2} \int_x G^{\mu\nu} \tilde{G}_{\mu\nu}\right) \\ &= \int \mathcal{D}A_\mu \exp(-S_{eff}[\phi, A^\mu]) \exp(-i\theta Q)\end{aligned}$$

$$\begin{aligned}\frac{d^2}{d\theta^2} \exp\left(-\int_x V(\theta)\right) &= \int \mathcal{D}A_\mu (-iQ)^2 \exp(-S_{eff}[\phi, A^\mu]) \exp(-i\theta Q) \\ &= -\langle Q^2 \rangle \\ &= -\mathcal{V} \chi_{top}\end{aligned}$$

$$\Rightarrow m_a^2 f_a^2 = -\chi_{top}$$

Axions and Axion-like Particles



**Add on
to yesterday's tutorial**

Topology of $U(1)$ vs $SU(3)$

Topological concepts in gauge theories

Frieder Lenz (Erlangen - Nuremberg U., Theorie III). 2001. 83 pp.

Published in *Lect.Notes Phys.* 659 (2005) 7-98

FAU-TP3-04-3

DOI: [10.1007/978-3-540-31532-2_2](https://doi.org/10.1007/978-3-540-31532-2_2)

Conference: [C01-09-24.6](#)

e-Print: [hep-th/0403286](#) | [PDF](#)

[References](#) | [BibTeX](#) | [LaTeX\(US\)](#) | [LaTeX\(EU\)](#) | [Harvmac](#) | [EndNote](#)
[ADS Abstract Service](#)

Consider inequivalent
pure gauge
vacua

$$\mathbf{A} = \frac{1}{ig} U(\mathbf{x}) \nabla U^\dagger(\mathbf{x}).$$

$$U(\mathbf{x}) \rightarrow \text{const.} \quad \text{for } |\mathbf{x}| \rightarrow \infty.$$

$$U(\mathbf{x}) : S^3 \longrightarrow S^3$$

$$U(\mathbf{x}) : S^3 \rightarrow S^1$$

For $U(1)$

Toward a theory of the strong interactions

Curtis G. Callan, Jr.* and Roger Dashen
Institute for Advanced Study, Princeton, New Jersey 08540

David J. Gross[†]
Joseph Henry Laboratories, Princeton University, Princeton, New Jersey 08540
(Received 26 August 1977)

$$\pi_3(S^3) = \mathbb{Z}$$

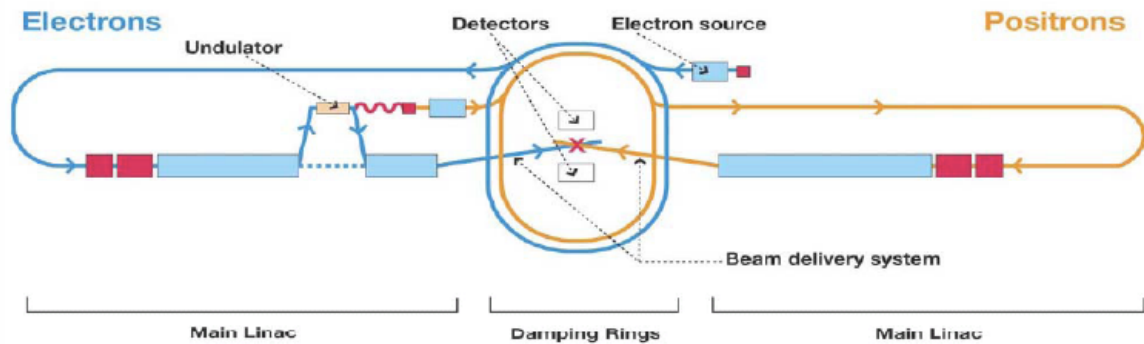
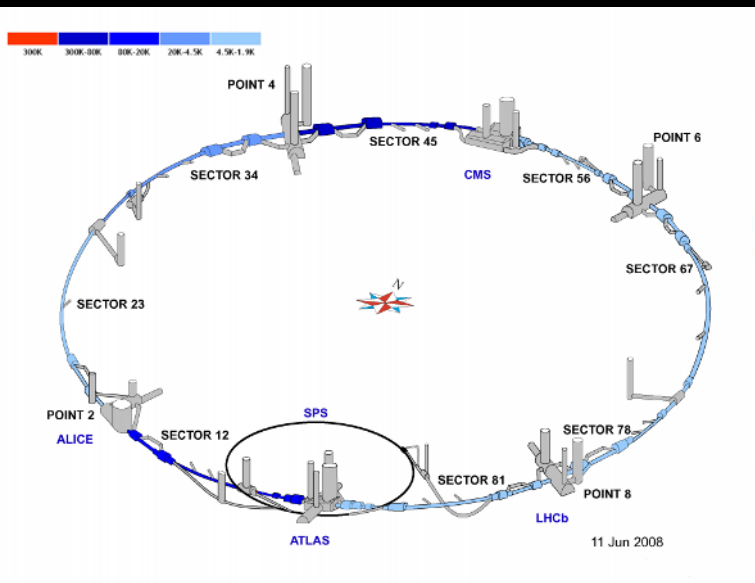
$$\pi_3(S^1) = 0$$

How to find the Axion...

Exploring fundamental high energy physics...

- The direct approach: **MORE POWER**

LHC, Tevatron + ILC, CLIC



- Detects most things within energy range
- E.g. may find SUSY particles, WIMPs etc.

But...

- May miss very weakly interacting matter (Axions, WIMPs, WISPs...)
- Current maximal energy few TeV

- Or much much more horrifying:

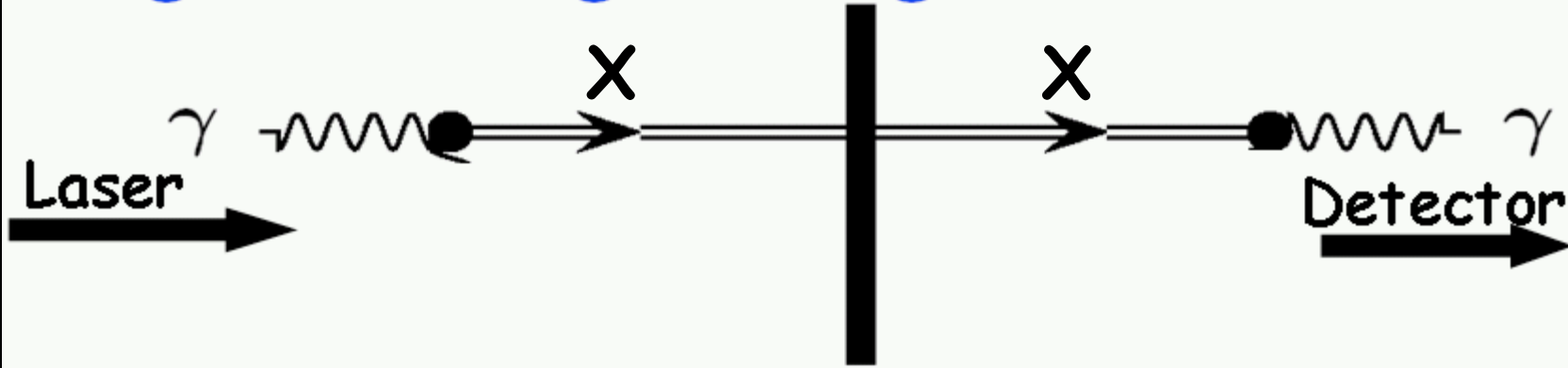
No signal above background!

The Power of Low Energy Experiments

Complementary approaches

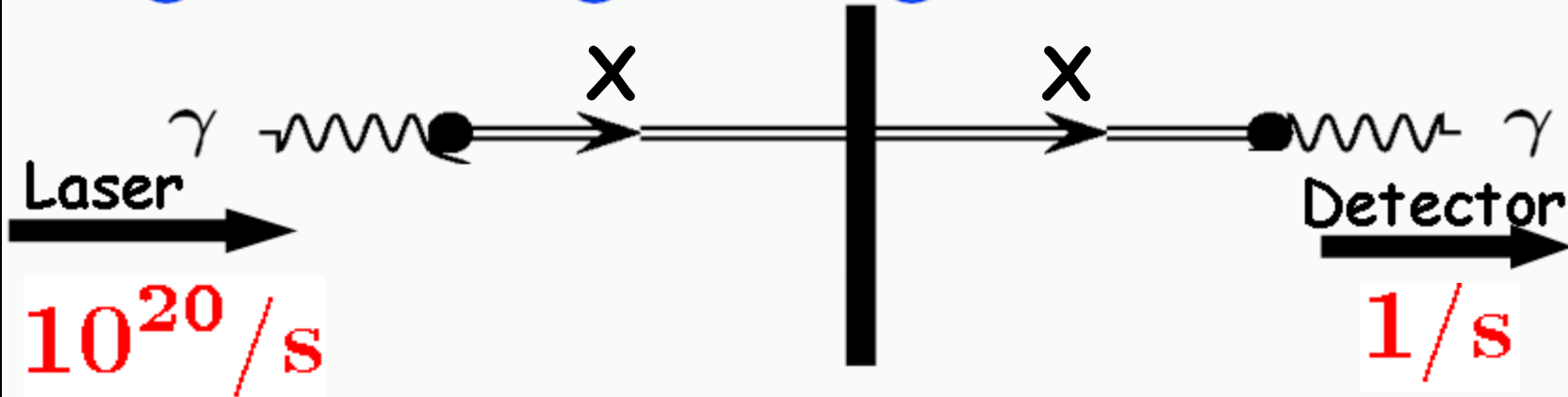
Light shining through walls

“Light shining through a wall”



Light shining through walls

“Light shining through a wall”

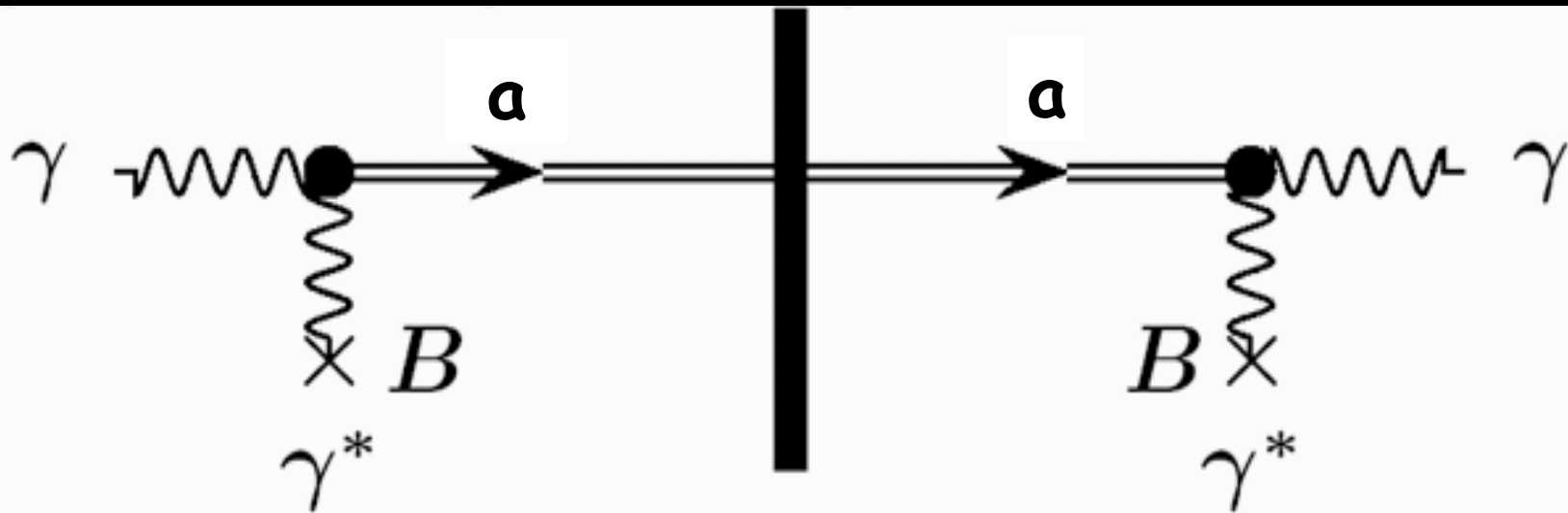


- **Test** $P_{\gamma \rightarrow X \rightarrow \gamma} \lesssim 10^{-20}$
- **Enormous precision!**
- **Study extremely weak couplings!**

Photons coming through the wall!

- It could be Axion(-like particle)s!

- Coupling to two photons: $\frac{1}{M} a \tilde{F} F \sim \frac{1}{M} a \vec{E} \cdot \vec{B}$



$$P_{\gamma \rightarrow a \rightarrow \gamma} \sim N_{\text{pass}} \left(\frac{BL}{M} \right)^4$$

Light Shining Through Walls

- A lot of activity

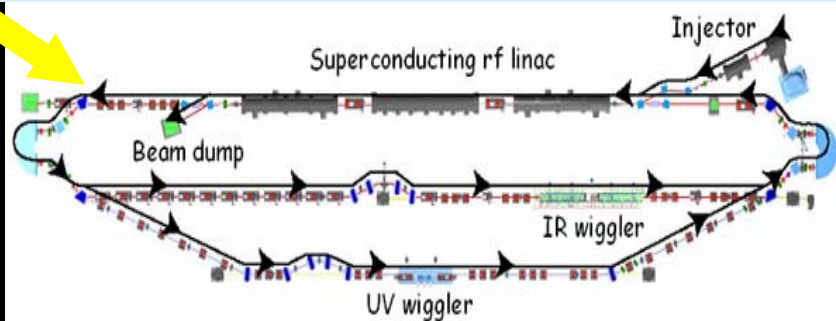
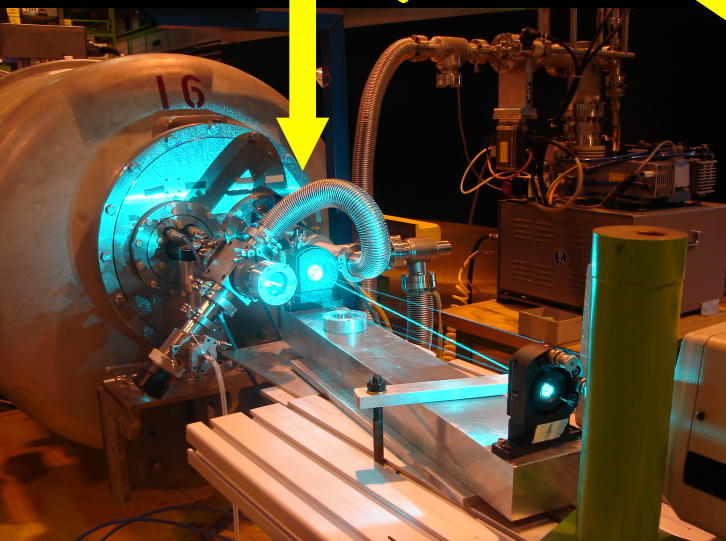
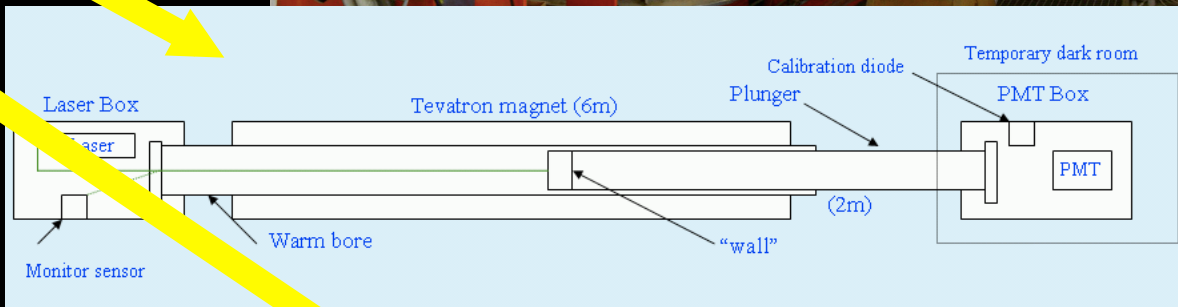
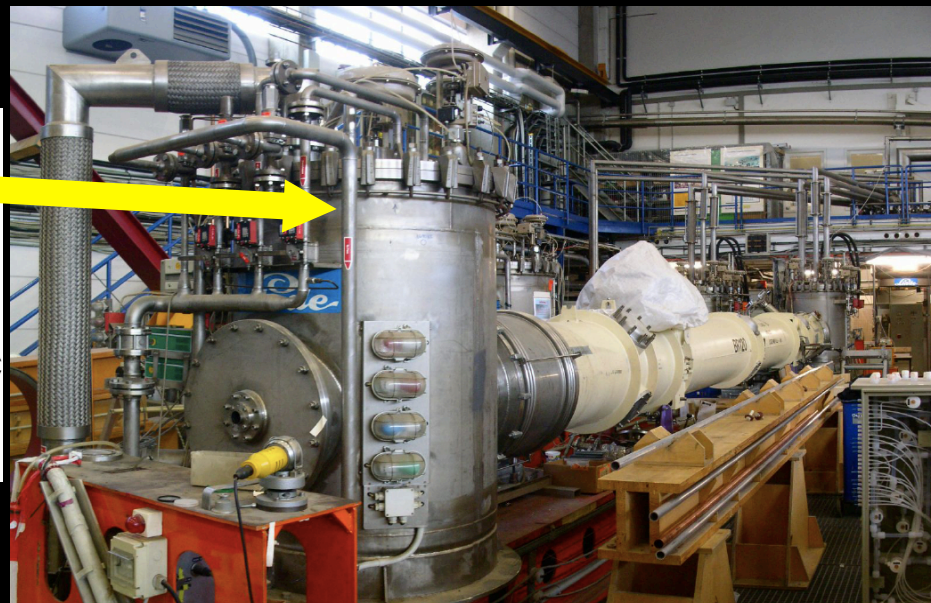
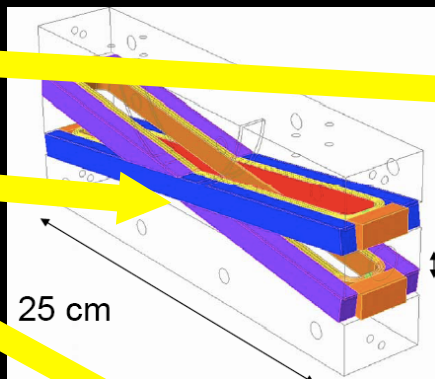
- ALPS

- BMV

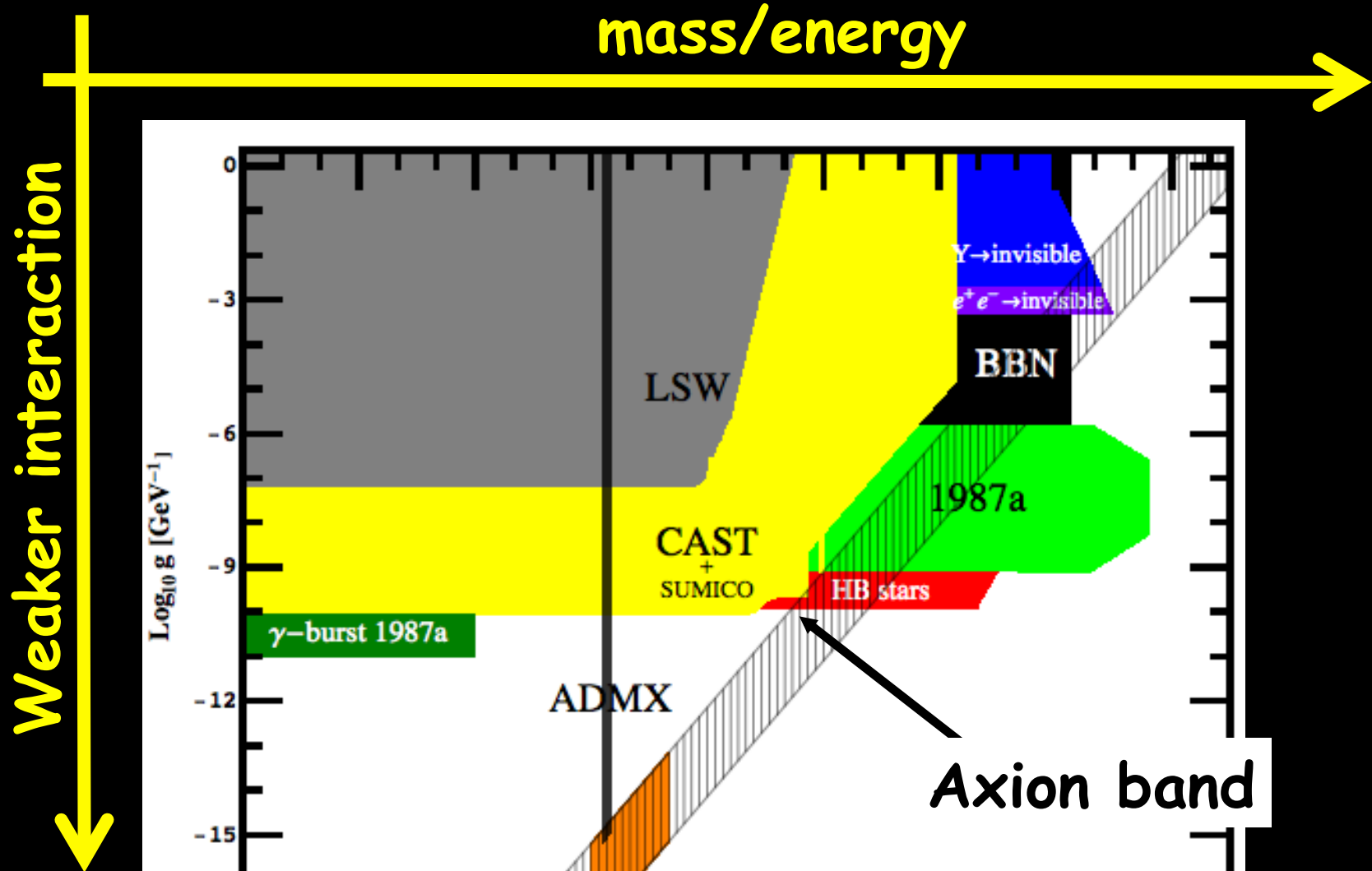
- GammeV

- LIPPS

- OSQAR



Small coupling, small mass

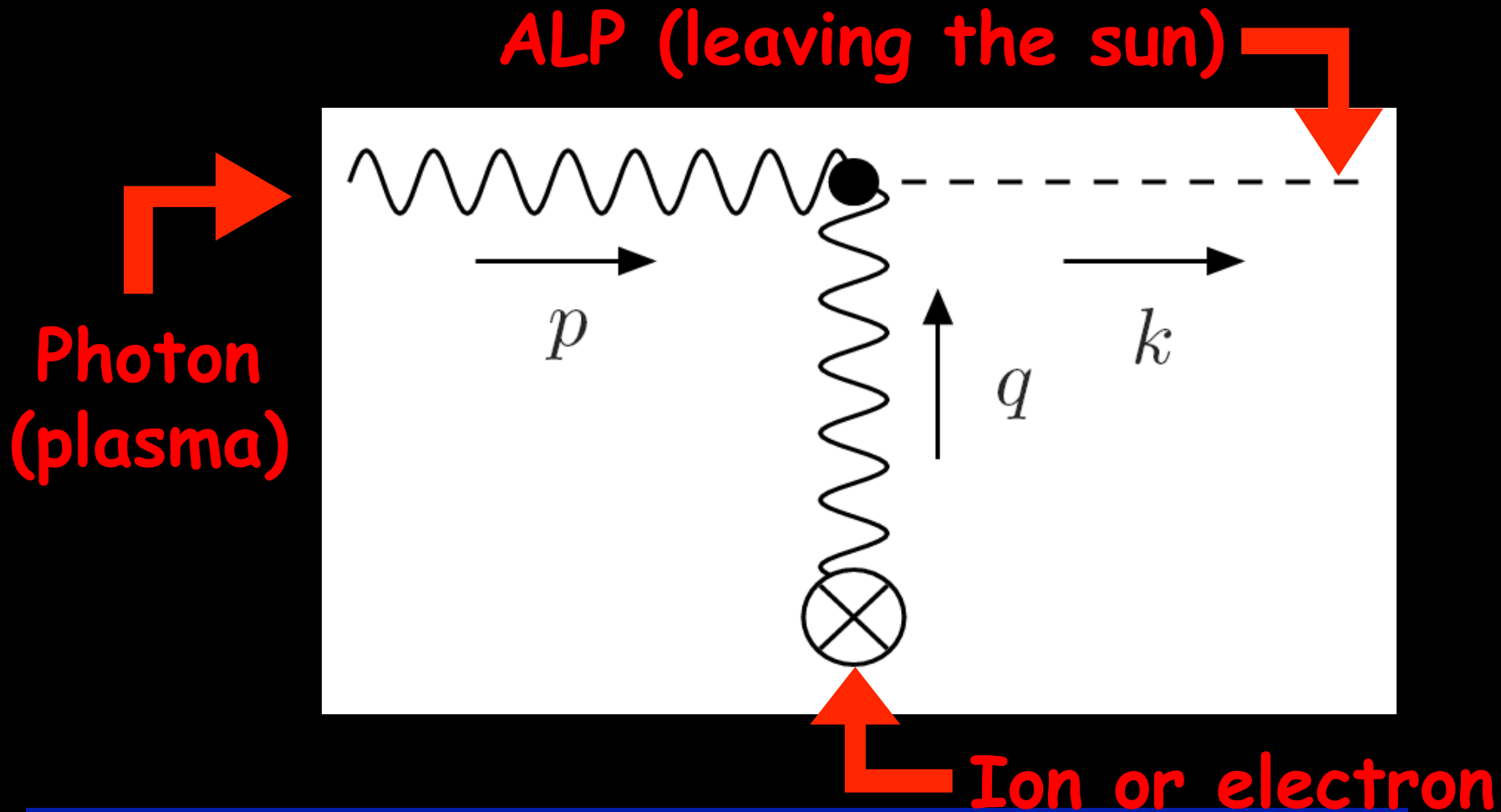


Interlude:

Think and make life hard
for experimentalists...

Energy loss in stars.

- Primakoff process (in the sun)



We would freeze...

- If the coupling g is too large the sun would have died long ago.
- Why?

Axions can leave the sun without further interaction (in contrast to photons)

- ➔ Large energy loss from axion emission
 - ➔ Sun burns fuel faster
 - ➔ Sun would have died long ago
-

A (Very) Moderate Bound

- Without ALPs sun has fuel for about 10^{10} years
- Energy loss via ALPs:

- Sun Lifetime with ALPs

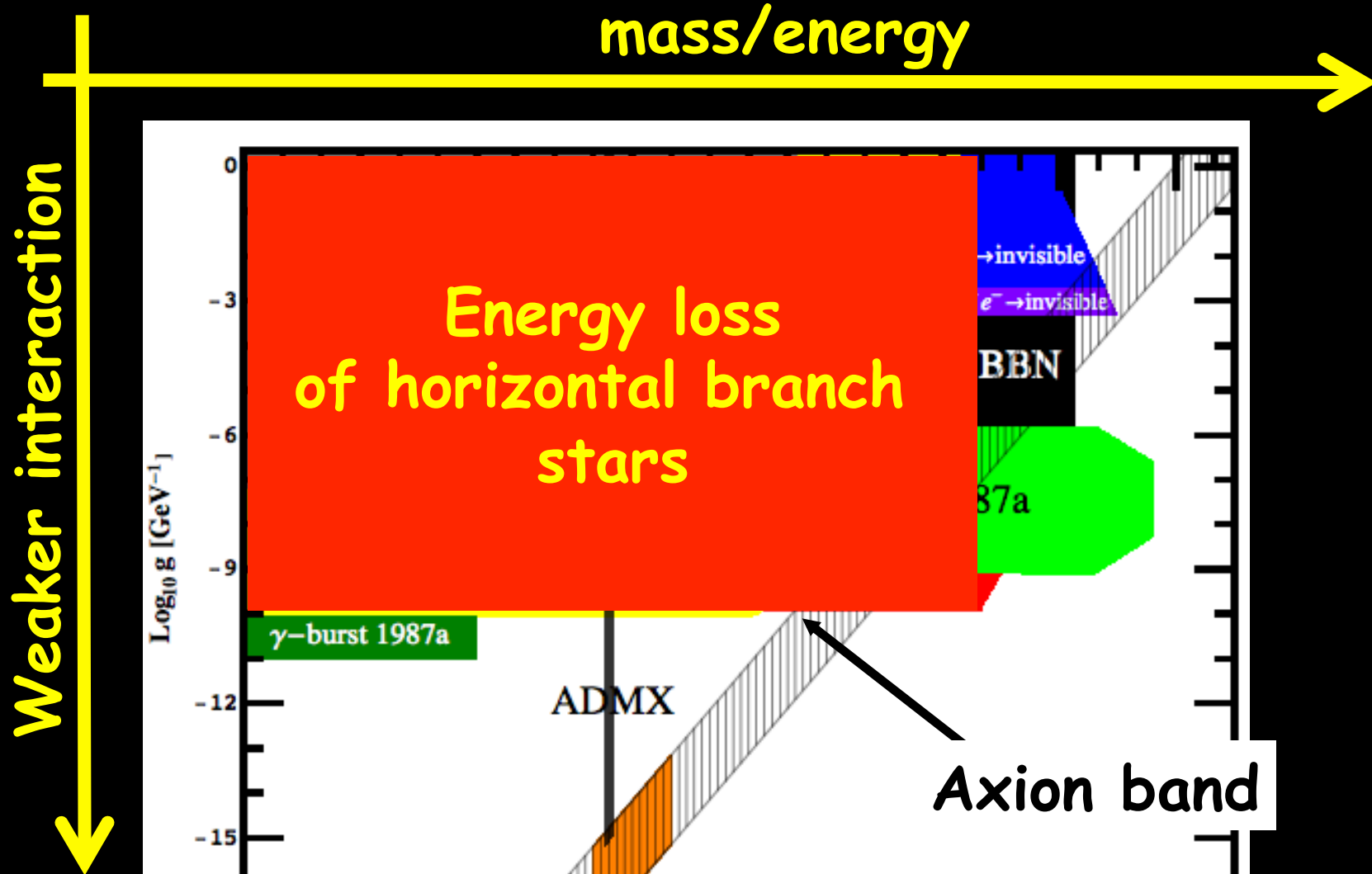
$$L_a \approx 1.7 \cdot 10^9 (g \cdot 10^4 \text{ GeV})^2 L_\gamma$$

- Pretty sure sun has been around for more than 10 years

$$t_{sun} \sim 10 \text{ years} \times (g \cdot 10^4 \text{ GeV})^{-2}$$

 $g \leq 10^{-4} \text{ GeV}^{-1}$

A Real killer bound



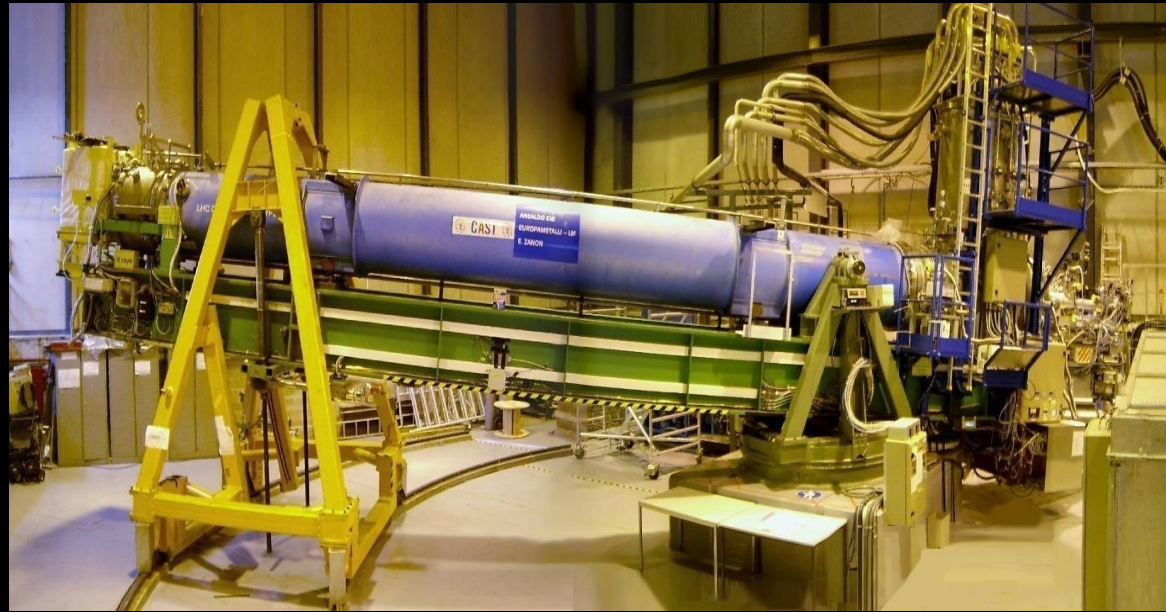
Back to experiments...

Helioscopes

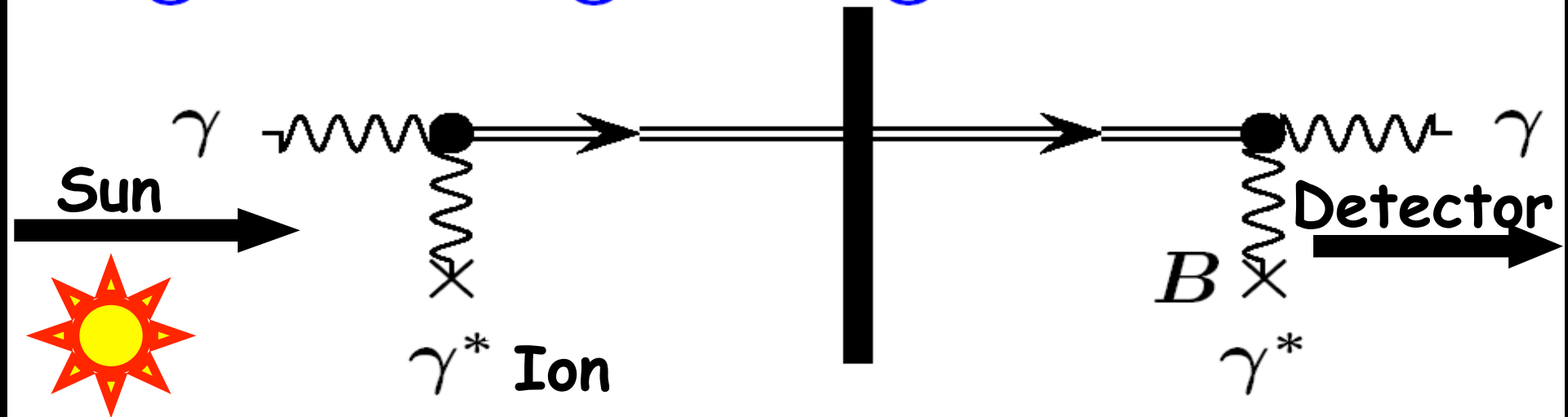
CAST@CERN

SUMICO@Tokyo

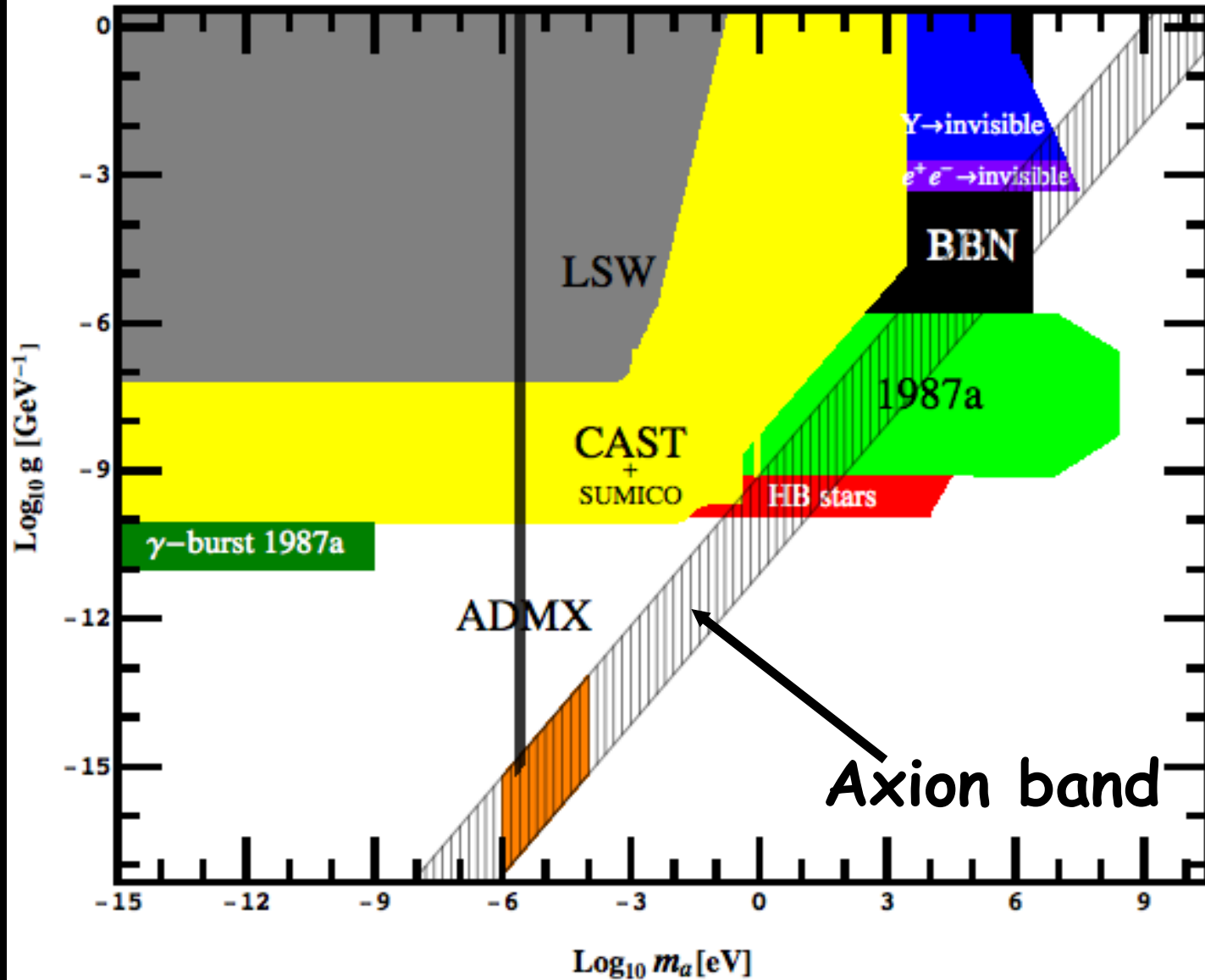
SHIPS@Hamburg



“Light shining through a wall”

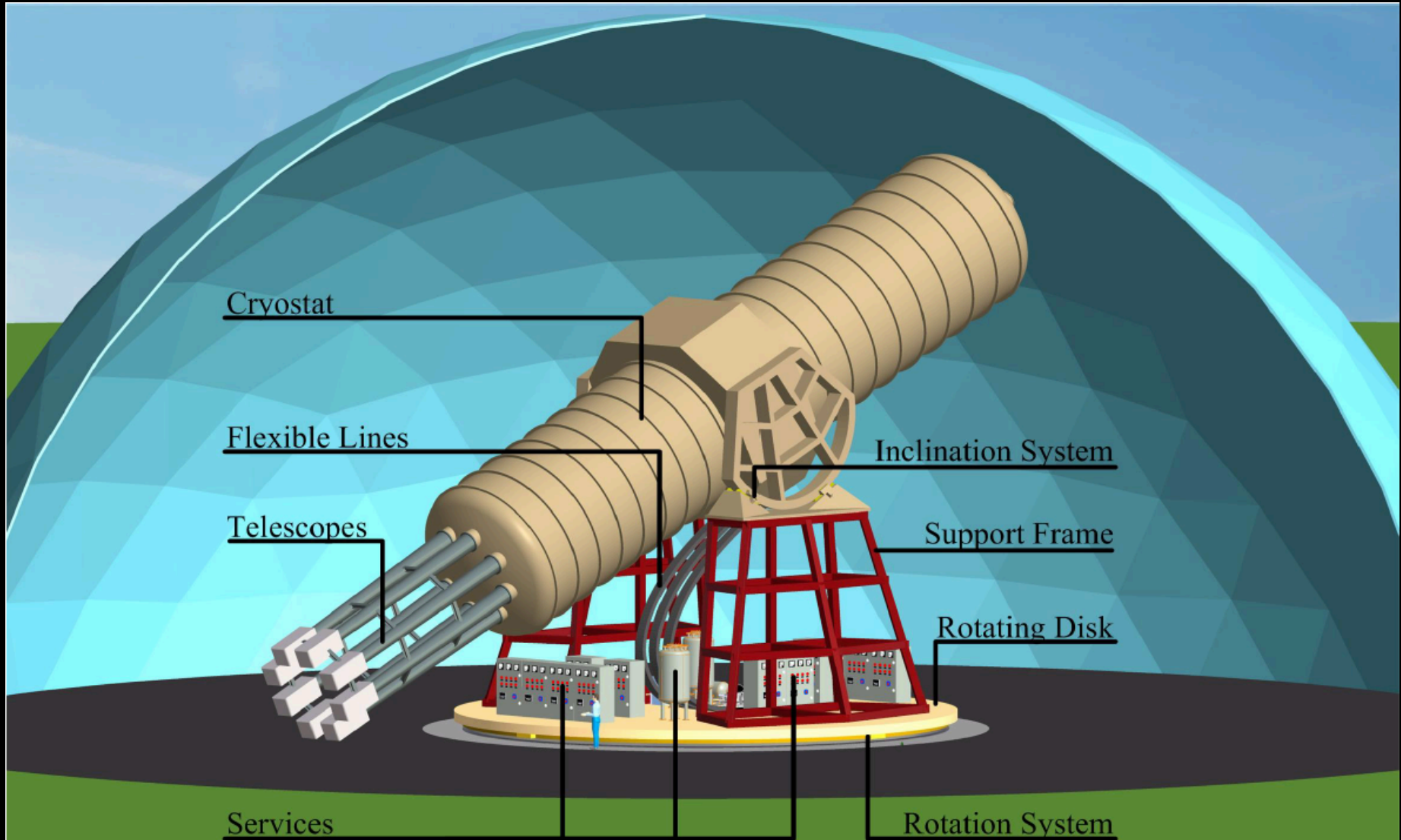


Sensitivity

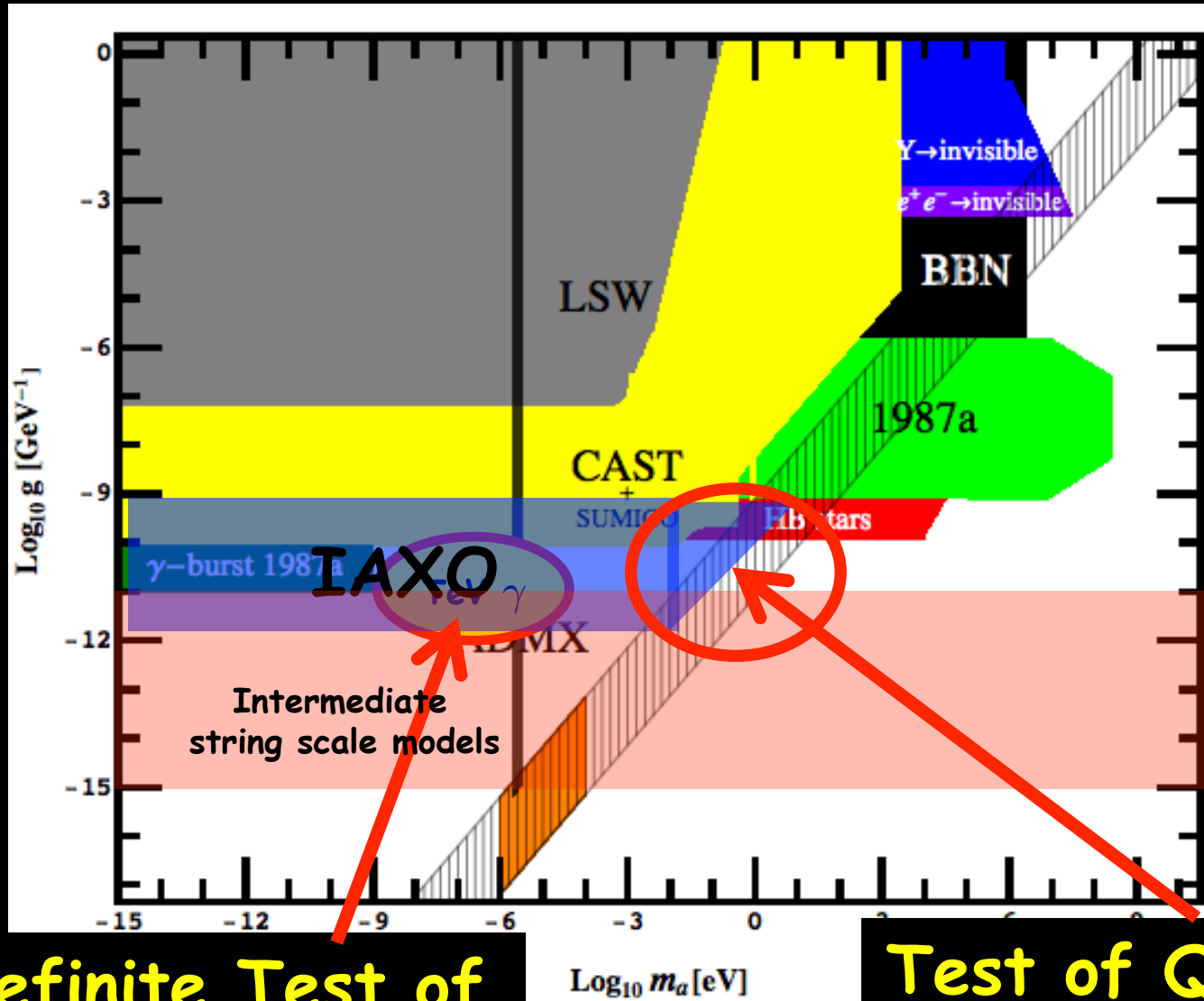


Going to the future: IAXO

The International Axion Observatory



An interesting area...

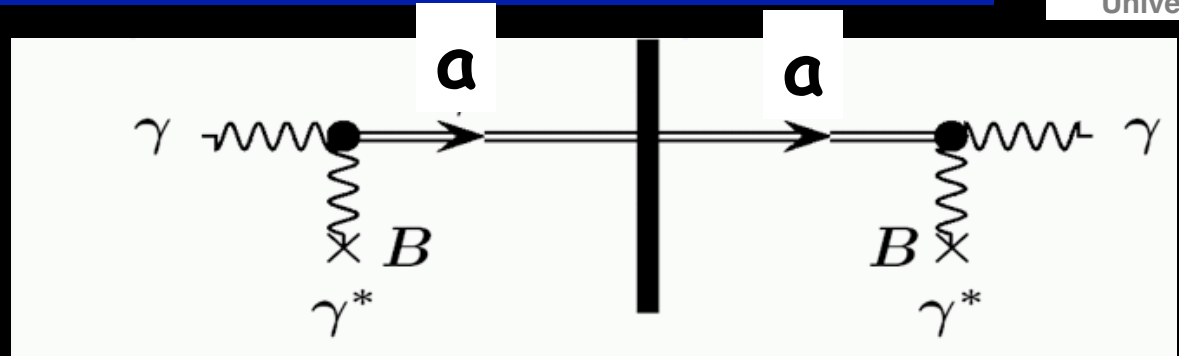


Definite Test of
TeV transparency

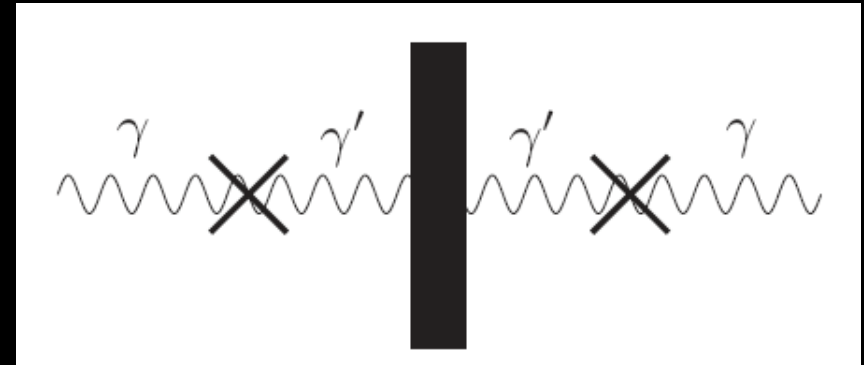
Test of QCD axion
+ white dwarf anomaly

WISPS=Weakly interacting sub-eV particles

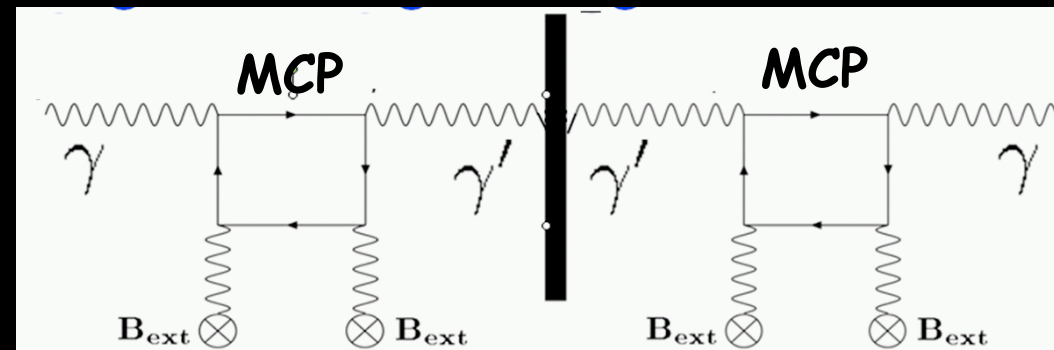
- Axions



- Massive hidden photons (without B-field) = analog ν -oscillations



- Hidden photon + minicharged particle (MCP)

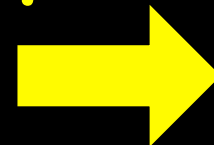


Dark Matter(s)

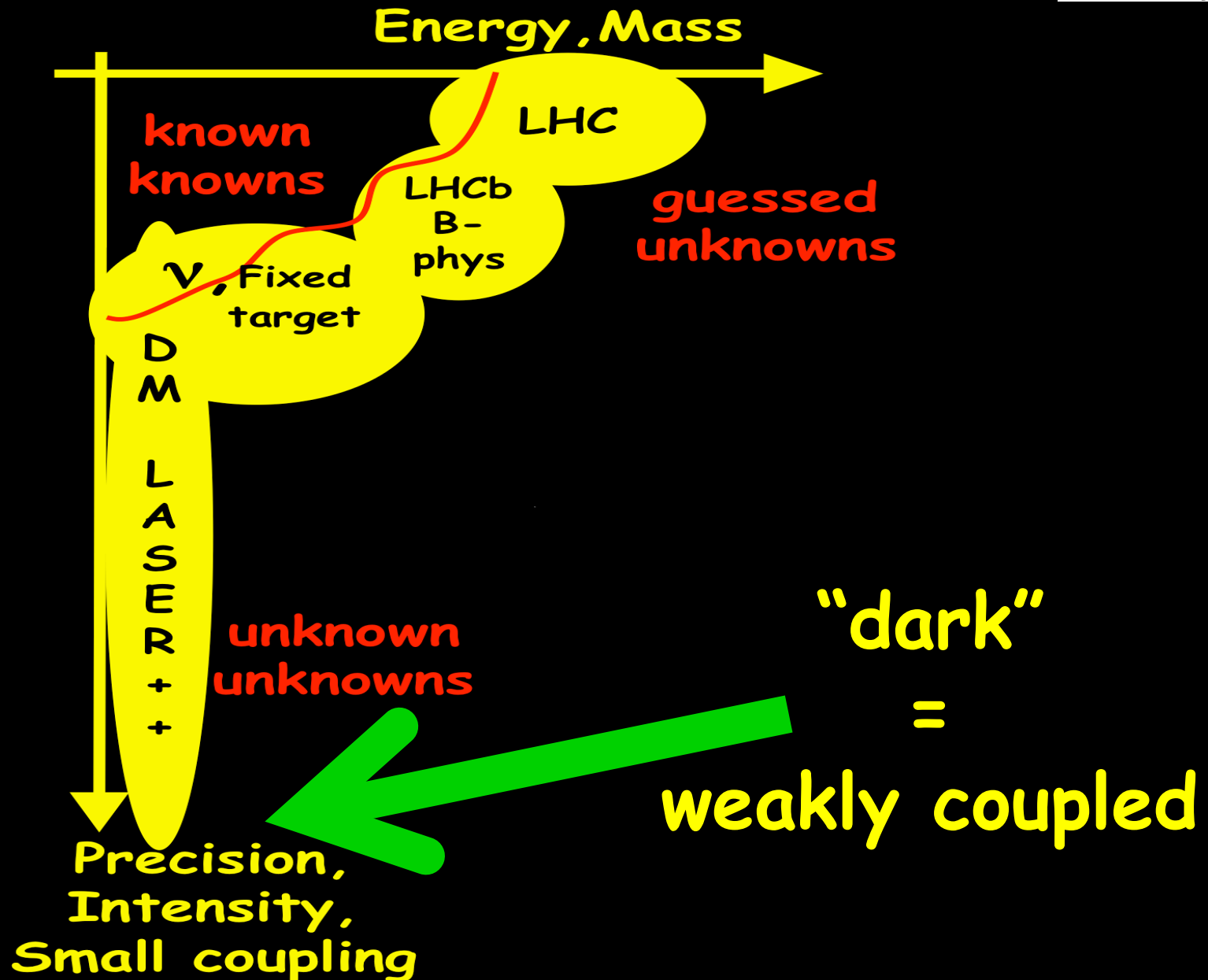
Can Dark Matter
be Axiony/WISPy?
(Weakly Interacting Sub-eV Particley)
Slim

Properties of Dark Matter

- Dark matter is dark, i.e.
it doesn't radiate!
(and also doesn't absorb)
- very, very weak interactions with light
and with ordinary matter
- Exactly the property of
Axions/WISPs



Exploring is (at least) 2 dimensional

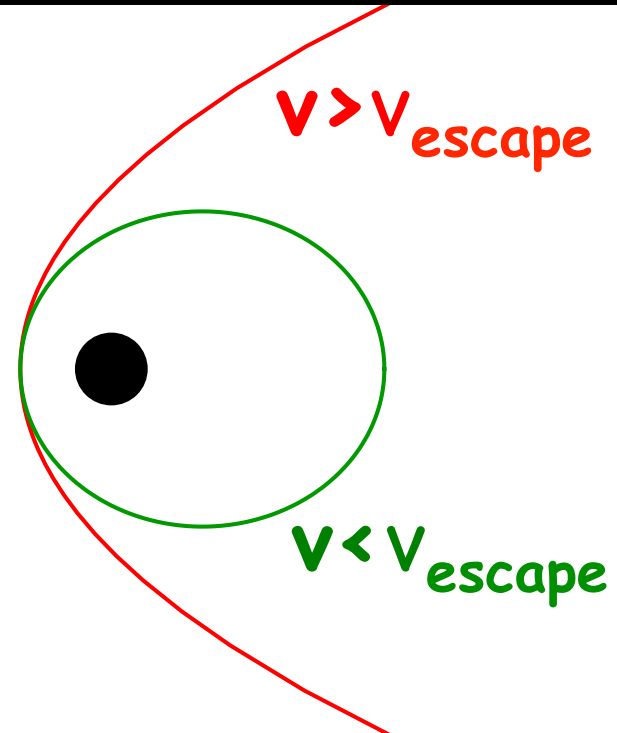


A common prejudice

- Dark Matter has to be heavy: $m_{\text{DM}} \gtrsim \text{keV}$.
- Prejudice based on thermal production!
and/or fermionic DM!

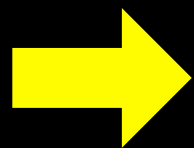
Both assumptions give
minimal velocity

→ galaxy,
i.e. structure,
formation inhibited!



Weakly interacting sub-eV DM

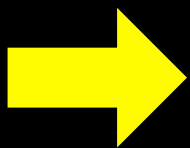
- Has to be non-thermally (cold!!!) produced



See misalignment mechanism



- Bosonic!



Axion(-like particles)
Hidden Photons



Dark matter has to be heavy...

Dark matter has to be heavy $m_{\text{DM}} \gtrsim \text{keV}$?

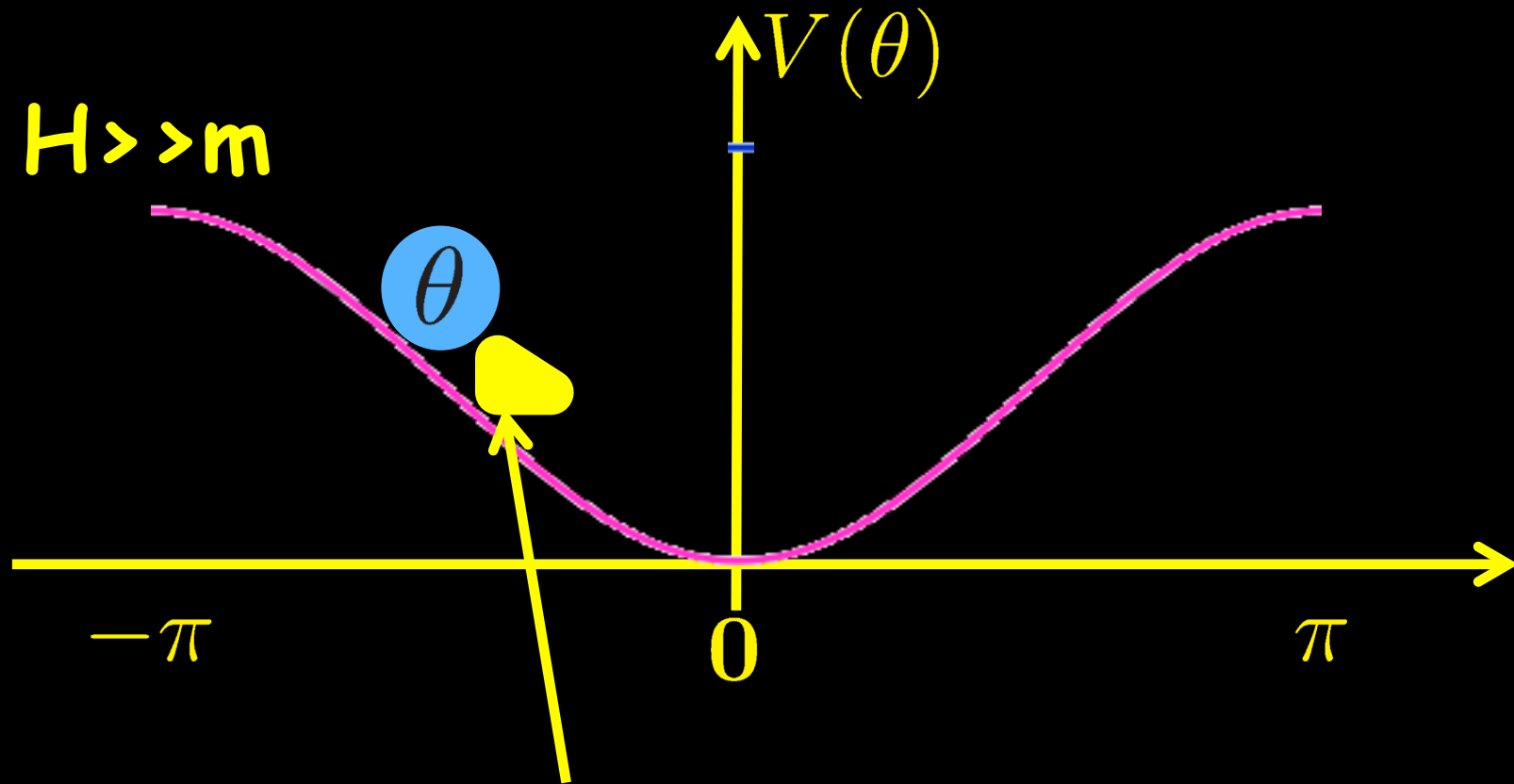
Dark matter has to be heavy...

Dark matter has heavy $m_{\text{DM}} \gtrsim \text{keV}$?

MYTH BUSTED

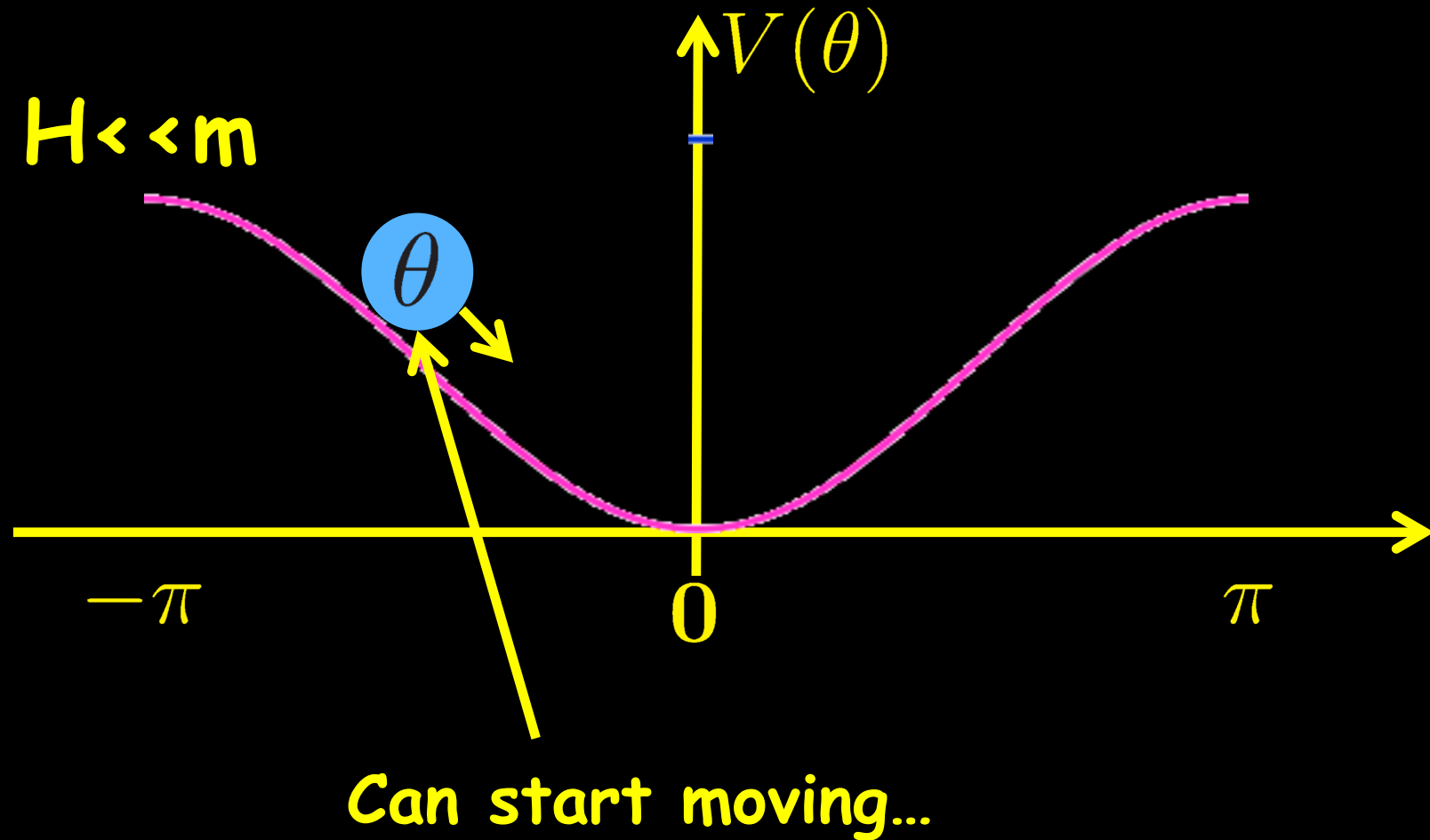
SuperCold Dark Matter

The axion has no clue where to start

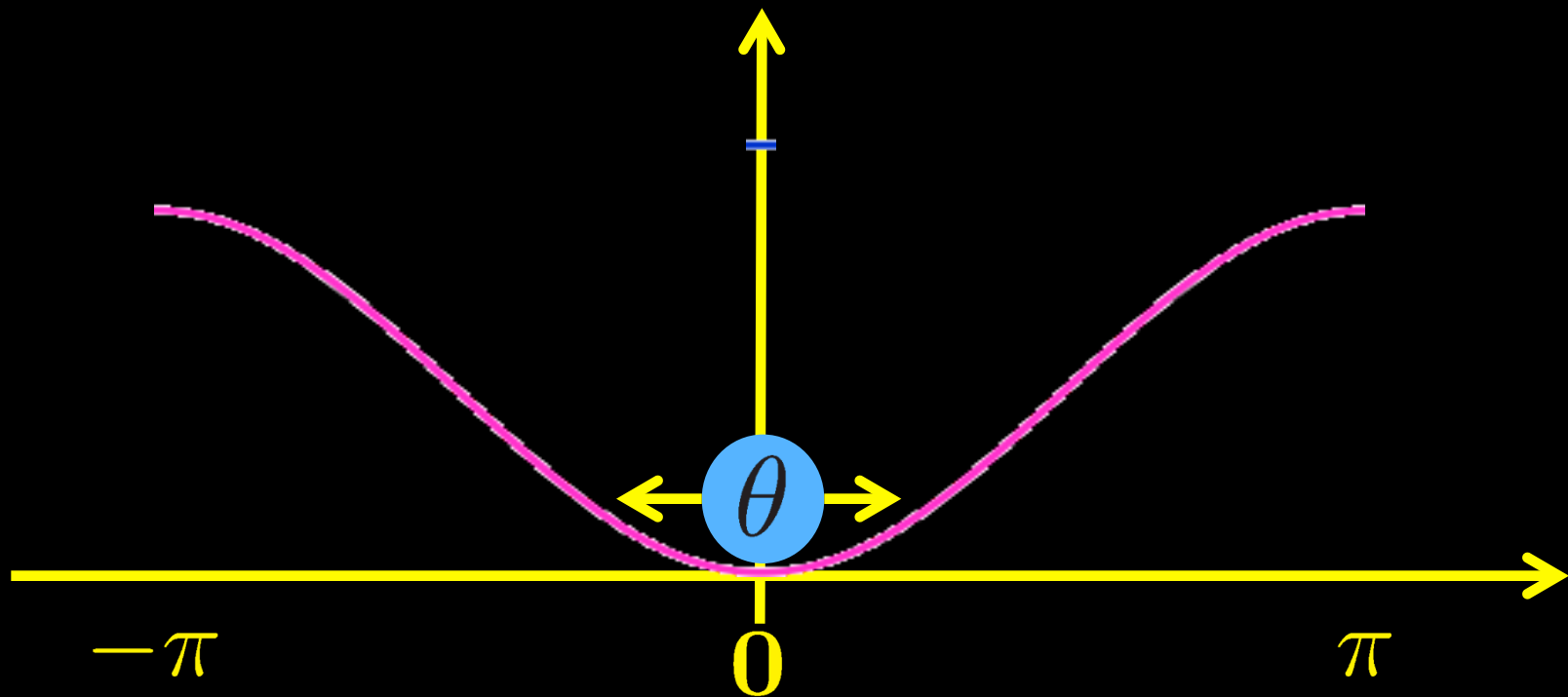


Field is stuck because of Hubble "breaking"

The axion has no clue where to start



The axion solution to the strong CP problem



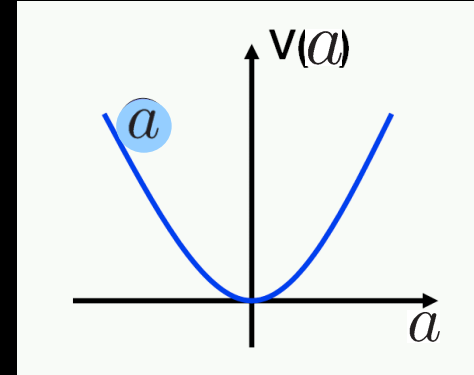
- Oscillations contain energy
- behave like non-relativistic particles ($T=0$)

Axion Dark Matter

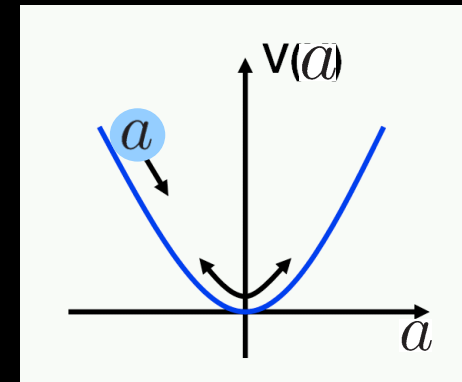
$$\ddot{a} + 3H\dot{a} + m_a^2 a = 0$$

$$H = \frac{\dot{R}(t)}{R(t)}$$

• $H \gg m_a \rightarrow$ overdamped oscillator



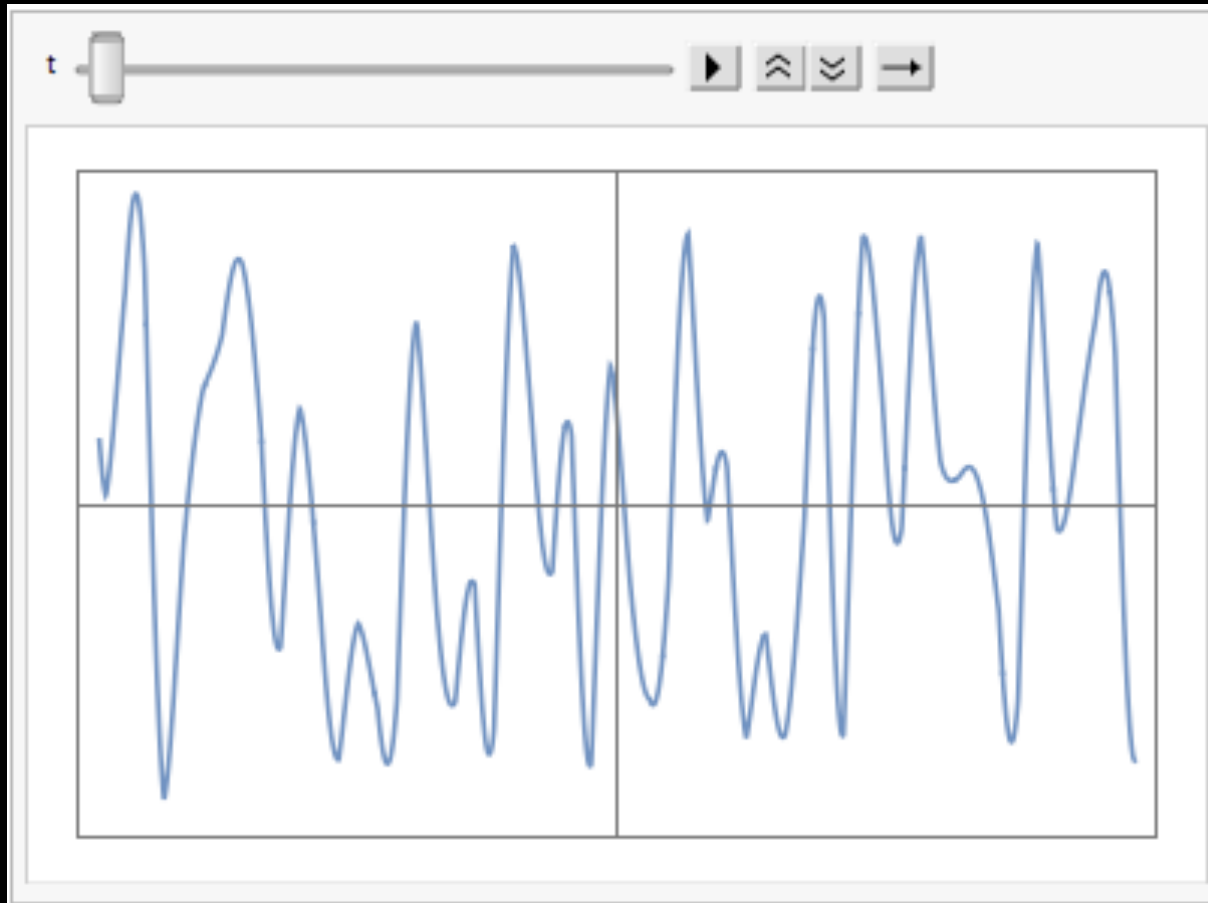
• $H \ll m_a \rightarrow$ damped oscillator



$$\rho_a(t) = \frac{\rho_{ini}}{R^3(t)} \rightarrow \text{Dark Matter}$$

Why Cold? Inflation!

Field
value



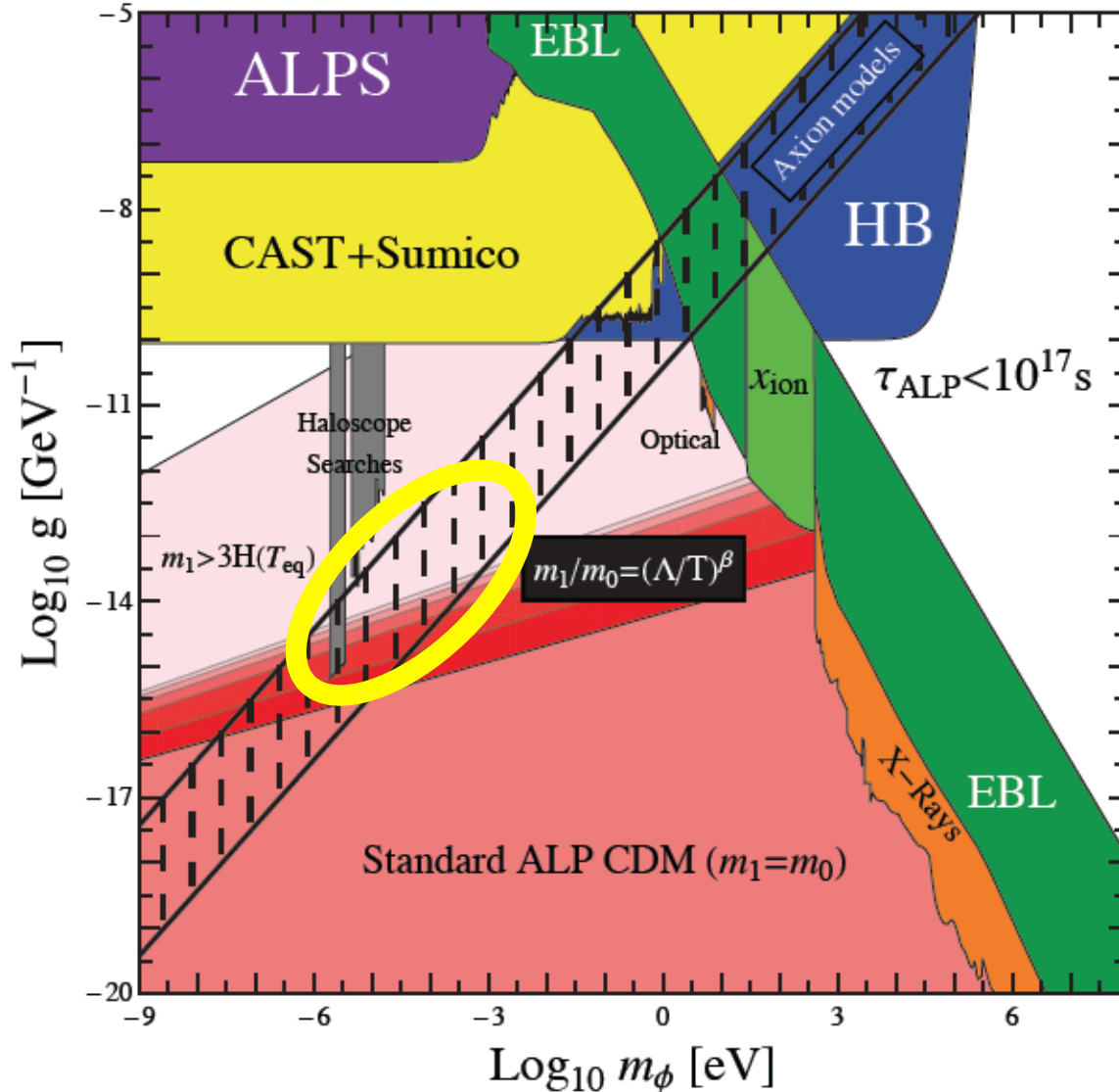
space

$$velocity \sim \frac{p}{m} \sim \frac{\hbar}{m} \frac{d}{dx} \rightarrow 0$$

Axion(-like particle) Dark Matter

$\sim 10^7 \text{ GeV}$

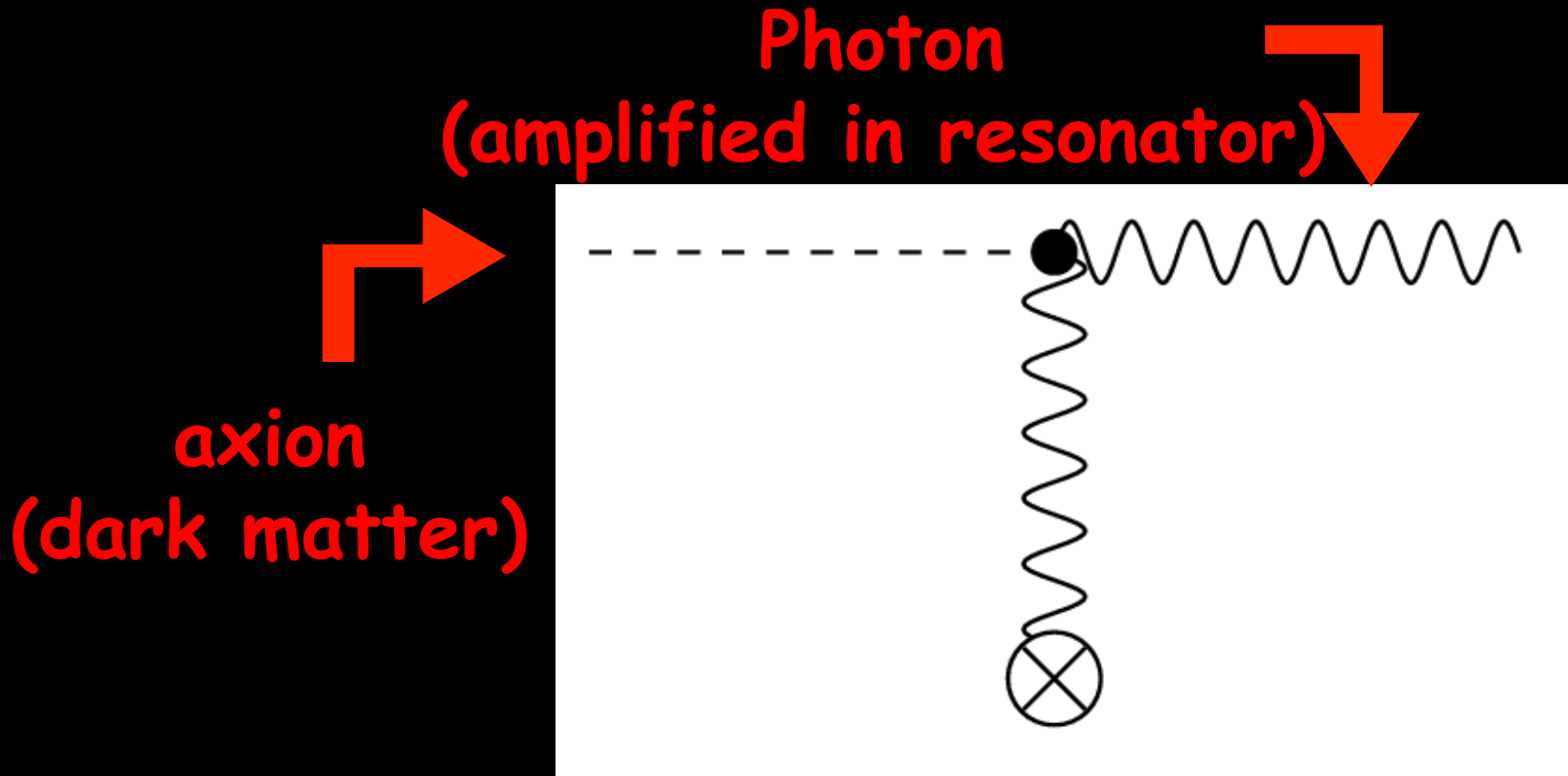
$\sim 10^{12} \text{ GeV}$



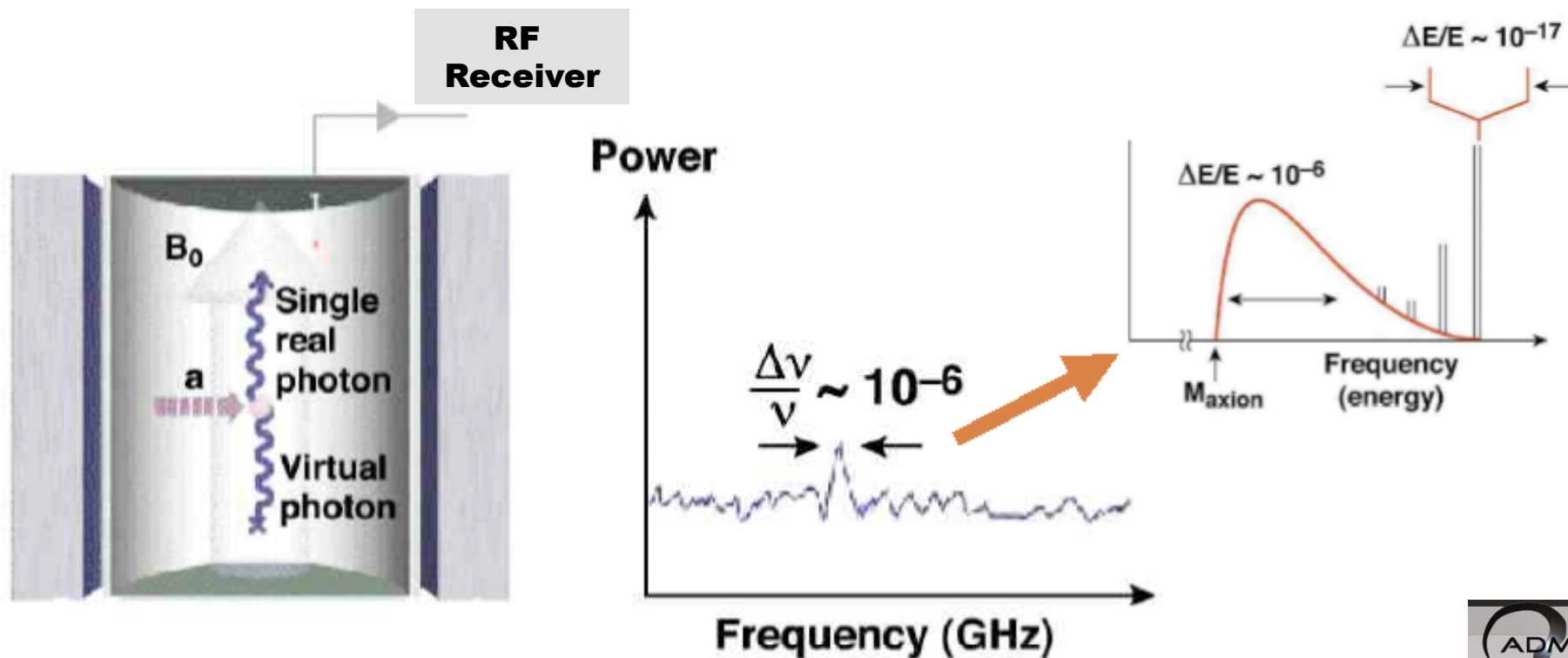
Detecting
Axion/WISPy
DM

Use a plentiful source of axions

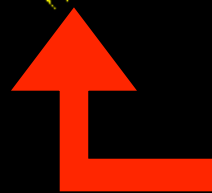
- Photon Regeneration



Signal: Total energy of axion

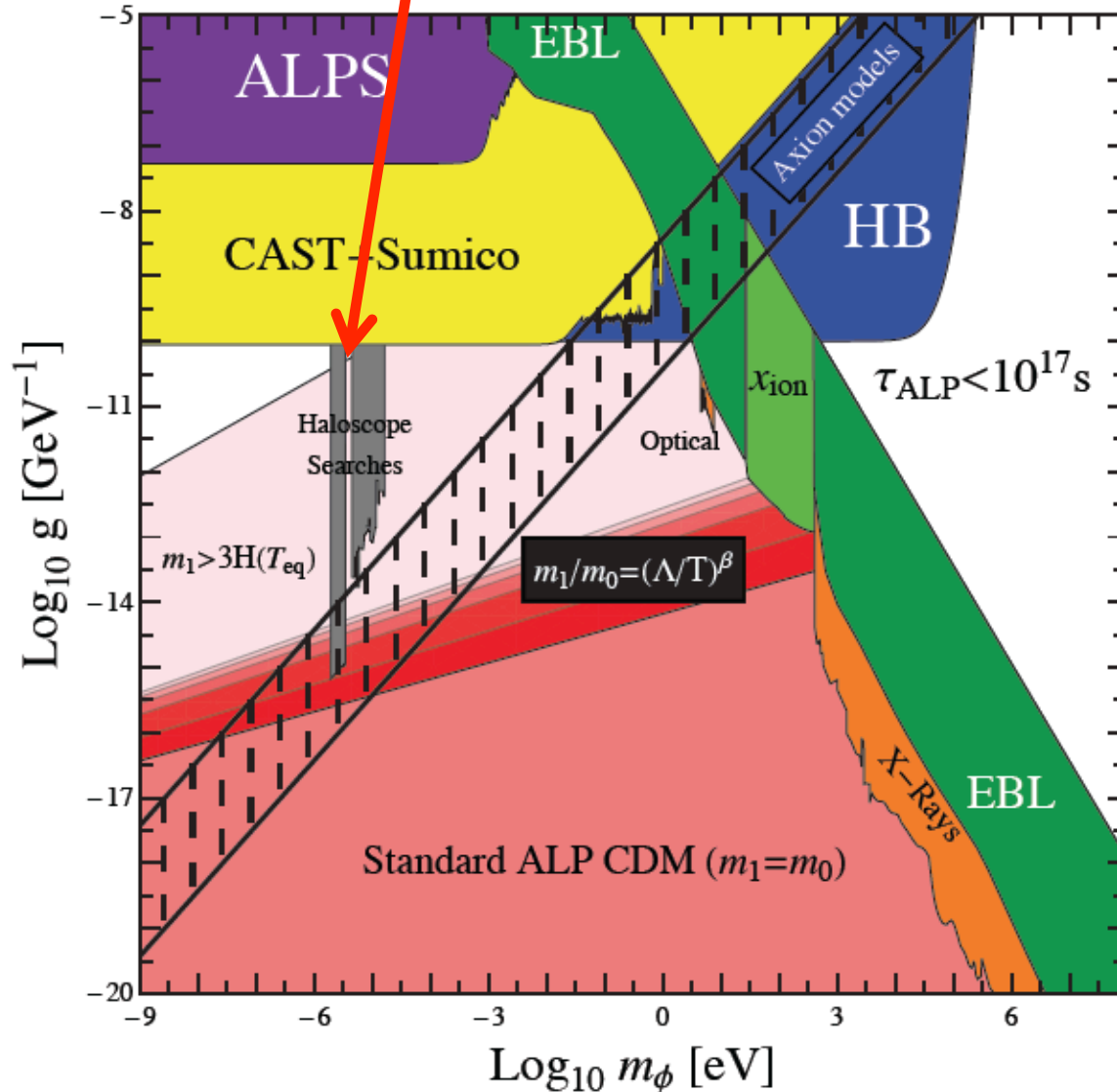


$$h\nu = m_a c^2 [1 + \mathcal{O}(\beta^2 \sim 10^{-6})]$$

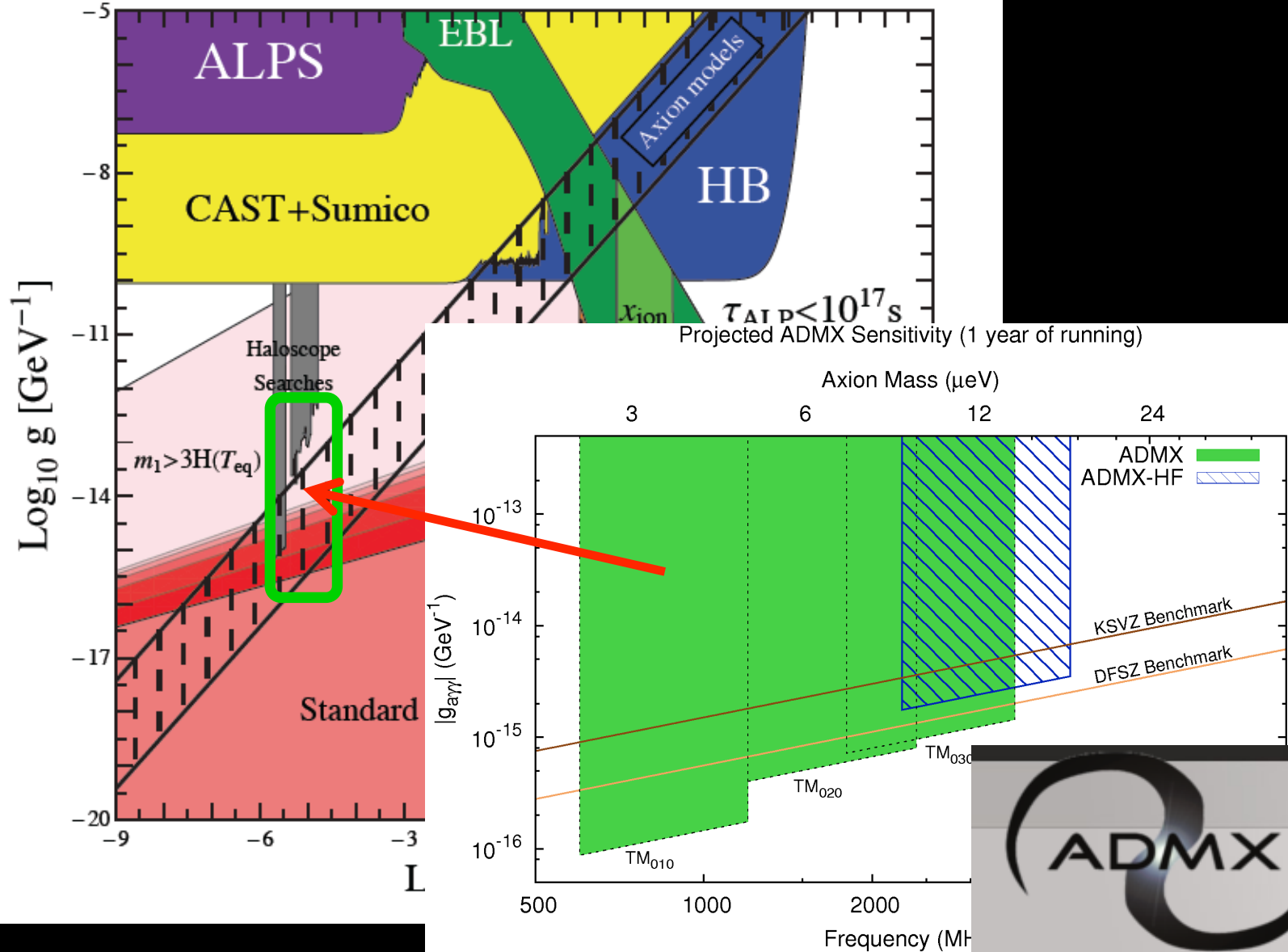


Virial velocity
in galaxy halo!

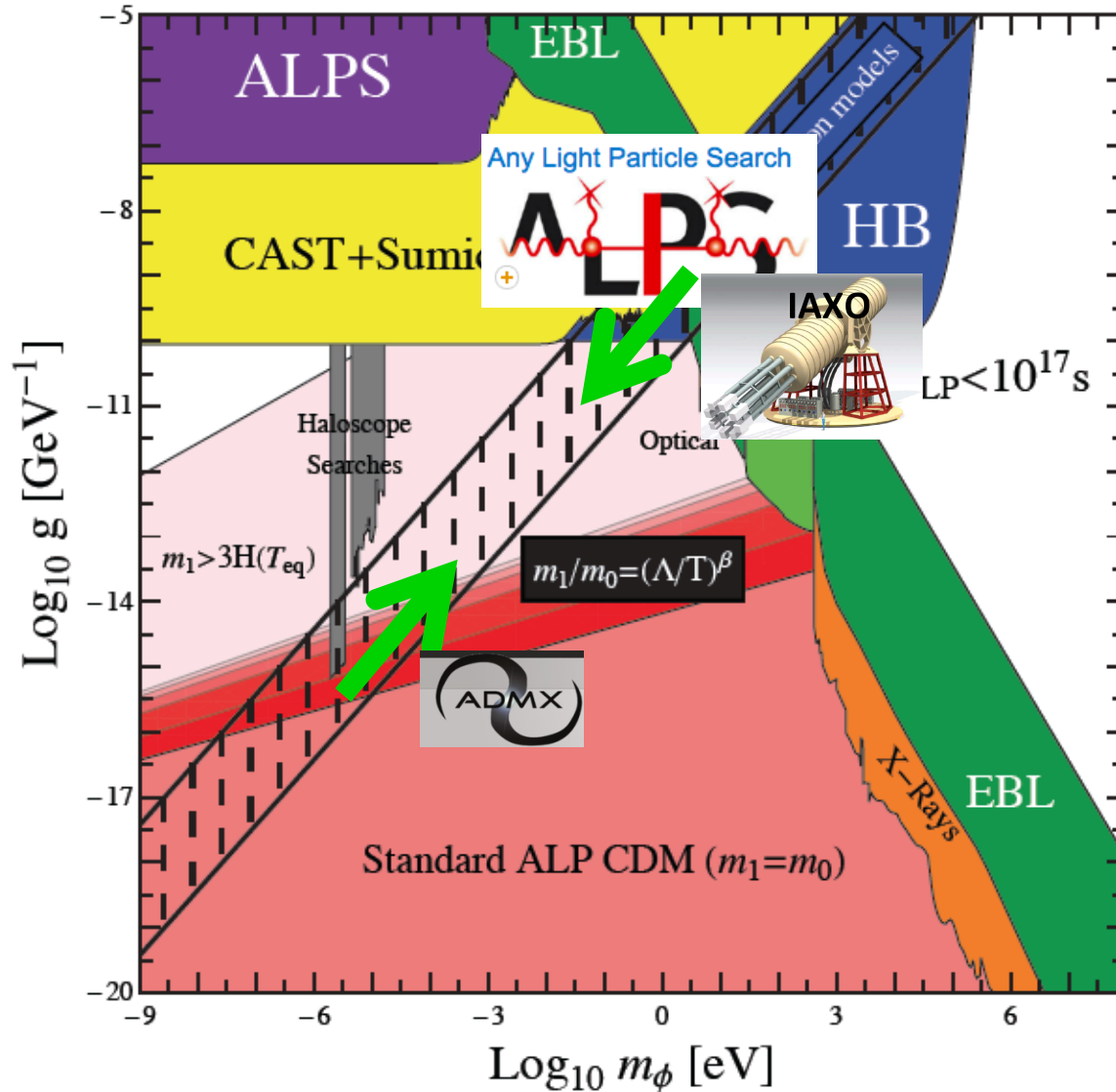
An extremely sensitive probe!!!



A discovery possible any minute!



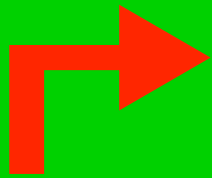
Encircling the axion...



Electricity from Dark Matter ;-).

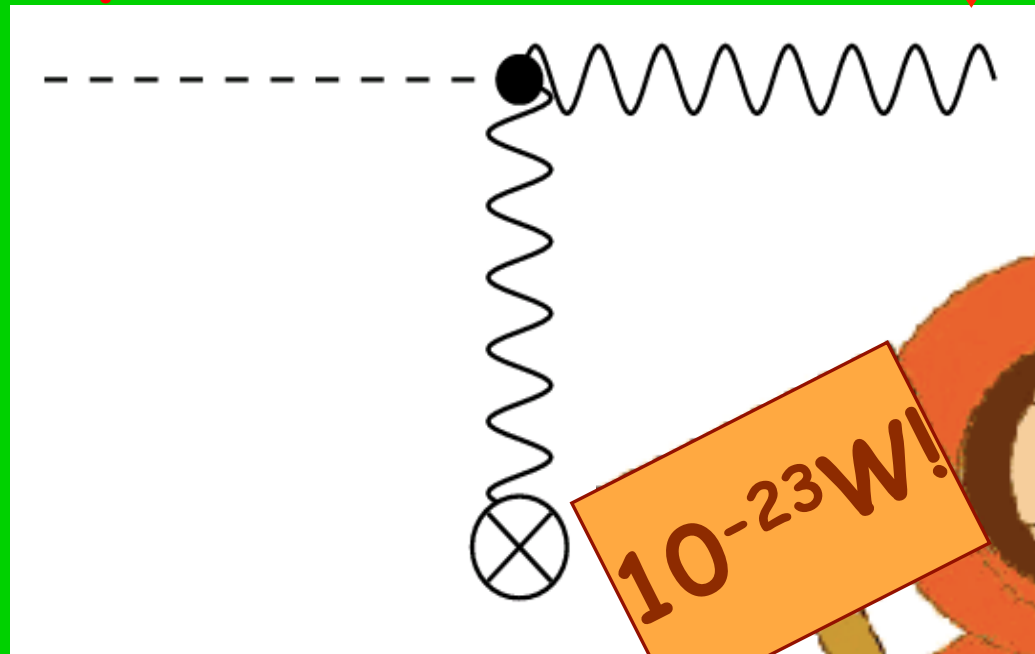
- Photon Regeneration

Photon
(amplified in resonator)



axion

(dark matter)



10^{-23}W!



Really sustainable Energy

- Galaxy contains $(6-30) \times 10^{11}$ solar masses of DM

→ $(3-15) \times 10^{43}$ TWh

@100000 TWh per year (total world today)

→ 10^{38} years ☺

DM power

$$\rho * v \sim 300 \text{ MeV/cm}^3 * 300 \text{ km/s} \sim 10 \text{ W/m}^2$$

compared to 2 W/m^2 for wind

**Dark
Matter**

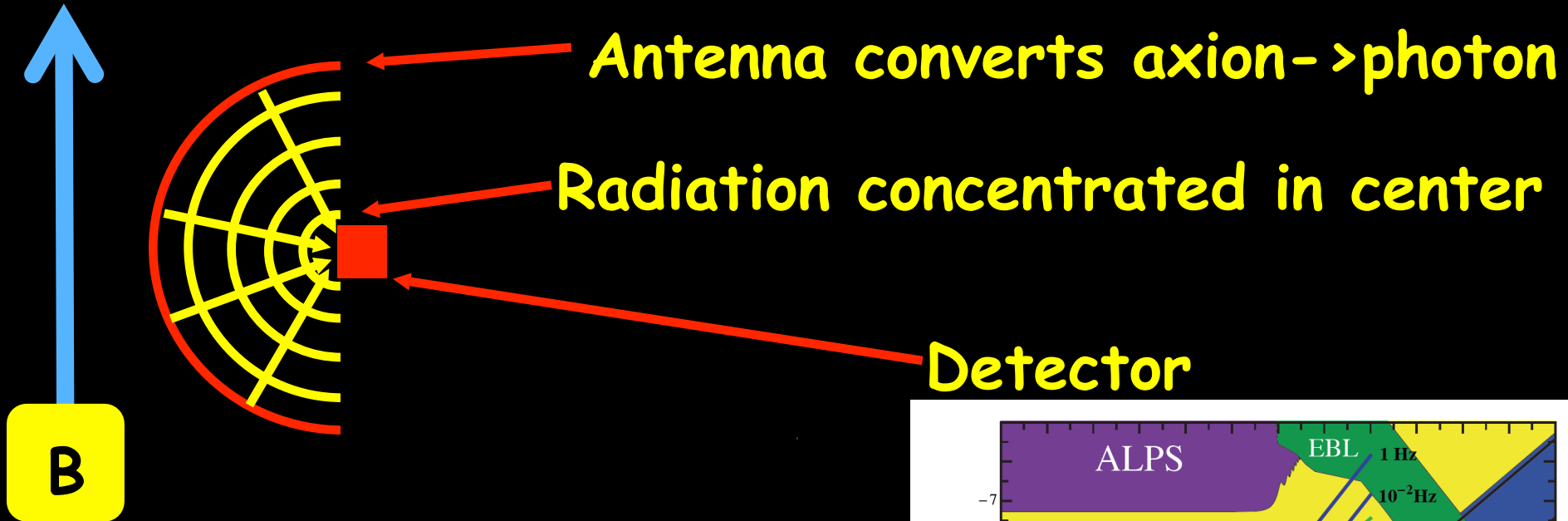


**Dark
Matter**

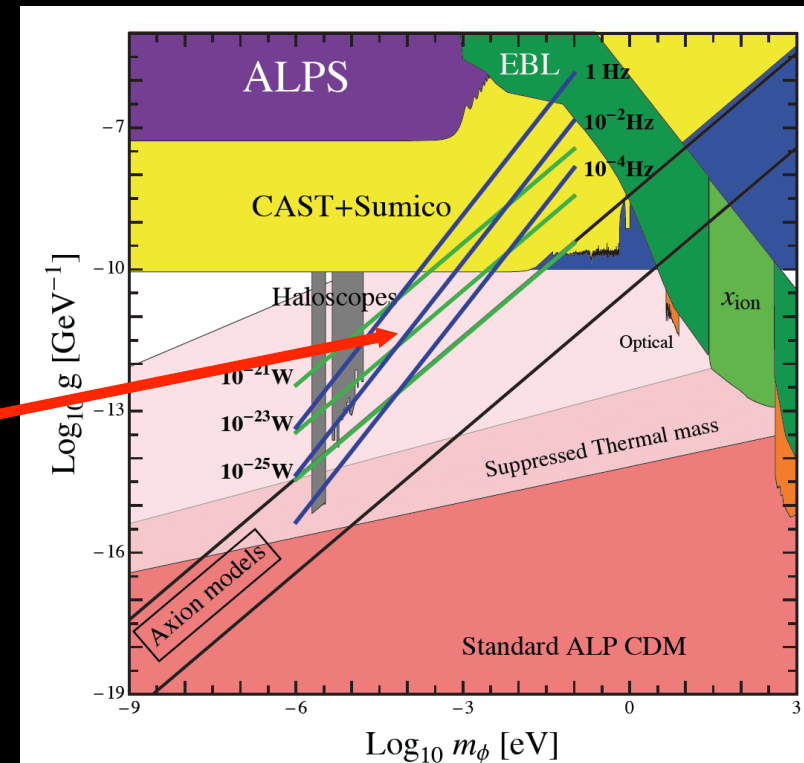


Broadband Search Strategy

Dark Matter Antenna



Probes here;
very sensitive!!



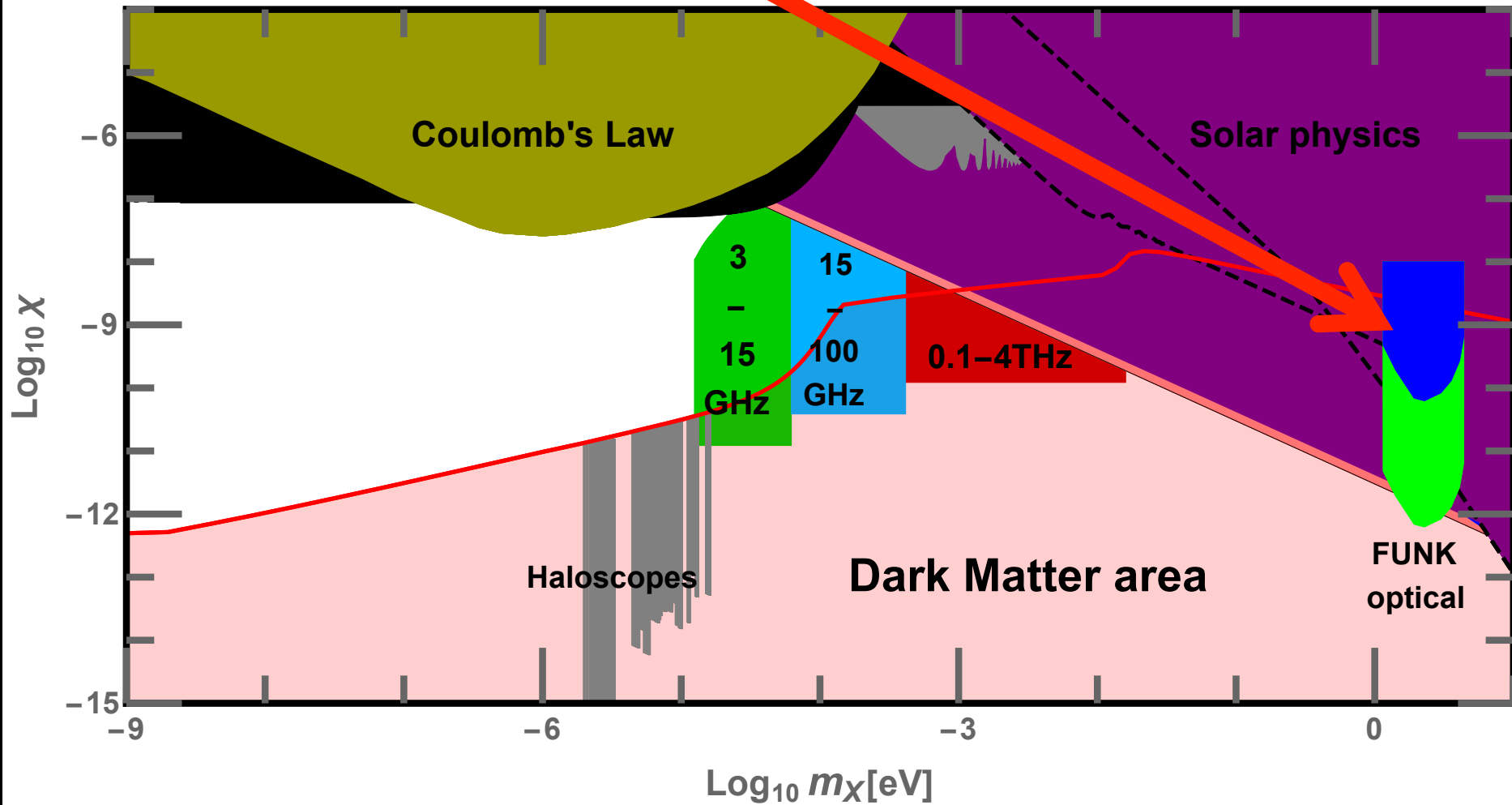
The FUNK Experiment

Recycle Auger mirror

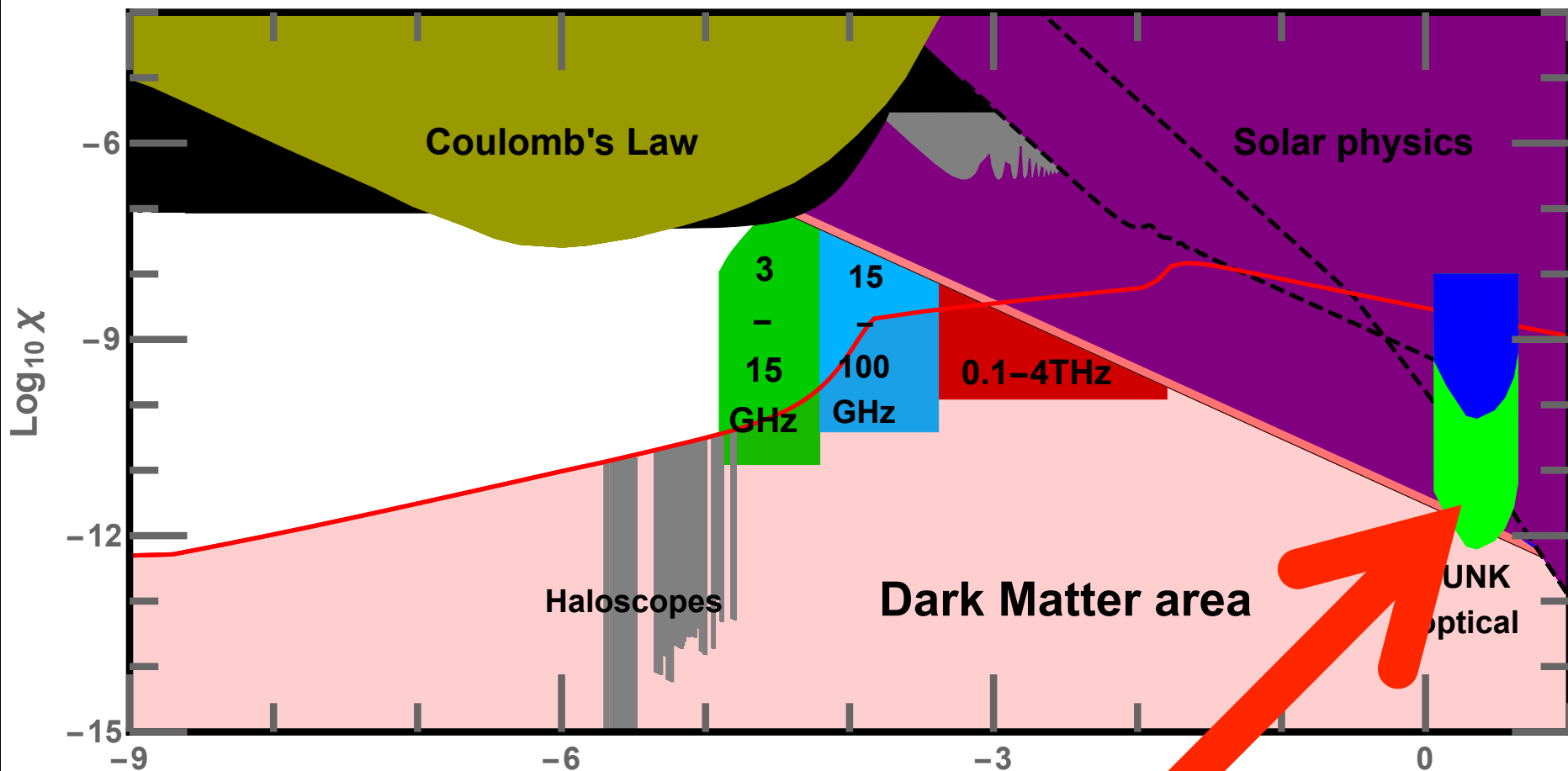
Detector



First Results

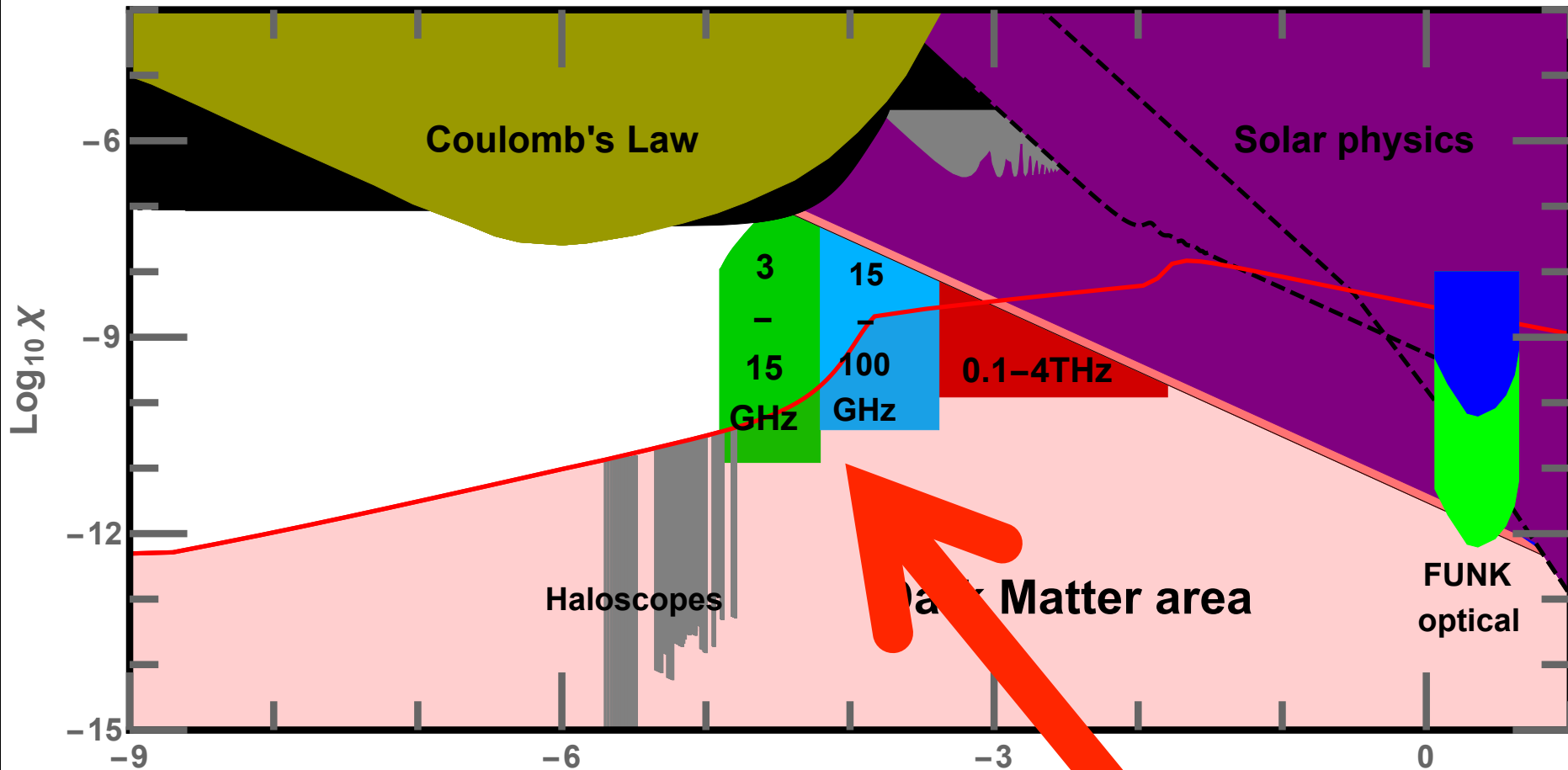


Upgrade: The PMT 9000(+107)



Discovery Potential 😊!!!

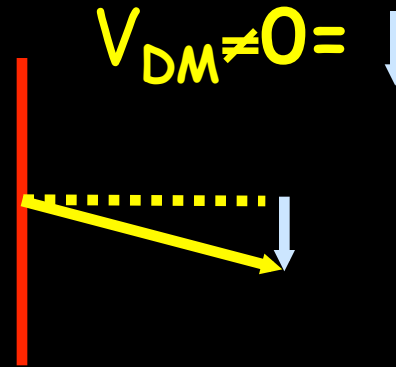
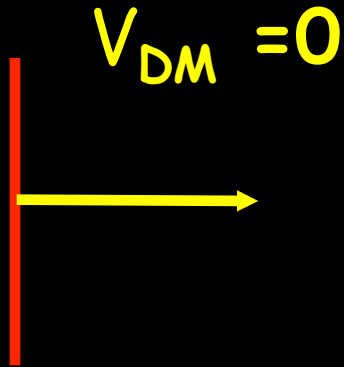
The next years → Lower frequency



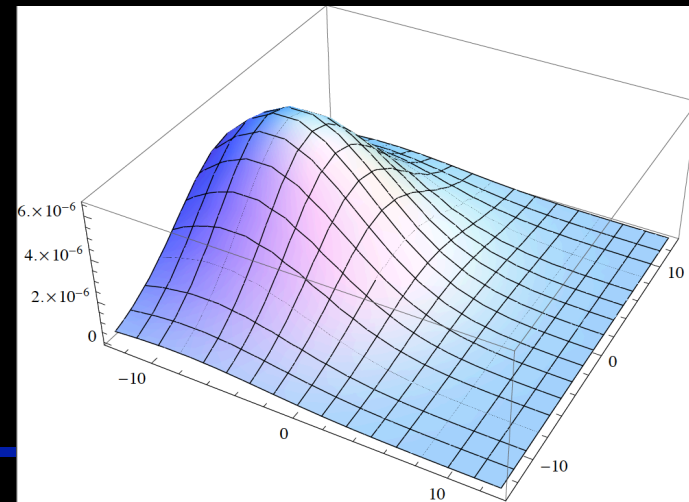
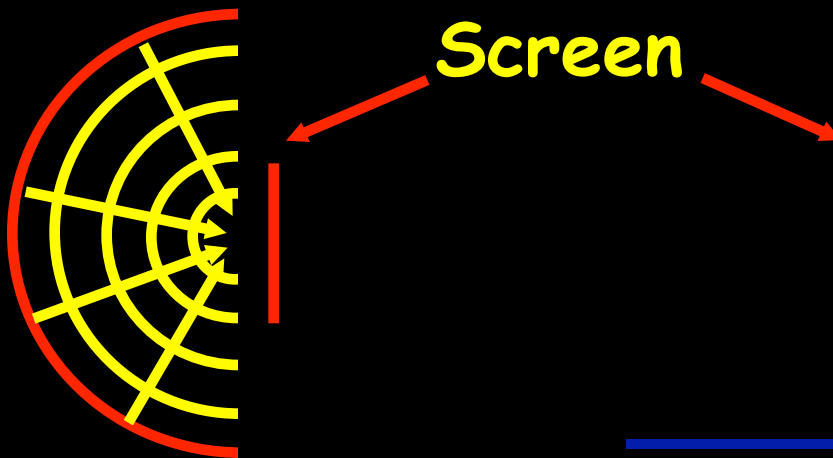
Discovery Potential 😊!!!

A Dream for Astrology ehm Astronomy

- Emission from moving dark matter

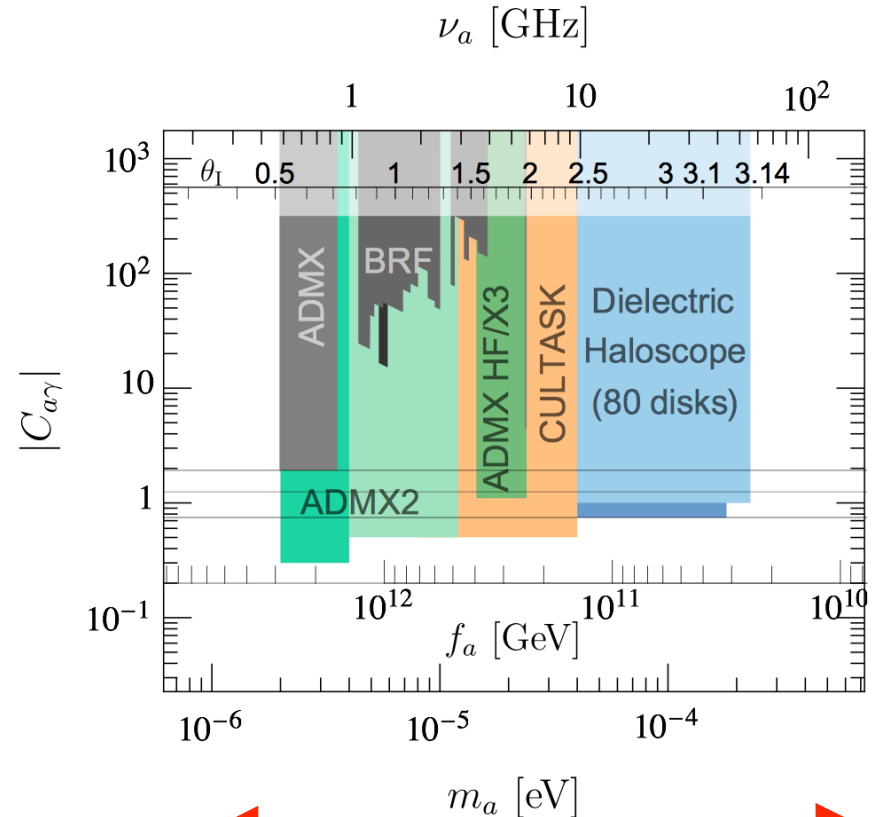
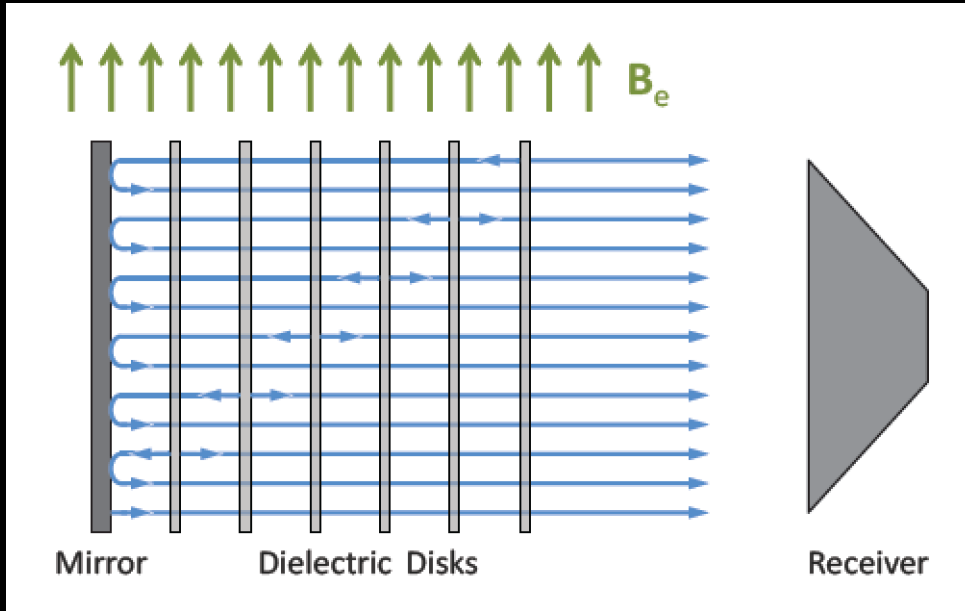


- A picture of the DM-velocity distribution



Going Mad(Max)

Ambitious new project at MPP



Dielectric Haloscopes: A New Way to Detect Axion Dark Matter

The MADMAX Working Group: Allen Caldwell, Gia Dvali, Bela Majorovits, Alexander Millar, Georg Raffelt, Javier Redondo, Olaf Reimann, Frank Simon, Frank Steffen

Natural DM

Many more experiments...

- Abracadabra
 - Alps
 - Ariadne
 - Casper
 - Cultask
 - EDM ring
 - Haystac
 - Iaxo
 - Organ
 - Sensei
 - Quax
 - ...
-

Conclusions

Conclusions

- Good Physics Case for Axions and WISPs
➡ explore 'The Low Energy Frontier'
- Low energy experiments test energy scales much higher than accelerators
➡ Complementary!
- May provide information on hidden sectors and thereby into the underlying fundamental theory
- Dark Matter may be WISPy 😊
➡ New cool Experiments underway.

