

QCD

Taller de Altas Energías - TAE 2019

Germán Rodrigo

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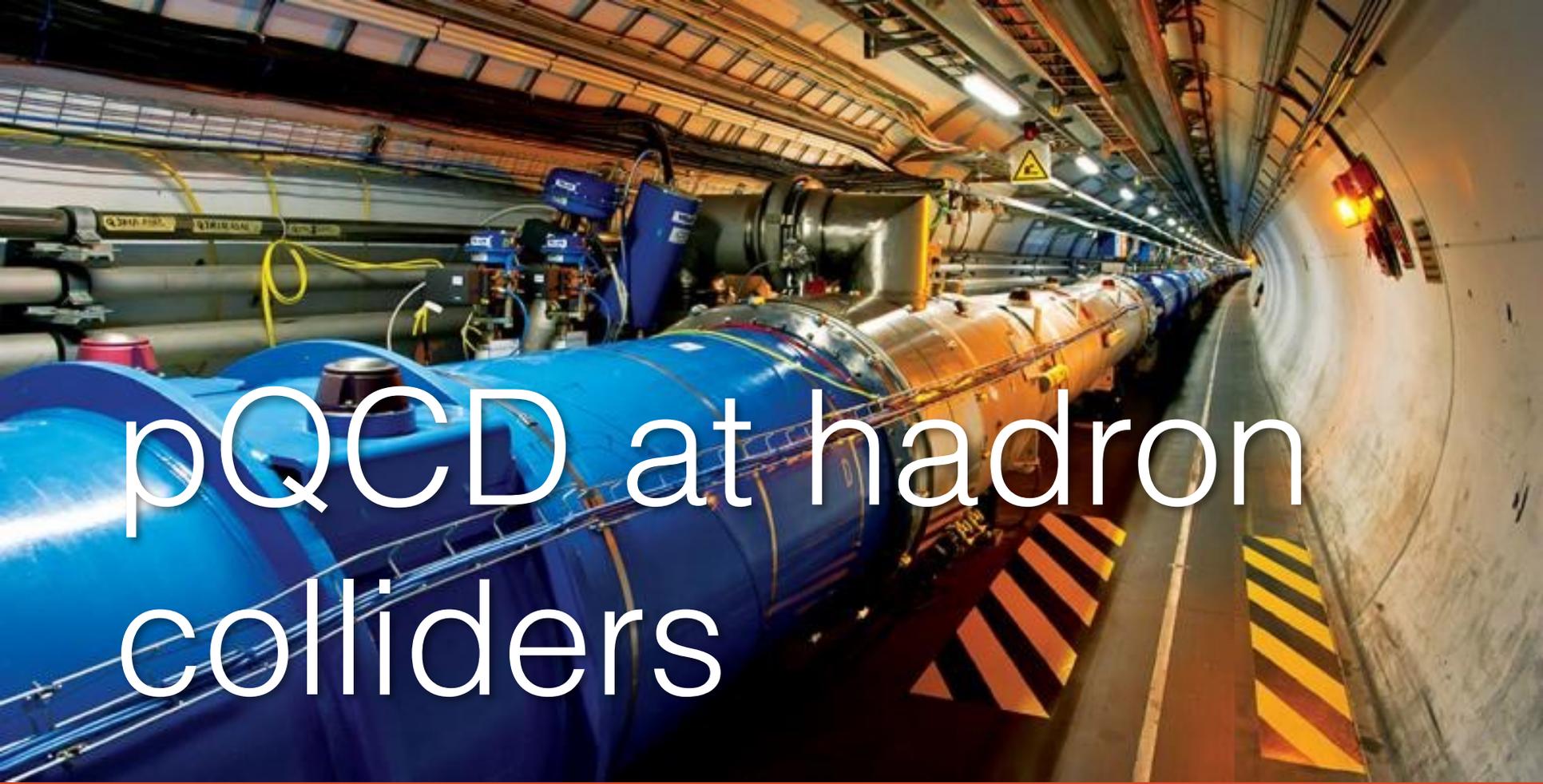
CSIC

VNIVERSITAT
ID VALÈNCIA



Lecture 3: pQCD at hadron colliders





pQCD at hadron colliders

THE THEORY OF ALMOST EVERYTHING

The Standard Model,
the Unsung Triumph of Modern Physics

ROBERT OERTER

- ▶ SM based in the simplest gauge symmetries: **$SU(3) \times SU(2) \times U(1)$**
- ▶ Also the **flavour sector very symmetric (GIM)**
- ▶ The **“natural”** theory at **“low” energies** (below the TeVs)
- ▶ We should expect that it will break at high energies: **departure scale undetermined | no theory guidance**

NO CLEAR BSM SIGNAL AT THE LHC SO FAR

WHERE TO EXPECT A BSM SIGNAL?

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- ▶ LHC results suggest that **new physics** will appear as a **gentle deviation** from the SM predictions / **rare events** suppressed in the SM

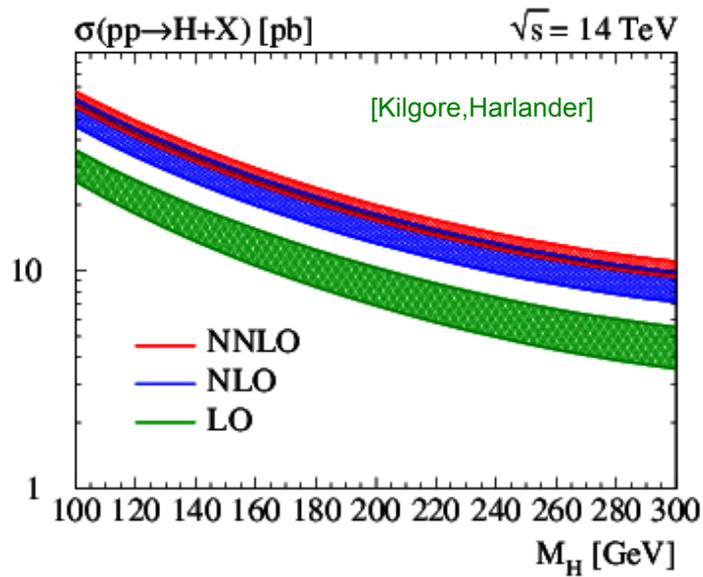
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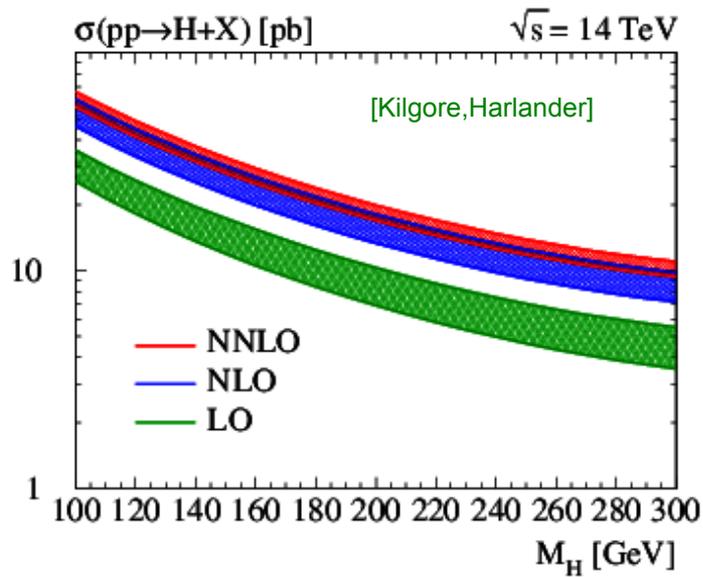
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- ▶ Very unlikely to be visible in inclusive observables or total decay rates of known particles: the bulk of the contributions at “low energies”, the characteristic hard scale is “**low energy**”
- ▶ Higher chances at the **tail** of differential distributions (not necessarily a clear bump) “**high energy**” characteristic hard scale: more sensitive to **quantum corrections** / missing quantum corrections can fake BSM

Perturbative view at hadron-hadron colliders



higher orders improve systematically the precision of the theoretical predictions (estimated by **varying the renormalization / factorization scales**) for background and signal. Uncertainty bands are **expected to narrow and overlap** from one order to the next one

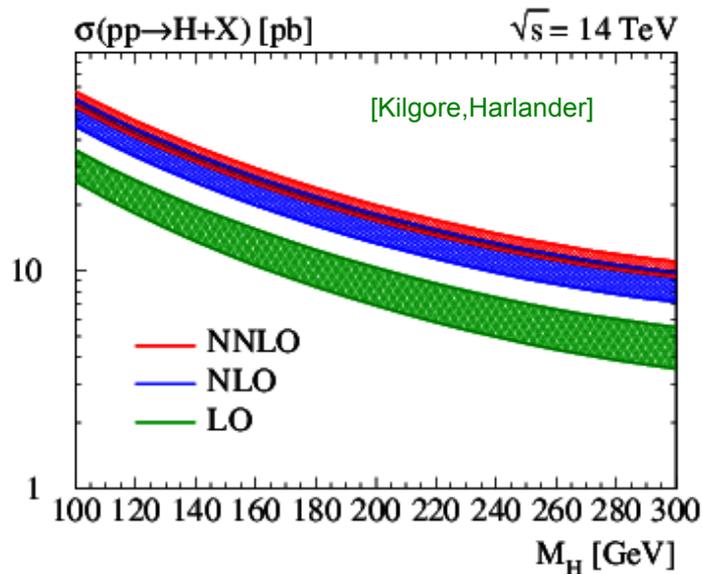
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- LO: fails to describe normalization (up to a factor 2). Monte Carlo event generators (LO + parton showers) : improves the shape of distributions, but normalization still underestimated

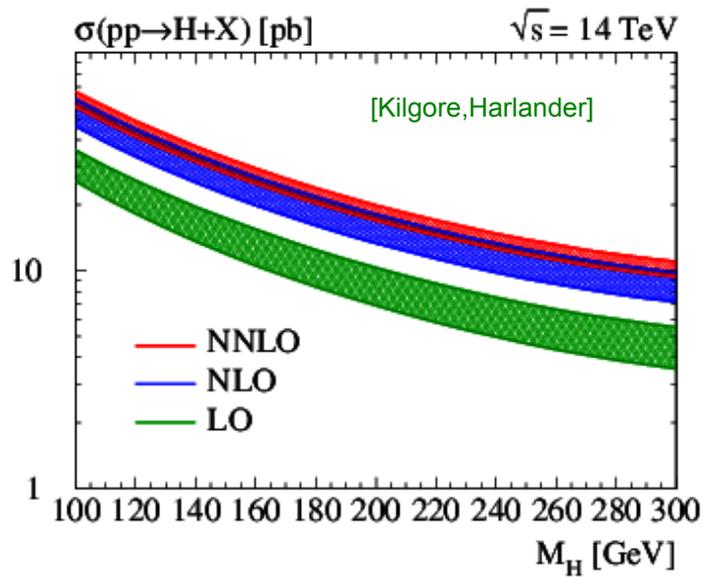
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- NLO: first reliable estimate of **central value**

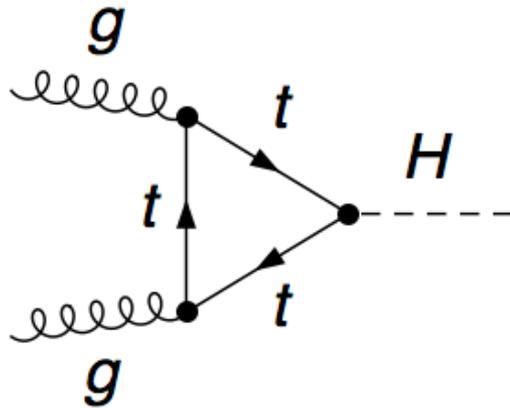
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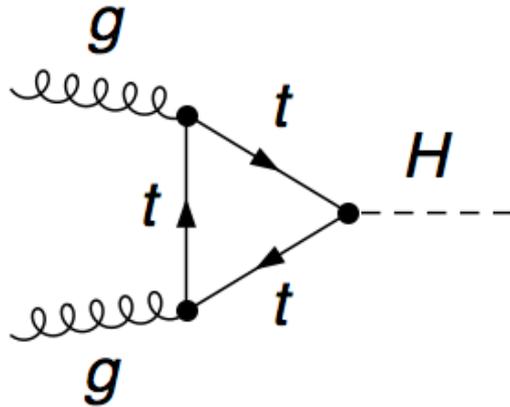
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- NLO: first reliable estimate of **central value**
- NNLO: first **serious estimate** of the theoretical uncertainty

New channels open from LO to NLO

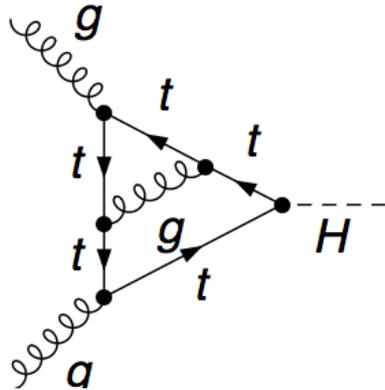


Higgs boson production is
one loop at **LO**

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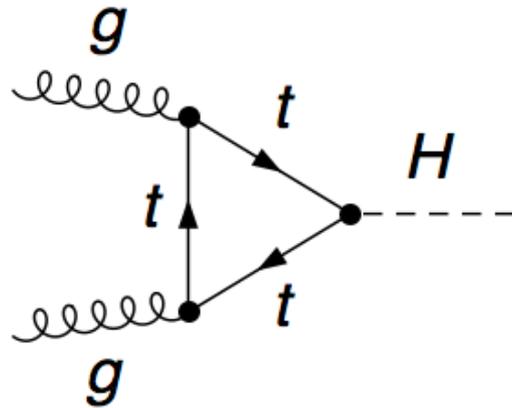


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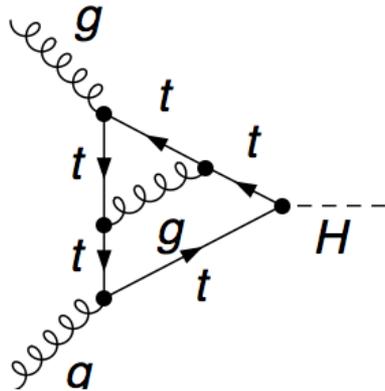


QCD correction to the **LO**

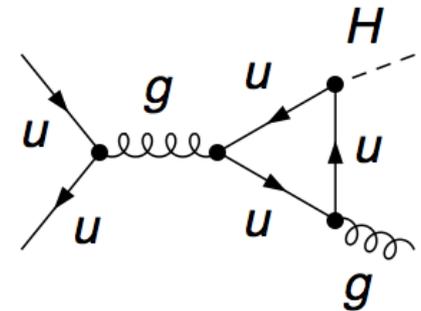
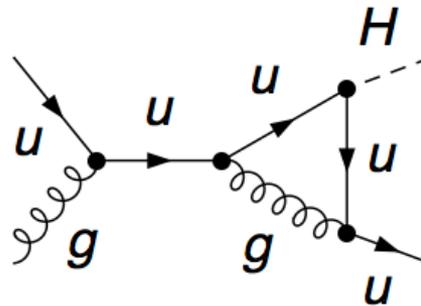
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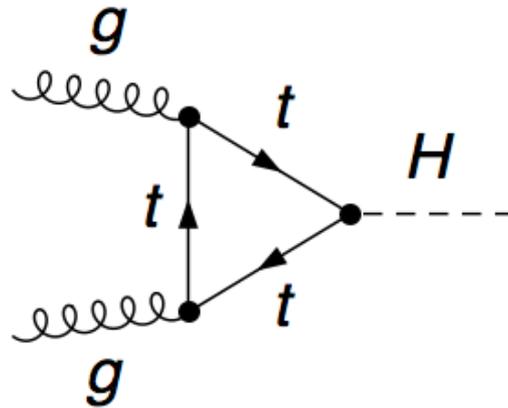


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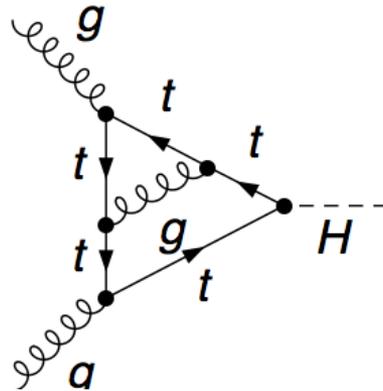


New channels at **NLO**
 $qg(\bar{q}g)$ and $q\bar{q}$

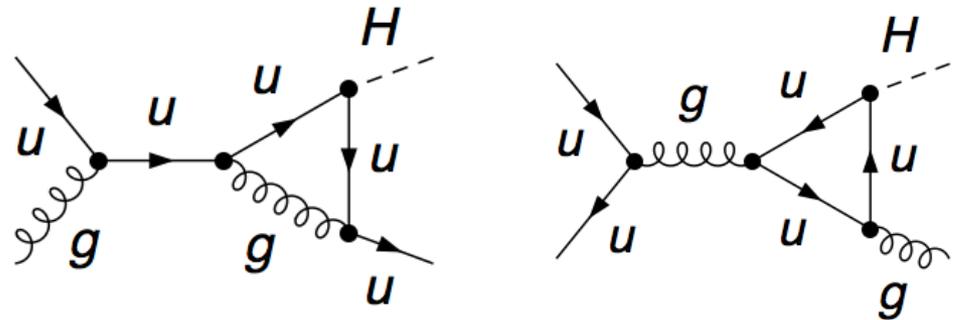
New channels open from LO to NLO



Higgs boson production is one loop at **LO**



QCD correction to the **LO**



New channels at **NLO**
 $qg(\bar{q}g)$ and $q\bar{q}$

Only **NNLO** is a correction to all the channels that appear at the NLO

STUNNING PROGRESS IN THEORETICAL CALCULATIONS IN THE PAST YEARS

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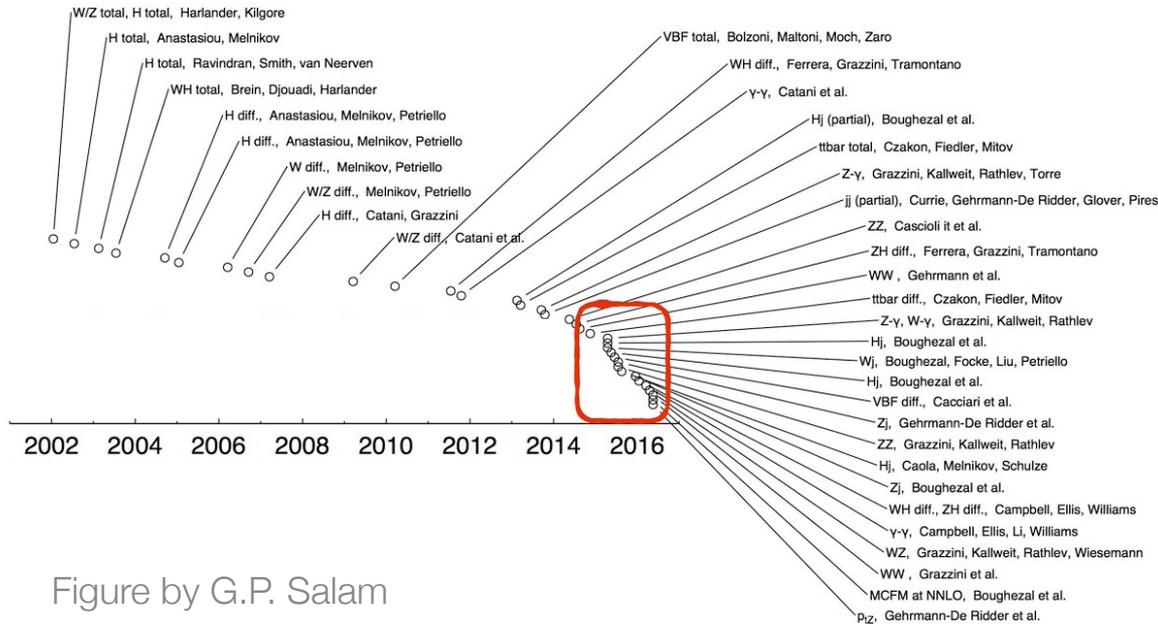
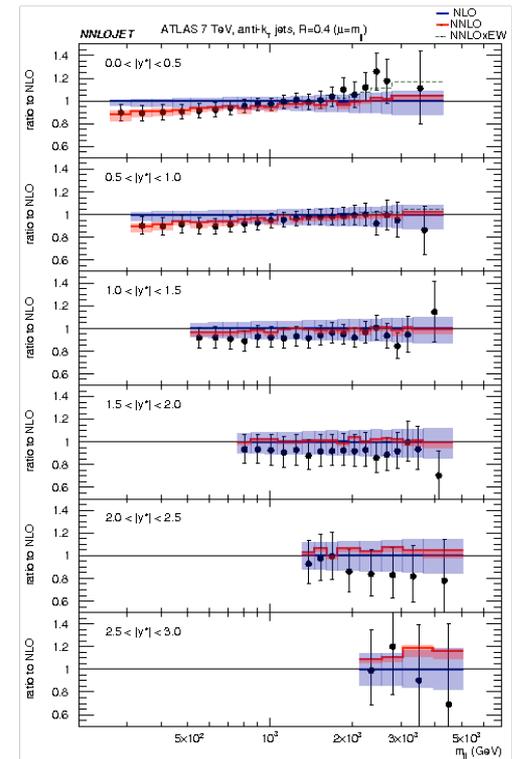
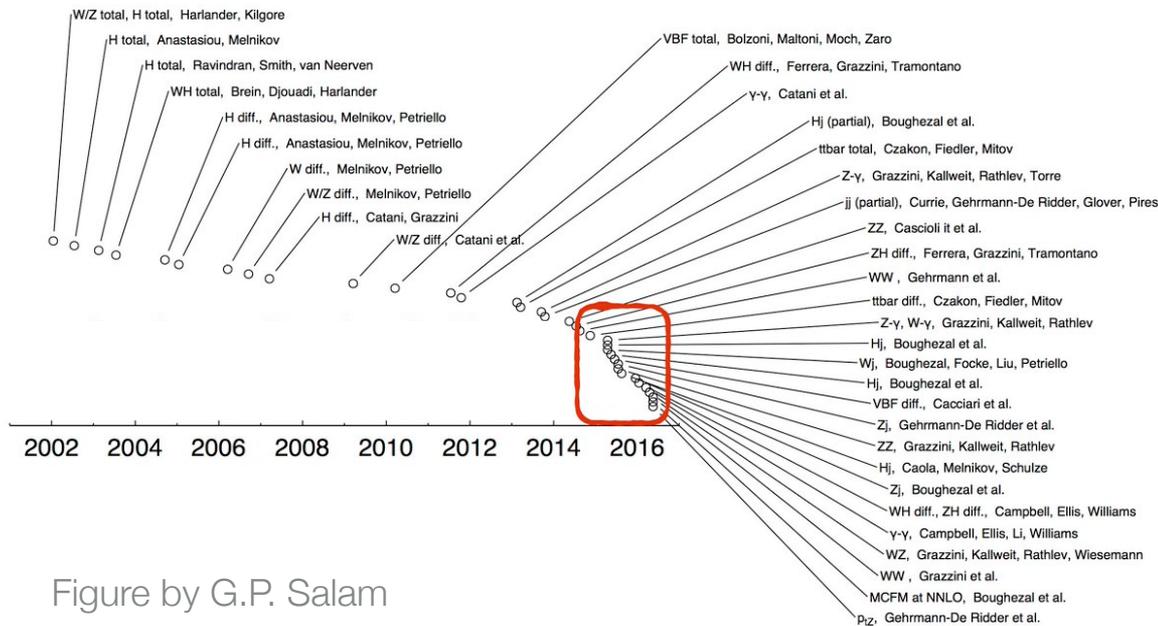


Figure by G.P. Salam

STUNNING PROGRESS IN THEORETICAL CALCULATIONS IN THE PAST YEARS

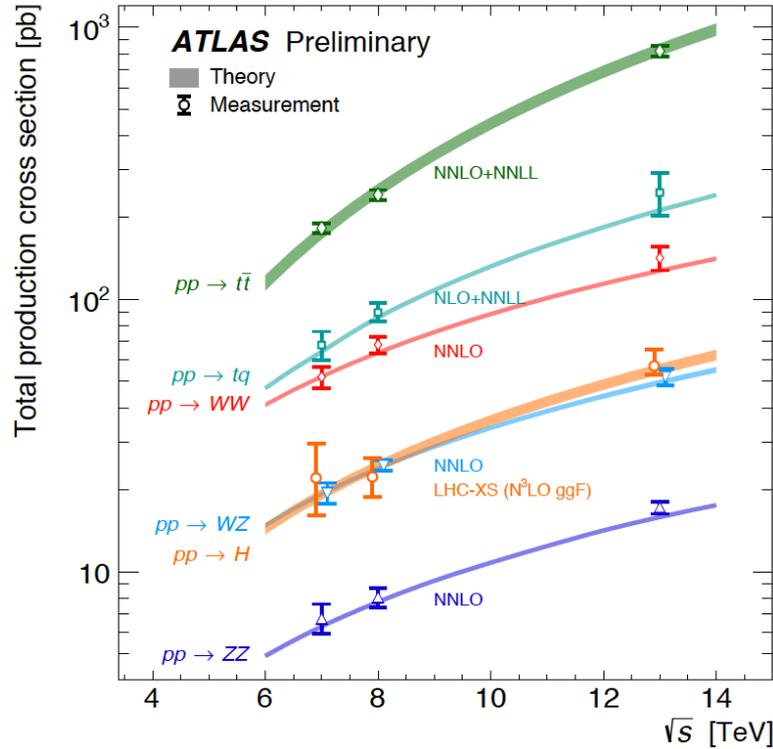
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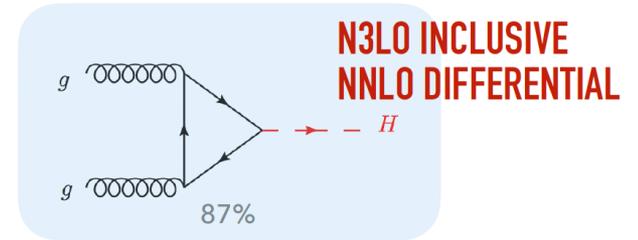
e.g. dijet production
data prefer NNLO

STUNNING PROGRESS IN THEORETICAL CALCULATIONS IN THE PAST YEARS

- ▶ **N3LO ggH (2→1): 5% th+3% (PDF- α_S)** [Anastasiou et al., 2016]



- $pp \rightarrow t\bar{t}$
7 TeV, 4.6 fb⁻¹, Eur. Phys. J. C 74:3109 (2014)
8 TeV, 20.3 fb⁻¹, Eur. Phys. J. C 74:3109 (2014)
13 TeV, 3.2 fb⁻¹, arXiv:1606.02699
- $pp \rightarrow tq$
7 TeV, 4.6 fb⁻¹, PRD 90, 112006 (2014)
8 TeV, 20.3 fb⁻¹, arXiv:1702.02859
13 TeV, 3.2 fb⁻¹, arXiv:1609.03920
- $pp \rightarrow WW$
7 TeV, 4.6 fb⁻¹, PRD 87, 112001 (2013)
8 TeV, 20.3 fb⁻¹, JHEP 09 029 (2016)
13 TeV, 3.2 fb⁻¹, arXiv:1702.04519
- $pp \rightarrow WZ$
7 TeV, 4.6 fb⁻¹, Eur. Phys. J. C (2012) 72:2173
8 TeV, 20.3 fb⁻¹, PRD 93, 092004 (2016)
13 TeV, 3.2 fb⁻¹, Phys. Lett. B 762 (2016)
- $pp \rightarrow H$
7 TeV, 4.5 fb⁻¹, Eur. Phys. J. C76 (2016) 6
8 TeV, 20.3 fb⁻¹, Eur. Phys. J. C76 (2016) 6
13 TeV, 36.1 fb⁻¹, ATLAS-CONF-2017-047
- $pp \rightarrow ZZ$
7 TeV, 4.6 fb⁻¹, JHEP 03, 128 (2013)
8 TeV, 20.3 fb⁻¹, JHEP 01, 099 (2017)
13 TeV, 36.1 fb⁻¹, ATLAS-CONF-2017-031

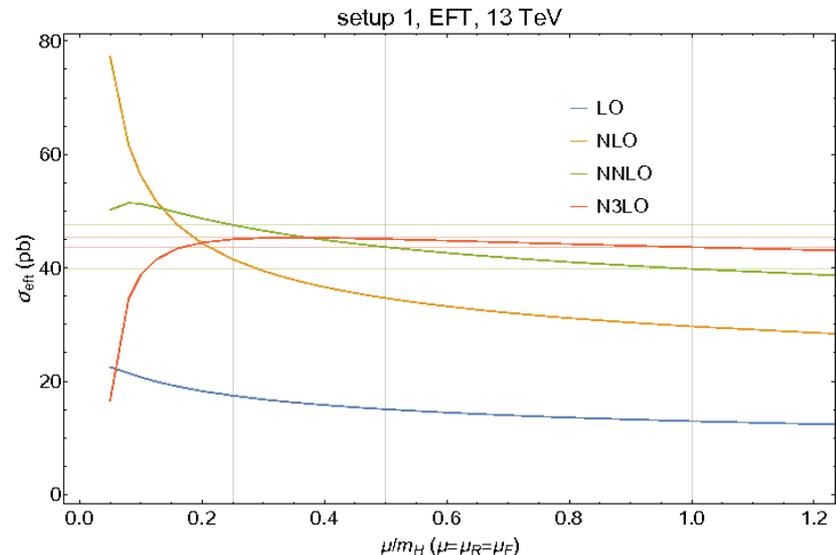


$m_t \rightarrow \infty$

$$\hat{\sigma} = \alpha_s^2 \sigma^{\text{LO}} + \alpha_s^3 \sigma^{\text{NLO}} + \alpha_s^4 \sigma^{\text{NNLO}} + \alpha_s^5 \sigma^{\text{N3LO}}$$

$\alpha_s = 0.1181 \pm 1\%$

[Dulat at PASCOS2018]

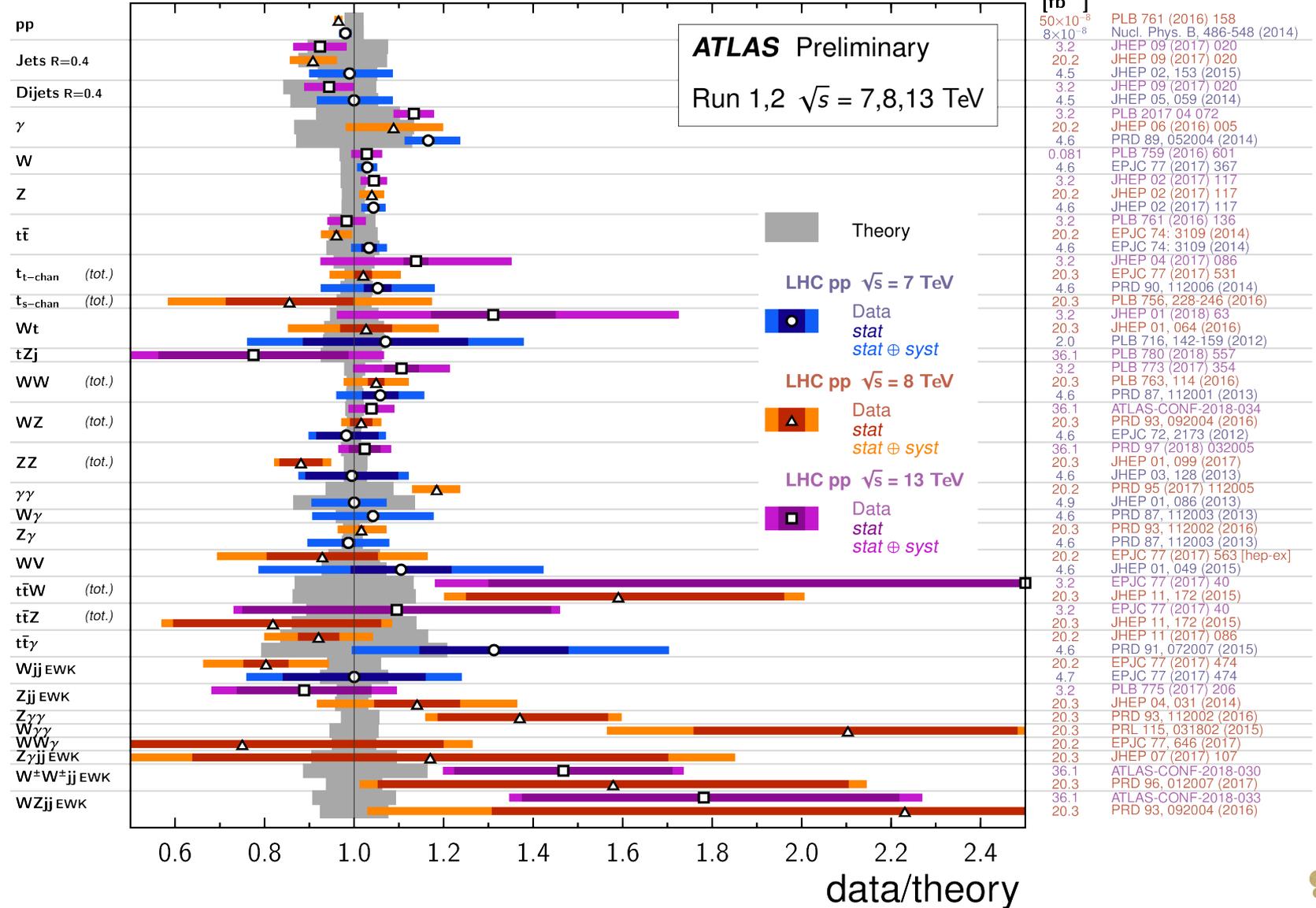


Standard Model Production Cross Section Measurements

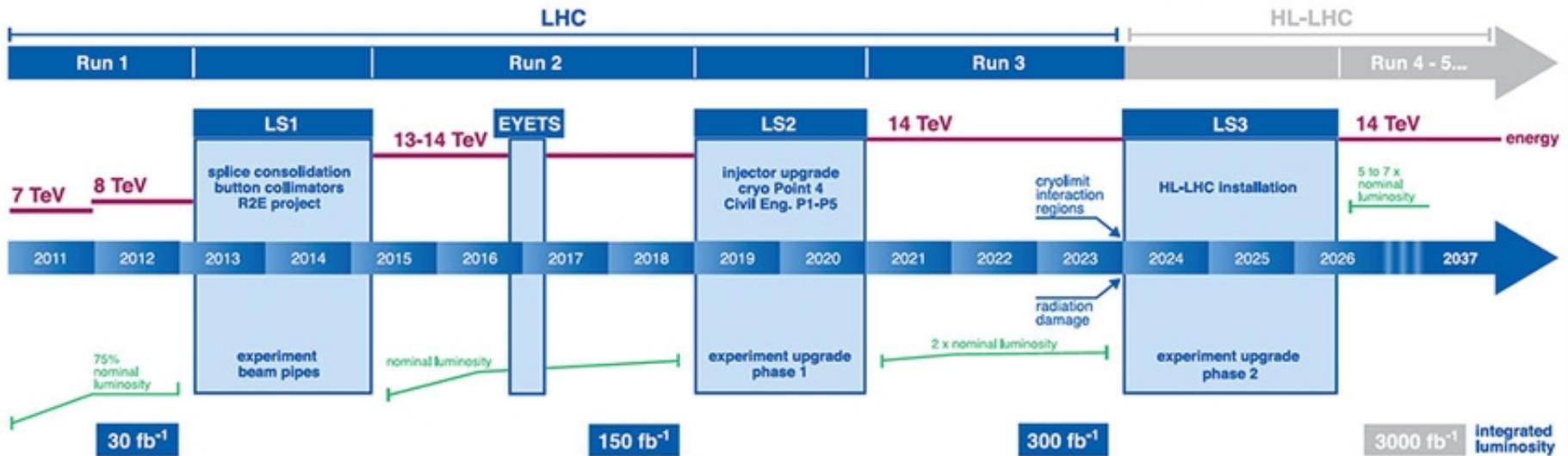
Status:
July 2018

$\int \mathcal{L} dt$
[fb⁻¹]

Reference

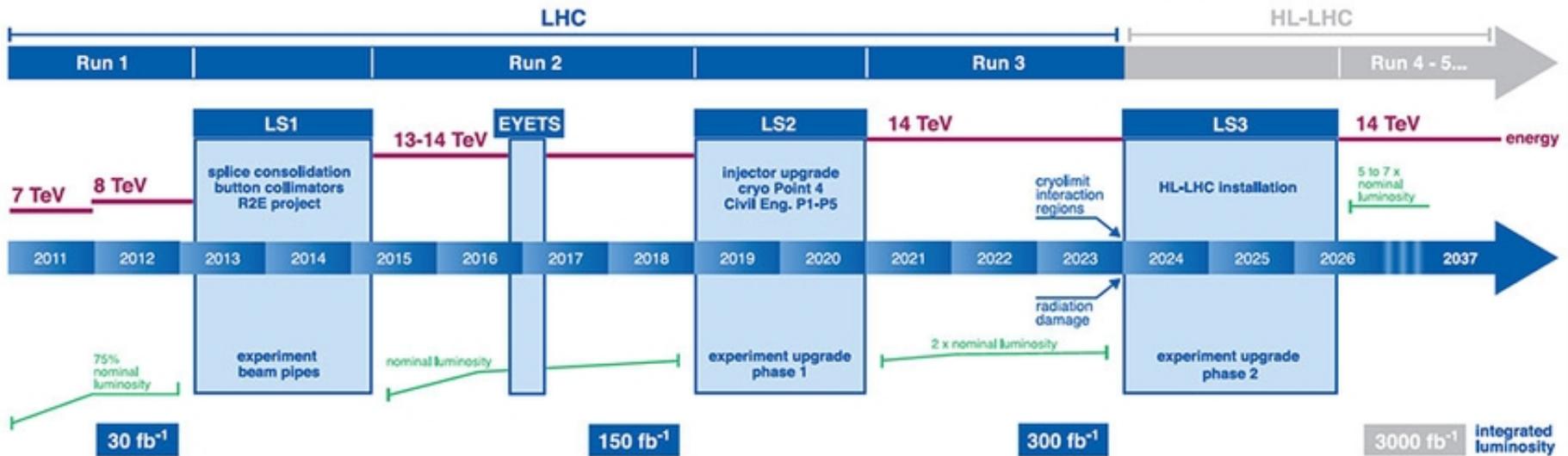


LHC / HL-LHC Plan



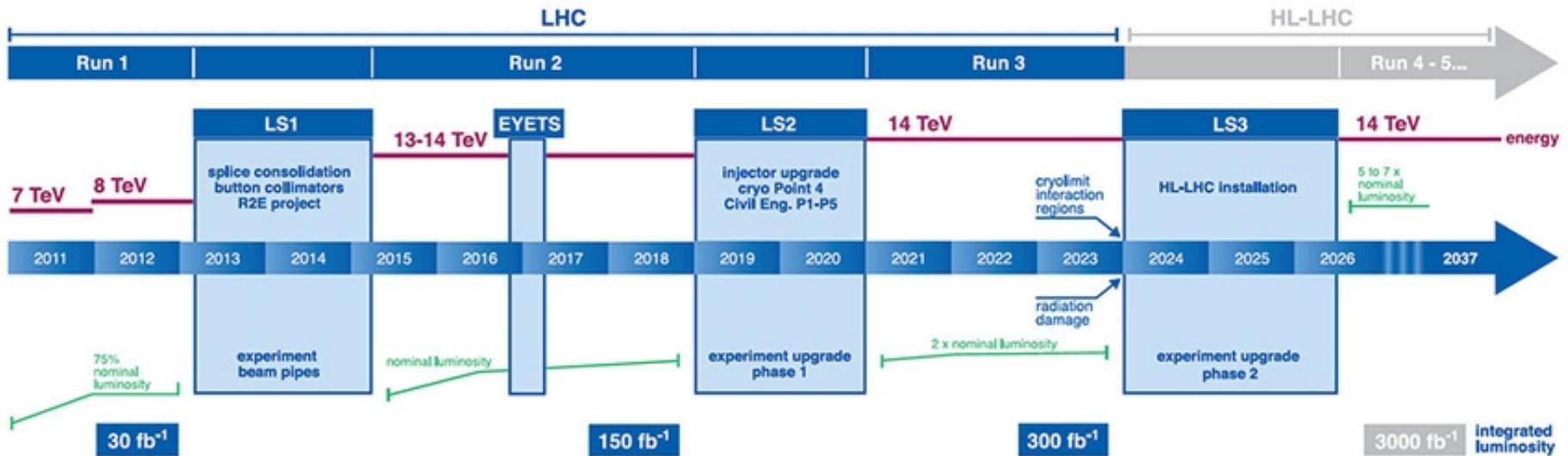
- ▶ 150 fb⁻¹ today (only ~ 1/3 analysed)
- ▶ 300 fb⁻¹ by 2023
- ▶ 3000 fb⁻¹ by 2037

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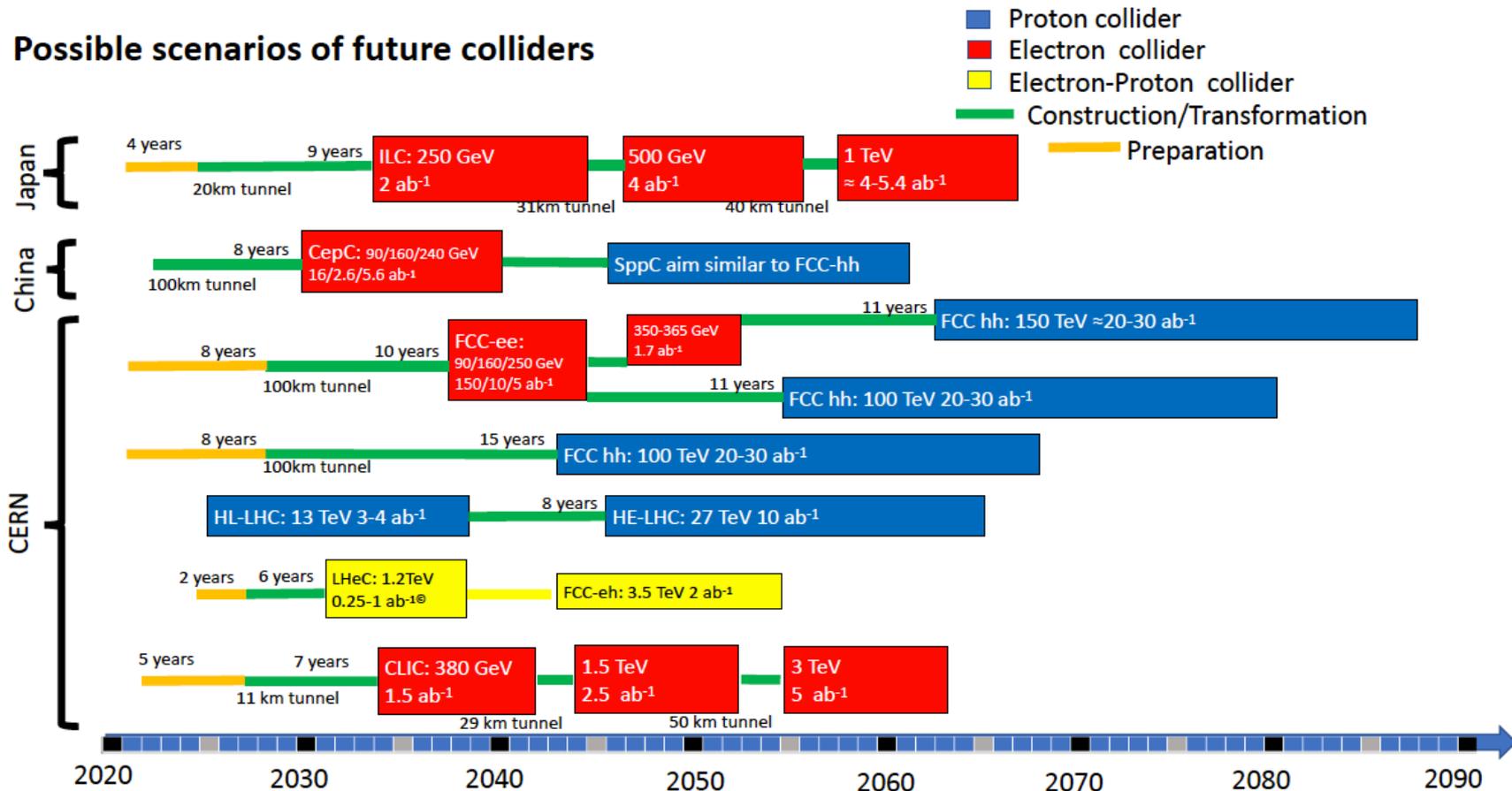
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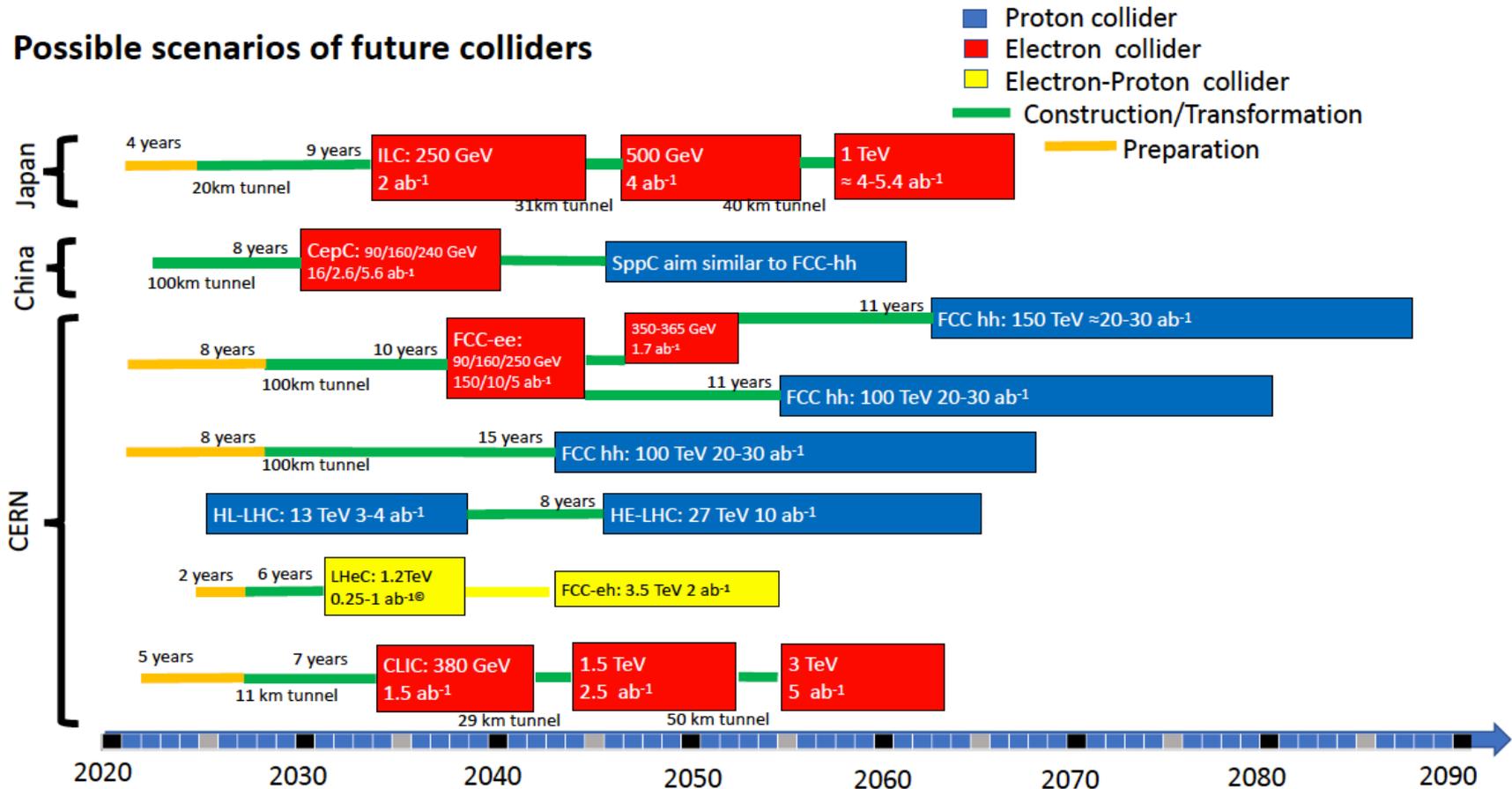
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LHC PHYSICS AT % PRECISION ?

Possible scenarios of future colliders

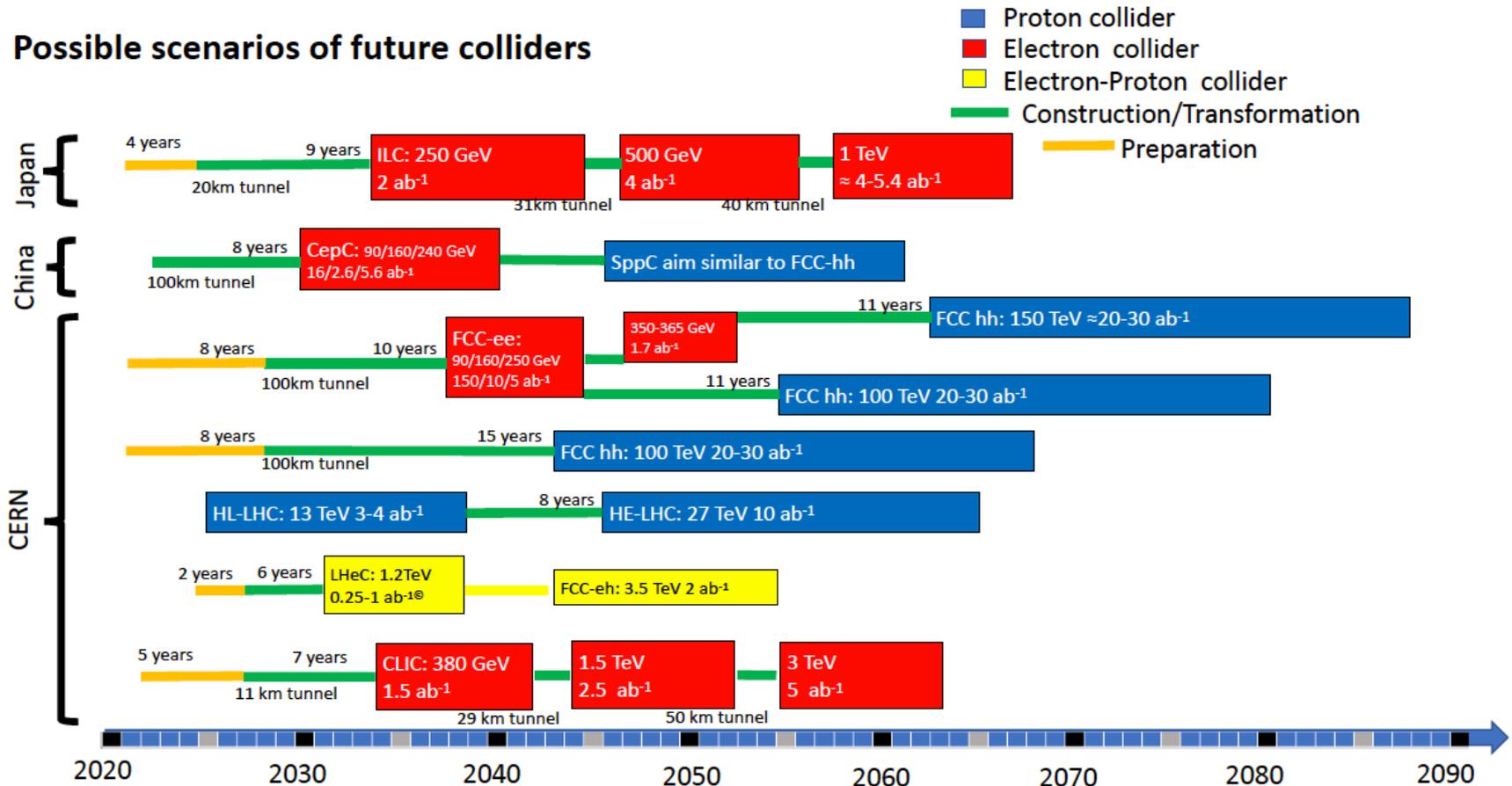


Possible scenarios of future colliders



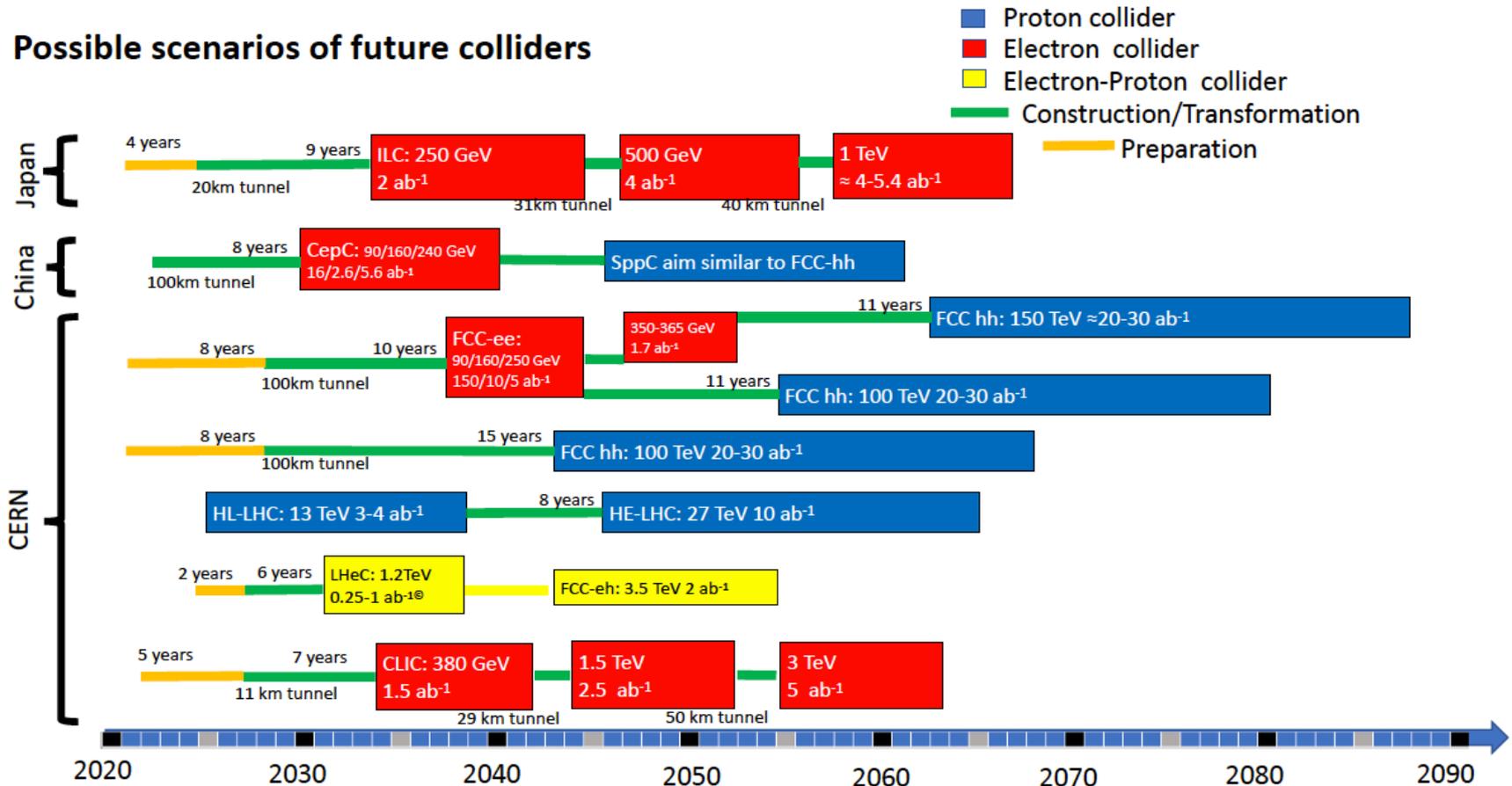
all options aimed at **attobarn⁻¹ physics**

Possible scenarios of future colliders



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- requires to go **far beyond NNLO for theory**

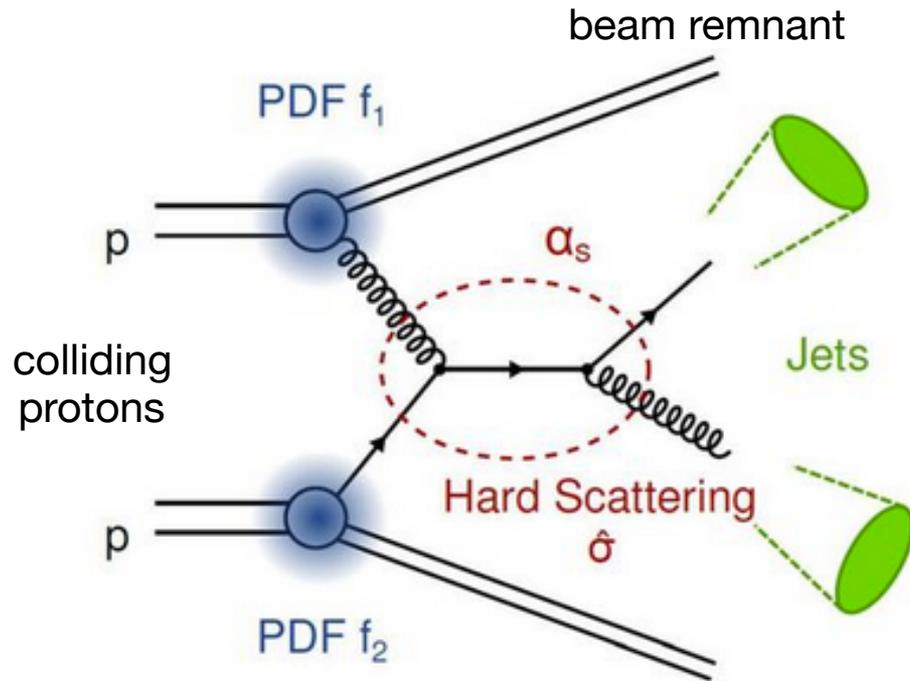
Possible scenarios of future colliders



13/05/2019 UB

- all options aimed at **attobarn⁻¹ physics**
- requires to go **far beyond NNLO for theory**
- Even conservative estimates **not reachable with current techniques**

Factorisation in hadronic collisions



- Factorise physics into **long distance** (hadronic $\sim M_{\text{had}}$) and **short distance** (partonic $Q \gg M_{\text{had}}$)
- factorisation violation is power suppressed $\sim \mathcal{O}(M_{\text{had}}/Q)^q$

$$\sigma = \sum_{a,b} \int dx_1 dx_2 f_a(x_1, \mu_F) f_b(x_2, \mu_F) \hat{\sigma}_{ab}(x_1 p_A, x_2 p_B; \mu_F, \mu_R) + \mathcal{O}\left(\frac{1}{Q}\right)$$

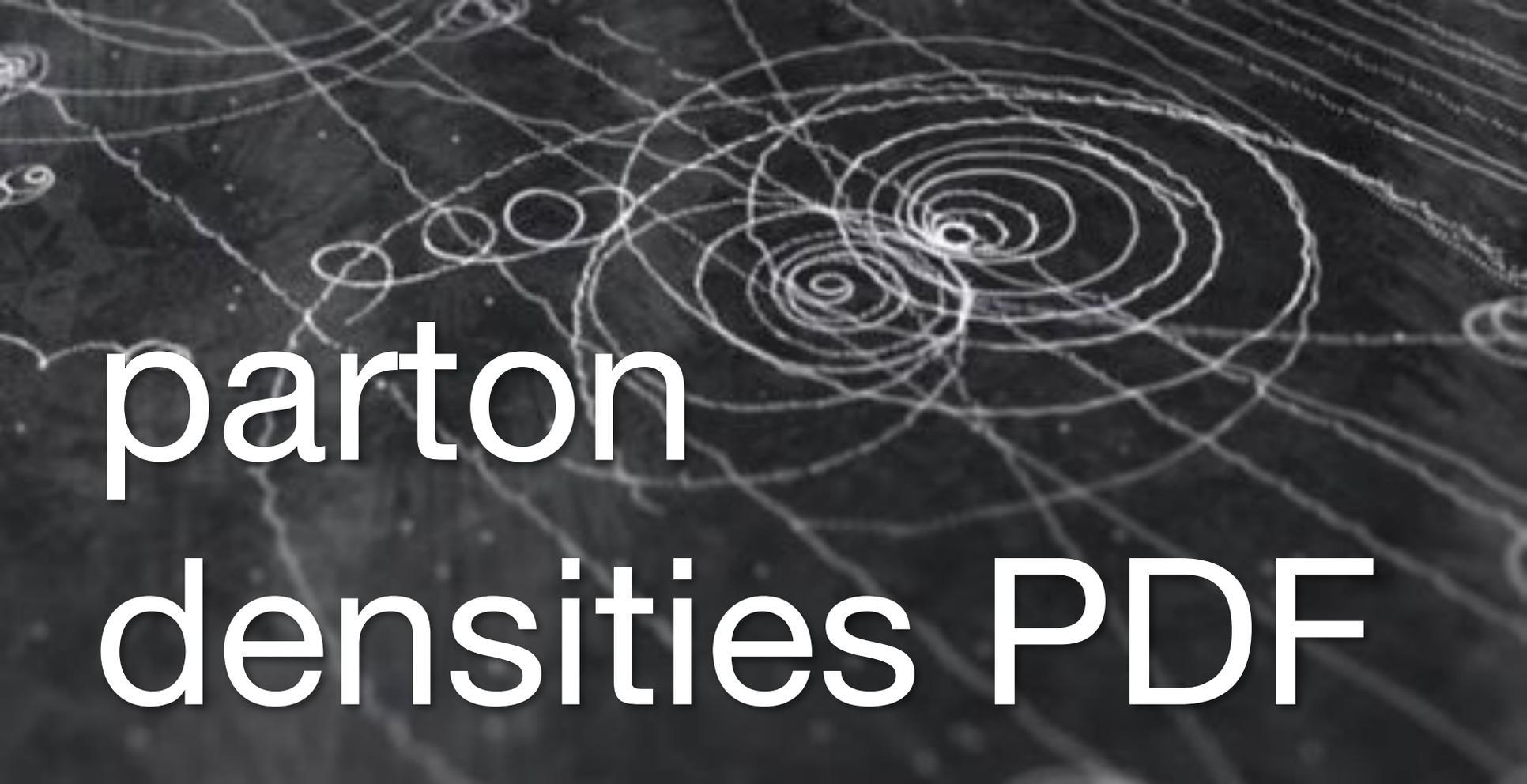
Parton densities PDF

Hard scattering cross-section

Factorization and renormalization scales

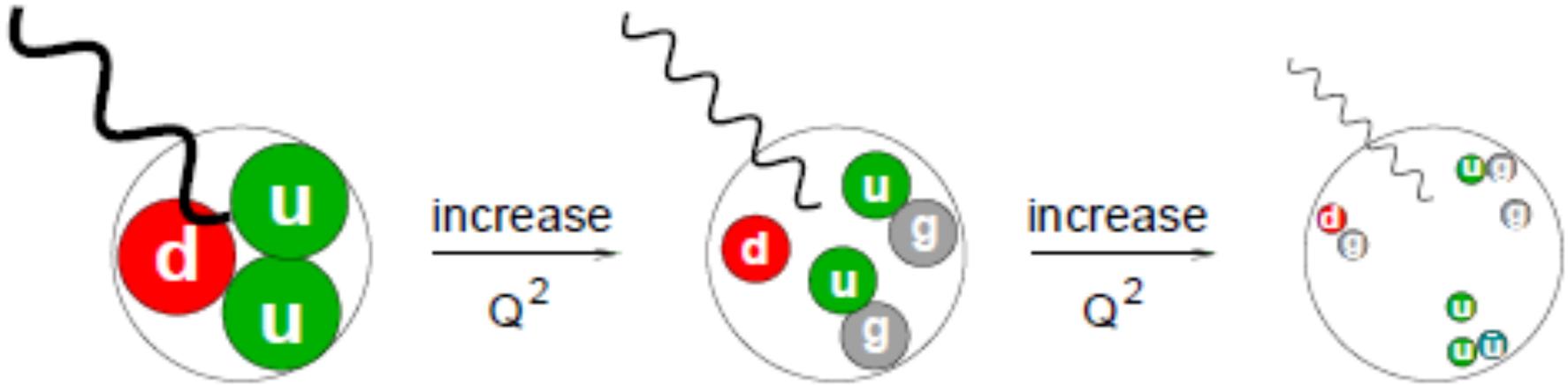
Partonic cms energy $\hat{s} = x_1 x_2 s$

Higher twist



parton densities PDF

Looking inside the proton

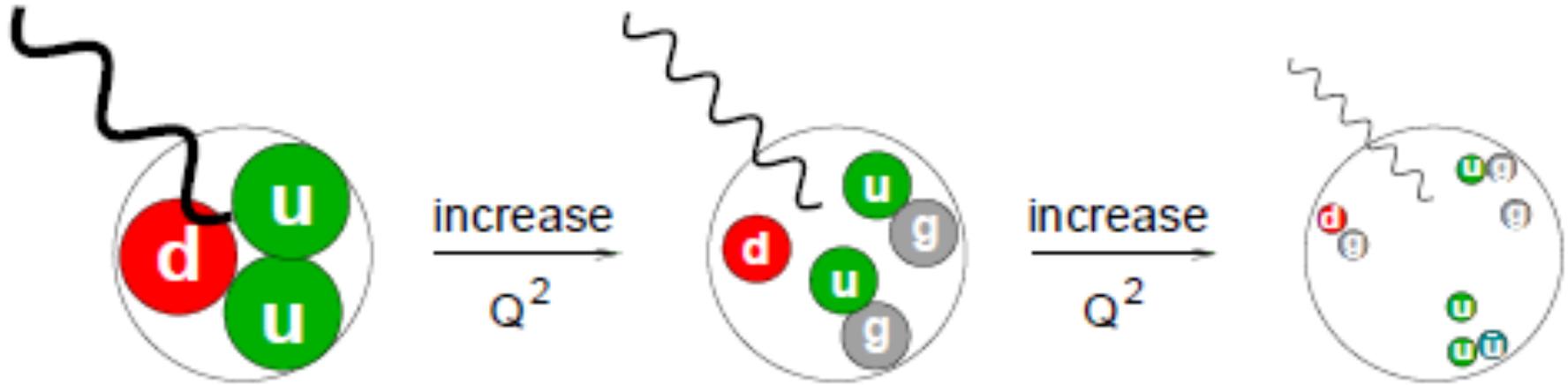


non-perturbative
input

scale evolution
determined by
pQCD



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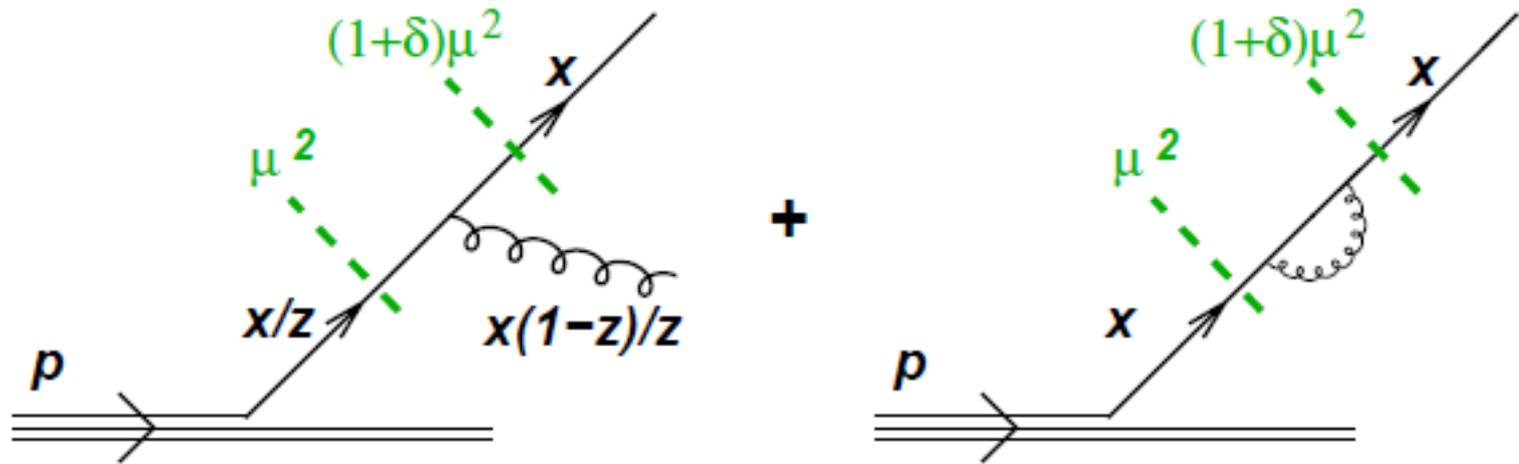


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Parton density (PDF): “probability” to find a parton of a given flavour carrying a longitudinal momentum fraction $x \in [0,1]$ of the momentum of the proton

DGLAP evolution [[Dokshitzer 1977](#)–[Gribov–Lipatov 1972](#)–[Altarelli–Parisi 1977](#)]



$$\frac{\partial q(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dz}{z} P_{q \rightarrow qg}(z) q(x/z, \mu^2)$$

DGLAP flavour structure

The proton contains both quarks and gluons: DGLAP is a **matrix in flavour space**

$$\frac{\partial}{\partial \log \mu^2} \begin{pmatrix} q \\ g \end{pmatrix} = \begin{pmatrix} P_{q \rightarrow qg} & P_{g \rightarrow q\bar{q}} \\ P_{q \rightarrow gq} & P_{g \rightarrow gg} \end{pmatrix} \otimes \begin{pmatrix} q \\ g \end{pmatrix}$$

spanning over all flavours and anti-flavours

$$P_{q \rightarrow qg} = C_F \left(\frac{1+z^2}{(1-z)_+} + \frac{3}{2} \delta(1-z) \right)$$

$$P_{q \rightarrow gq} = C_F \frac{1+(1-z)}{z}$$

$$P_{g \rightarrow q\bar{q}} = T_R [z^2 + (1-z)^2]$$

$$P_{g \rightarrow gg} = 2C_A \left[\frac{z}{(1-z)_+} + \frac{1-z}{z} + z(1-z) \right] + b_0 \delta(1-z)$$

with the plus-prescription

$z = 1$ is soft: only soft configurations

matches virtual with real corrections

$$\int_0^1 dz \frac{f(z)}{(1-z)_+} = \int_0^1 dz \frac{f(z) - f(1)}{1-z}$$

Parton densities

- Non-perturbative input determined from global fits to collider data, scale evolution from pQCD (NNLO)
- Vast choice: e.g. <http://hepdata.cedar.ac.uk/pdfs>

The Durham HepData Project



REACTION DATABASE • DATA REVIEWS • PDF PLOTTER ABOUT HEPDATA • SUBMITTING DATA

This site has now been superseded by the new hepdata.net site.

HepData Compilation of Parton Distribution Functions

On-line Unpolarized Parton Distribution Calculator with Graphical Display.

Unpolarized Parton Distributions

Access the parton distribution code, on-line calculation and graphical display of the distributions, from CTEQ, GRV, MRST/MSTW, Alekhin, ZEUS, H1, HERAPDF, BBG and NNPDF.

- CTEQ fortran code and grids
- CTEQ-Jefferson Lab (CJ) the CJ12 PDF sets
- GRV/GJR fortran code and grids
- MRST fortran code and grids, C++ code
- MSTW fortran, C++ and Mathematica codes + grids etc.
- ALEKHIN fortran, C++, Mathematica code, and grids
- ZEUS ZEUS 2002 PDFs, ZEUS 2005 jet fit PDFs
- HERAPDF Combined H1/ZEUS page, HERAPDF1.0 paper
- H1 H1 2000
- BBG BBG06_NS
- NNPDF Non Singlet PDF code - hep-ph/0701127

Polarized Parton Distributions

Currently available parametrizations

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REACTION DATABASE • DATA REVIEWS • PDF PL

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Polarized Parton Distributions

Currently available parametrizations

NNPDF23_nlo_as_0118 LHgrid members

APFEL Web

Web developers: D. Palazzo, S. Carrazza, A. Ferrara
 APFEL developers: V. Bertone, S. Carrazza, J. Rojo. ([Contact](#))

PDFs strategy in a nutshell

- Make an **ansatz** for the functional form of the PDFs at some fixed low scale value ($Q_0 \sim 1 \text{ GeV}$): e.g. in MRST/MSTW

$$x u_V = A_u x^{\eta_1} (1-x)^{\eta_2} (1 + \epsilon_u \sqrt{x} + \gamma_u x) \quad u_V = u - \bar{u}$$

$$x d_V = A_d x^{\eta_3} (1-x)^{\eta_4} (1 + \epsilon_d \sqrt{x} + \gamma_d x) \quad d_V = d - \bar{d}$$

$$x g = A_g x^{-\lambda_g} (1-x)^{\eta_g} (1 + \epsilon_g \sqrt{x} + \gamma_g x)$$

- Note: **NNPDF** use neural networks and does not need such explicit functional form
- Collect data at various (x, Q^2) from different experiments (e.g. DIS), use DGLAP equations to evolve down to Q_0 and fit parameters, including α_S

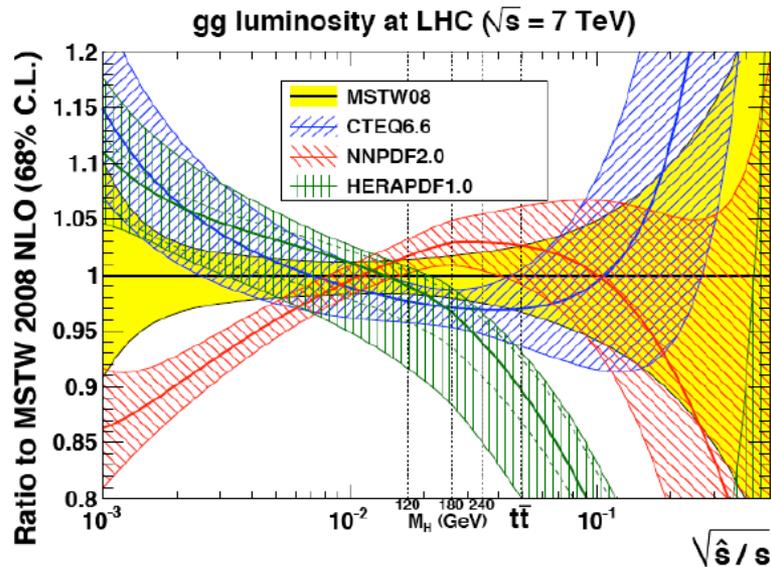
- Ensure **sum rules**: (Gottfried, momentum, ...).
$$\int dx x \sum_i f_i(x, Q^2) = 1$$

Parton densities

- Differences are due to different:

Data sets in fits, parameterization of starting distributions, order of pQCD evolution, power law contributions, nuclear target corrections, resummation corrections ($\ln 1/x$, ...), treatment of heavy quarks, strong coupling, choice of factorization and renormalization scales.

- at least 5-10% uncertainty in theoretical predictions

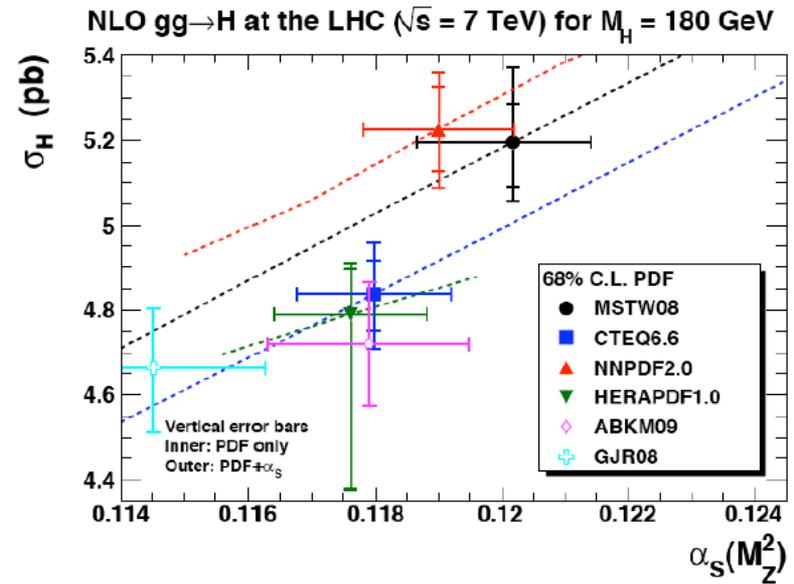
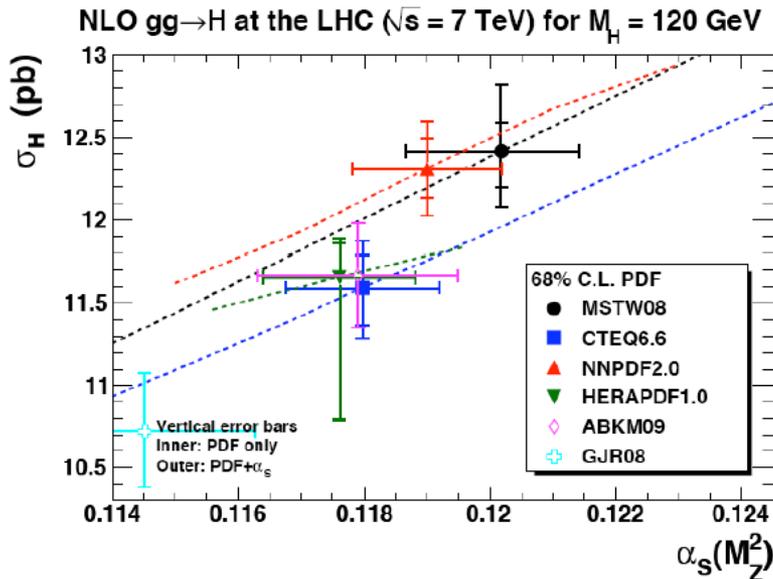


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Online PDF plotting and calculation

$xf(x, Q^2) \nu x$

Using the form below you can calculate, in real time, values of $xf(x, Q^2)$ for any of the PDFs from the different groups. You can also generate and compare plots of $xf(x, Q^2) \nu x$ at any Q^2 for up to 4 different parton types or PDF sets.

Select:	Parton	Group	Set
<input checked="" type="checkbox"/>	up	MSTW-nnlo	MSTW2008nnlo
<input checked="" type="checkbox"/>	down	MSTW-nnlo	MSTW2008nnlo
<input checked="" type="checkbox"/>	strange	MSTW-nnlo	MSTW2008nnlo
<input checked="" type="checkbox"/>	gluon	MSTW-nnlo	MSTW2008nnlo

Xmin = 0.01 Xmax = 0.8 Xinc = 0.01

Q2 = 1 GeV²

x axis: lin log

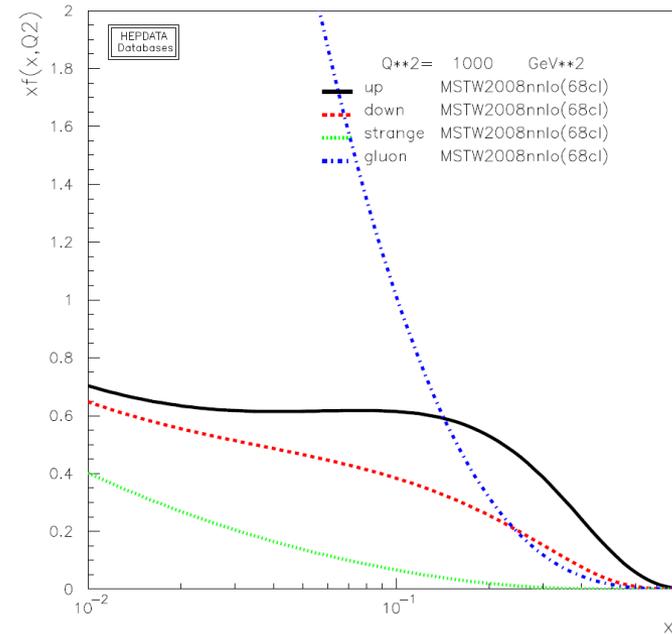
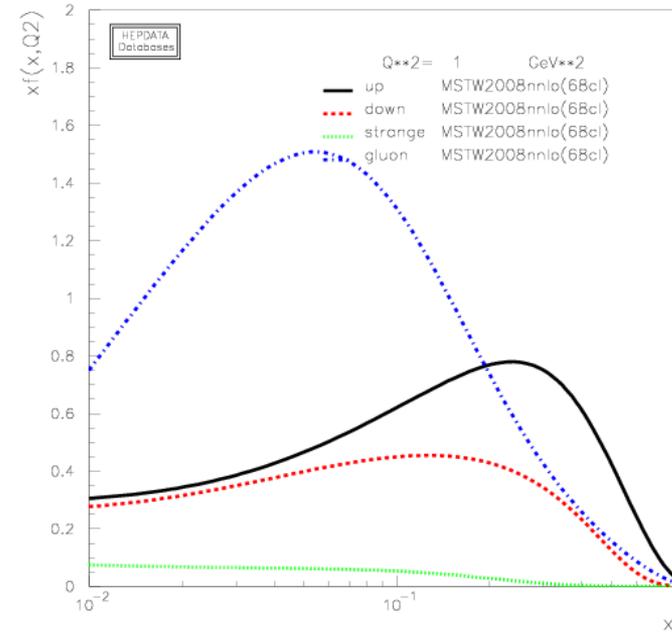
y axis: lin log, ymin = 0.0 ymax = 2.0

Output as: numbers or plot (line width = 10) as ratio

[Make the Plot](#) [add sets](#) [remove sets](#)

[Change to plotting versus Q²](#)

[Change to Error Set plotting](#)



Online PDF plotting and calculation

$xf(x, Q^2) \nu x$

Using the form below you can calculate, in real time, values of $xf(x, Q^2)$ for any of the PDFs from the different groups. You can also generate and compare plots of $xf(x, Q^2)$ νx at any Q^2 for up to 4 different parton types or PDF sets.

Select:	Parton	Group	Set
<input checked="" type="checkbox"/>	up	MSTW-nnlo	MSTW2008nnlo
<input checked="" type="checkbox"/>	down	MSTW-nnlo	MSTW2008nnlo
<input checked="" type="checkbox"/>	strange	MSTW-nnlo	MSTW2008nnlo
<input checked="" type="checkbox"/>	gluon	MSTW-nnlo	MSTW2008nnlo

Xmin = 0.01 Xmax = 0.8 Xinc = 0.01

Q2 = 1 GeV²

x axis: lin log

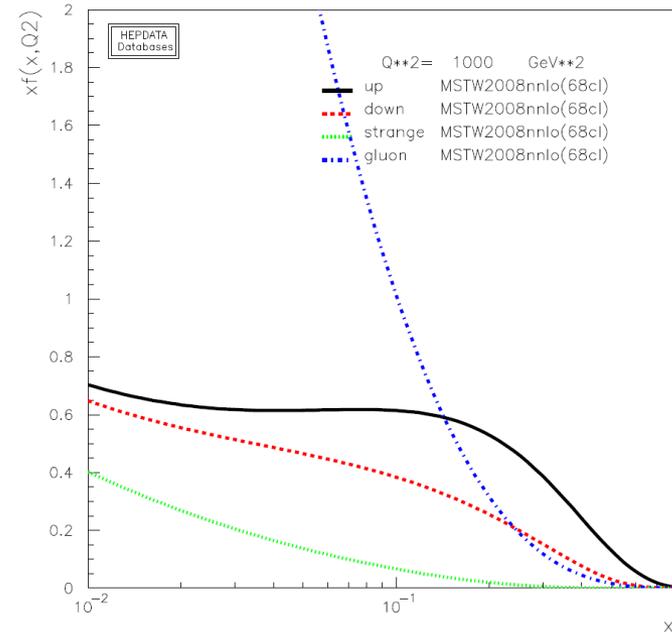
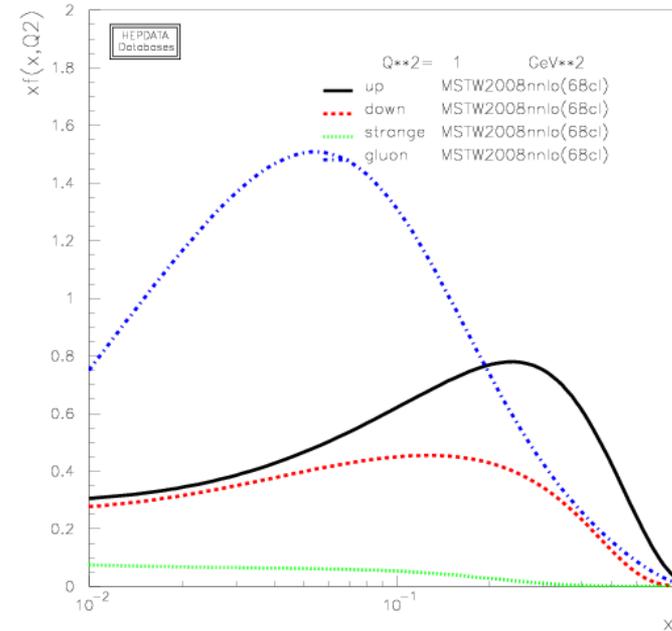
y axis: lin log, ymin = 0.0 ymax = 2.0

Output as: numbers or plot (line width = 10) as ratio

Make the Plot **add sets** **remove sets**

Change to plotting versus Q²

Change to Error Set plotting



- Maximum of up and down at $x=1/3$: three quarks sharing the proton momentum

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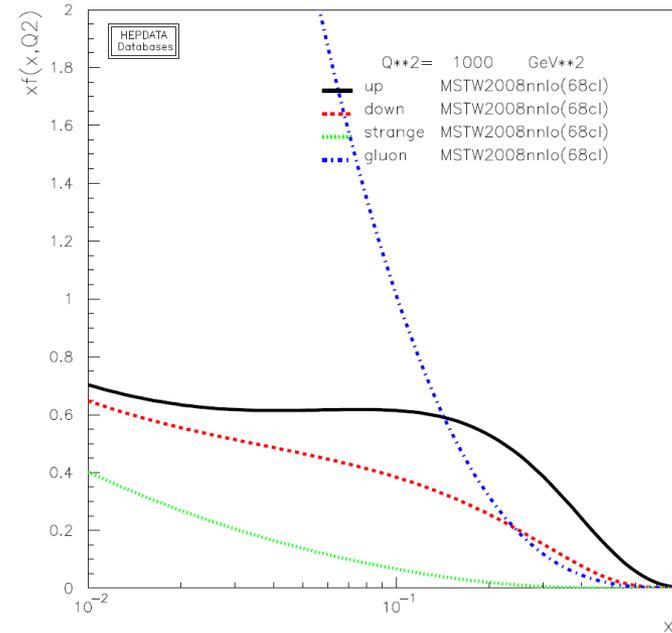
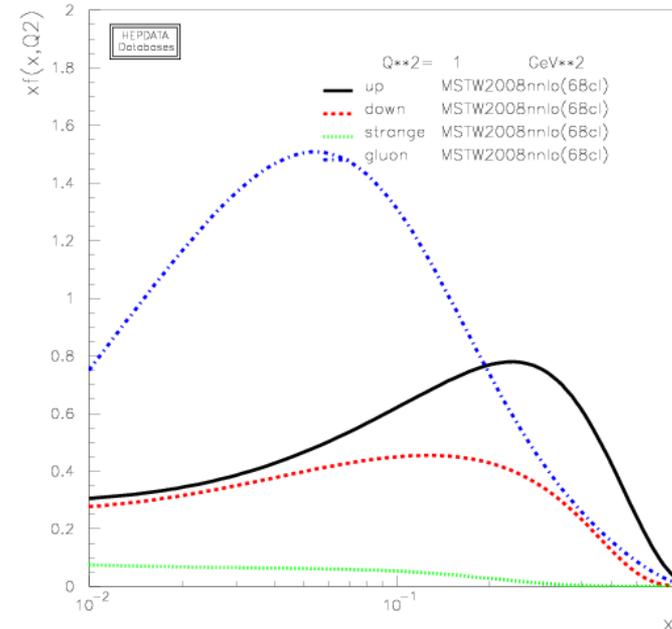
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Output as: numbers or plot (line width = 10) as ratio

[Make the Plot](#) [add sets](#) [remove sets](#)

[Change to plotting versus Q²](#)

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- Maximum of up and down at $x=1/3$: three quarks sharing the proton momentum
- up quark = 2 x down quark

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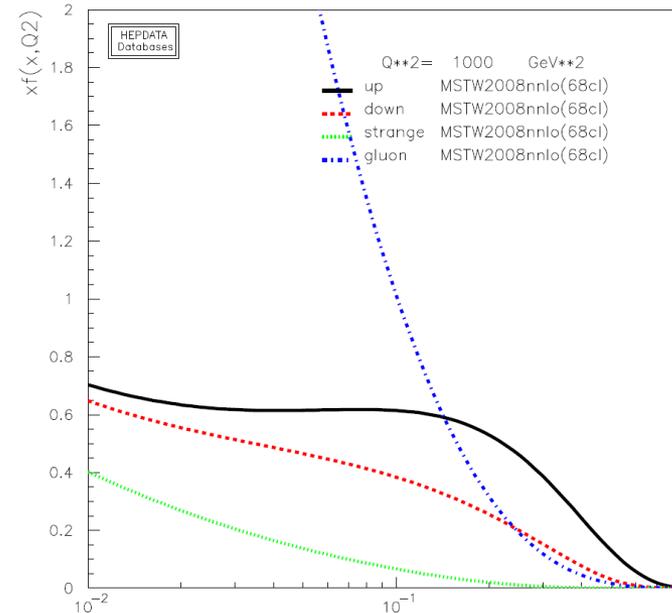
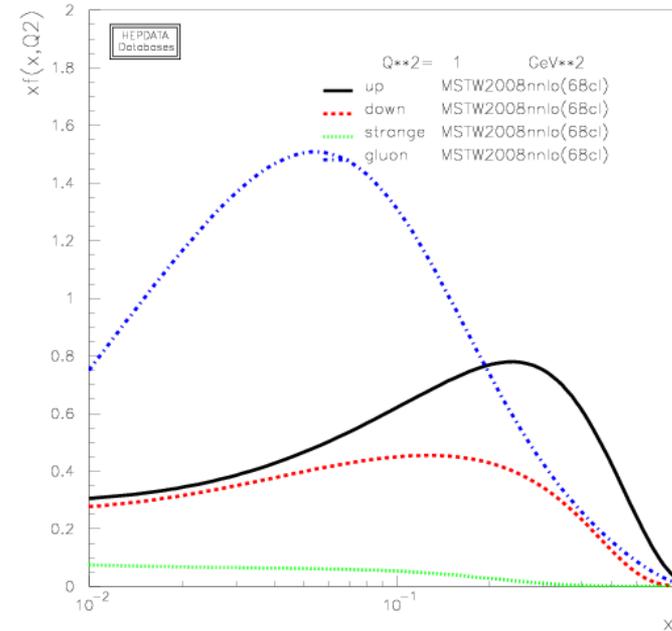
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- Maximum of up and down at $x=1/3$: three quarks sharing the proton momentum
- up quark = 2 x down quark
- gluon density evolves faster: colour charge $C_A = 3$ versus quark colour charge $C_F = 4/3$



Jets

What's a jet



What's a jet



- a bunch of energetic and collimated particles

What's a jet



- a bunch of energetic and collimated particles
- 60% of LHC papers use jets [Salam, Soyez]

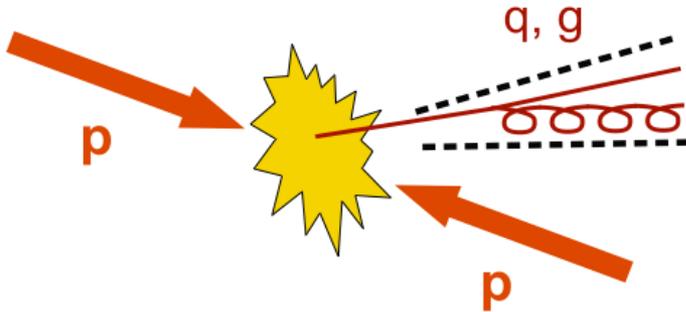
Why and how do we see jets?

Gluon emission

$$\int \alpha_s \frac{dE}{E} \frac{d\theta}{\theta} \gg 1$$

higher probability at small angle
(collinear) and small energy
(soft)

Parton level



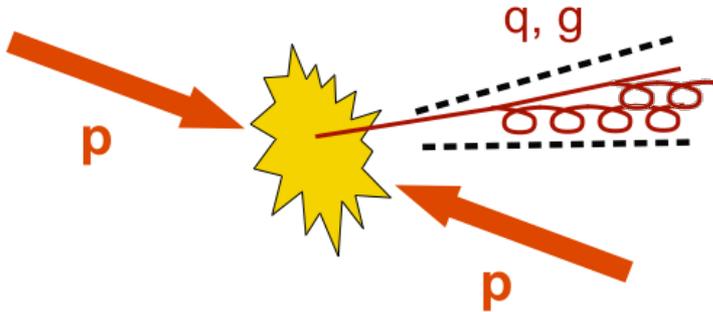
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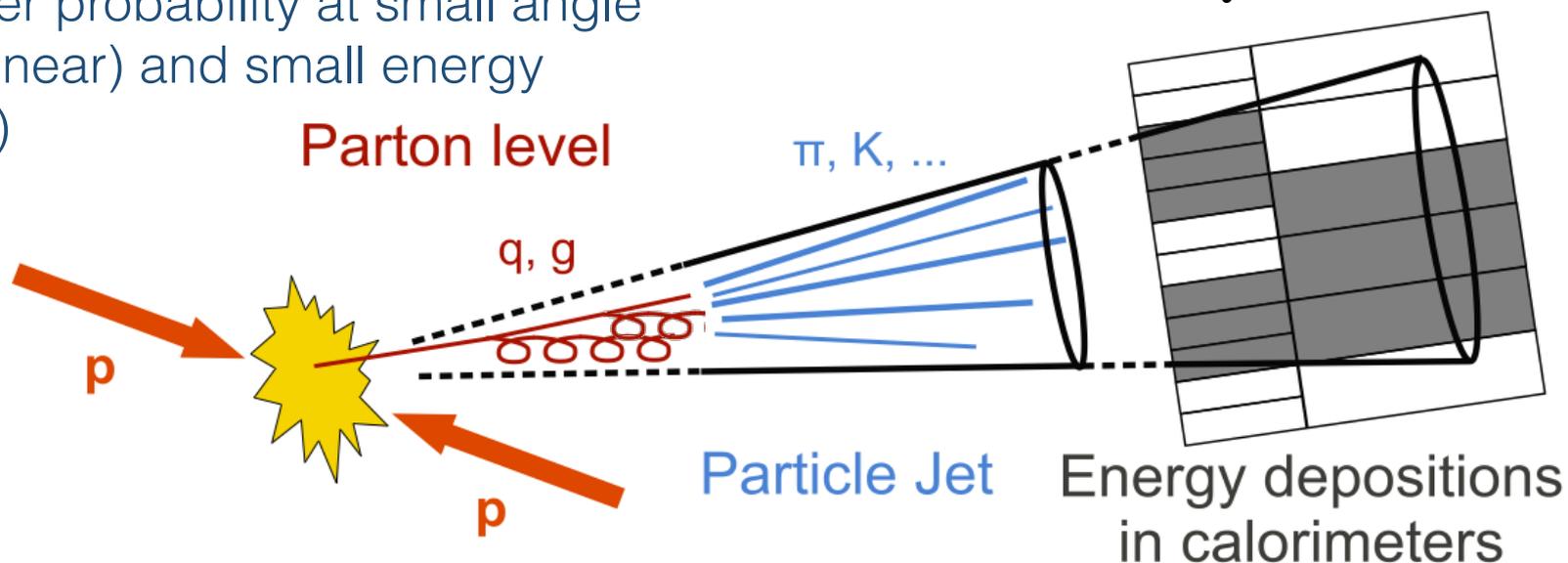
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Non-perturbative
transition to hadrons

$$\alpha_S \sim 1 \quad \Lambda_{\text{QCD}} \sim 200\text{MeV}$$



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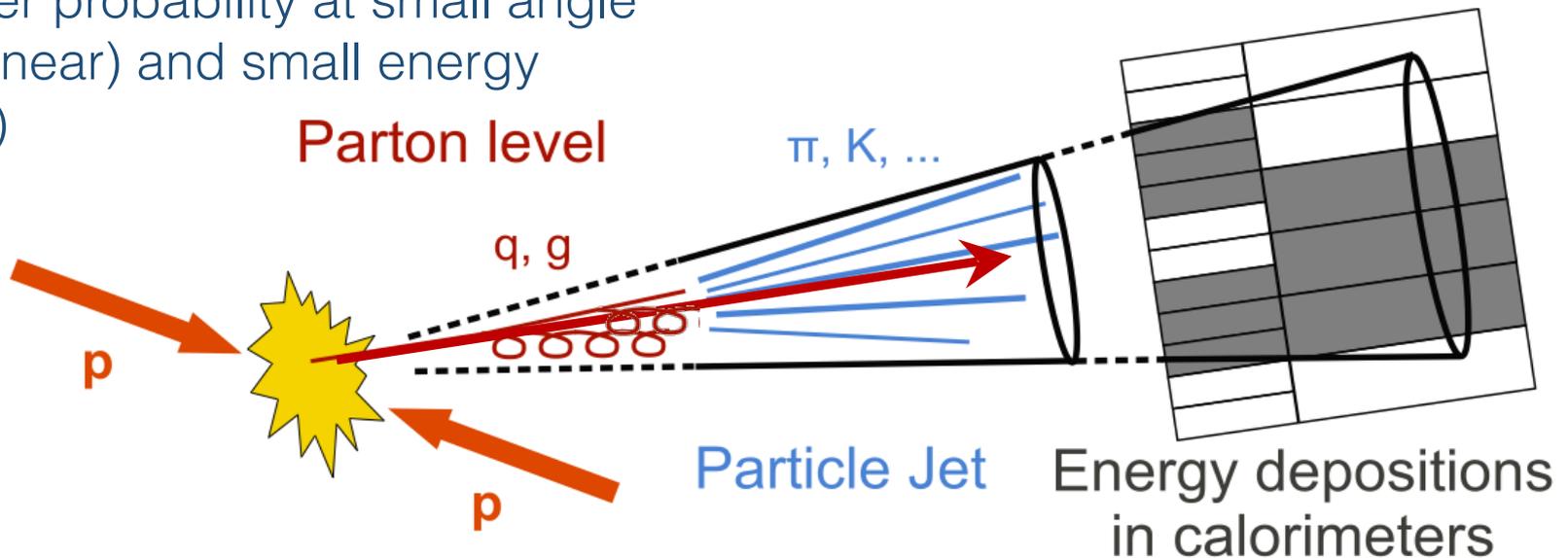
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$\{j_k\}$

jets

jet definition
←

$\{p_i\}$

final-state
4-momenta

Why and how do we see jets?

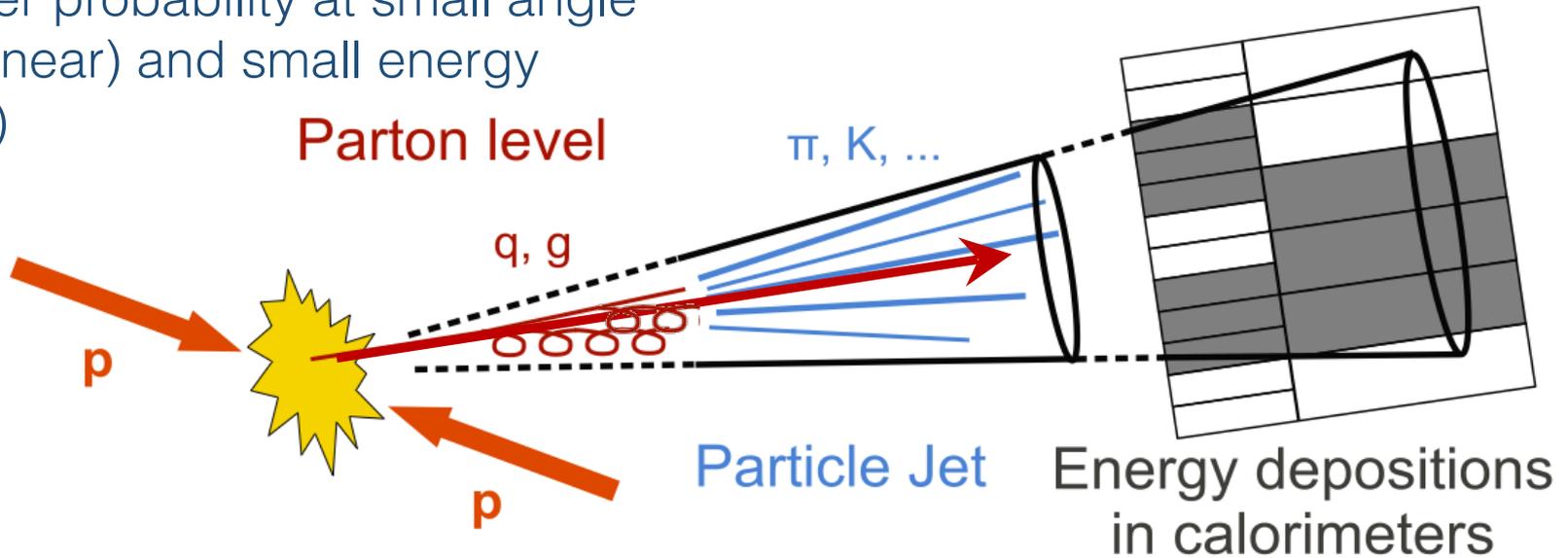
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hard partons

interpretation ←

 $\{j_k\}$

jets

jet definition ←

 $\{p_i\}$

final-state 4-momenta

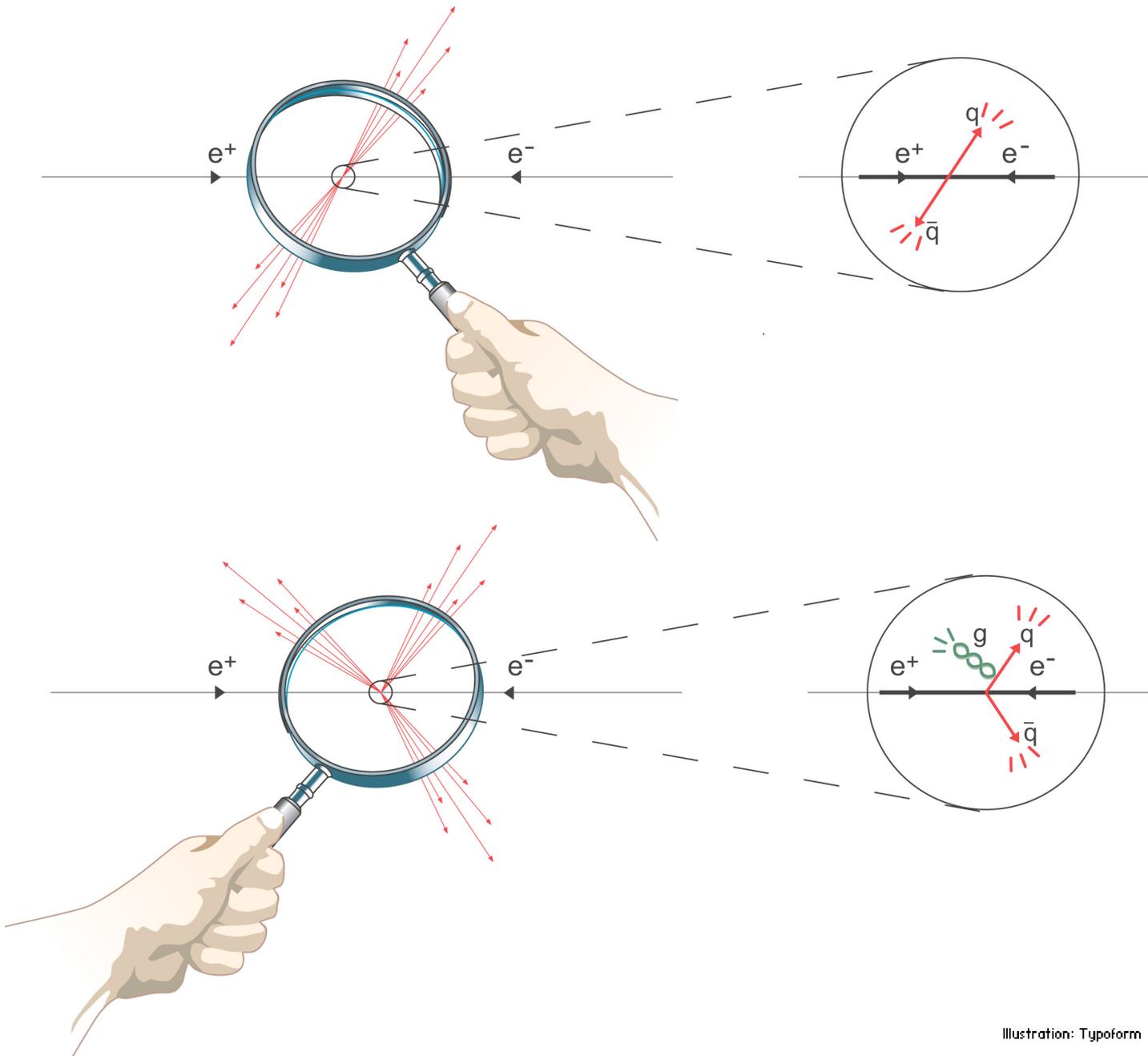
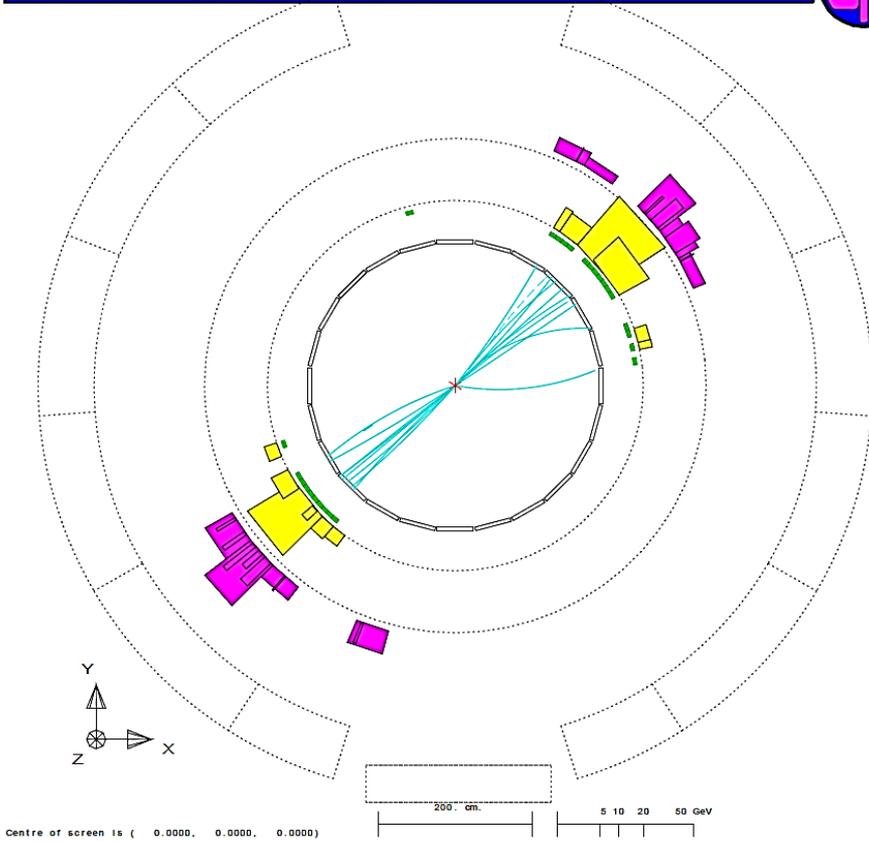
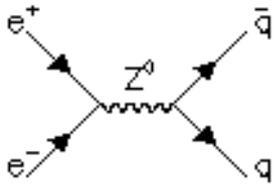
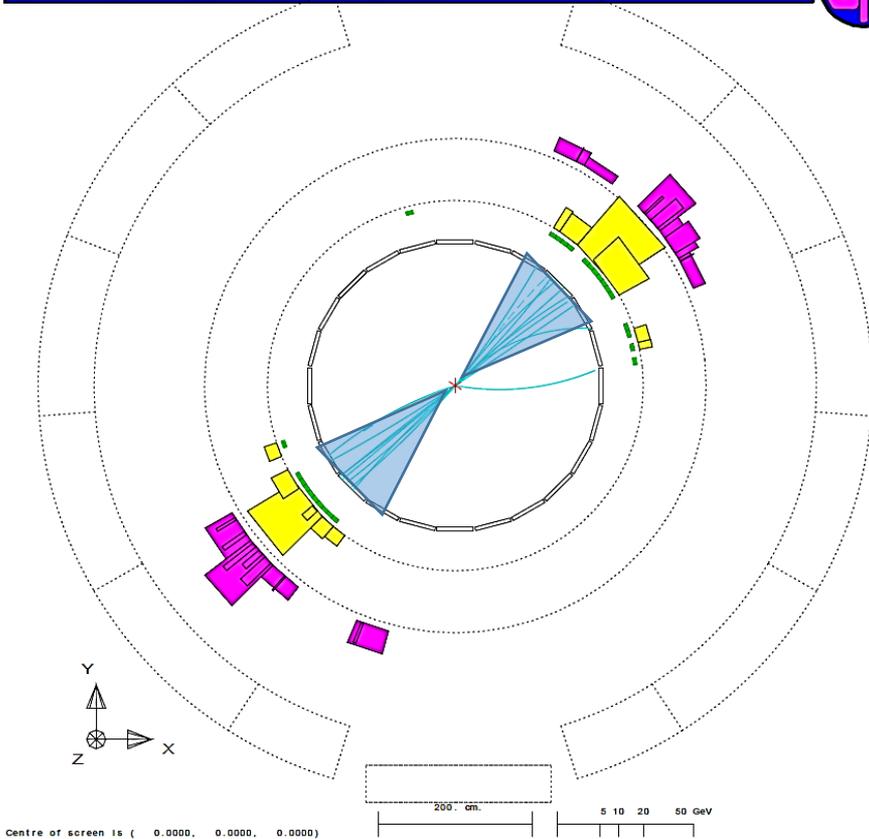


Illustration: Typoform

Run: event 4093: 1000 Date 930527 Time 20716 Ctrk(N= 39 Sump= 73.3) Ecal(N= 25 SumE= 32.6) Hcal(N=22 SumE= 22.6)
Ebeam 45.658 Evis 99.9 Emiss -8.6 Vtx (-0.07, 0.06, -0.80) Muon(N= 0) Sec Vtx(N= 3) Fdet(N= 0 SumE= 0.0)
Bz=4.350 Thrust=0.9873 Aplan=0.0017 Oblat=0.0248 Spher=0.0073

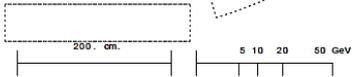
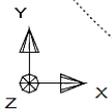
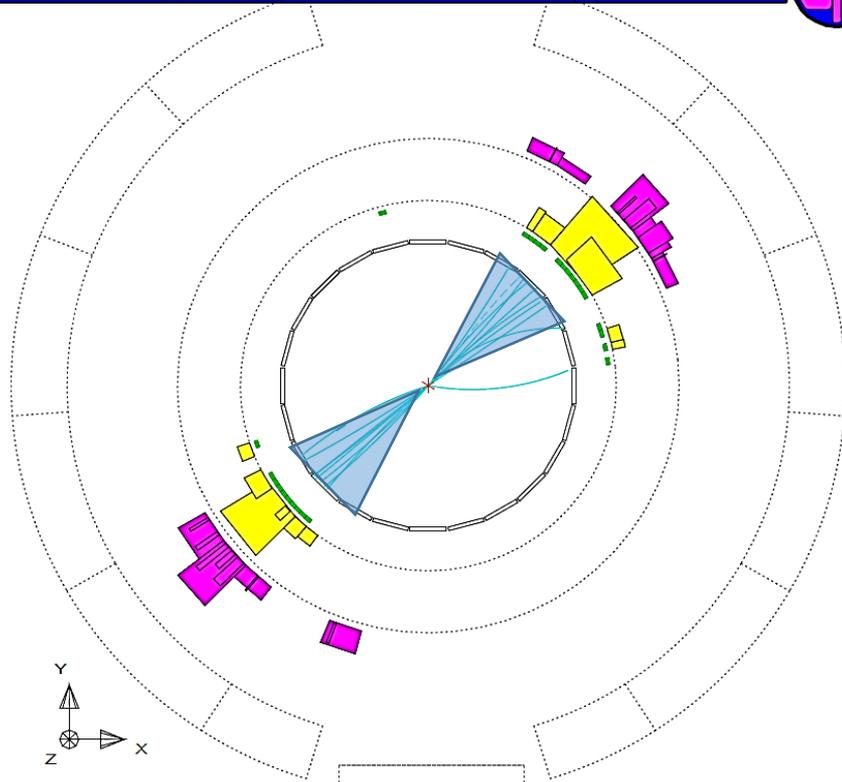


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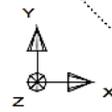
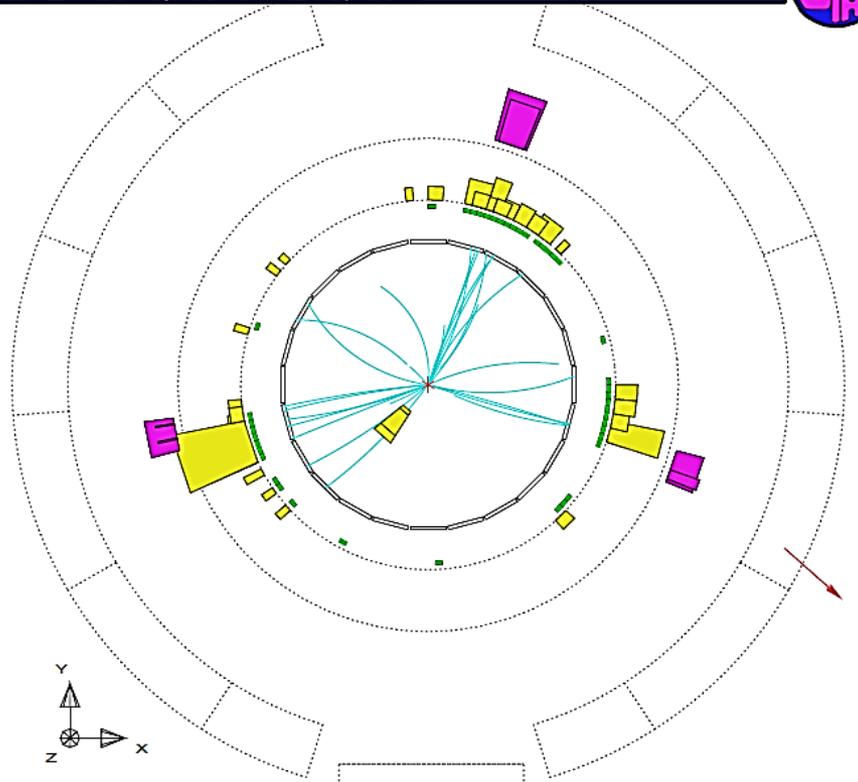
■ Clearly a two-jet event

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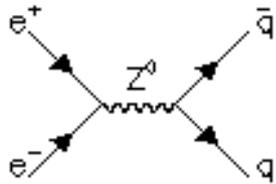


Centre of screen is (0.0000, 0.0000, 0.0000)

Run: event 2542: 63750 Date 911014 Time 35925 Ctrk(N= 28 Sump= 42.1) Ecal(N= 42 SumE= 59.8) Hcal(N= 8 SumE= 12.7)
 Ebeam 45.609 EvIs 86.2 Emiss 5.0 Vtx (-0.05, 0.12, -0.90) Muon(N= 1) Sec Vtx(N= 0) Fdet(N= 2 SumE= 0.0)
 Bz=4.350 Thrust=0.8223 Aplan=0.0120 Oblat=0.3338 Spher=0.2463

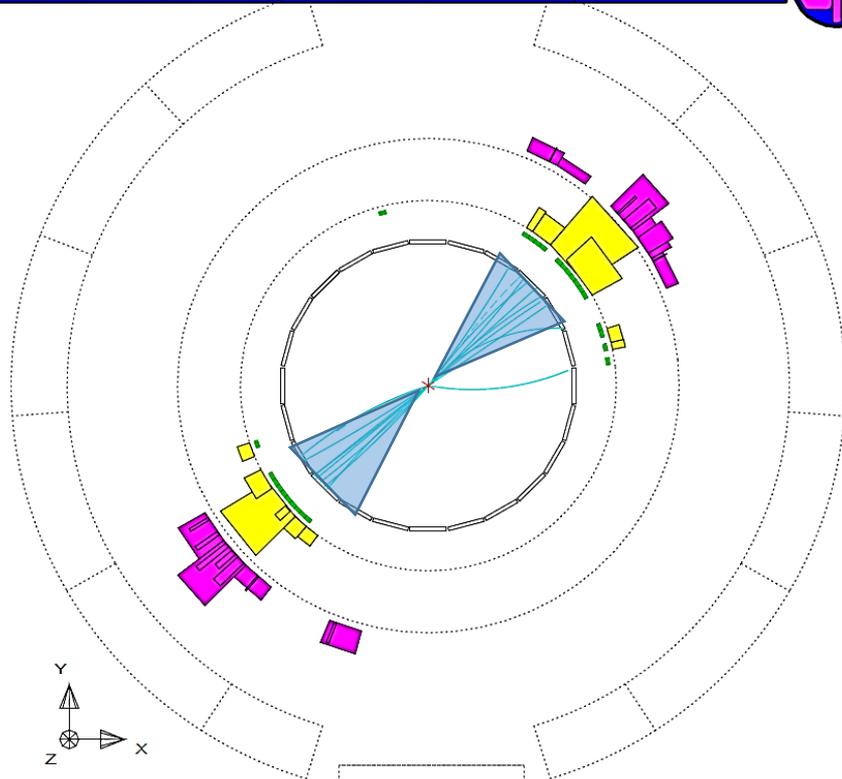


Centre of screen is (0.0000, 0.0000, 0.0000)



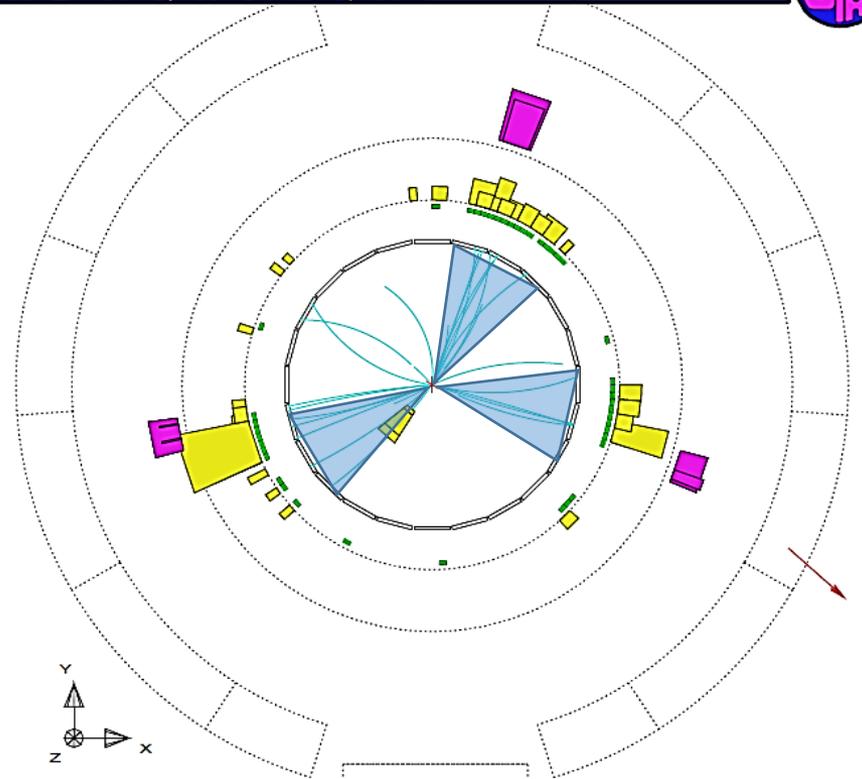
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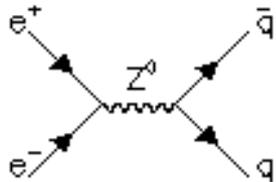


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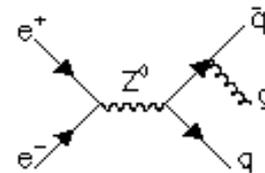
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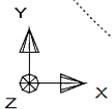
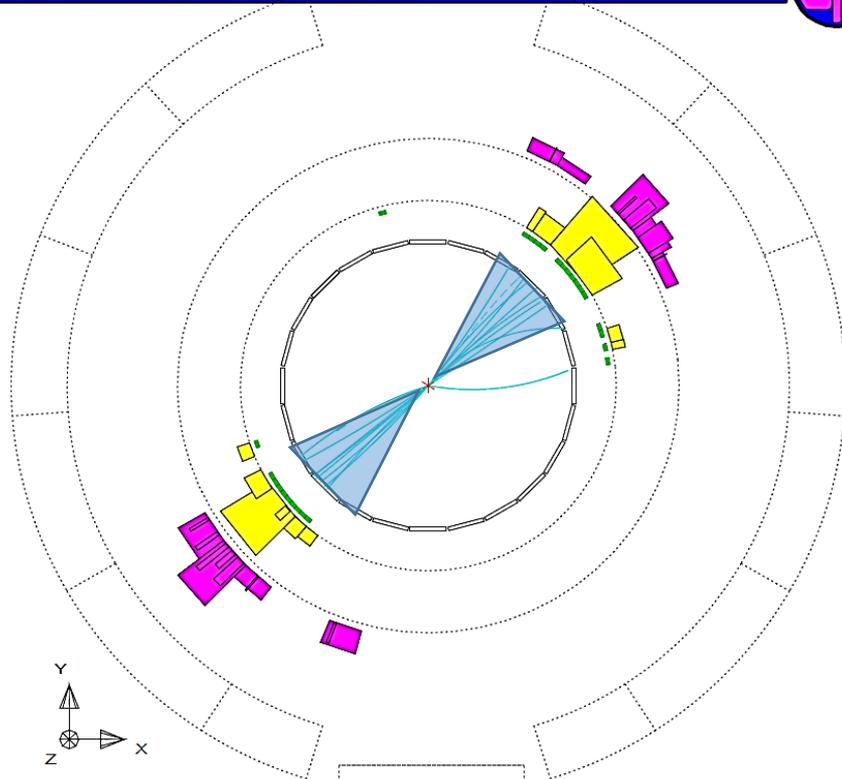
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Clearly a two-jet event

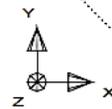
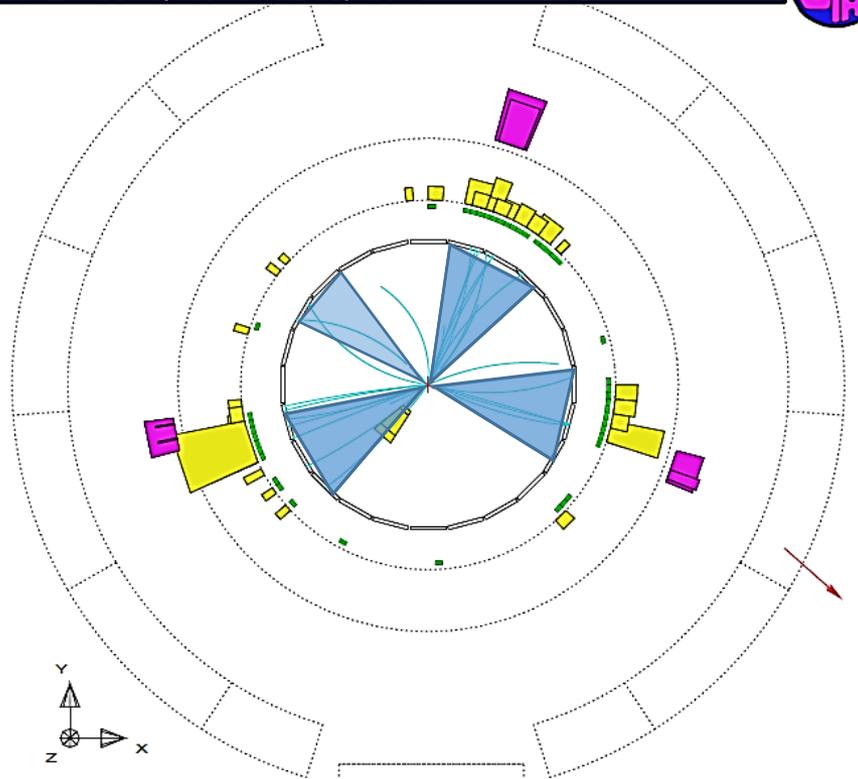


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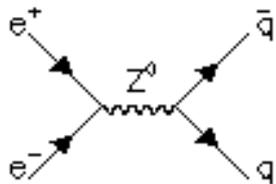


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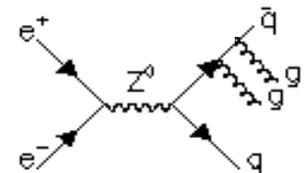
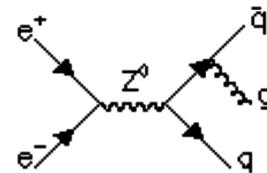
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Centre of screen is (0.0000, 0.0000, 0.0000)



Clearly a two-jet event



- Three- or four-jet event ?
- Depends on the jet resolution parameter

The k_T algorithm at hadron colliders

[Catani, Dokshitzer, Seymour, Webber, 93]

[Ellis, Soper, 93]

- Define distance among particles: e.g. $d_{ij} = (p_i + p_j)^2$

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 $d_{iB} = p_{Ti}^2 = 2E_i^2(1 - \cos \theta_{iB})$

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Inclusive k_T

$$d_{ij} = \min(p_{Ti}^2, p_{Tj}^2) \frac{\Delta R_{ij}^2}{R^2} \quad d_{iB} = p_{Ti}^2 \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

- Compute the smallest distance d_{ij} or d_{iB}
- If d_{ij} , cluster i and j together
- If d_{iB} , call i a jet and remove from the list of particles
- Repeat until no particle is left
- Two parameters R and minimal transverse momentum $p_{Ti} > p_{T,\min}$

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$$y = \frac{1}{2} \log \frac{E + p_z}{E - p_z} \quad \neq \quad \eta = -\log(\tan(\theta/2)) \quad \text{for massive particles}$$

The anti- k_T algorithm

[Cacciari, Salam, Soyez 08]

- **k_T has a physical meaning:** the stronger divergence between a pair of particles, the more likely it is they will be associated with each other

The anti- k_T algorithm

[Cacciari, Salam, Soyez 08]

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- However: ATLAS and CMS use anti- k_T

The anti- k_T algorithm

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anti- k_T

$$d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2} \quad d_{iB} = p_{Ti}^{-2} \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

- Cluster hardest particles first
- Cone-shaped cones but it is IRC safe, contrary to cone algorithms widely used at Tevatron
- Easier to energy jet energy scale right

The anti- k_T algorithm

[Cacciari, Salam, Soyez 08]

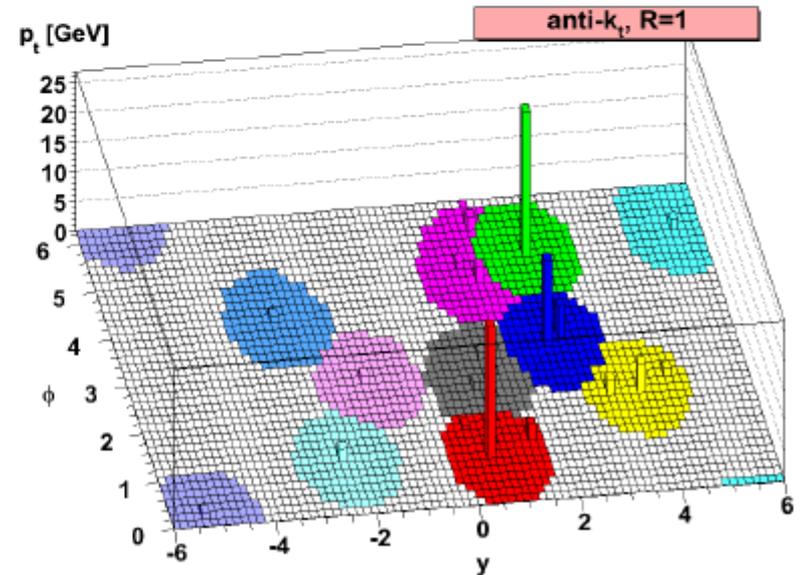
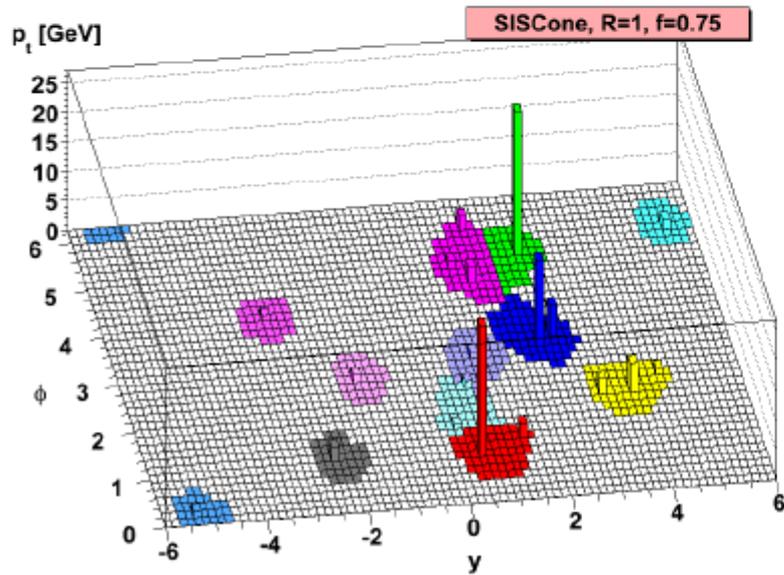
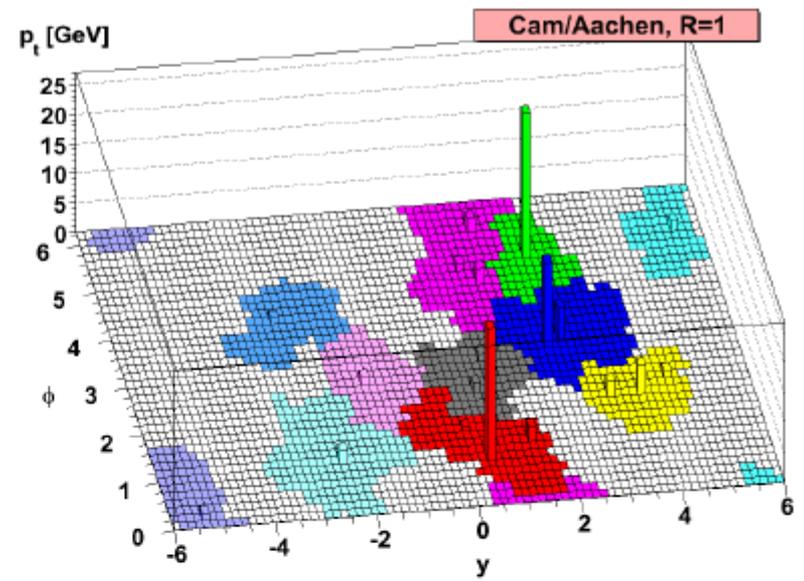
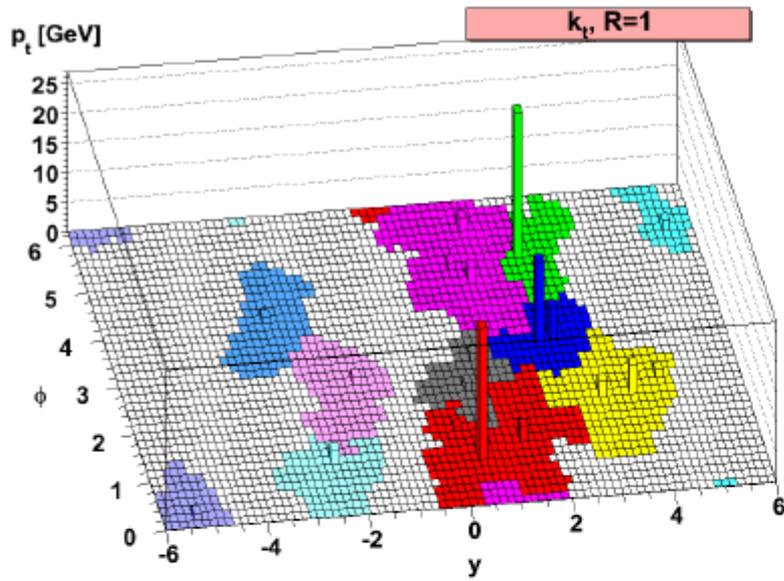
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anti- k_T

$$d_{ij} = \min(p_{Ti}^{-2}, p_{Tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2} \quad d_{iB} = p_{Ti}^{-2} \quad \Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

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- Cambridge/Aachen: $d_{ij} = \frac{\Delta R_{ij}^2}{R^2}$





“

Precise measurements of known particles and interactions are just as important as finding new particles



Maximilien Brice and Julien Marius Ordan, CERN

The unseen progress of the LHC

05/02/19 | By Sarah Charley

It's not always about what you discover.

“This work naturally pushes our search methods towards making more detailed and higher precision measurements that will help us constrain possible deviations by new physics,” Willocq says.

Exploring through precision

The universe is full of fields, and what we think of as particles are just excitations of those fields, like waves in an ocean. An electron, for example, is just an excitation of an electron field. Resonances and wave crests break up out of the fields and thus we reproduce very rare processes study to search for new physics. The key to observe these very rare processes is a particle accelerator for electrons and anti-electrons in a new 100 km tunnel.