

Topological pumping in Aharonov-Bohm rings

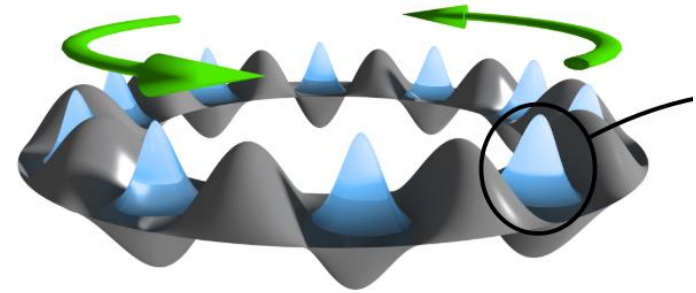
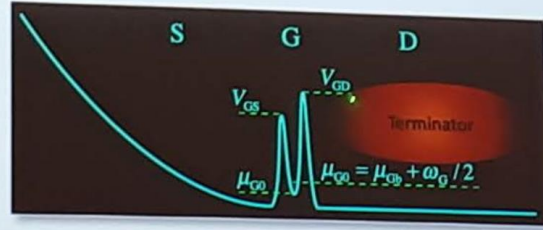
arXiv:1810.08525

Tobias Haug, Rainer Dumke, Leong-Chuan
Kwek, Luigi Amico

06.05.2019

ATOMTRONIC TRANSISTOR

- A triple-well structure
- Electronic FET nomenclature: Source, Gate, Drain = SGD
- Barriers and biasing is defined by magnetic and optical fields
- Terminator beam couples output flux to the impedance of vacuum



- Transistors/Lead-system dynamics
- Time dependent lattices
- Ring with flux

Time-dependent optical lattices: transitions, cooling and chaos assisted tunneling



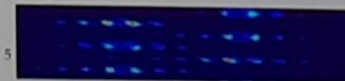
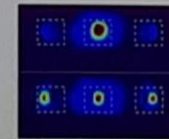
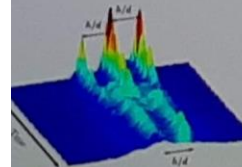
Laboratoire Collisions Agrégats Réactivité

David Guéry-Odelin

Assistant professor: J. Billy

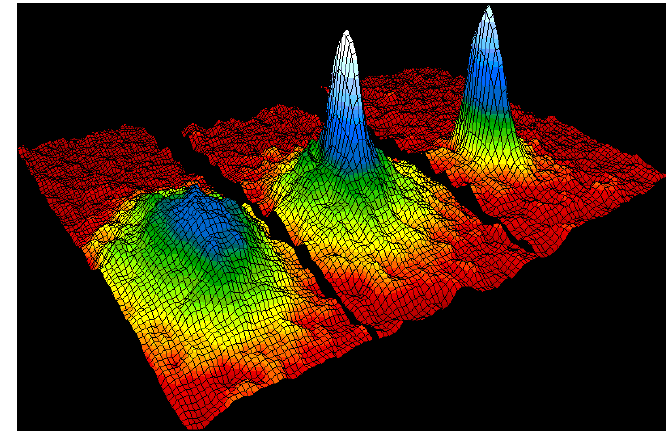
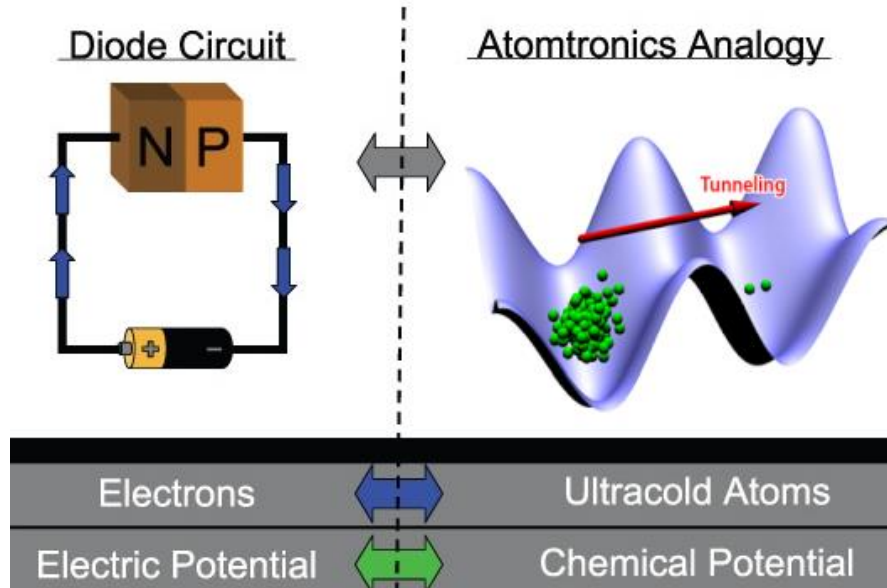
PhD students: M. Arnal, G. Chatelain, E. Michon, V. Brunaud

Collaborations: P. Schlagheck, G. Lemarié, B. Georgeot



Atomtronics

Atomtronics: Cold atoms are analog to electronics



Opportunities

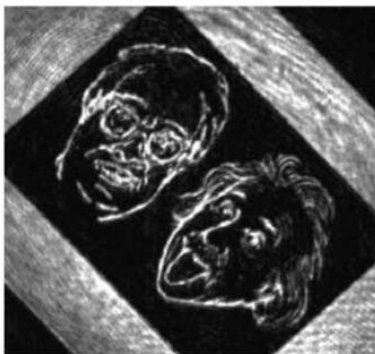
- Improve cold atom **quantum simulators**
- Bridging **mesoscopic** and cold-atoms physics
- New quantum **devices/Quantum sensing**

Advantages: - Neutral atoms → No charge and long coherence (~1 minute)
 - Flexible trapping with light

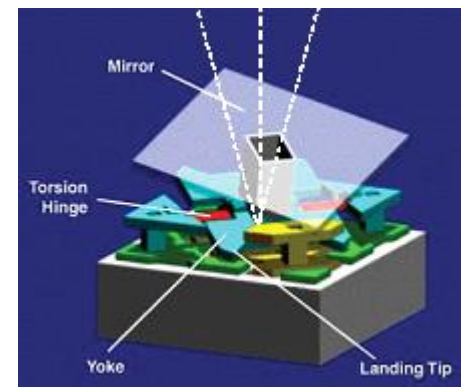
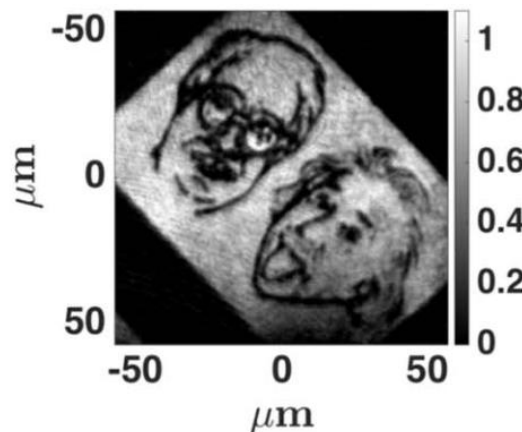
Light shaping techniques

- Digital micromirror device (DMD) for arbitrary light potentials

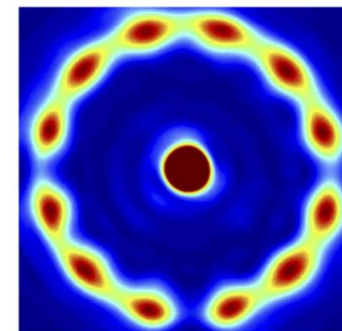
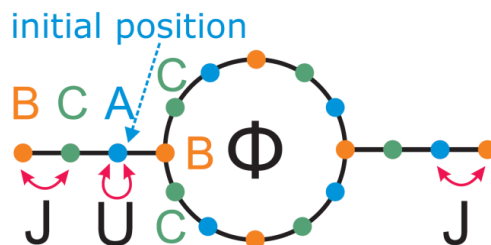
Laser field

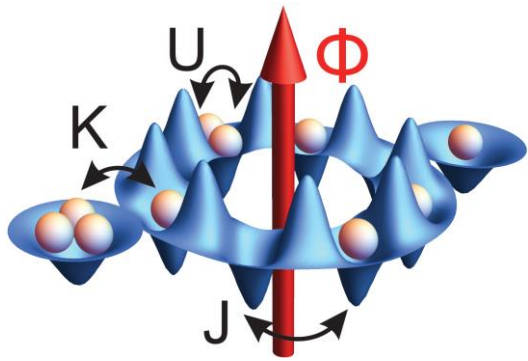


Actual trapped atoms



- Possible to create potentials for complex circuits
- Repetition rate $\sim 100\mu\text{s}$ \rightarrow Modulate potential in time during experiment to change local potential energy





Aharonov-Bohm effect

TH, H. Heimonen, R. Dumke, L.-C. Kwek, L. Amico
arXiv:1706.05180

Quantum phases

TH, L. Amico, R. Dumke, L.-C. Kwek
Quantum Sci. Technol. (2018)
arXiv:1612.09109

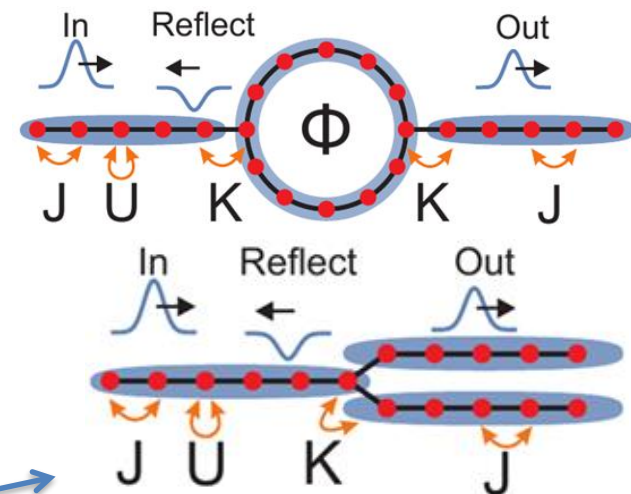
Topological pumping with spin dualities

TH, L. Amico, L.-C. Kwek, W.J. Munro, V.M. Bastidas
Soon on arXiv

Fragmented states

N. Victorin, TH, L.-C. Kwek, L. Amico, A. Minguzzi
Phys. Rev. A **99**, 033616
arXiv:1810.03331

Cold atoms + potential shaping + control currents



Transport

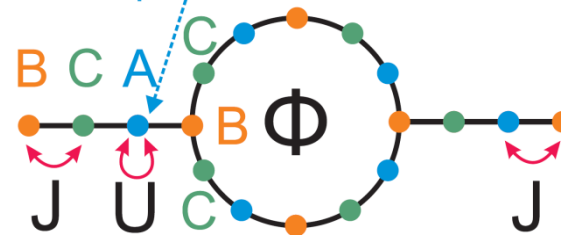
TH, R. Dumke, L.-C. Kwek, L. Amico
arXiv:1807.03616

AQUID read-out

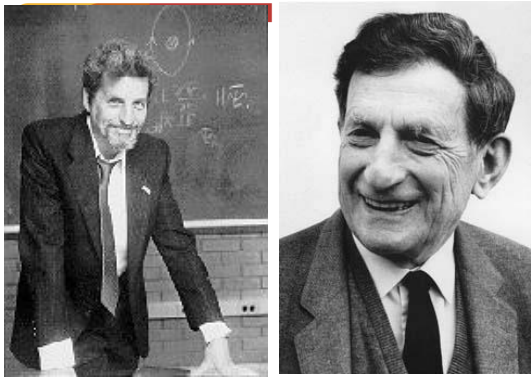
TH, J. Tan, M. Theng, R. Dumke, L.C. Kwek, L. Amico
Phys. Rev. A **97** (2018)
arXiv: 1707.09184

Topological pumping in rings

initial position



TH, R. Dumke, L.-C. Kwek, L. Amico
arXiv:1810.08525



Aharonov-Bohm effect

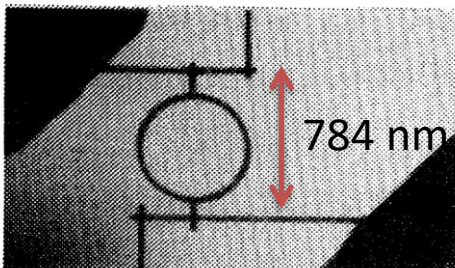
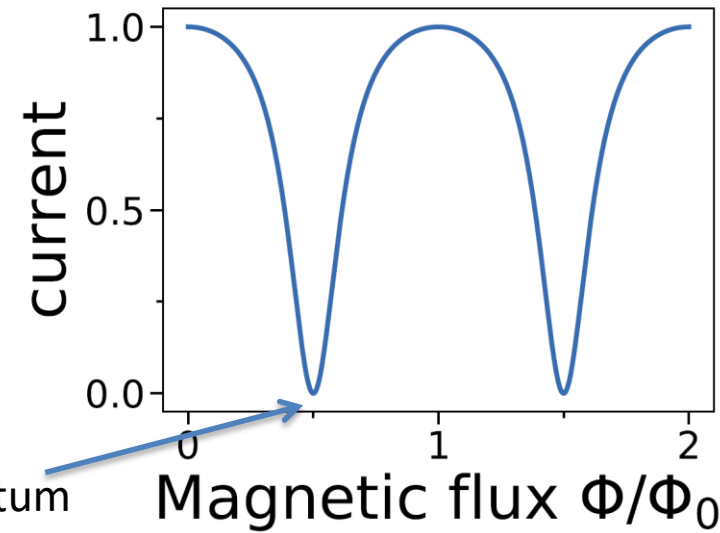
- Charged particle enclosing a region with magnetic field

$$\Delta\phi = \frac{e}{\hbar} \oint_C \mathbf{A}(\mathbf{r})d\mathbf{r} \propto \Phi$$

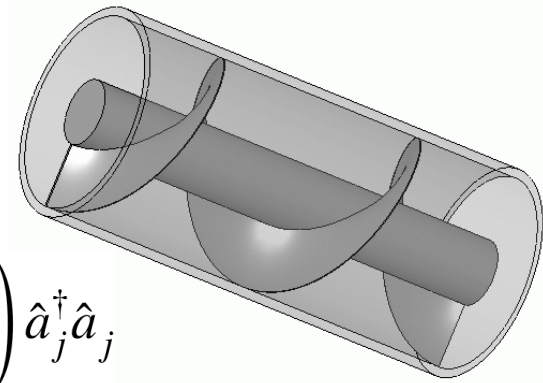
- Phase shift by magnetic field changes interference pattern/current



- Minimal current at $\Phi/\Phi_0 = 1/2$ (destructive interference)

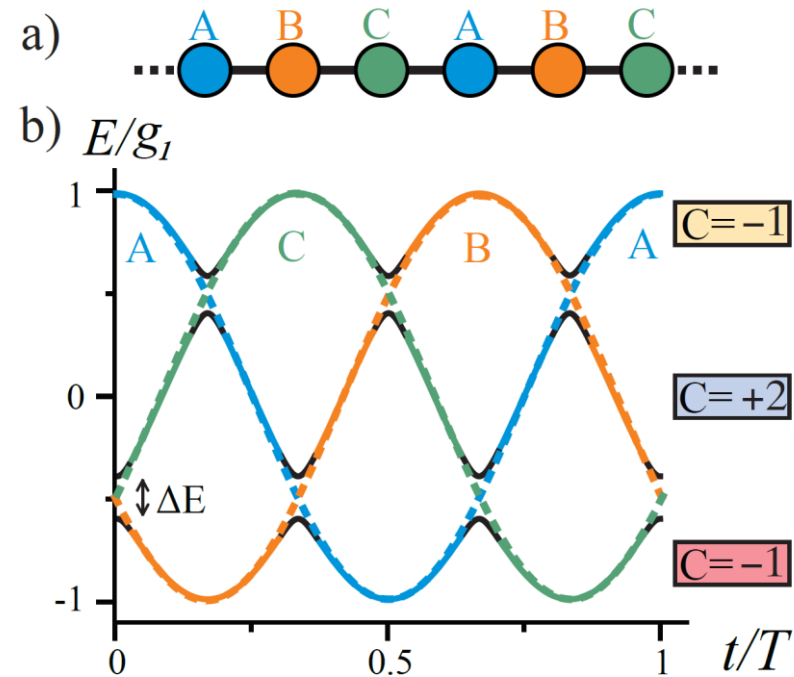


Topological pumping



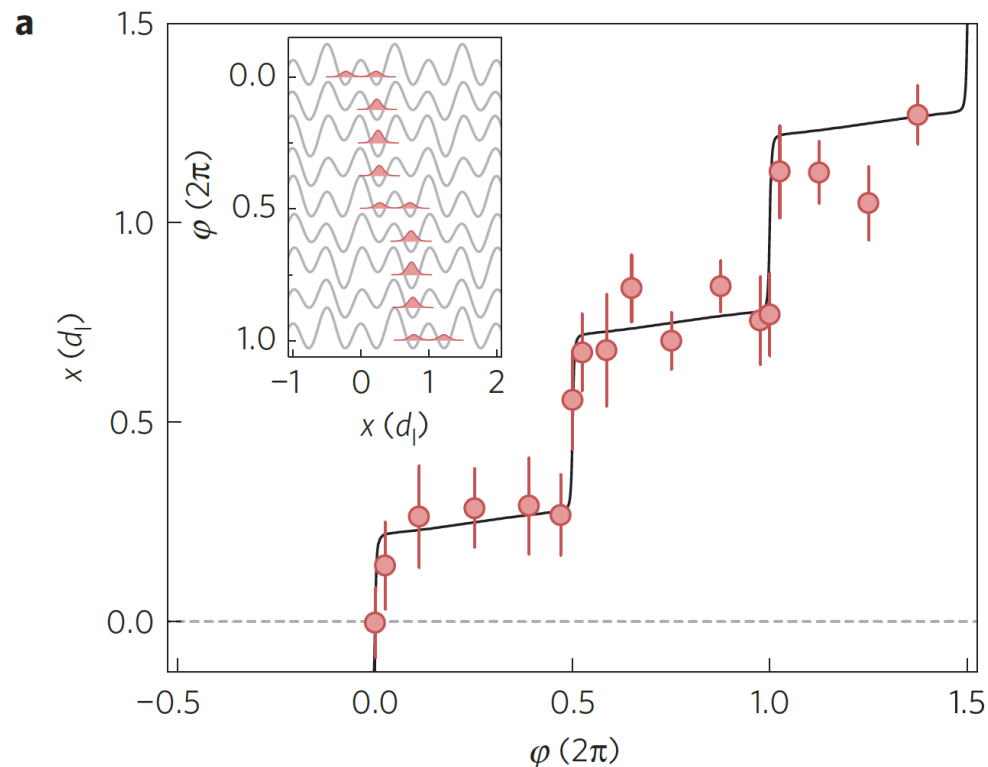
$$H(t) = -J \sum_j [\hat{a}_j^\dagger \hat{a}_{j+1} + \hat{a}_{j+1}^\dagger \hat{a}_j] + P \sum_j \cos\left(\frac{2\pi j}{3} - \Omega t\right) \hat{a}_j^\dagger \hat{a}_j$$

- on-site energy modulated in space (A,B,C) with period T
- $J=0$ disconnected (dashed)
- With $J>0$, three bands form (solid)
- Adiabatic modulation: Transport
- Speed of band depends on number of anti-crossings (Chern number \mathbf{C})
- Robust to random disorder if smaller than energy gap ΔE

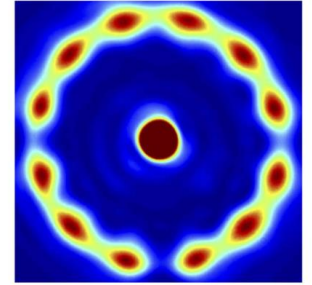
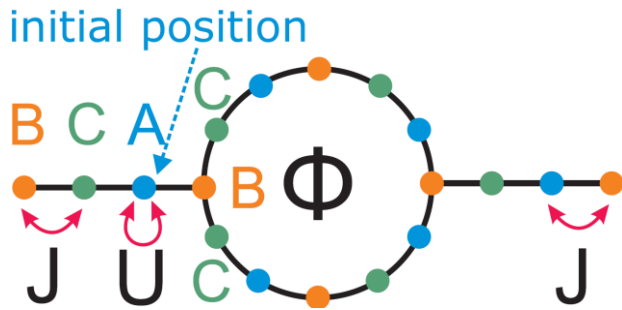


A Thouless quantum pump with ultracold bosonic atoms in an optical superlattice

M. Lohse^{1,2*}, C. Schweizer^{1,2}, O. Zilberberg³, M. Aidelsburger^{1,2} and I. Bloch^{1,2}



Topological Pumping in ring-lead system



$$H = H_R + H_S + H_D + H_L + H_P$$

$$H_R = - \sum_{j=1}^{L_R} (J e^{i2\pi\Phi} \hat{a}_j^\dagger \hat{a}_{j+1} + HC) + U/2 \sum_{j=1}^{L_R} \hat{n}_j^a (\hat{n}_j^a - 1)$$

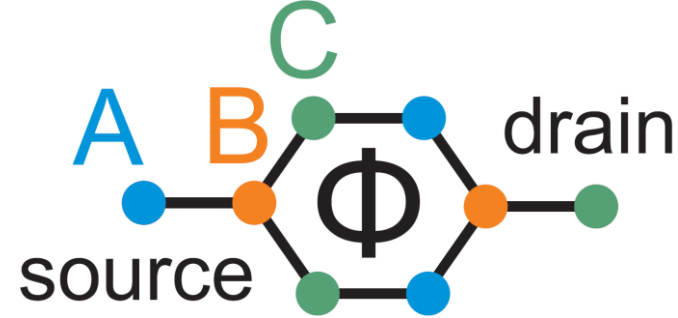
$$H_S = - \sum_{j=1}^{L_R} (J \hat{s}_j^\dagger \hat{s}_{j+1} + HC) + U/2 \sum_{j=1}^{L_R} \hat{n}_j^s (\hat{n}_j^s - 1)$$

$$H_D = - \sum_{j=1}^{L_R} (J \hat{d}_j^\dagger \hat{d}_{j+1} + HC) + U/2 \sum_{j=1}^{L_R} \hat{n}_j^d (\hat{n}_j^d - 1)$$

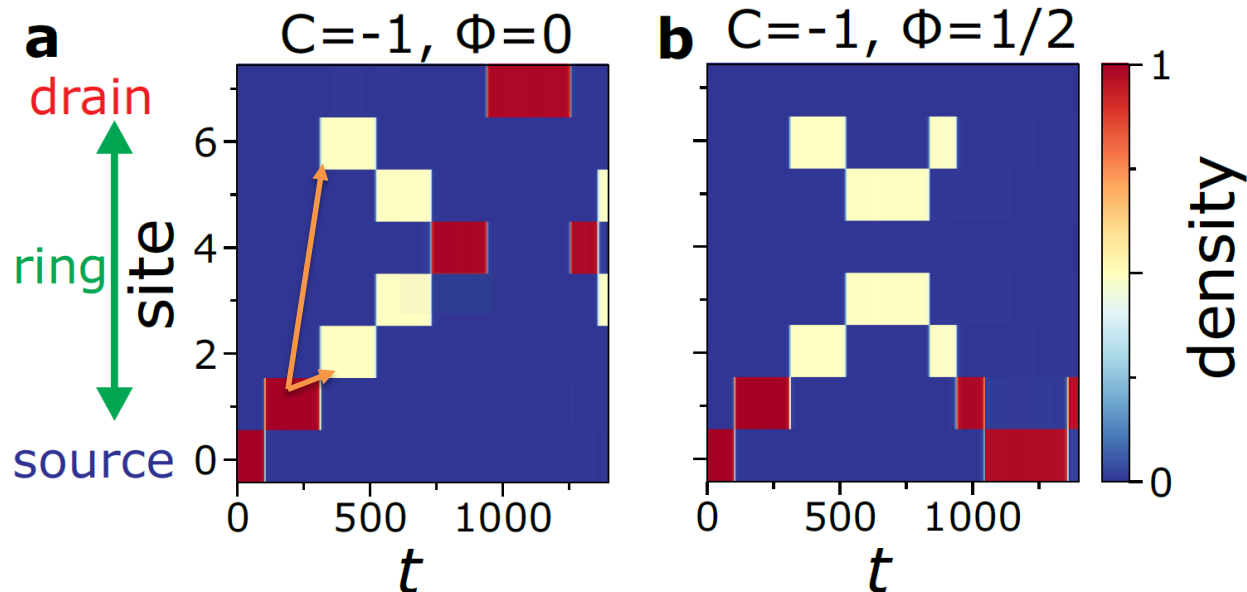
$$H_L = -J(\hat{a}_0^\dagger \hat{s}_0 + \hat{a}_{L_r/2}^\dagger \hat{d}_0 + HC)$$

$$H_P(t) = P_0 \sum_j \cos \left(\frac{2\pi j}{3} - \phi_0 - \Omega t \right) \hat{n}_j$$

Single atom dynamics



- Prepare in bottom band (Chern number -1)
- Φ phase shift between upper and lower path
- Total transmission for $\Phi=0$, total reflection for $\Phi=1/2$
- Reflected atom moves twice as fast in band with Chern number $2 \rightarrow$ AB reflection occur via transitions to band with Chern number of opposite sign!



Interaction and pumping

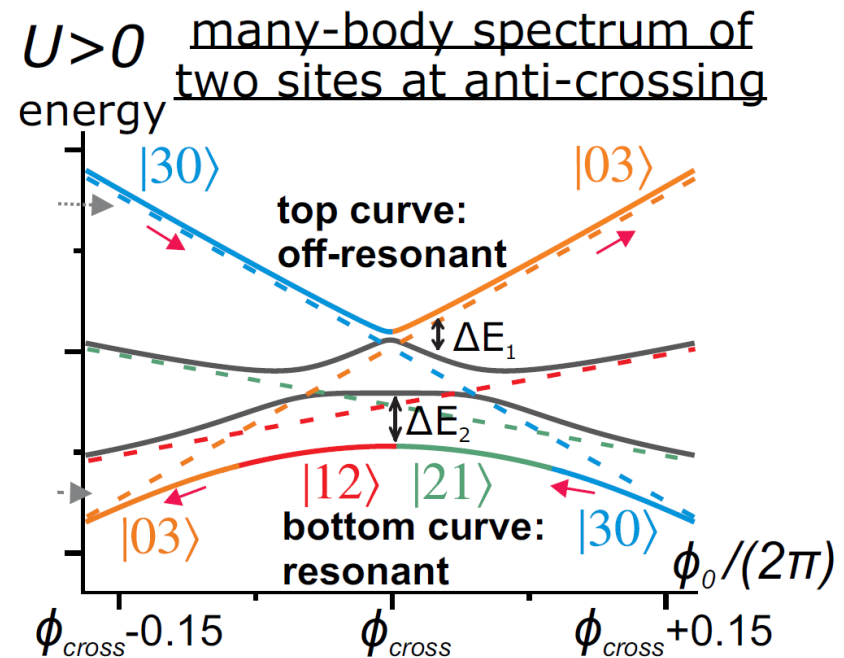
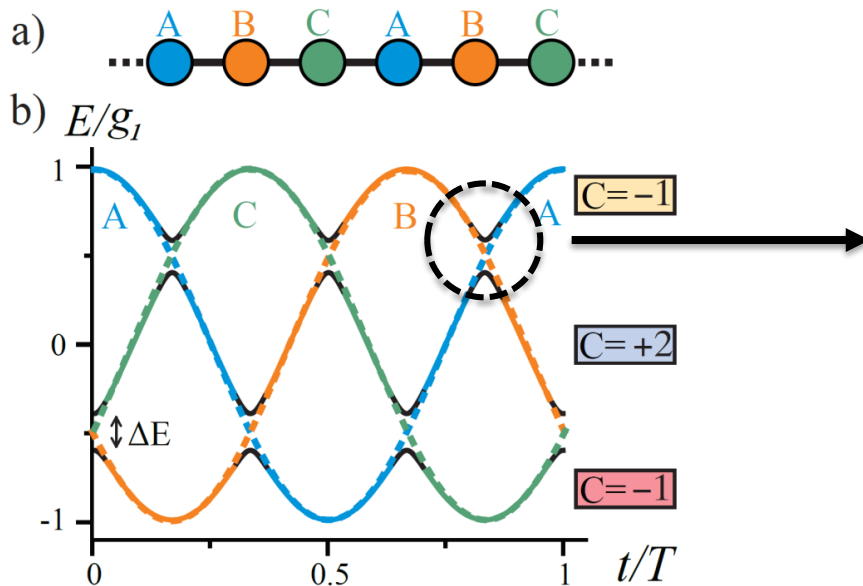
- Topology is property of non-interacting bands
- How does it fare with interacting atoms?



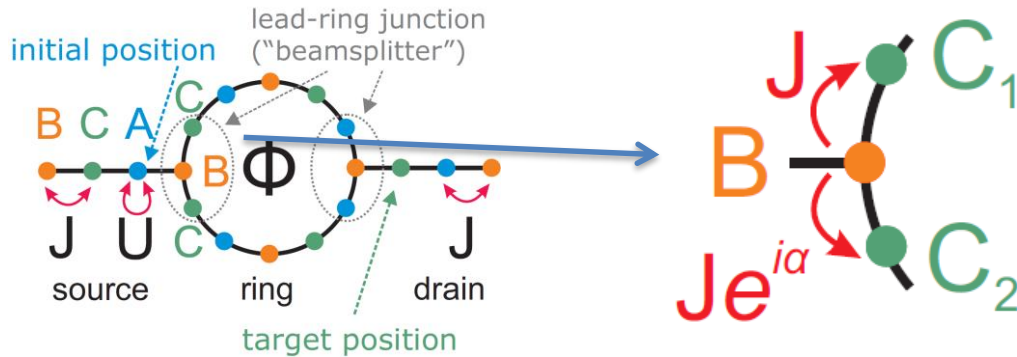
- Interaction → Topological pumping can break down
 - However: Highly localized states of many particles (=bound states) behave similar to free particles → Pumping survives
- can generate **entanglement** and modify energy gaps

Effect of interaction

- Gap without interaction U : $\Delta E = 2J$
- U creates asymmetry in upper&lower path in anti-crossing
- Top band: Off-resonant coupling, all particles tunnel as a whole $\Delta E_1 \propto J^N / U^{N-1}$
- Bottom band: Resonant coupling, single particles tunnel one after the other $\Delta E_2 = 2\sqrt{N}J$



Effect of interaction at ring-lead interface



- Top band: NOON states
 - Enhanced AB phase $\sim N$

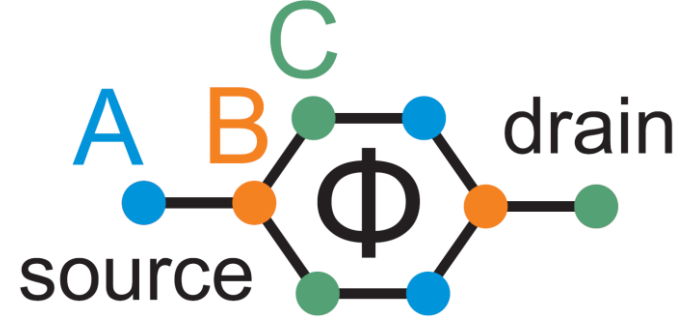
<i>Initial Fock state</i>	<i>Final Fock state</i>
$ 3\rangle_B \otimes 00\rangle_{C_1 C_2}$	$ 0\rangle_B \otimes 30\rangle_{C_1 C_2} + e^{i3\alpha} 0\rangle_B \otimes 03\rangle_{C_1 C_2}$
$ 4\rangle_B \otimes 00\rangle_{C_1 C_2}$	$ 0\rangle_B \otimes 40\rangle_{C_1 C_2} + e^{i4\alpha} 0\rangle_B \otimes 04\rangle_{C_1 C_2}$

- Bottom band: Bell-like states
 - Even number of atoms: absence of AB phase

$$|3\rangle_B \otimes |00\rangle_{C_1 C_2} \rightarrow |0\rangle_B \otimes |21\rangle_{C_1 C_2} + e^{i\alpha} |0\rangle_B \otimes |12\rangle_{C_1 C_2}$$

$$|4\rangle_B \otimes |00\rangle_{C_1 C_2} \rightarrow |0\rangle_B \otimes |22\rangle_{C_1 C_2}$$

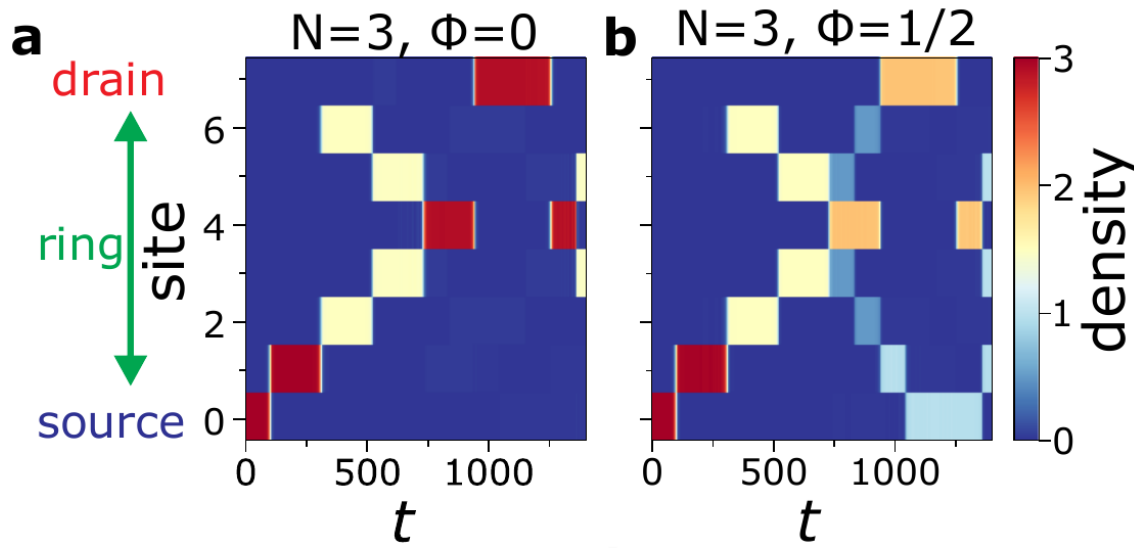
Many-atom dynamics



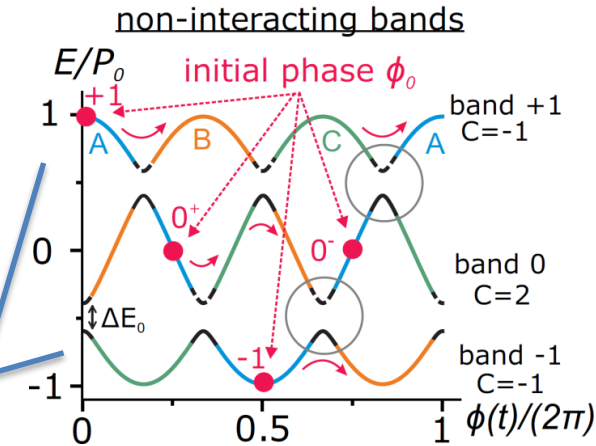
- Prepare N atoms in bottom band (Chern number -1)
- Odd N :
 - $\Phi=0$: Total transmission
 - $\Phi=1/2$: one atom reflected, $N-1$ transmitted
- Even N :
 - Always total transmission for any Φ

$$|3\rangle_B \otimes |00\rangle_{C_1 C_2} \rightarrow |0\rangle_B \otimes |21\rangle_{C_1 C_2} + e^{i\alpha} |0\rangle_B \otimes |12\rangle_{C_1 C_2}$$

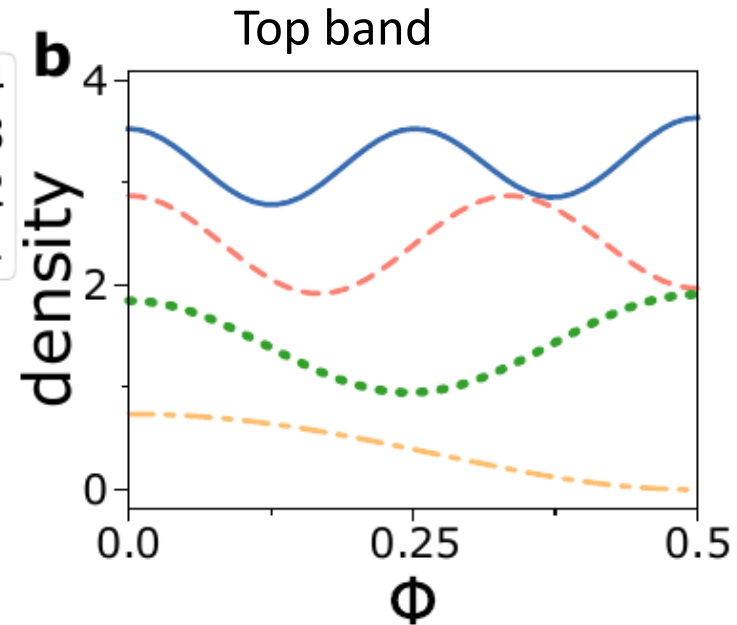
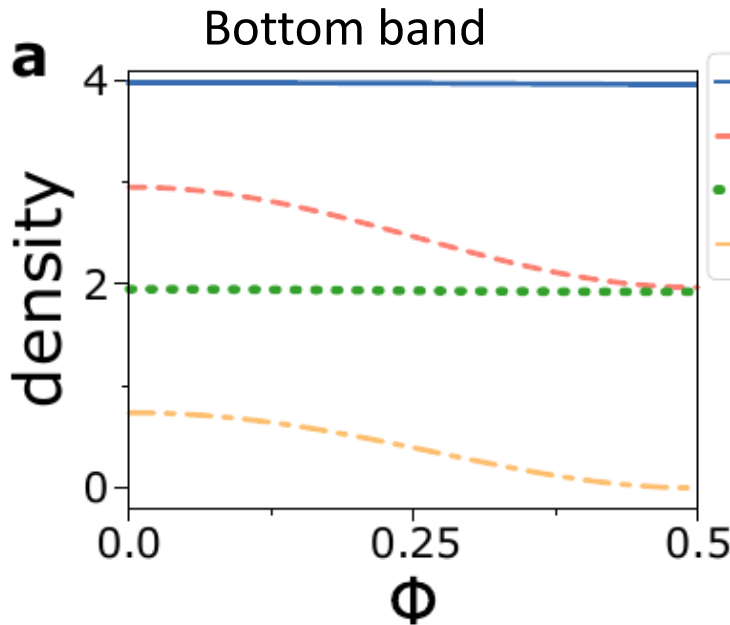
$$|4\rangle_B \otimes |00\rangle_{C_1 C_2} \rightarrow |0\rangle_B \otimes |22\rangle_{C_1 C_2}$$



AB transmission



- Density pumped into the drain (transmission) depends on flux

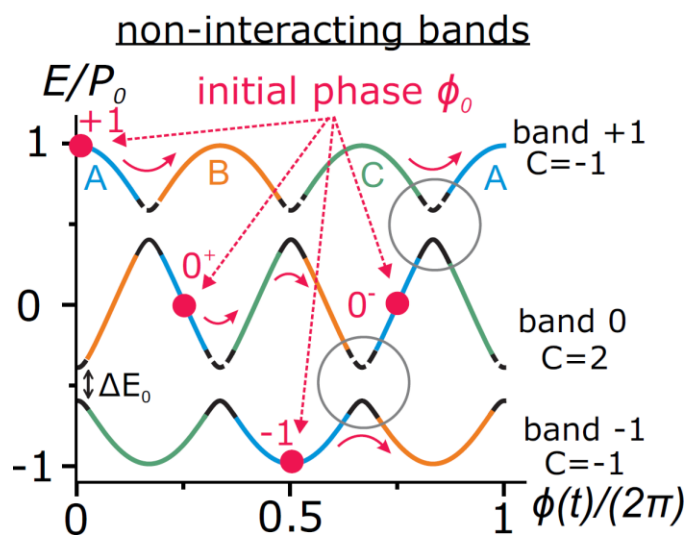


- Parity effect: Even and odd number of particles N behave differently

- Periodicity of flux $1/N$
- NOON states in ring

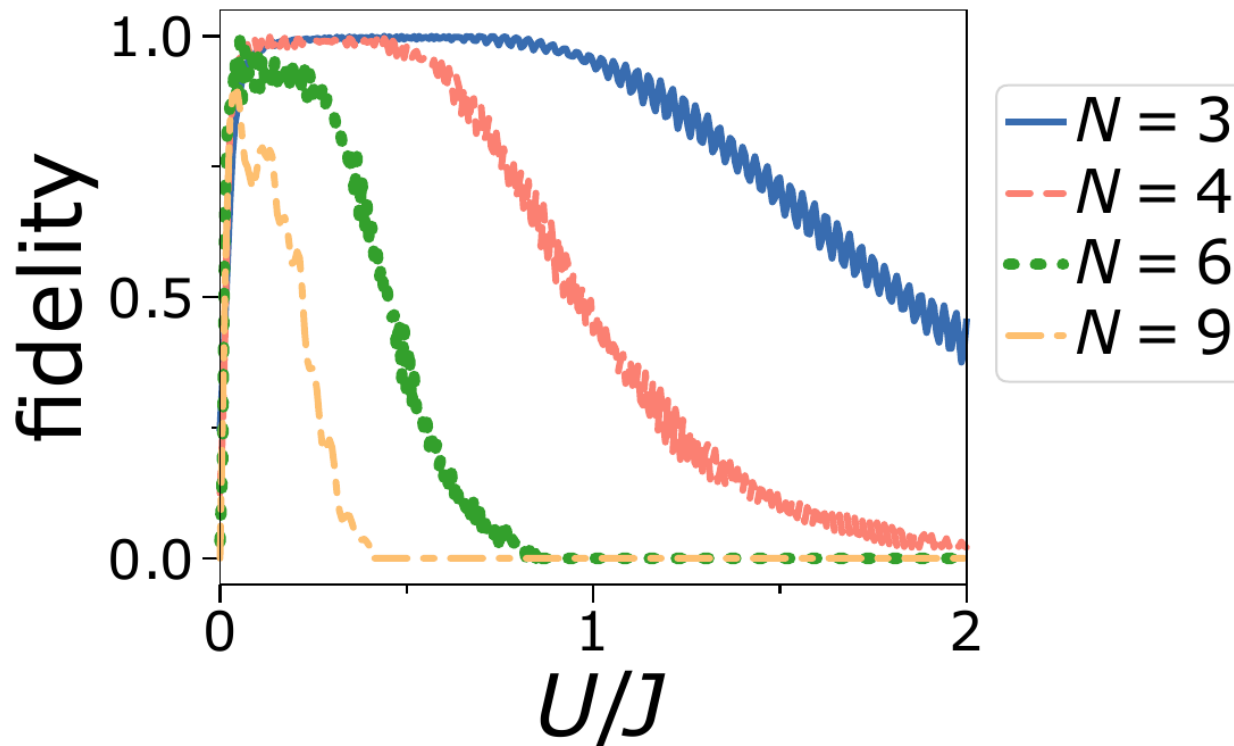
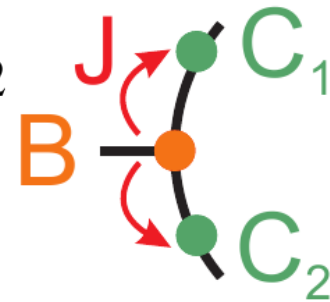
Topological pumping and Aharonov-Bohm

band $U > 0$	ring length L_R	transmission N even $T_{\text{even}}(\Phi, N)$	transmission N odd $T_{\text{odd}}(\Phi, N)$	Chern number	ϕ_0	AB period Φ_0	parity effect	state in ring	band gap ΔE
+1	$2n$	$N - 1 + \cos^2(\pi\Phi N)$	$N - 1 + \cos^2(\pi\Phi N)$	-1	0	$1/N$	no	NOON type	J^N / U^{N-1}
0^+	$4n + 2$	$N - 1 + \cos^2(\pi\Phi N)$	$N - 1 + \cos^2(\pi\Phi N)$	2	$\pi/2$	$1/N$	no	NOON type	J^N / U^{N-1}
0^+	$4n$	$\sin^2(\pi\Phi N)$	$\cos^2(\pi\Phi N)$	2	$\pi/2$	$1/N$	yes	NOON type	J^N / U^{N-1}
0^-	$4n$	0	$\cos^2(\pi\Phi)$	2	$-\pi/2$	1	yes	varies	J^N / U^{N-1}
0^-	$4n + 2$	N	$N - 1 + \cos^2(\pi\Phi)$	2	$-\pi/2$	1	yes	varies	J^N / U^{N-1}
-1	$2n$	N	$N - 1 + \cos^2(\pi\Phi)$	-1	π	1	yes	varies	$2\sqrt{N}J$
$U = 0$ all bands	$2n$	$N \cos^2(\pi\Phi)$	$N \cos^2(\pi\Phi)$			1	no	superposition	$2J$



Fidelity to generate NOON state

- Consider lead-ring junction only
- Fidelity of adiabatically generating a NOON state for N particles for interaction U $F = |\langle \Psi_{\text{NOON}} | \Psi \rangle|^2$



Conclusions

- Topological pumping and topological AB phase interact in a non-trivial way
- AB reflection occur by transfer to different band with Chern number of opposite sign
- Can engineer highly entangled NOON states for quantum information or sensing
- Realize using time-dependent laser potentials for cold atoms