

# Symmetry reduction induced by anyon condensation: a tensor network approach

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*(Soon on the ArXiv...)*

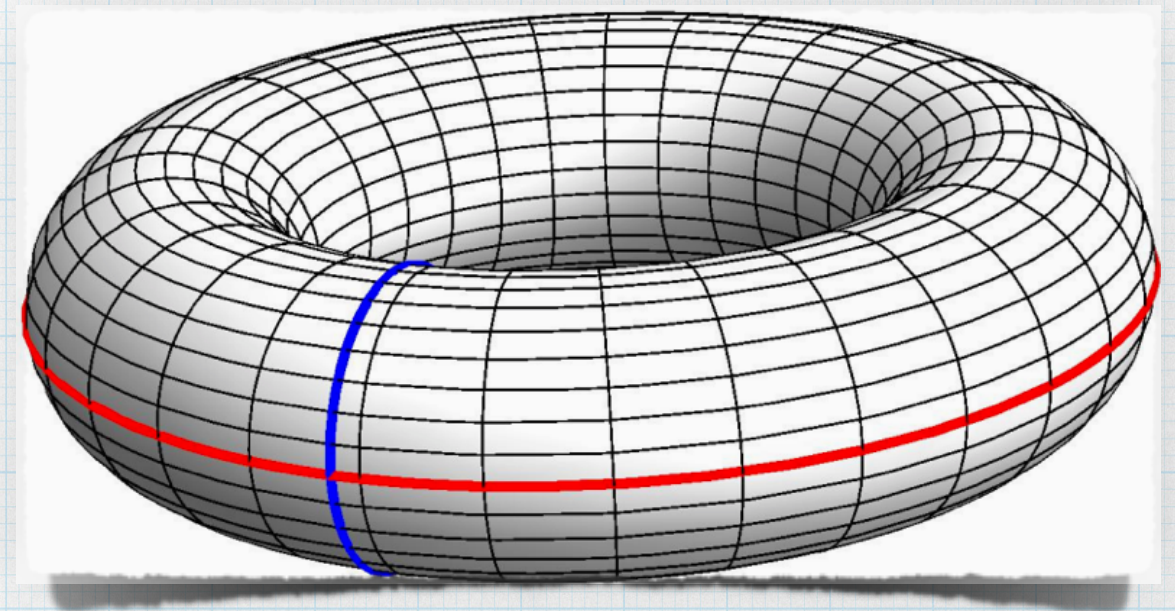
Funded by





# Topological order

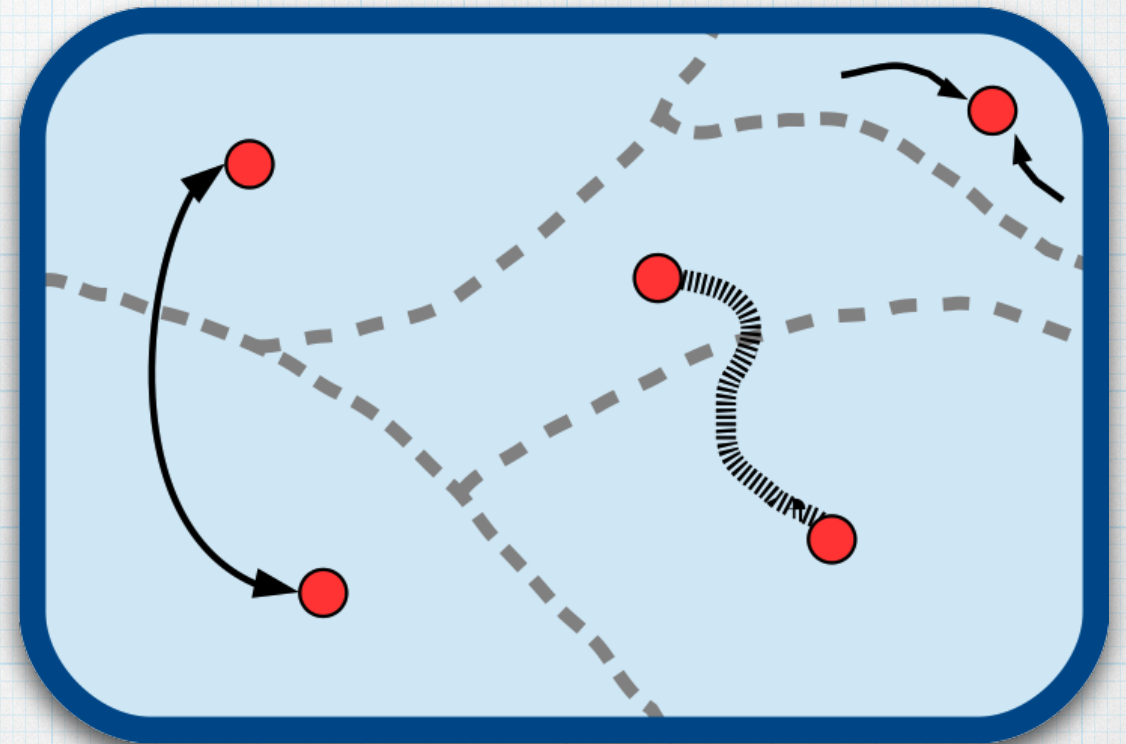
- \* No local order parameter classification
- \* GS Degeneracy- Exotic statistics of quasiparticle excitations
- \* RFP. Properties of anyons: Braiding-Fusion
- \* How do we go from one phase to another?





# Topological phase transitions and TN

- \* Relate two topological model restricting the topological content [1]
- \* Anyon Condensation: Spontaneous Symmetry Breaking (Sharp)
- \* Modelled with PEPS (path) [2]



[1] JHEP05(2003)068 Alexander F. Bais, Bernd J. Schroers, Joost K. Slingerland

[2] *Nature Communications* 6, 8284 (2015) J. Haegeman, V. Zauner, N. Schuch, F. Verstraete

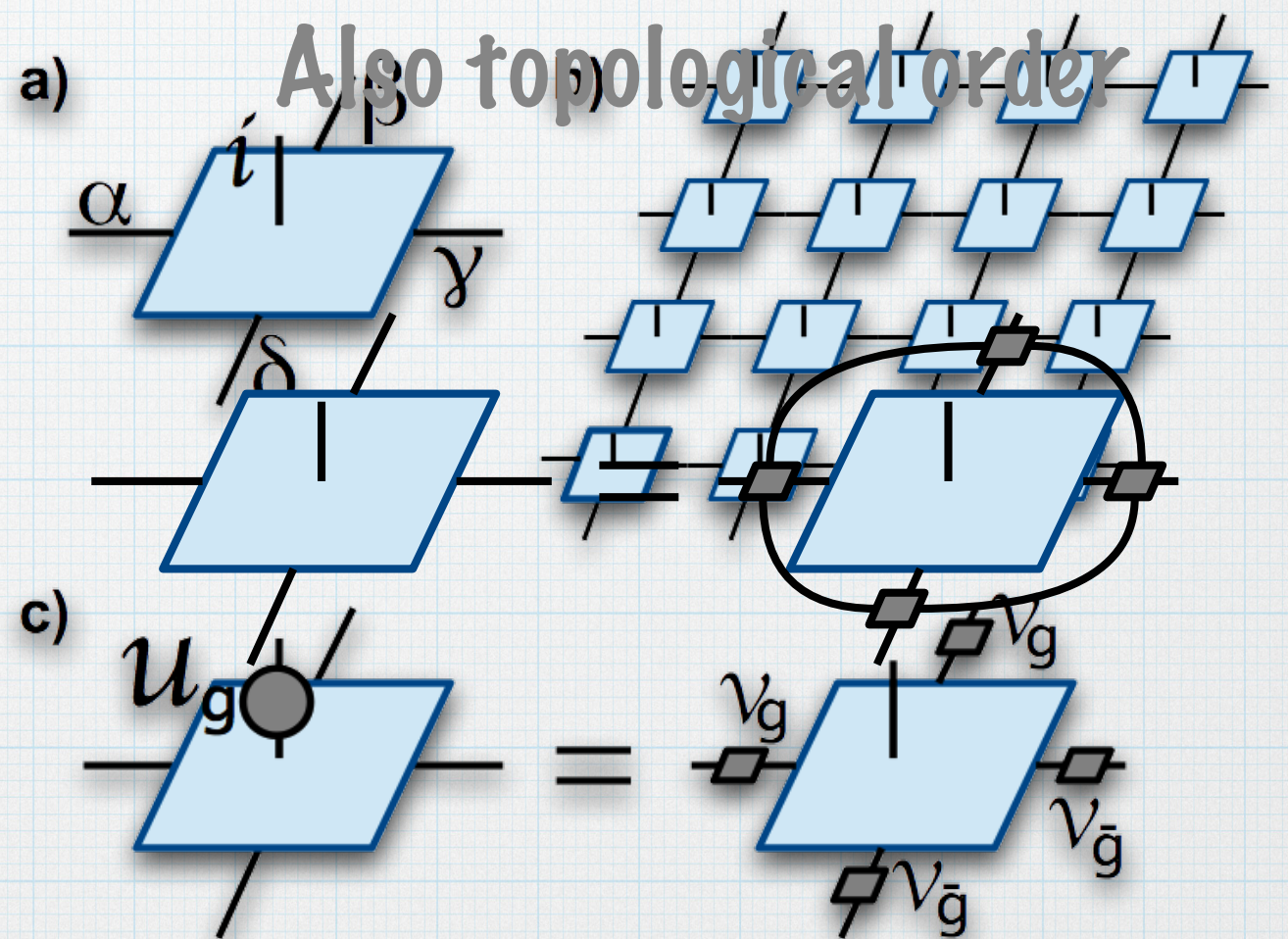


# Projected Entanglement Pair States (PEPS)

\* GS of local Hamiltonian-Area Law and topological order

\* Tensor Construction: Auxiliary d.o.f

\* Action under Global Symmetries





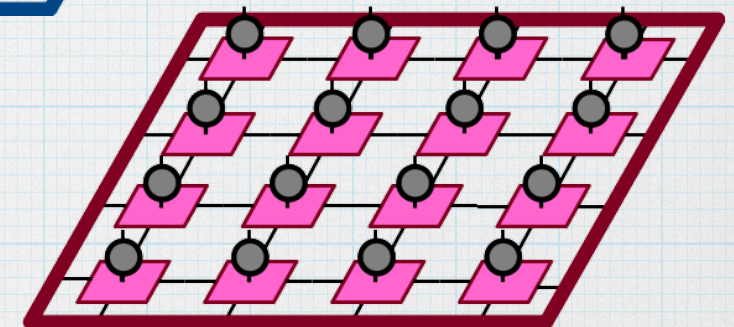
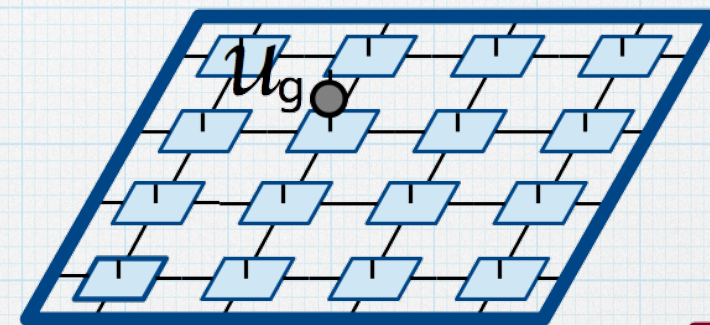
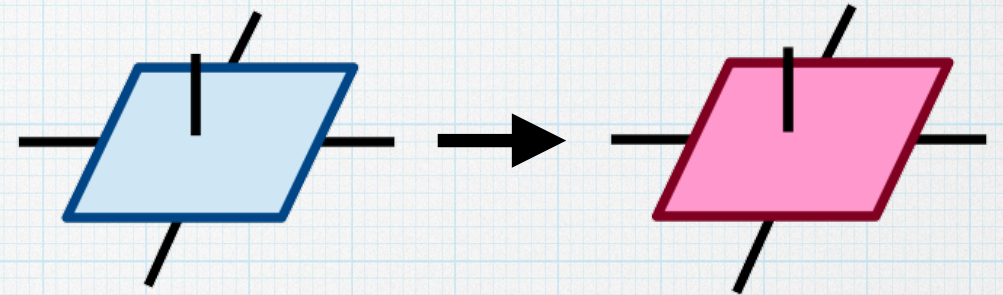
# Overview

- \* Motivation and introduction
- \* Our Work
- \* Global and gauge symmetries
- \* Symmetries over anyons
- \* Approach in 1D



# Our Work

- \* Pairs of PEPS connected by Anyon condensation (QD)
- \* We study symmetries: From Gauge to Global
- \* Charge condensation and Flux Confinement
- \* Global Symmetry over Anyons



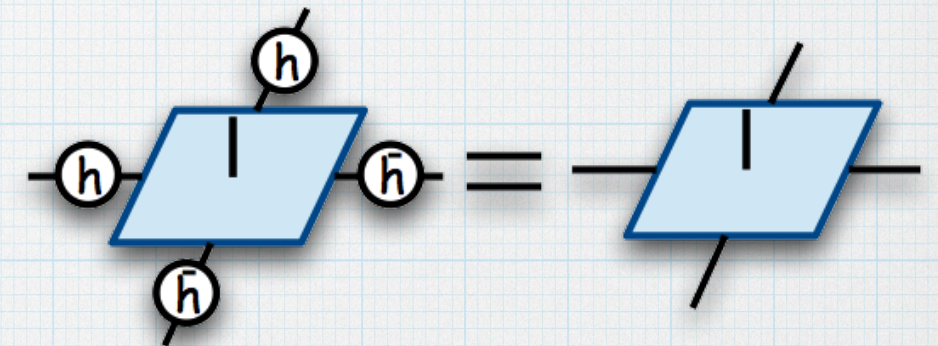
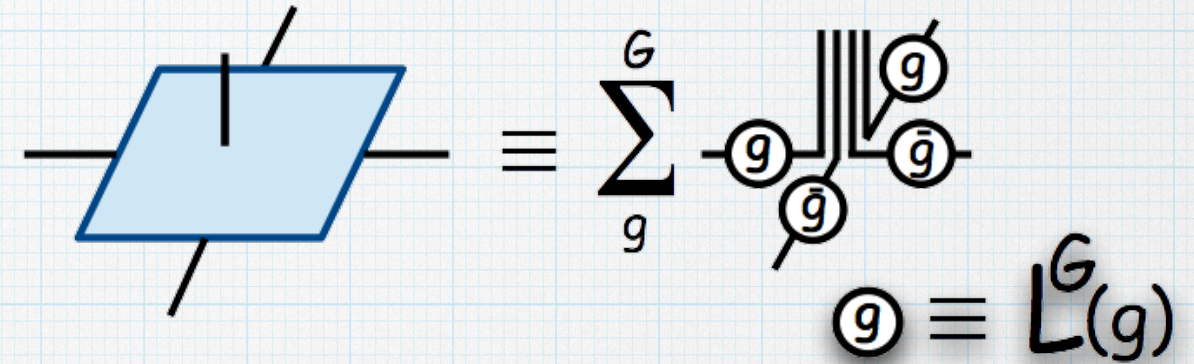


# Parent Tensor: $G$ -isometric PEPS [2]

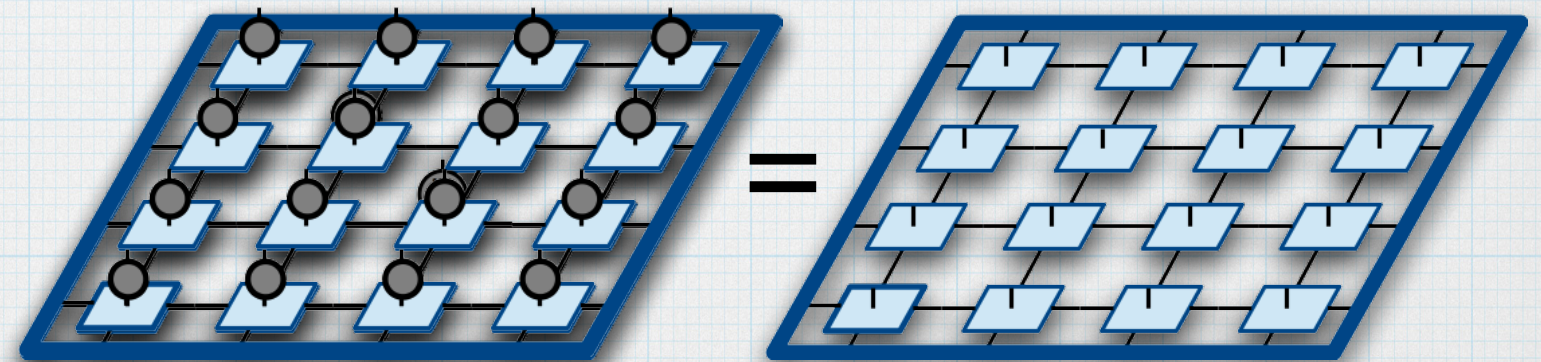
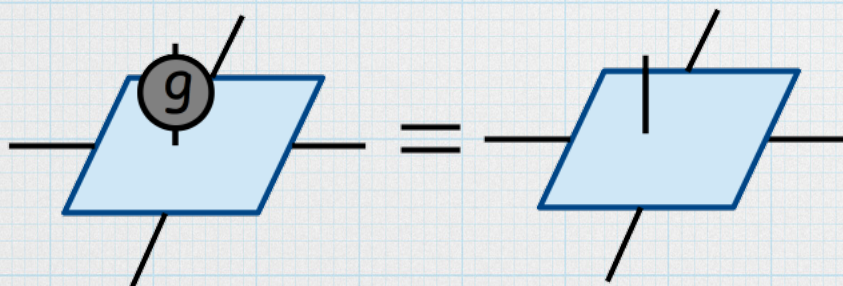
\* Quantum Double of  $G$ .

\* Local Gauge Symmetry of  $G$

\* Gauge invariance on the virtual d.o.f



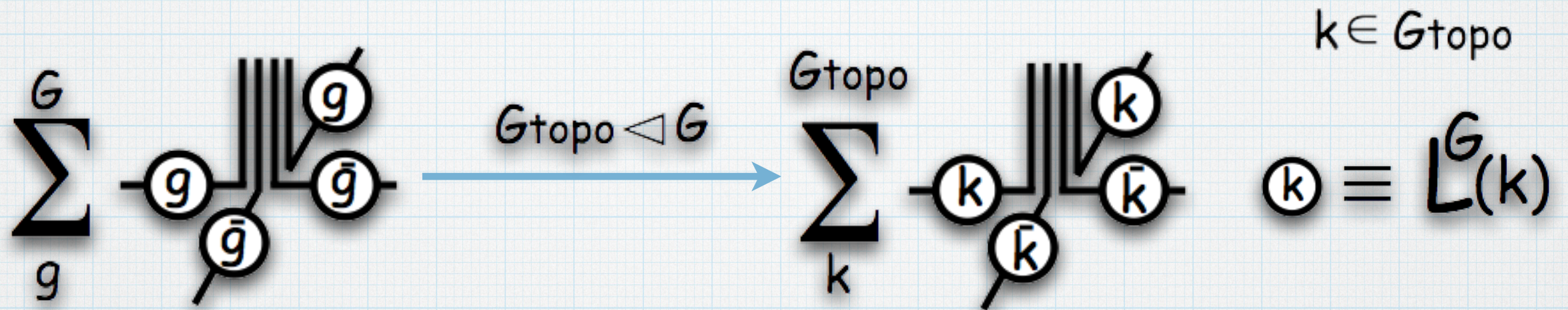
$$U_h = \begin{array}{c} | \textcircled{h} \\ | \textcircled{h} \\ | \textcircled{h} \\ | \textcircled{h} \end{array} \equiv \textcircled{h}$$



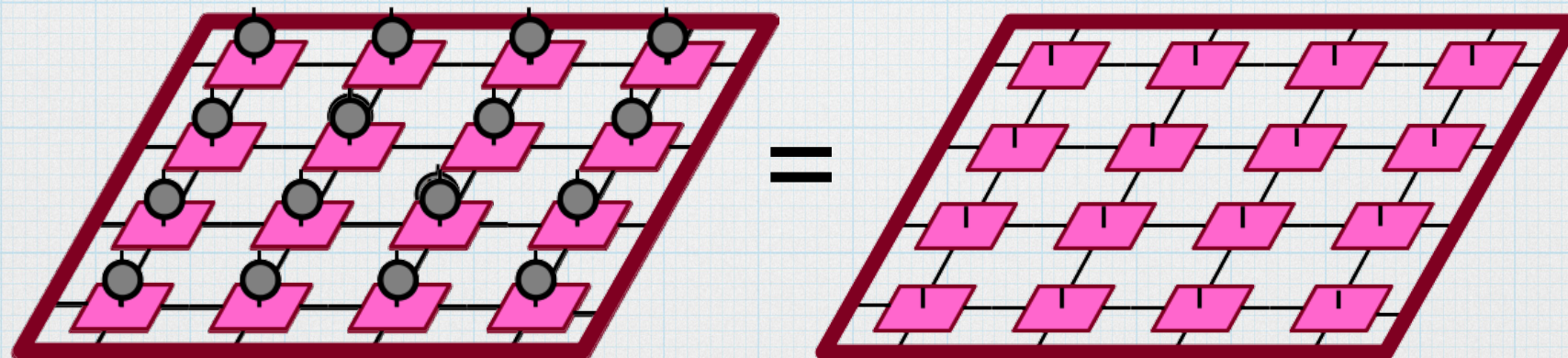
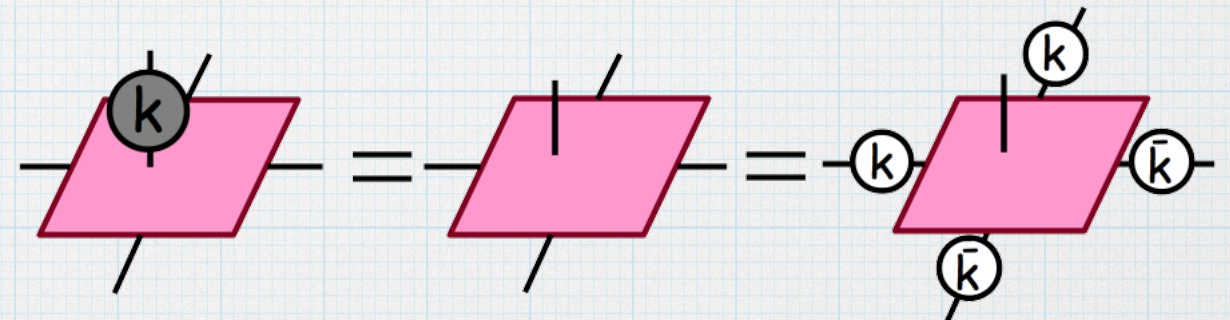


# Restricted Tensor

Anyon Condensation  $\longleftrightarrow$  Restrict Gauge invariance

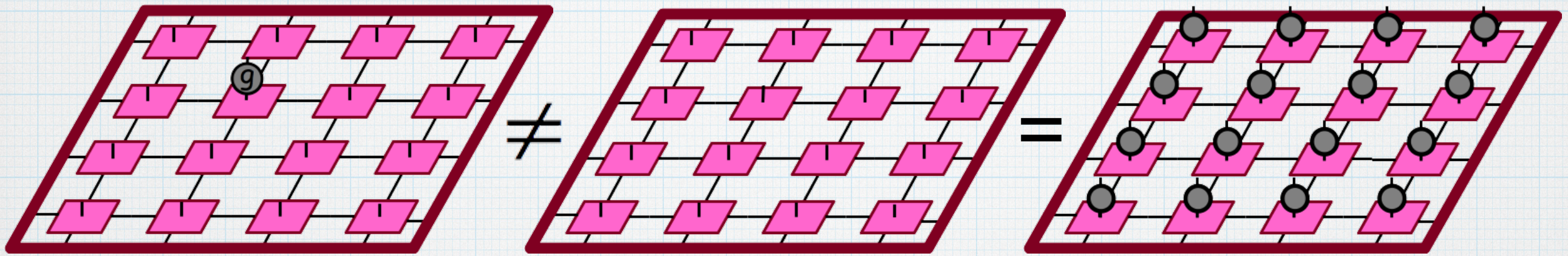
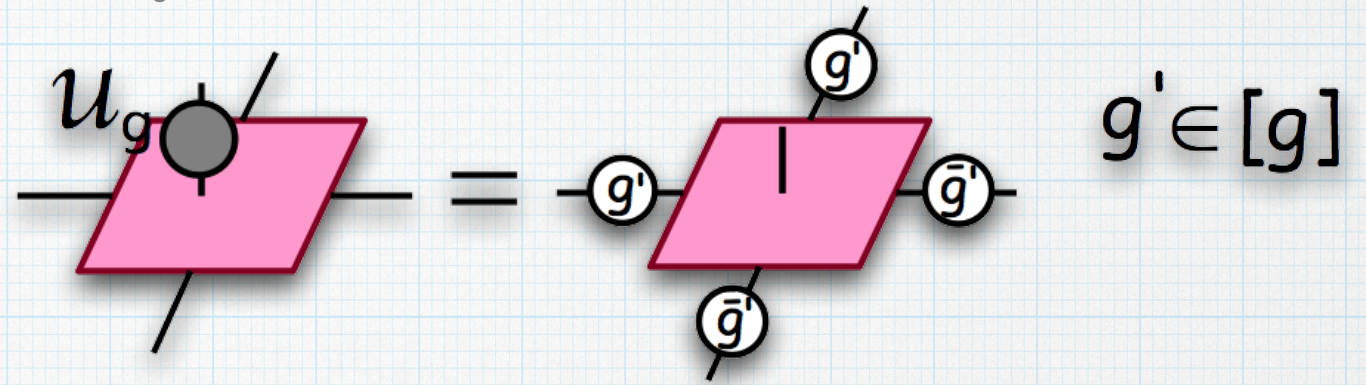


$G_{\text{topo}}$  Gauge invariance

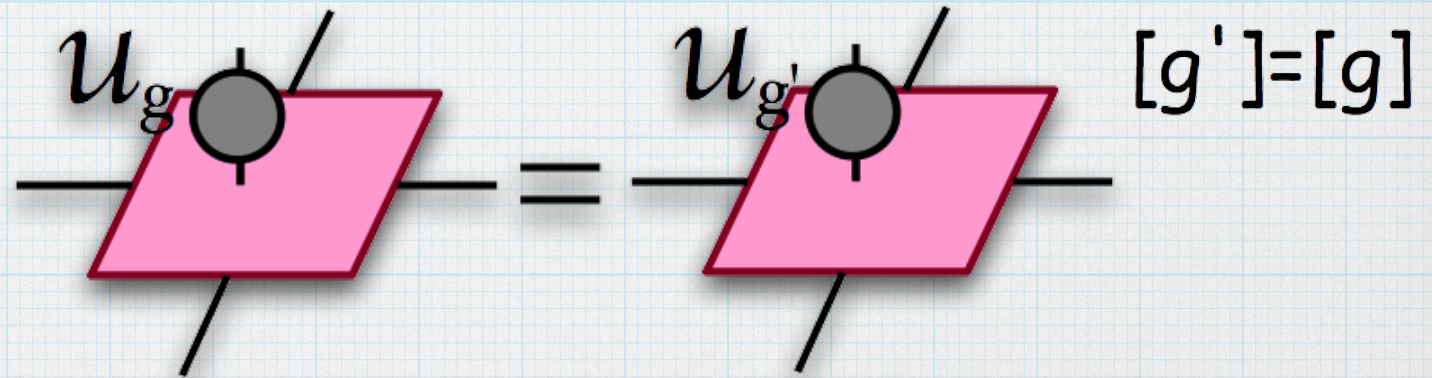




$G$  is no longer a gauge symmetry



$$G/G_{\text{topo}} \simeq G_{\text{sym}}$$



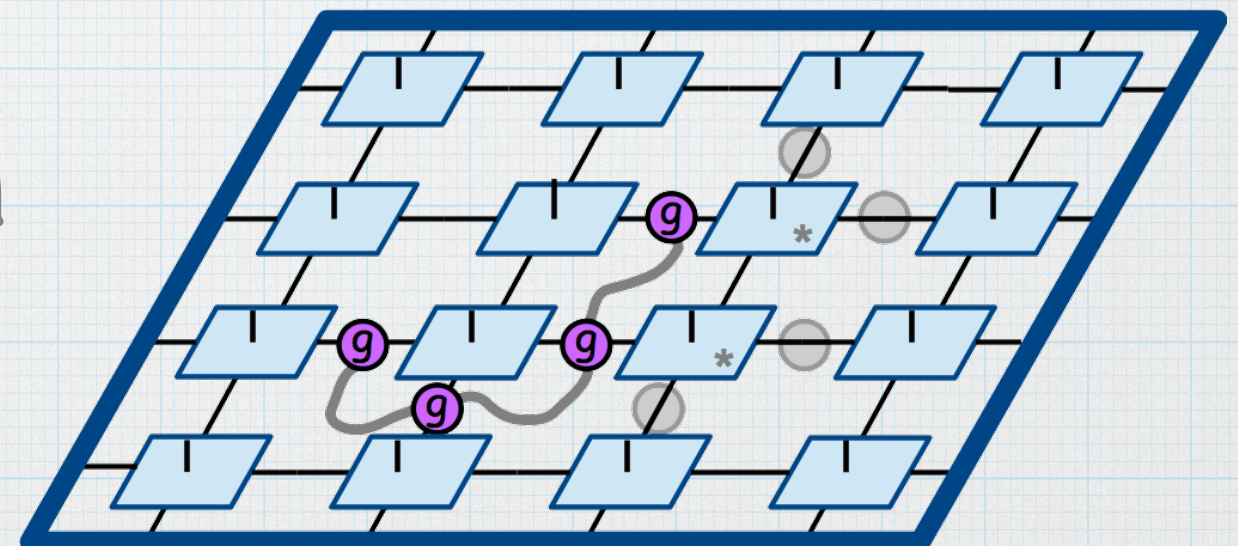
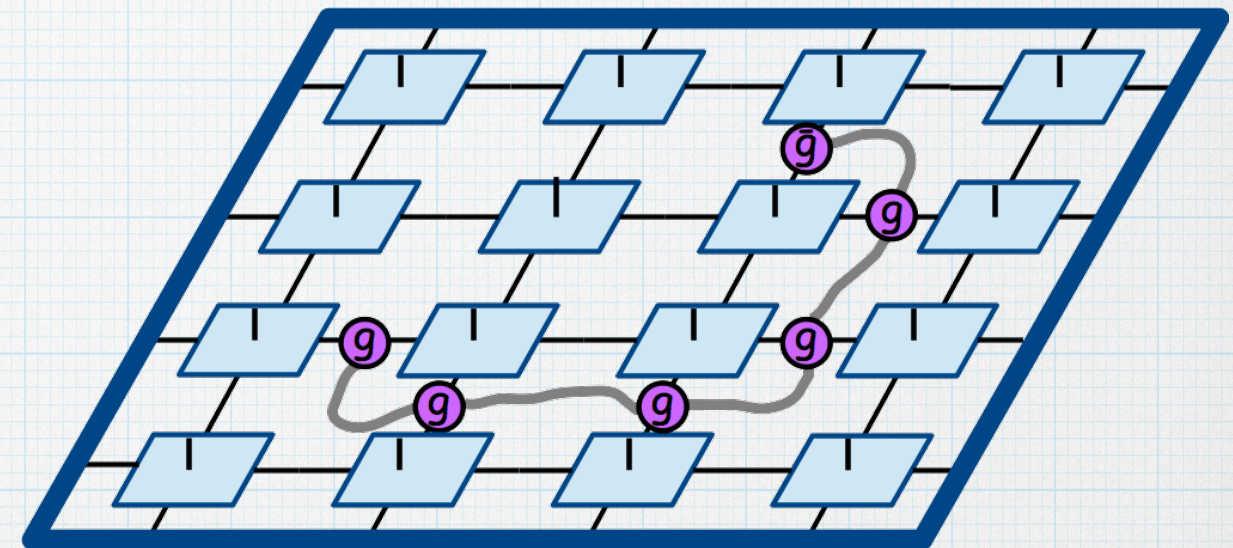
Pure  $G$  Gauge symmetry

$G_{\text{topo}}$  Gauge symmetry +  $G_{\text{sym}}$  Global symmetry



# Pure Flux excitations

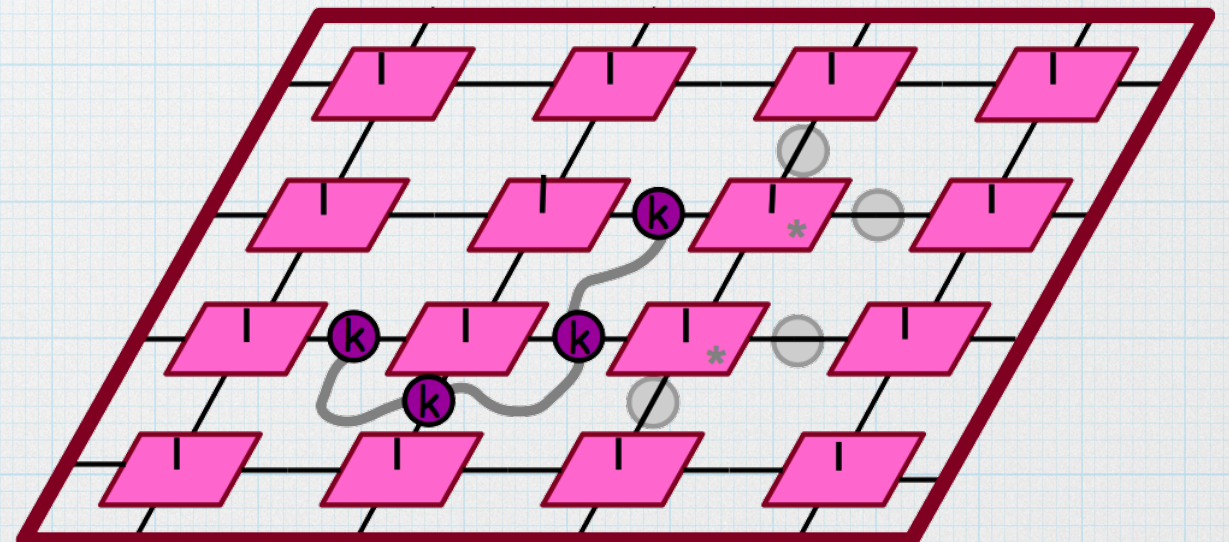
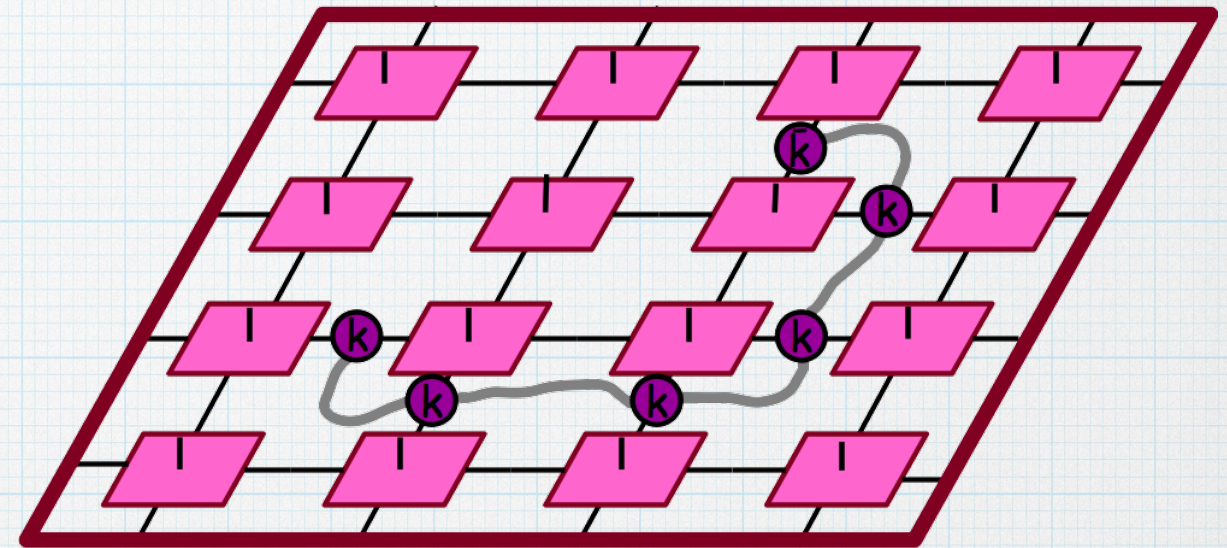
- \* Flux Excitations on Parent Model
- \* Possibility of deforming freely
- \* Energy independence on length





# Pure Flux excitations

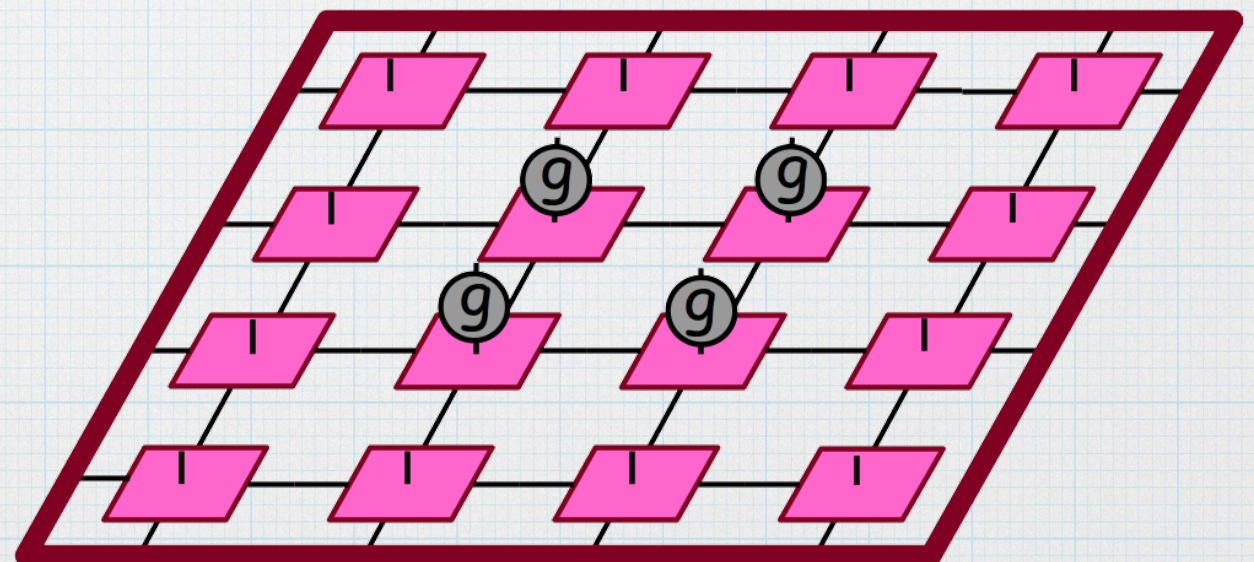
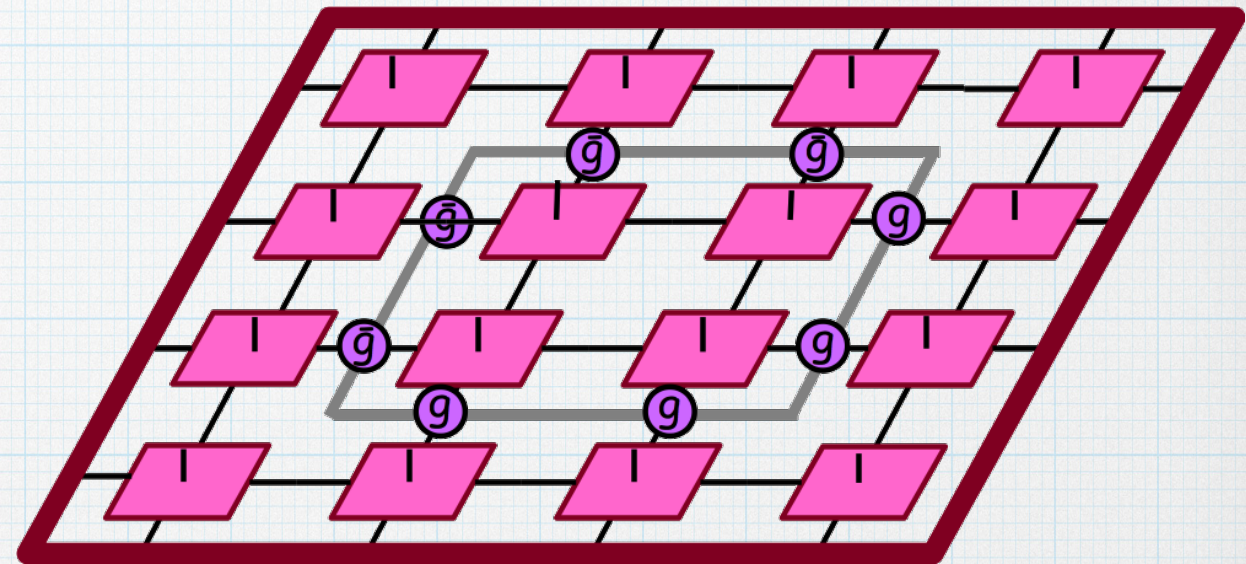
- \* Flux Excitations on Restricted Model
- \* Possibility of deforming freely
- \* Energy independence on length





# Flux Confinement

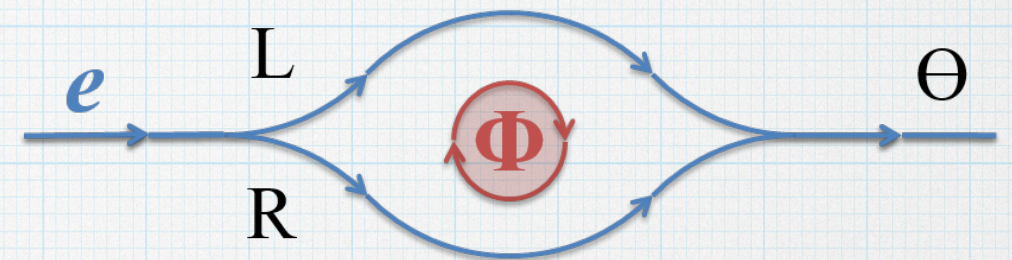
- \* Insert Flux Excitation on Restricted Model
- \* Impossibility of moving freely
- \* Energy dependence on length





# Charge Condensation

- \* Braiding with unconfined fluxes



- \* Indistinguishable from vacuum using braiding

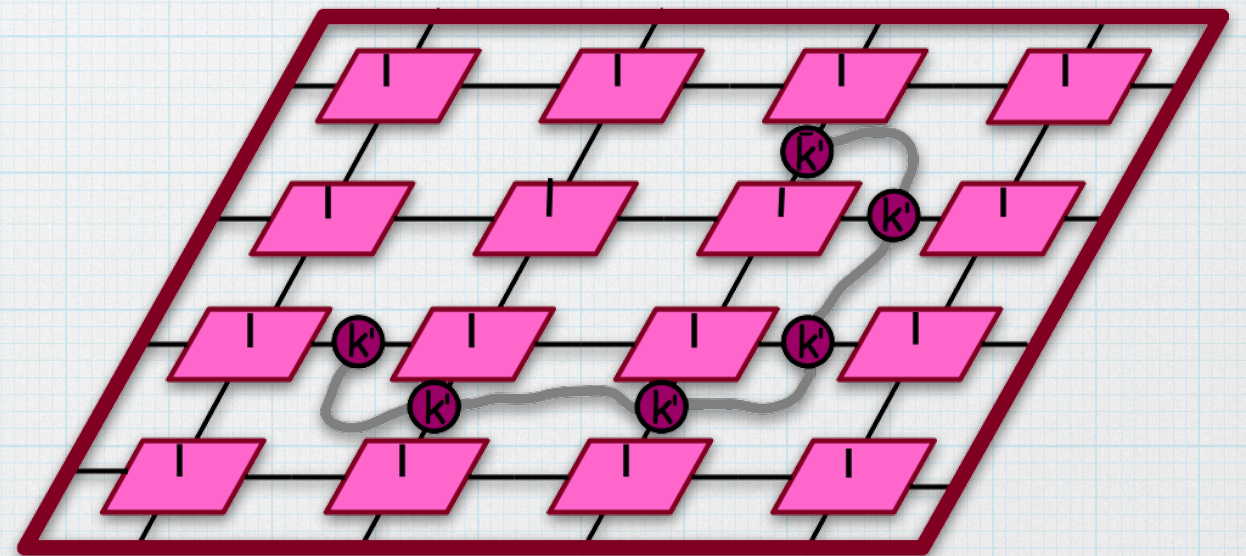
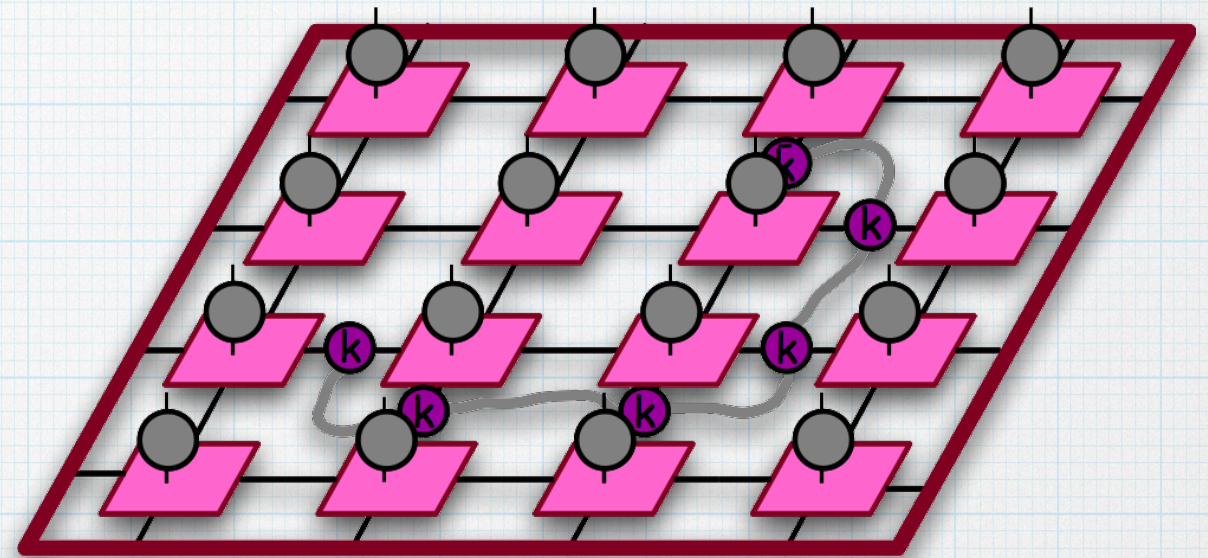
- \* Not topological excitation- Trivial Sector

$$\left| \frac{\chi_R^G(k)}{|R|} \right|^2 = 1$$



# Global Symmetries over Anyons: Pure Flux case

- \* Pair of fluxes  $C[k]$  + global symmetry action  $Ug$
- \* The action of  $Ug$  conjugates:  
 $k' = gkg^{-1}$ ;  $C[k] \rightarrow C[k']$
- \* Homomorphism:  
 $p: G_{\text{sym}} \rightarrow \text{Aut}(G_{\text{topo}})$



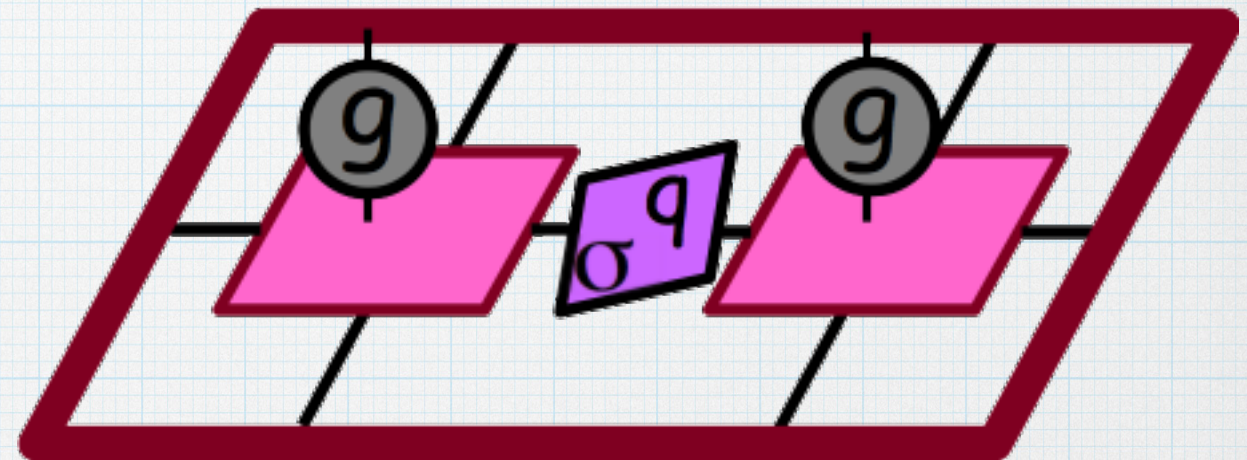


# Global Symmetries over Anyons: Pure Charge case

- \* Action of the symmetry permutes irreps [4]

- \* Cocycle function:  
 $w: G_{\text{sym}} \times G_{\text{sym}} \rightarrow G_{\text{topo}}$   
 $g'h'(gh')^{-1} = w(g,h)$

- \* Extension groups:  $(p, w)$



[4] H. Clifford, *Representations Induced in an Invariant Subgroup*, Annals of Mathematics 38 (3): 533-550, (1937)



# 1-D Approach: MPS

\* Topological order  $\rightarrow$  Symmetry Breaking Pattern

\* Action of Operator: Virtual representation of all phases

\* Induced Representation: Permutation + Projective representation [5]

$$\text{Pink Square} = \sum_k^N \text{Circle}(k) \otimes \text{Circle}(\bar{k})$$

$$\text{Pink Square} \stackrel{S_g}{=} \text{Circle}(g') \otimes \text{Pink Square} \otimes \text{Circle}(g')$$

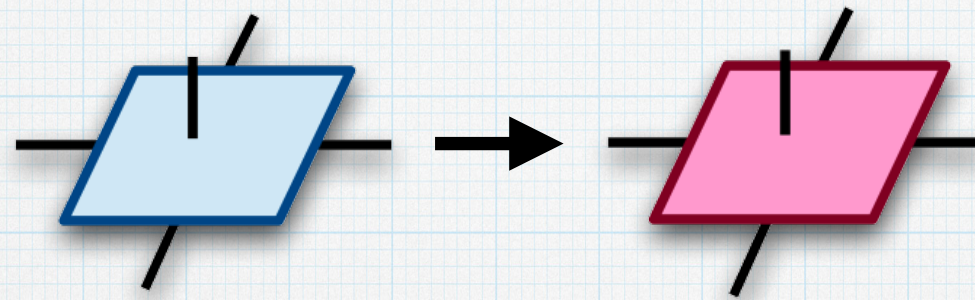
$$P_{g'} \left[ \bigoplus_{\alpha=1}^A V_{g'}^{\alpha} \otimes \bar{V}_{g'}^{\alpha} \right]$$

[5] Phys. Rev. B 84, 165139 (2011) Norbert Schuch, David Perez-Garcia, Ignacio Cirac

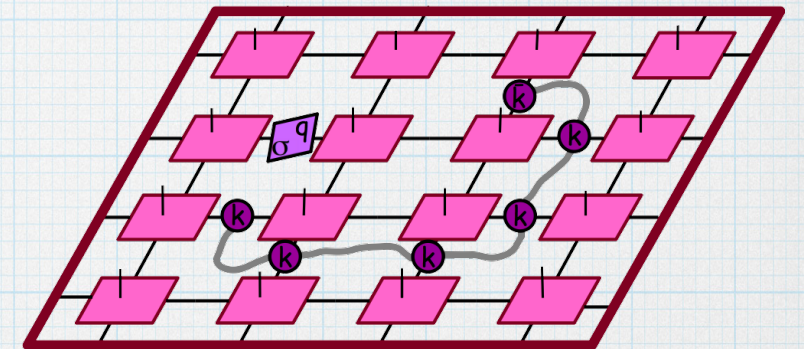


# Conclusion and Outlook

- \* Modifying the tensor: Symmetries by Condensation

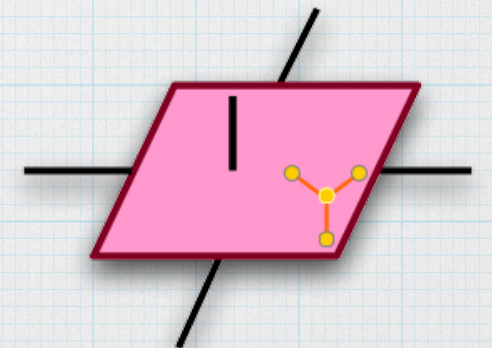


- \* TO, Local-Global, Anyon symmetries



- \* Generalizing the restricted tensor to flux condensator

- \* Combined Symmetry in all sectors  
(\* S.F. with twisted QD?)





Thank You!

CENTRO DE CIENCIAS DE BENASQUE  
PERDRO PASQUA

