The Niels Bohr Institute

UNIVERSITY OF COPENHAGEN

Quantum information processing with atoms coupled to waveguides and cavities

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Quantum Plasmonics, March 2015

Plasmonics: Strong confinement => emitters decay to wire



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∧ γ' ν γ1D

Theoretical model: Two level system coupled to waveguide.

Figure of merit $\beta = \frac{\gamma_{1D}}{\gamma_{1D} + \gamma'}$

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 $\gamma \gamma'$

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Figure of merit $\beta = \frac{\gamma_{1D}}{\gamma_{1D} + \gamma'}$

$$\begin{pmatrix} g \\ \kappa \\ \kappa \\ \gamma \end{pmatrix} \begin{pmatrix} \kappa \\ \kappa \\ \kappa \\ \kappa \end{pmatrix}$$

Plasmonics: Strong confinement => emitters decay to wire

 $\gamma \gamma'$

Theoretical model: Two level system coupled to waveguide.

Figure of merit $\beta = \frac{\gamma_{1D}}{\gamma_{1D} + \gamma'}$

$$\begin{pmatrix} \varphi \\ \varphi \\ \gamma \end{pmatrix} \stackrel{\kappa}{\checkmark} \qquad \text{Limit } \kappa \rightarrow \infty, \quad C = \frac{g^2}{\kappa \gamma} \quad \text{and } \gamma \text{ fixed}$$

Plasmonics: Strong confinement => emitters decay to wire

 $\gamma \gamma'$

Theoretical model: Two level system coupled to waveguide.

Figure of merit $\beta = \frac{\gamma_{1D}}{\gamma_{1D} + \gamma'}$

$$\begin{array}{ccc} & g \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & &$$

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Challenge: make gates between atoms

Cavity:





Challenge: make gates between atoms

Cavity:





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Cavity:



K

Works in principle

Challenge: make gates between atoms

Cavity:





Works in principle Fidelity limited $1 - F \propto \frac{1}{\sqrt{C}}$

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Waveguide:

Challenge: make gates between atoms

Cavity:





Works in principle Fidelity limited $1 - F \propto \frac{1}{\sqrt{C}}$

Waveguide:



Limited fidelity*: $1 - F \propto \sqrt{1 - \beta}$

Making use of imperfect coupling

Bad scaling can be overcome

Possible solutions:

- Probabilistic generation of entanglement¹

$$F \approx 1$$
, $P < 1$

- Measurement and feedback²

$$1 - F \propto \frac{1}{\eta C}$$

- Dissipative generation of entanglement³

$$1 - F \propto \frac{1}{C}$$

- Heralded quantum gates⁴ $F \approx 1, P < 1$
- ¹ C. Cabrillo, J. I. Cirac, P. García-Fernández, and P. Zoller, Phys. Rev. A 59, 1025 (1999).

² AS. and Klaus Mølmer, Phys. Rev. Lett. **91**, 097905 (2003).

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⁴L.-M. Duan, B. Wang, and H. J. Kimble, Phys. Rev. A **72**, 032333 (2005), J. Borregaard, P. Komar, E. Kessler, AS, and M. D. Lukin, arXiv: 1501.00956, PRL in press

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This talk

- Heralded quantum gates⁴ $F \approx 1$, P < 1

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Entangling superconducting qubits coupled to molecules in waveguides

Preliminary work

Probabilistic entanglement



Start $|00\rangle$ Photon click => $\frac{1}{\sqrt{2}}(|01\rangle \pm |10\rangle)$

Probabilistic entanglement



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Non-local entanglement generation

Highly important for quantum communication

Probabilistic entanglement



Start $|00\rangle$ Photon click => $\frac{1}{\sqrt{2}}(|01\rangle \pm |10\rangle)$

Non-local entanglement generation

Highly important for quantum communication

Waveguides: increase efficiency



Picture: Schoelkopf group

Highly advanced system for quantum computation

Can't couple to light => not useful for communication



Picture: Schoelkopf group

Highly advanced system for quantum computation

Can't couple to light => not useful for communication

Proposals: Put atom nearby => mediate coupling to light



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Problem: superconductors don't like light



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Highly advanced system for quantum computation

Can't couple to light => not useful for communication

Proposals: Put atom nearby => mediate coupling to light

Problem: superconductors don't like light

Send in light through waveguide => need very little light (one photon)

Molecules in waveguides

Experiments S. Faez, V. Sandoghdar: molecules in hollow core fiber



Can have good coupling^{*} $\beta \approx 10\%$

Low temperatures: transitions nearly radiatively limited

Only a single ground state => not useful as a qubit

*S. Faez, P.Türschmann, H. R. Haakh, S. Götzinger, and V. Sandoghdar, Phys. Rev. Lett. 113, 213601 (2014)



Transitions can have linear AC-Stark shift => couple to (charge) qubits



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Absorption





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Estimate: Dipole ID, distance 500 nm, Shift: 45 MHz



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Can in principle give "strong coupling"
Coupling molecules and qubits



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Can in principle give "strong coupling"



 $\begin{array}{l} |1\rangle \text{ Cooper pair on island} \\ |0\rangle \text{ No Cooper pair on island} \end{array} => Charge qubit \end{array}$



|1⟩ Cooper pair on island
|0⟩ No Cooper pair on island
=> Charge qubit

Qubit couple to molecular dipole



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Qubit couple to molecular dipole and all other dipoles



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Qubit couple to molecular dipole and all other dipoles = charge noise



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Noise suppressed by going to degeneracy $E_0=E_1$



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New eigenstates:

$$|\pm\rangle = \frac{|0\rangle \pm |1\rangle}{\sqrt{2}}$$



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$$|\pm\rangle = \frac{|0\rangle \pm |1\rangle}{\sqrt{2}}$$

Tunnelling average out noise => coupling to dipole average out





Add extra molecule



Add extra molecule

Nearby molecules: strong (optical) dipole-dipole interaction*



Add extra molecule

Nearby molecules: strong (optical) dipole-dipole interaction*

Tune into resonance => interaction don't average out



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Raman transition of coupled system





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Raman transition of coupled system



Entangling two qubits



Entangling two qubits





Entangling two qubits













Detect red photon =>
$$\frac{1}{\sqrt{2}}(|+-\rangle \pm |-+\rangle)$$



Detect red photon =>
$$\frac{1}{\sqrt{2}}(|+-\rangle \pm |-+\rangle)$$

Good coupling $\beta \gtrsim 10\%$

Qubits can be entangled by pulses containing 1-10 photons

Heralded gates in optical cavities

Heralded gates

Probabilistic generation of entanglement

Quantum gates



Click generate entangled state $\frac{1}{\sqrt{2}}(|01\rangle \pm |10\rangle)$

$$\frac{1}{\sqrt{2}}(|01\rangle \pm |10\rangle)$$

F ≈ 1, *P* << 1

Insensitive to losses



Deterministic, limited fidelity

$$1 - F \propto \frac{1}{\sqrt{C}}$$

Heralded gates

Probabilistic generation of entanglement

Quantum gates



- Click generate entangled state $\frac{1}{-}(|01\rangle + |10\rangle)$
- $\frac{1}{\sqrt{2}}(|01\rangle \pm |10\rangle)$

F ≈ 1, *P* << 1

Insensitive to losses



Deterministic, limited fidelity

$$1 - F \propto \frac{1}{\sqrt{C}}$$

Heralded gates: $F \approx 1, P < 1$?

Scattering gates





Scatter resonant photon off cavity

Atoms in $|0\rangle$ block cavity Photon only enters cavity if atoms are $|11\rangle$

^{*} L.-M. Duan, B. Wang, and H. J. Kimble, Phys. Rev. A 72, 032333 (2005)

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Works in principle but sensitive to losses



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\begin{array}{l} |00\rangle \rightarrow |00\rangle \\ |01\rangle \rightarrow |01\rangle \\ |10\rangle \rightarrow |10\rangle \\ |11\rangle \rightarrow -|11\rangle \end{array}
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 $|e\rangle$

g

 $|0\rangle$

Works in principle but sensitive to losses

Detect photon leaving cavity => high fidelity when detector clicks

^{*} L.-M. Duan, B. Wang, and H. J. Kimble, Phys. Rev. A **72**, 032333 (2005)

 $|0\rangle$



Requires: single photon source and efficient in/output, detection





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Solution: add auxiliary atom as source and detector



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Assume $|g\rangle$ to $|f\rangle$ transition closed





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Assume $|g\rangle$ to $|f\rangle$ transition closed

Any decay leaves the atom in |f
angle





Requires: single photon source and efficient in/output, detection

Solution: add auxiliary atom as source and detector

Assume $|g\rangle$ to $|f\rangle$ transition closed

Any decay leaves the atom in $|f\rangle$

Atom heralds succesful gate







Drive closed transition with two photon driving



Drive closed transition with two photon driving => It works



Drive closed transition with two photon driving => It works

Can make gate with $F \approx 1$ for ANY cavity



Drive closed transition with two photon driving => It works

Can make gate with $F \approx 1$ for ANY cavity

Probabilistic $1 - P \propto \frac{1}{\sqrt{C}}$



Drive closed transition with two photon driving => It works

Can make gate with $F \approx 1$ for ANY cavity Probabilistic $1 - P \propto \frac{1}{\sqrt{C}}$

Realistic Ex: ⁸⁷Rb, C = 100 $F = 1-10^{-3}$ P = 67% $\tau = 10 \ \mu s$

Loss in optical fibers: exponential damping

Long distance communication requires repeaters



Loss in optical fibers: exponential damping

Long distance communication requires repeaters



Generate entanglement over short distance

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Generate entanglement over short distance

Gates=> swap entanglement get swapped to long distance

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Generate entanglement over short distance

Gates=> swap entanglement get swapped to long distance

Loss in optical fibers: exponential damping

Long distance communication requires repeaters



Generate entanglement over short distance

Gates=> swap entanglement get swapped to long distance

Still works for probabilistic gates (scaling polynomial, not exponential)

Distance 1000 km, optimize over "all" parameters



^{*} J. Borregaard, P. Komar, E. Kessler, AS, and M. D. Lukin, in preparation

Distance 1000 km, optimize over "all" parameters



It is better to admit you don't know what to do than to do something wrong

^{*} J. Borregaard, P. Komar, E. Kessler, AS, and M. D. Lukin, in preparation

Conclusion

Light matter interaction essential for quantum communication

Direct connections with light have a bad scaling

Bad scaling can be overcome

Examples:

Entangling superconducting qubits through nearby molecules in waveguides

Heralded gates in optical cavities $F \approx 1$ $1 - P \sim 1/\sqrt{C}$

Thanks to

<u>Copenhagen:</u> Malte Dueholm Darling Lucca Delantonio Emil Zeuthen Ivan lakoupov Johannes Borregaard Florentin Reiter Sumanta Das Johan Ott Oleksandr Kyriienko



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<u>Harvard:</u> Peter Kómár Eric Kessler Mikhail Lukin





