



# Spectroscopy from experimentalist's viewpoint II

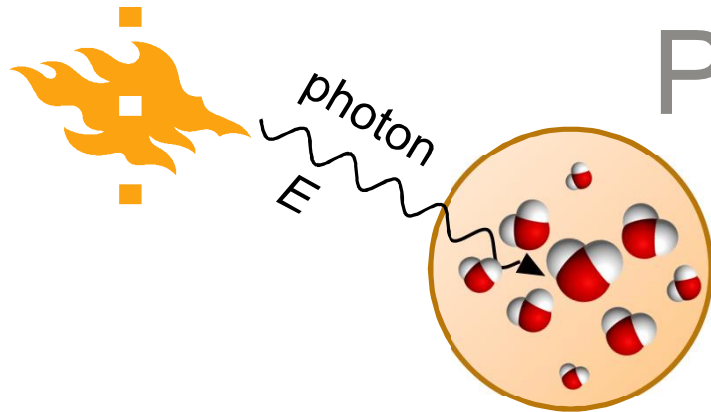
**Simo Huotari**

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Inelastic x-ray scattering group  
University of Helsinki, Finland**

**<http://www.helsinki.fi/people/simo.huotari>**

**TDDFT school, Benasque, Spain, January 2014**

# Photon absorption

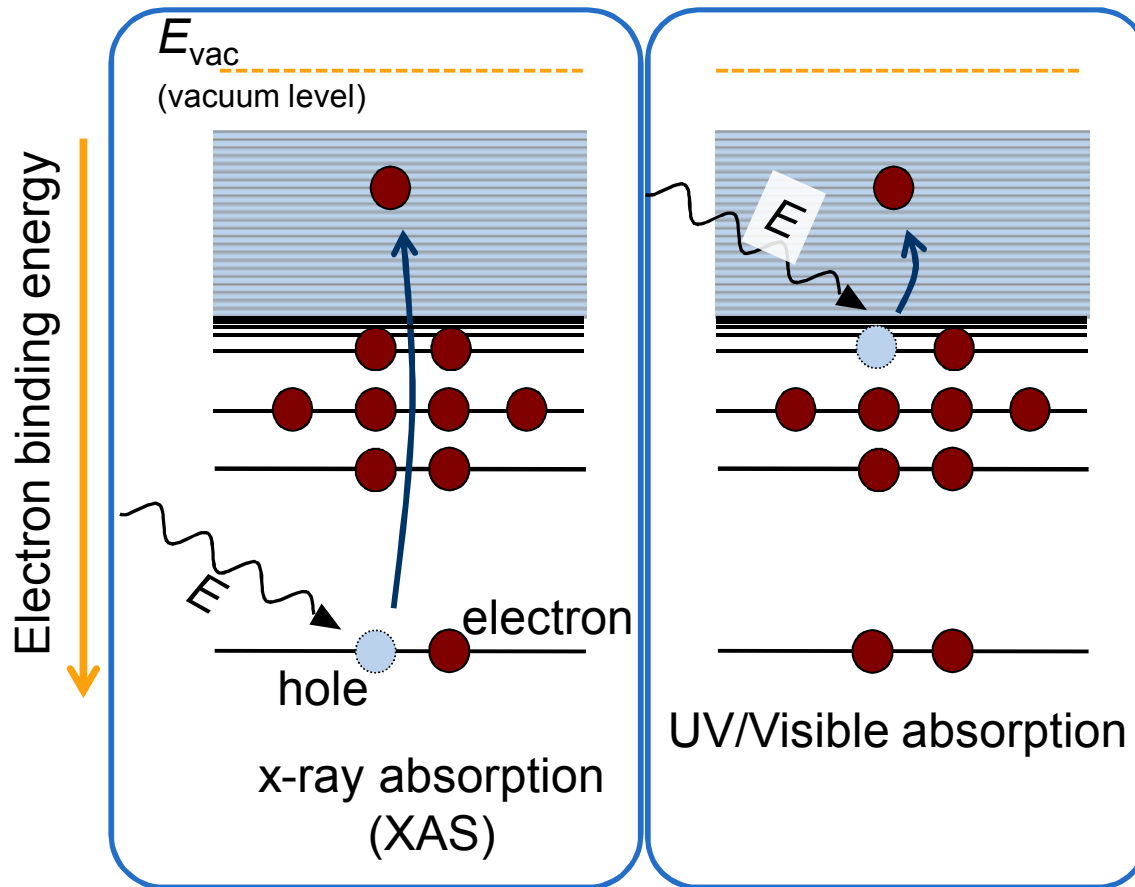


**What is used:**

Photon energy  $E$ , polarisation

**Interaction term:**

$\mathbf{p} \cdot \mathbf{A}$  term in first order



**Quantity:**

*Optical terminology*

$\alpha$  [1/cm] = attenuation coefficient

*X-ray terminology*

$\mu$  [1/cm] = absorption coefficient

$\alpha/\rho$  or  $\mu/\rho$  [cm<sup>2</sup>/g]

= mass attenuation coefficient

**Beer-Lambert law:**  $I = I_0 e^{-\alpha x}$



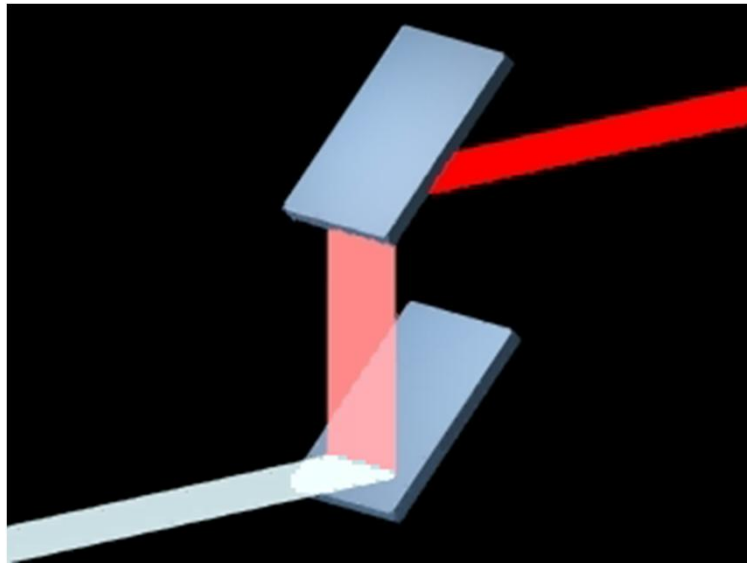
# Absorption spectroscopy

Need monochromatic radiation!

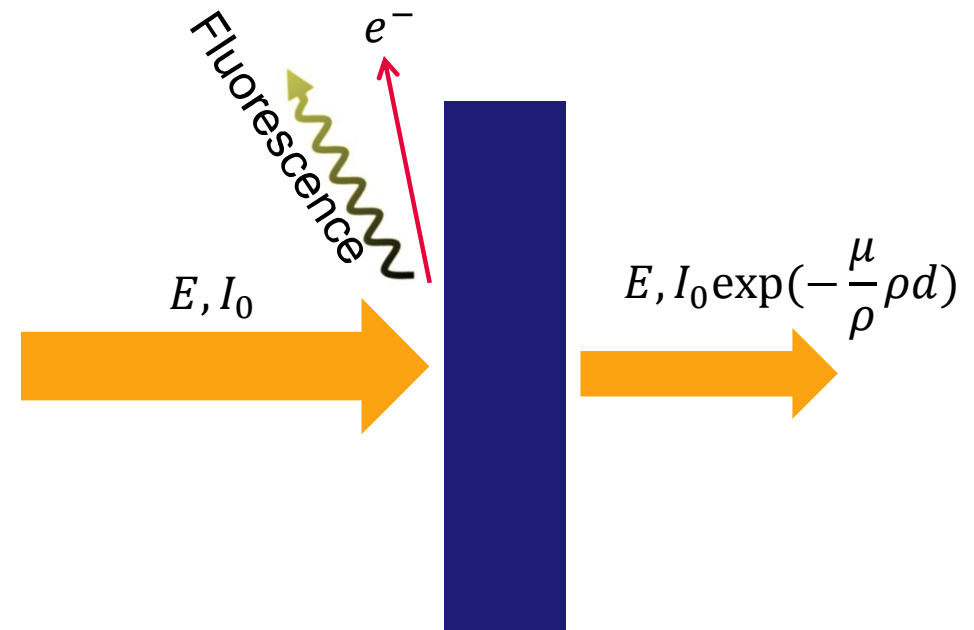
A double-crystal x-ray monochromator:

perfect Si crystals

Optical grating for UV/Vis



Bragg's law:  $\lambda = 2d \sin \theta$

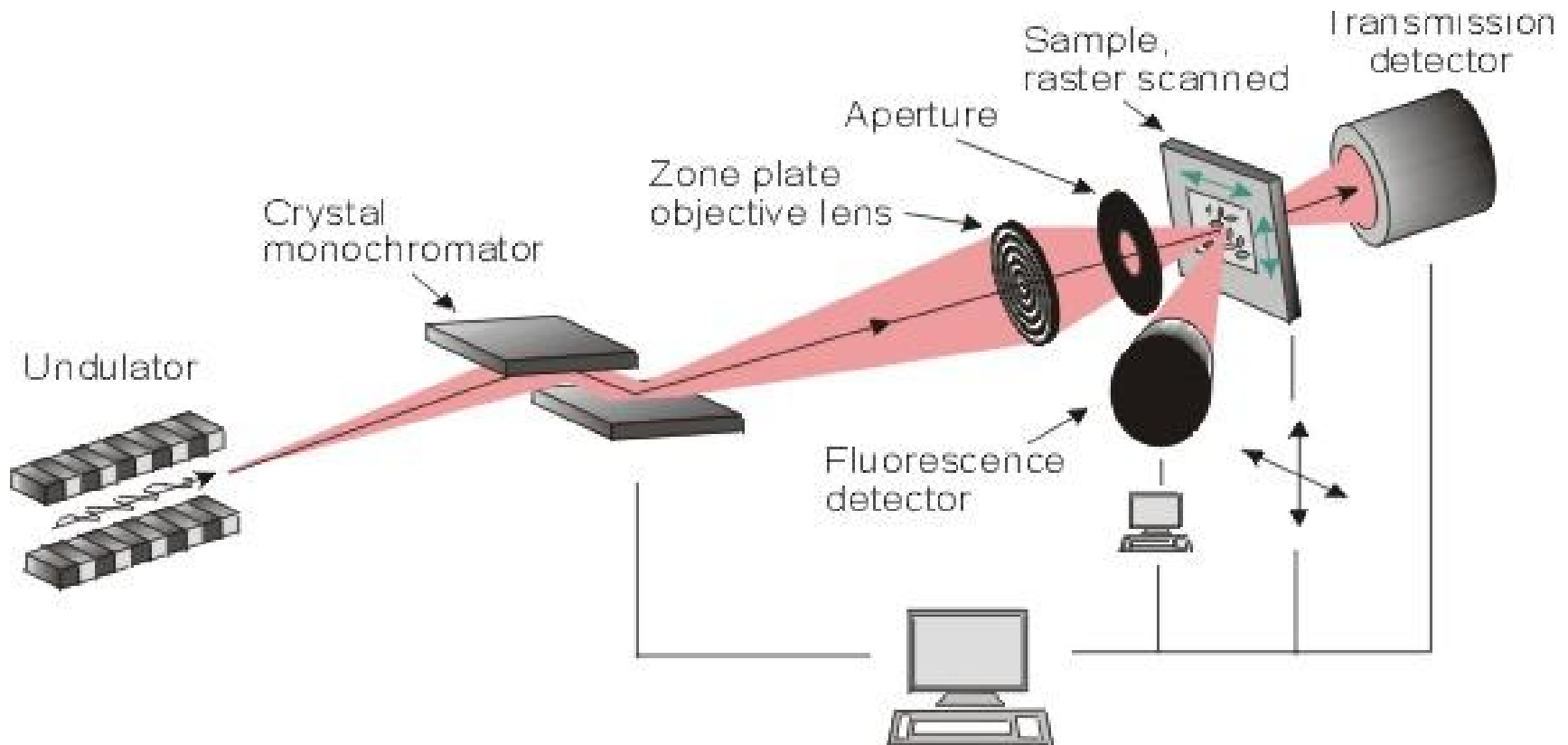


Measure at least one of:

- transmission
- fluorescence yield
- electron yield



# Vacuum ultraviolet + x-ray absorption



Scanning x-ray microscope, ESRF ID21

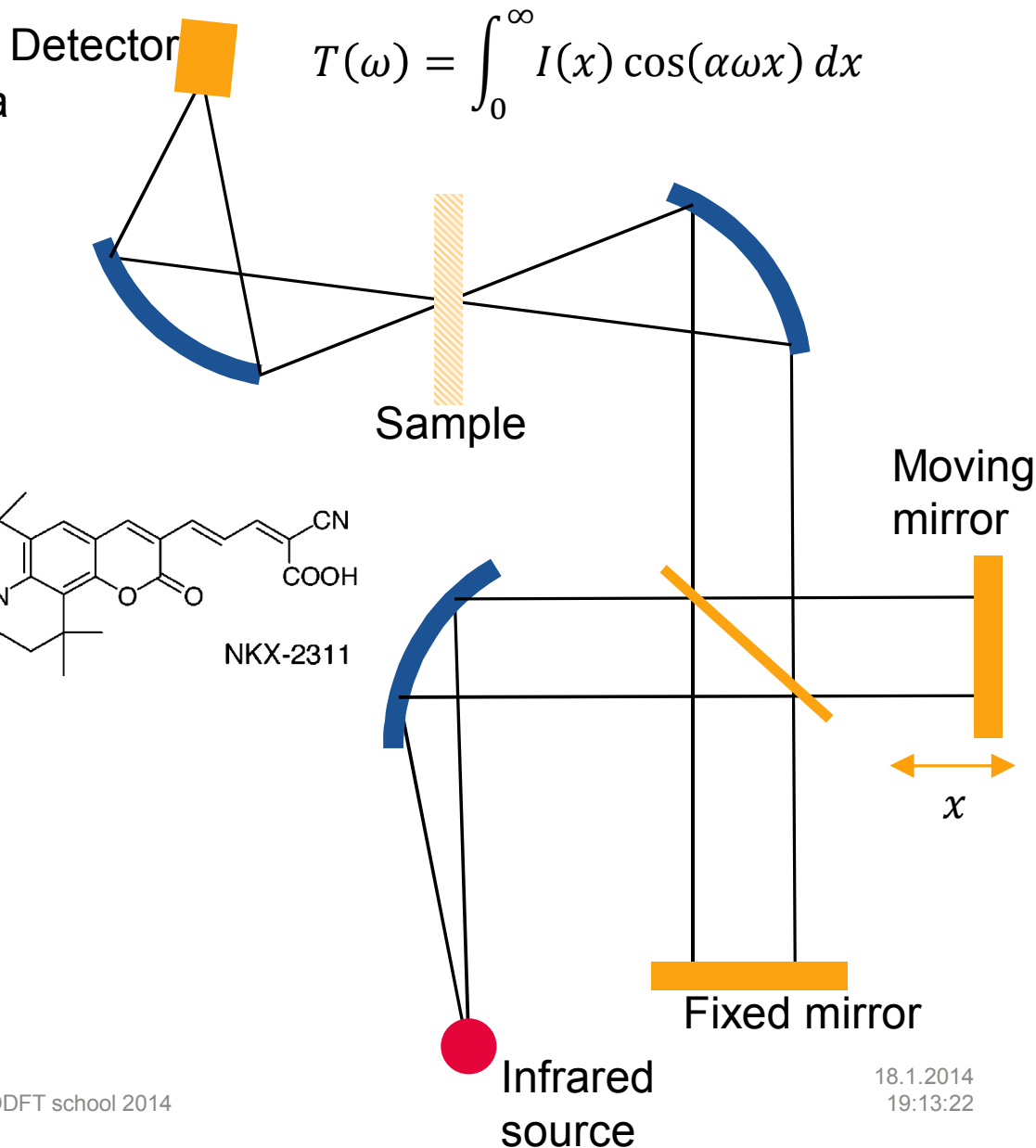
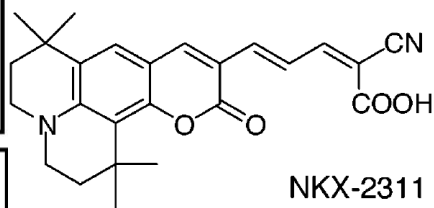
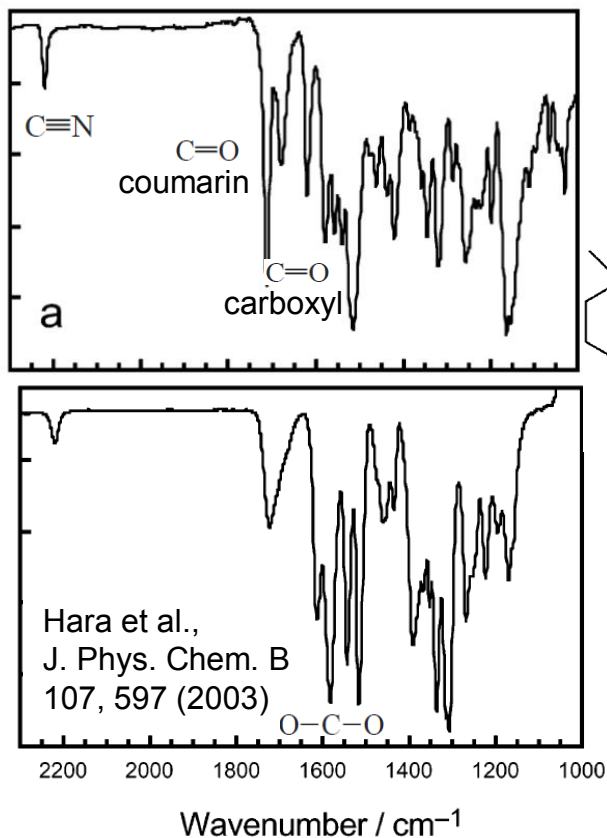
<http://www.esrf.eu/UsersAndScience/Experiments/Imaging/ID21/Sxm/Sxm>



# Fourier transform IR

Fourier transform of signal as a function of wave path length difference

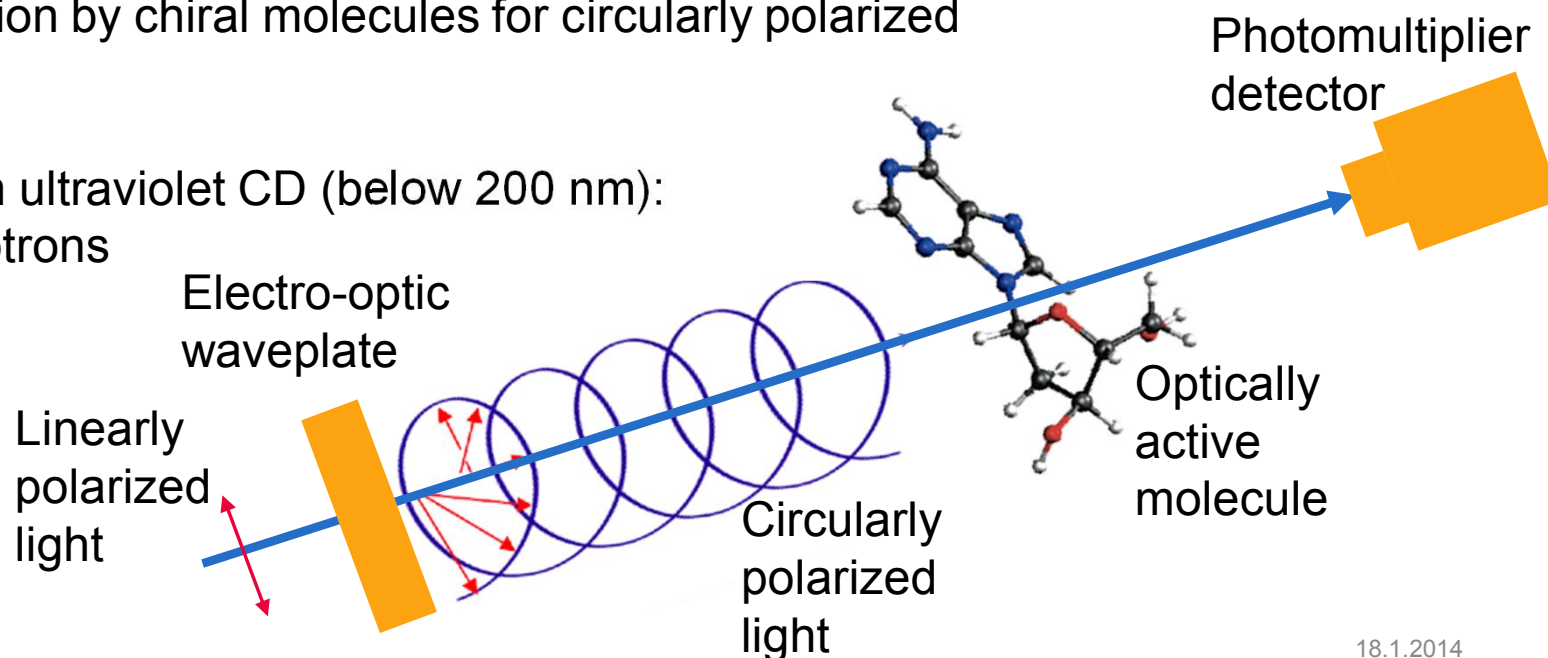
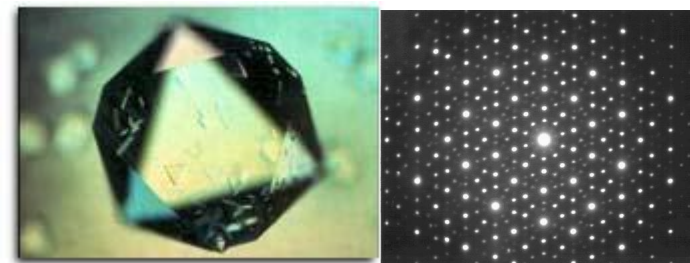
$$T(\omega) = \int_0^{\infty} I(x) \cos(\alpha\omega x) dx$$





# Circular Dichroism

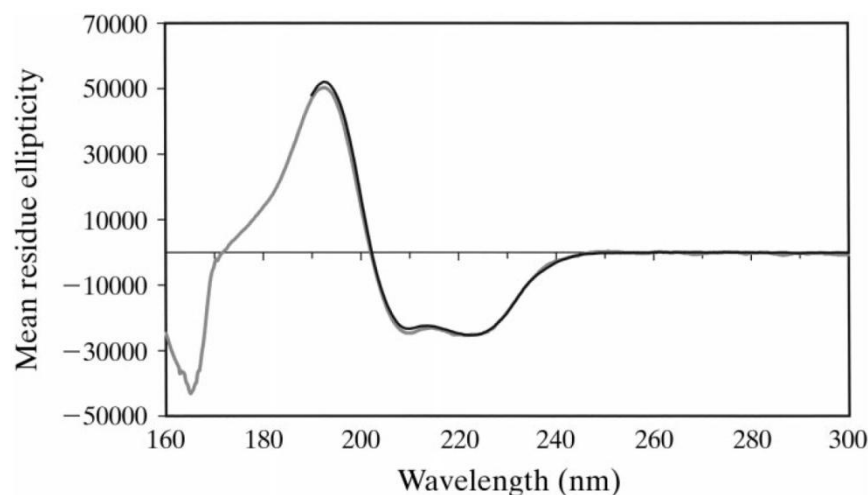
- Crystallography is an excellent tool for structure solving but needs crystals.
- Absorption spectroscopy is a good tool for studies of proteins in solution or molecules in gas phase
- Circular dichroism (CD) is the difference of light absorption by chiral molecules for circularly polarized light
- Vacuum ultraviolet CD (below 200 nm): synchrotrons



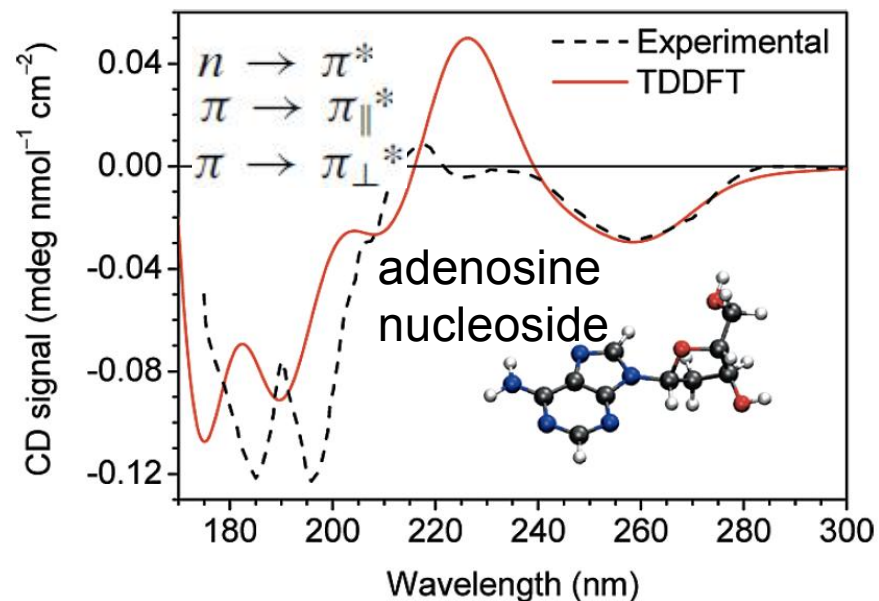


# Circular Dichroism

- Each secondary structure of an optically active molecule has a unique fingerprint in the spectrum
- Time resolved studies, formation and change of structures in real conditions
- Traditional UV lamps in laboratory equipment
- Synchrotron radiation sources powerful sources of vacuum UV (<200 nm)



Wallace, J. Synchrotron Radiat. 7, 289 (2000)



Nielsen *et al.*, J. Phys. Chem. B 113, 9614 (2009)

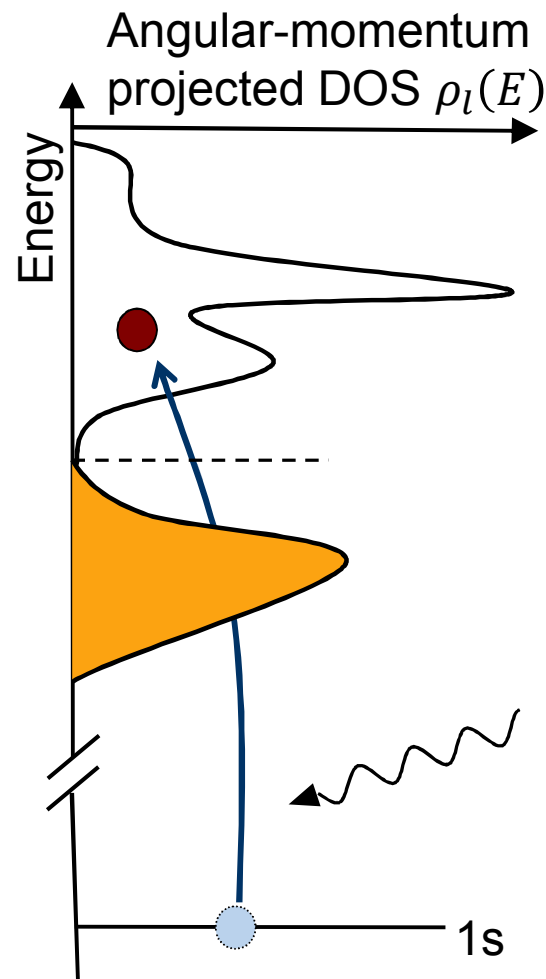
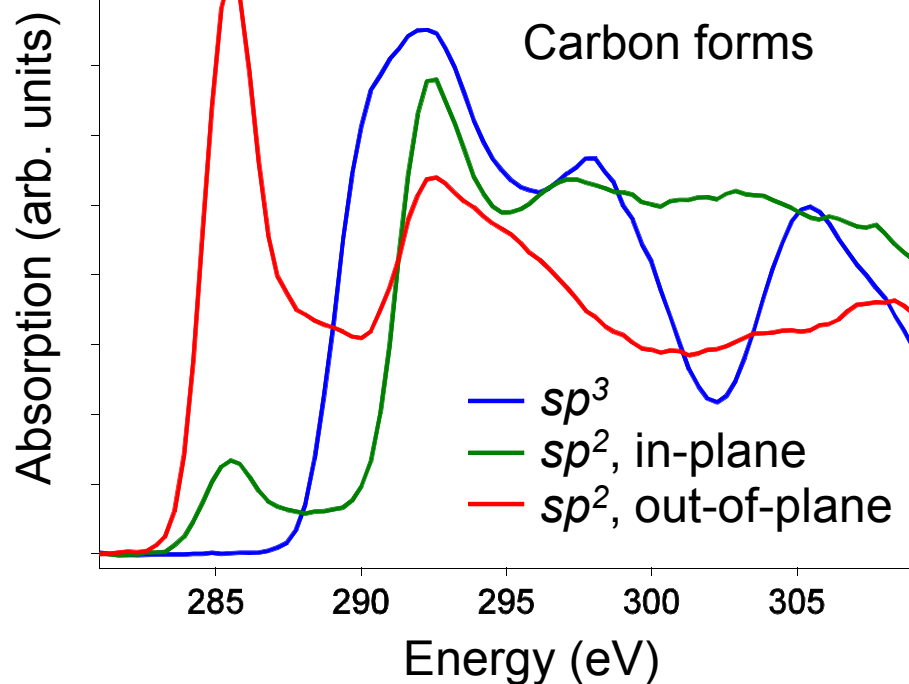


# X-ray absorption

$\mathbf{p} \cdot \mathbf{A}$  term in first order

$$\mu(E) = M(E)\rho_l(E)$$

$M(E)$  is the matrix element  
(depends weakly on  $E$ )

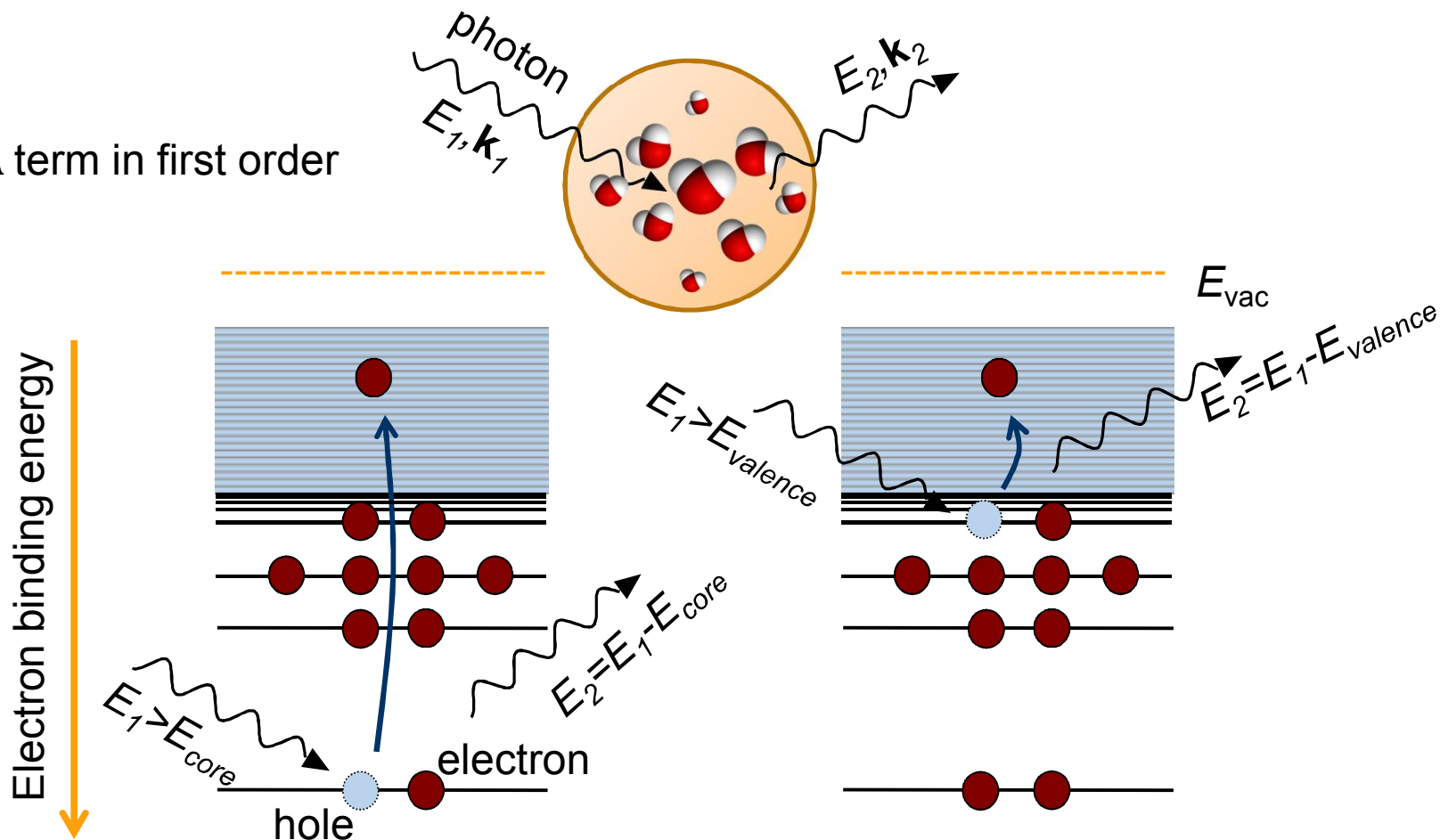






# Inelastic scattering

A · A term in first order

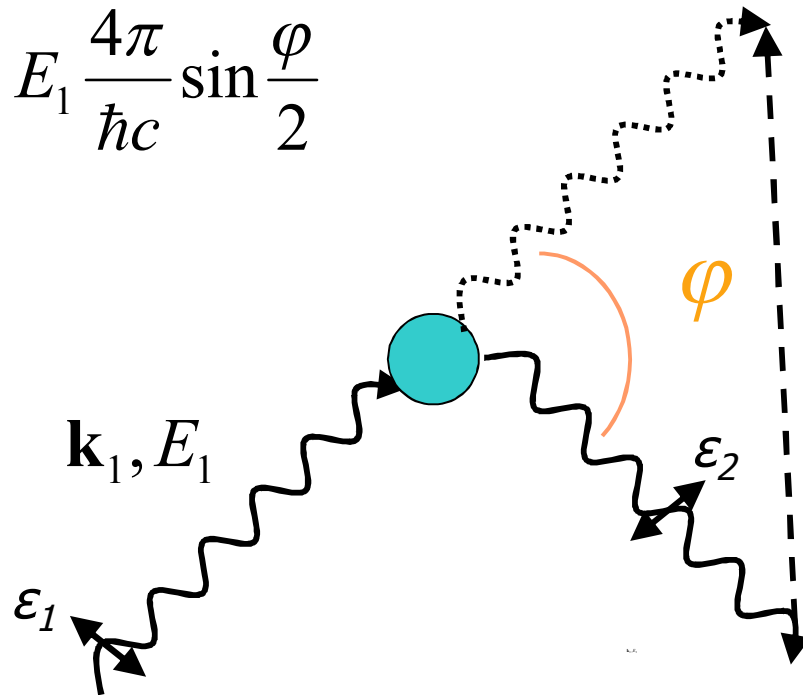


Energy transfer  $E = E_1 - E_2$   
 Momentum transfer  $q = k_1 - k_2$



# Non-resonant x-ray scattering

$$Q \approx E_1 \frac{4\pi}{\hbar c} \sin \frac{\varphi}{2}$$



$$\mathbf{Q} = \mathbf{k}_1 - \mathbf{k}_2$$

$$\frac{d^2\sigma}{dE d\Omega} = r_e^2 (\boldsymbol{\epsilon}_1 \cdot \boldsymbol{\epsilon}_2)^2 S(\mathbf{Q}, E)$$

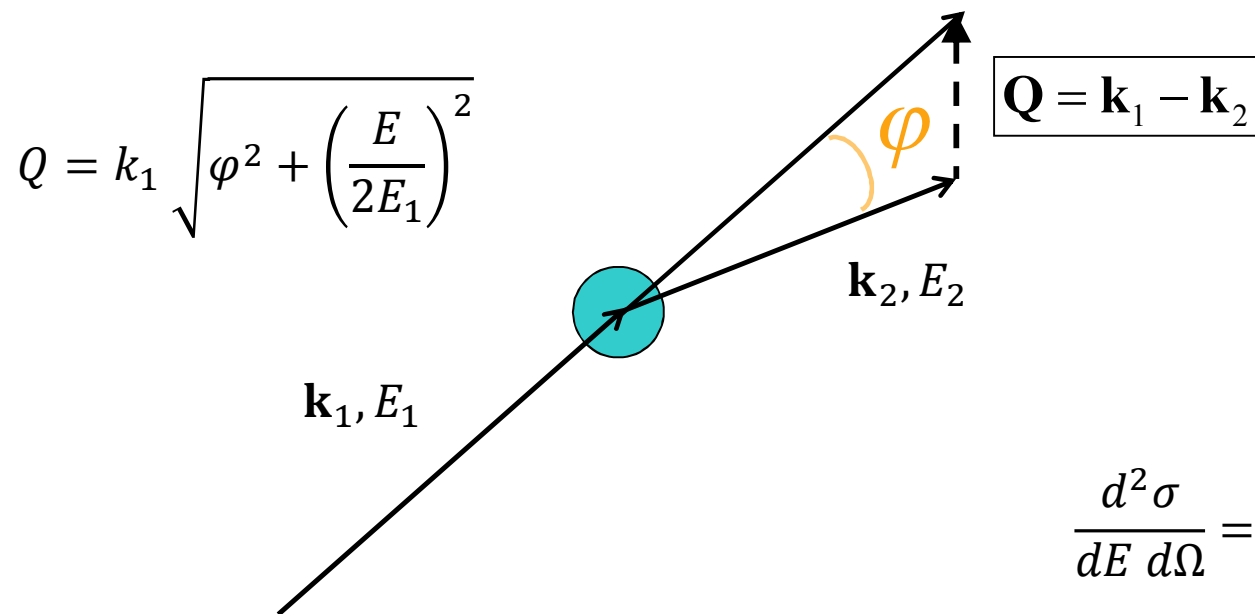
Momentum transfer	$\mathbf{Q} = \mathbf{k}_1 - \mathbf{k}_2$
Energy transfer	$E = E_1 - E_2$

Dynamic structure factor  $S(\mathbf{Q}, E)$

$$S(\mathbf{Q}, E) = \frac{Q^2}{4\pi^2 n} \text{Im} \left[ \frac{-1}{\varepsilon(\mathbf{Q}, E)} \right]$$



# Electron scattering



$$Q = k_1 \sqrt{\varphi^2 + \left(\frac{E}{2E_1}\right)^2}$$

$$\mathbf{Q} = \mathbf{k}_1 - \mathbf{k}_2$$

$$\frac{d^2\sigma}{dE d\Omega} = \frac{4\hbar\gamma^2}{a_0^2 Q^4} S(\mathbf{Q}, E)$$

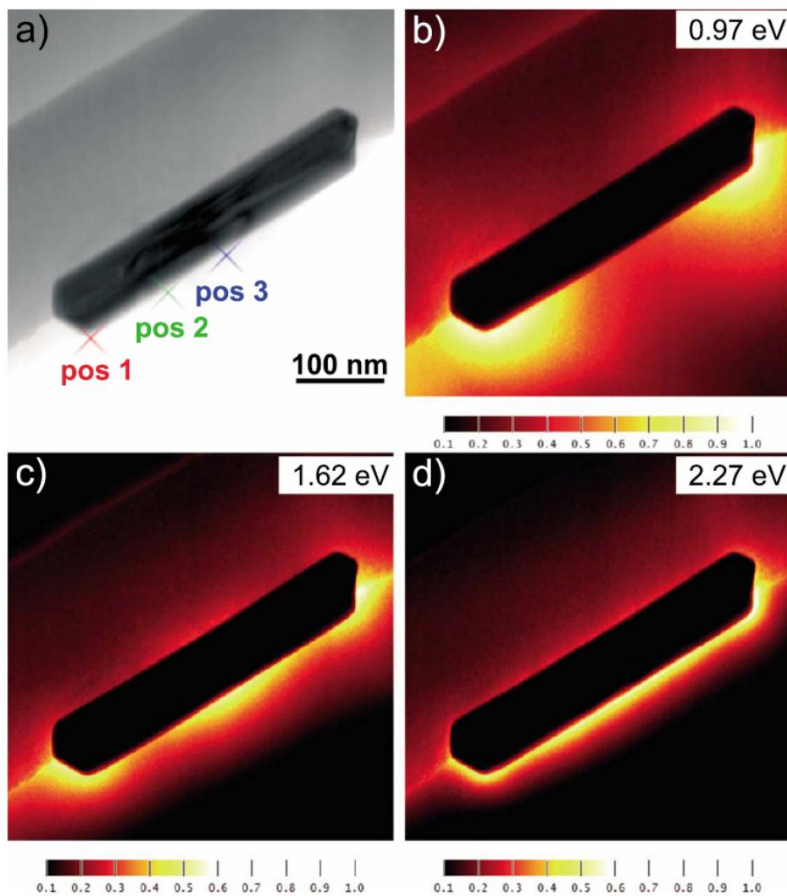
Dynamic structure factor  $S(\mathbf{Q}, E)$

$$S(\mathbf{Q}, E) = \frac{Q^2}{4\pi^2 n} \text{Im} \left[ \frac{-1}{\varepsilon(\mathbf{Q}, E)} \right]$$

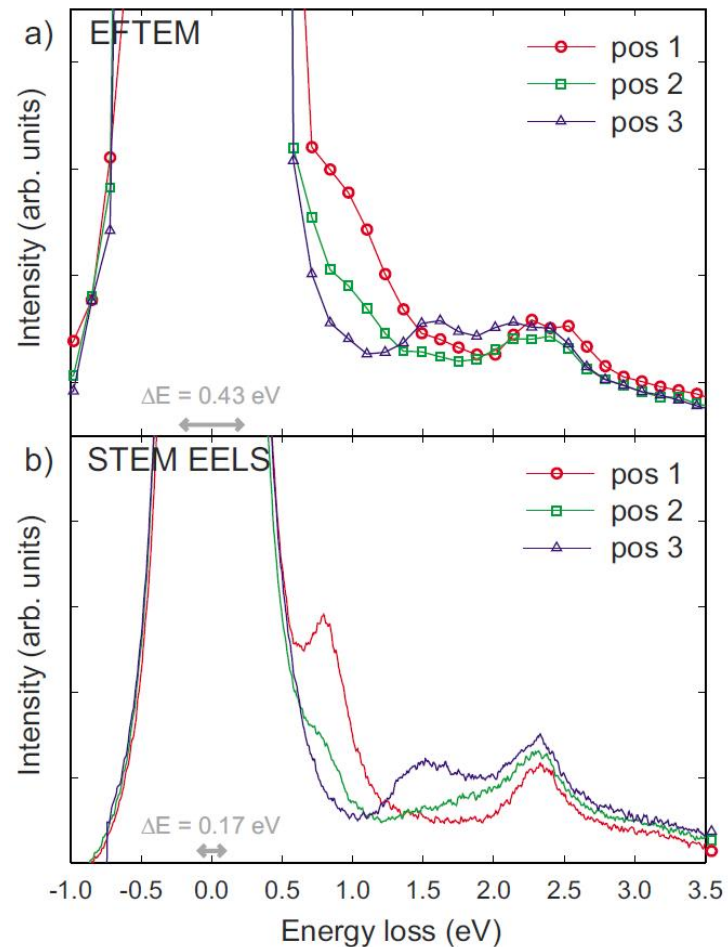
Momentum transfer	$\mathbf{Q} = \mathbf{k}_1 - \mathbf{k}_2$
Energy transfer	$E = (\hbar^2/2m)(k_1 - k_2)$



# Electron microscopy



Plasmon eigenmodes of a gold nanoparticle



B. Schaffer et al. PRB 79, 041401(R) (2009)



# First Born approximation

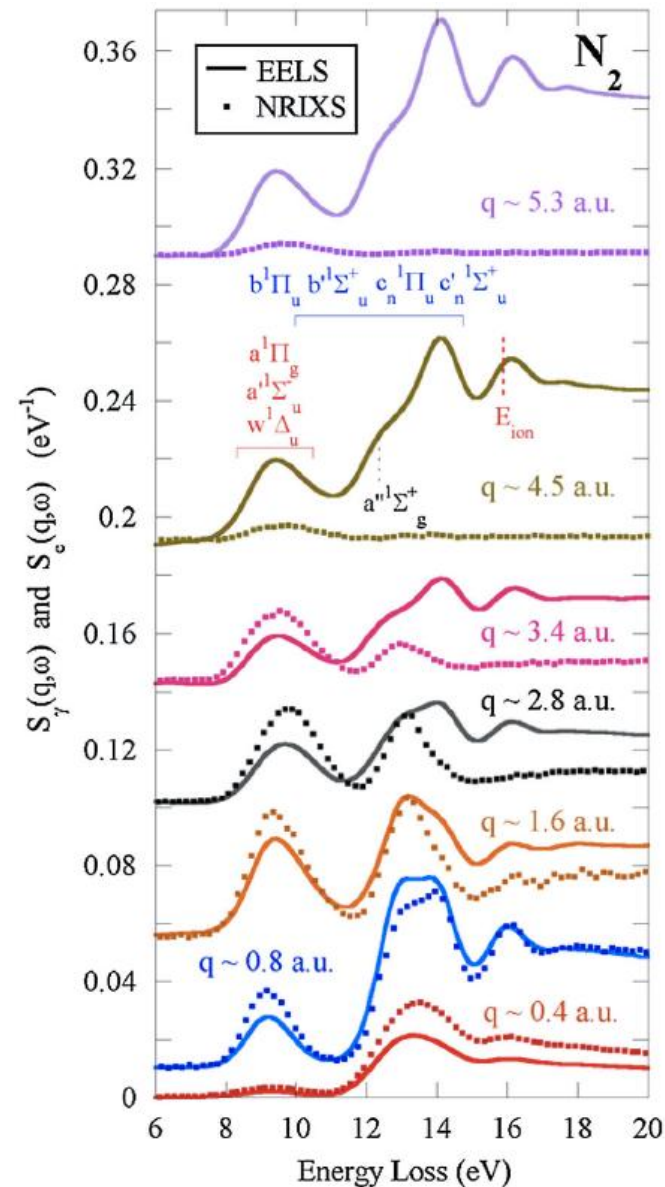
Comparative study of EELS and IXS valence excitations from nitrogen molecule

J. A. Bradley et al.,  
PRL 105, 053202 (2010)

$$\left(\frac{d^2\sigma}{d\Omega d\omega}\right)_{\gamma,e} = \left(\frac{d\sigma}{d\omega}\right)_{\text{Th,Ru}} S(\mathbf{q}, \omega)$$

In principle..  
But true for all dynamic range?

Lyman-Birge-Hopfield (LBH) band

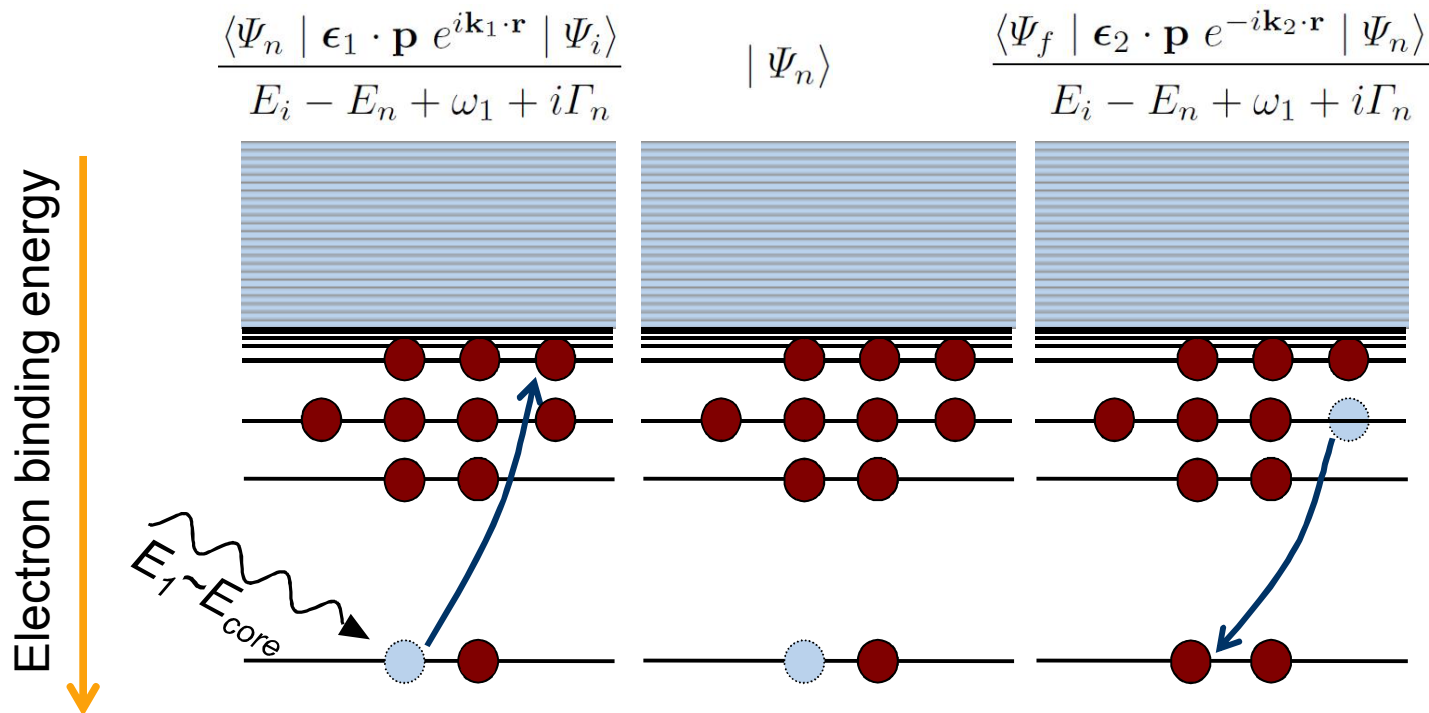




# Resonant inelastic scattering

$\mathbf{p} \cdot \mathbf{A}$  term in second order

Ground state  $\longrightarrow$  Intermediate state  $\longrightarrow$  Final state



Photon energies  $E_1, E_2$ , polarisation, momentum

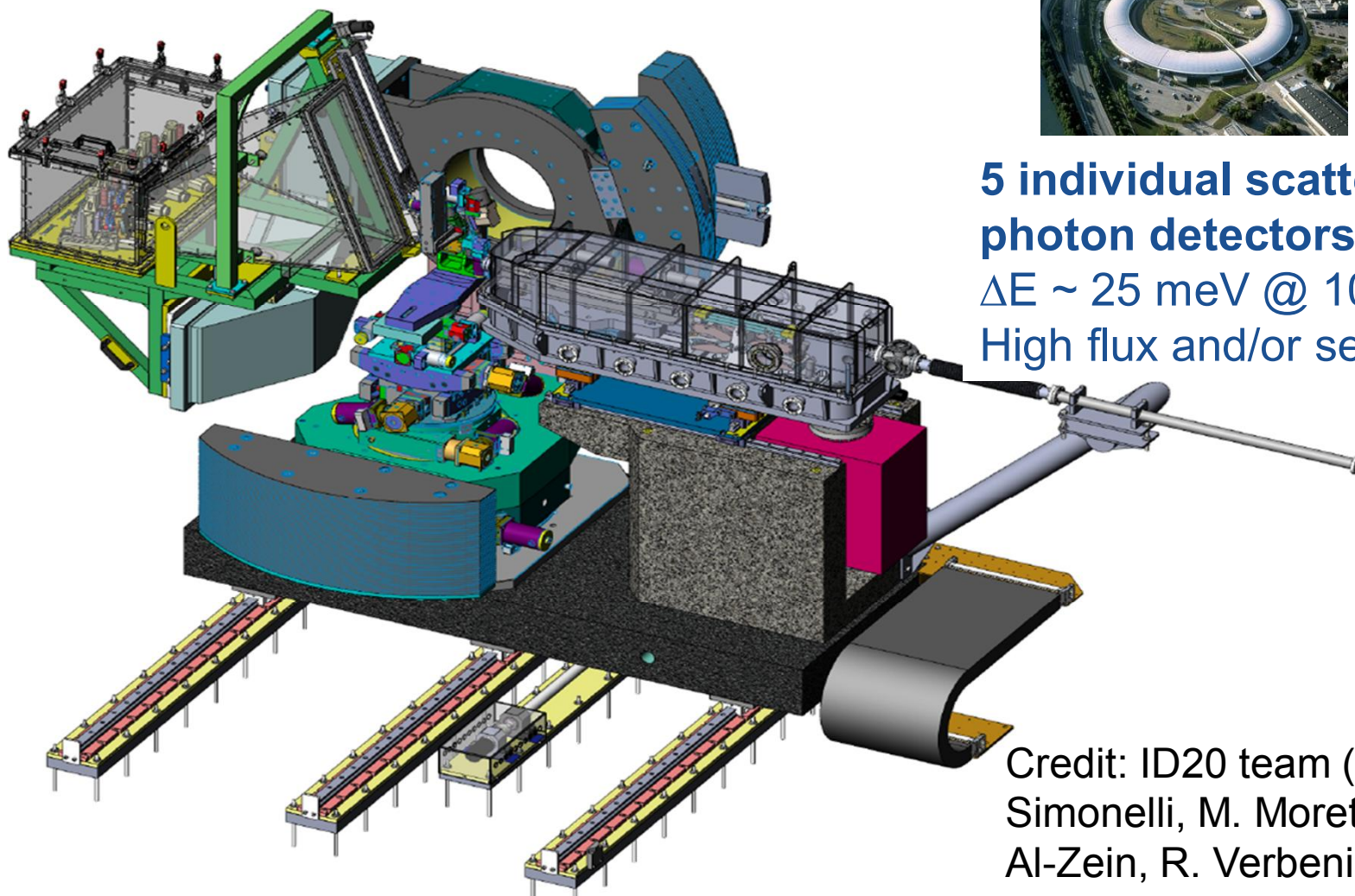




# ID20 @ ESRF: Resonant IXS



ESRF

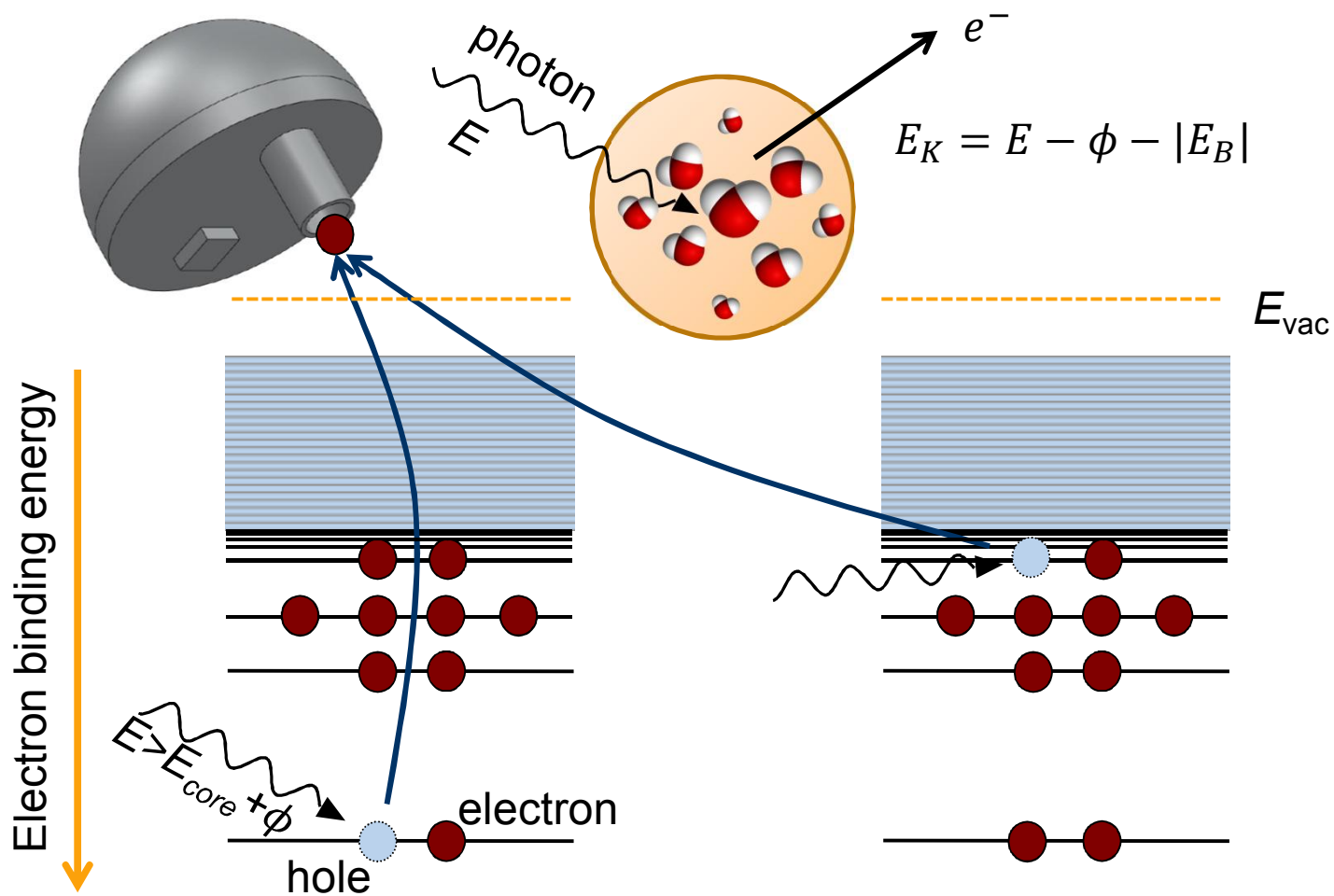


**5 individual scattered  
photon detectors**  
 $\Delta E \sim 25 \text{ meV @ } 10 \text{ keV}$   
High flux and/or several  $q$ 's

Credit: ID20 team (Laura Simonelli, M. Moretti Sala, Ali Al-Zein, R. Verbeni, M. Krisch, G. Monaco, et al.)



# Photoemission



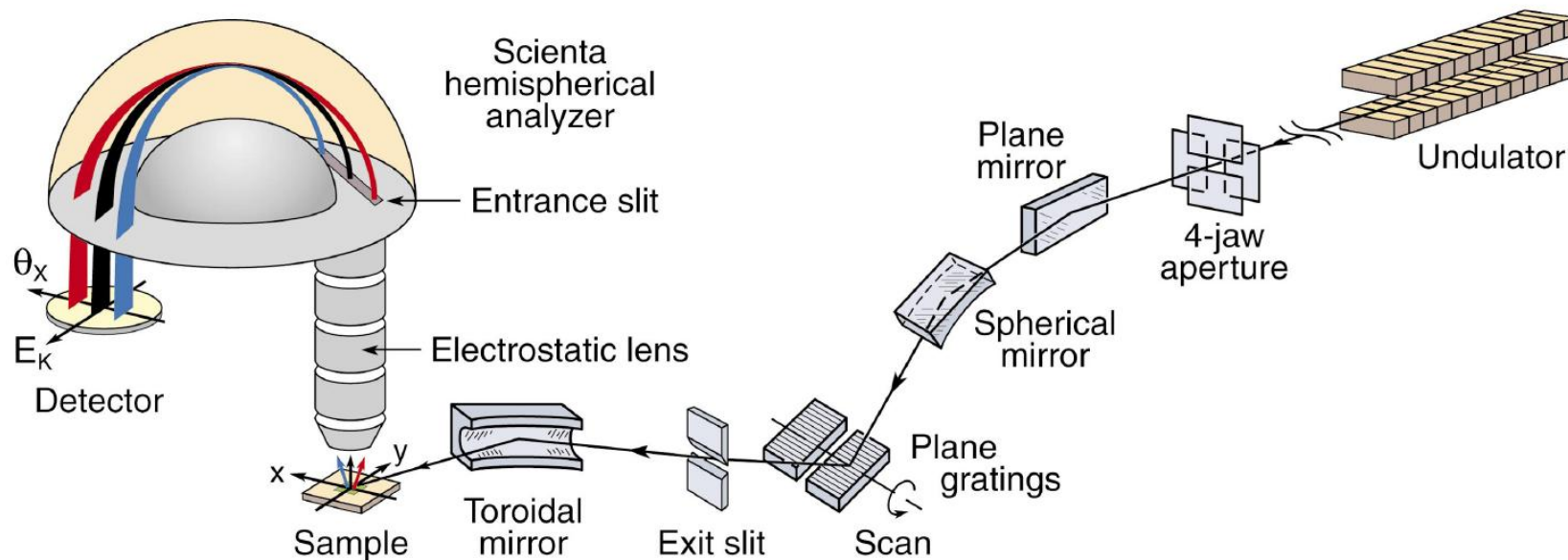
Photon energy  $E$ , polarisation, momentum...





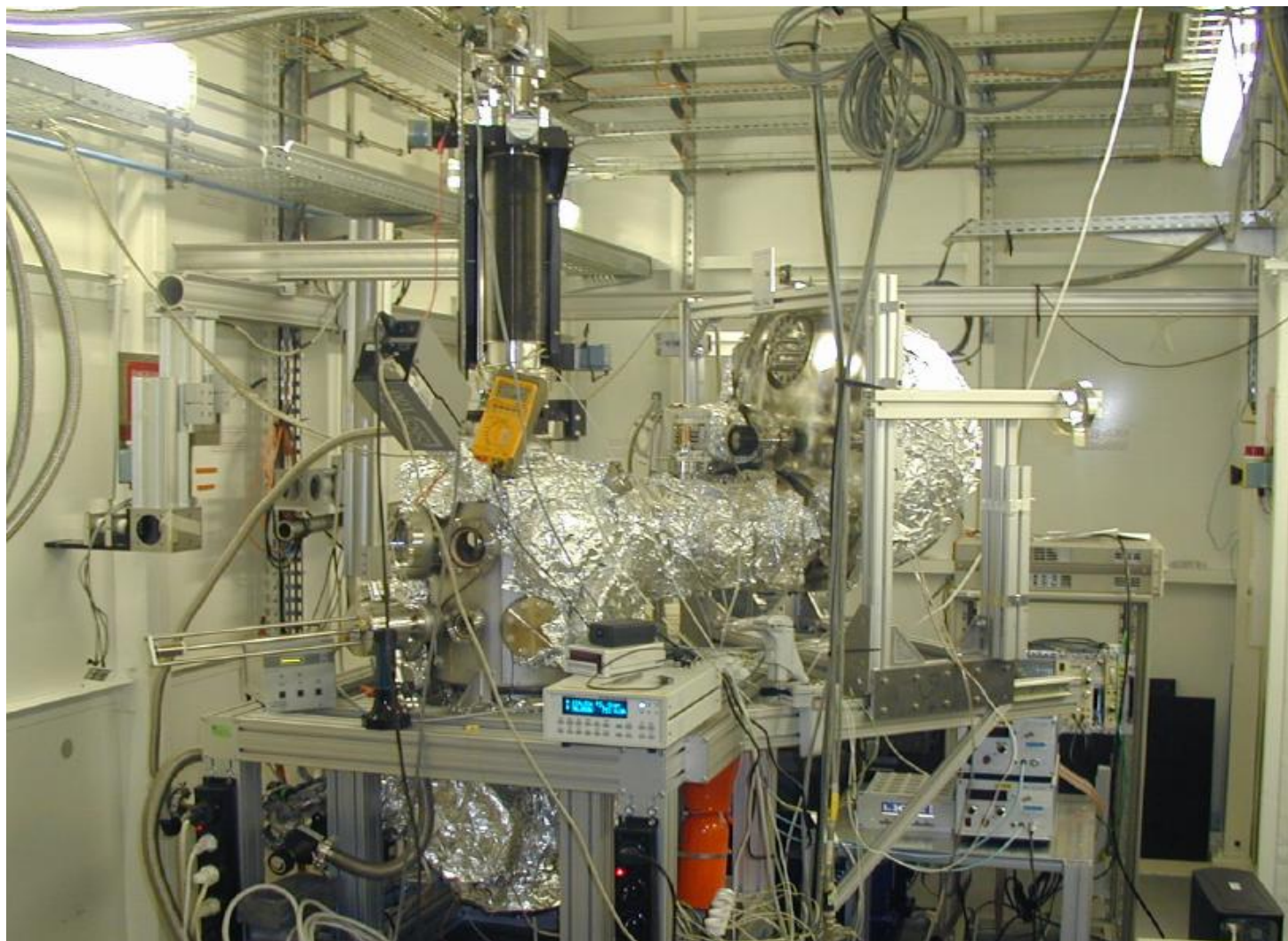
# Photoemission

A. Damascelli et al., Rev. Mod. Phys 75, 473 (2003)



Powerful tool for

- ESCA (electron spectroscopy for chemical analysis): identification of core levels, shifts, shape
- Valence PES for band mapping (ARPES)
- Circular dichroism



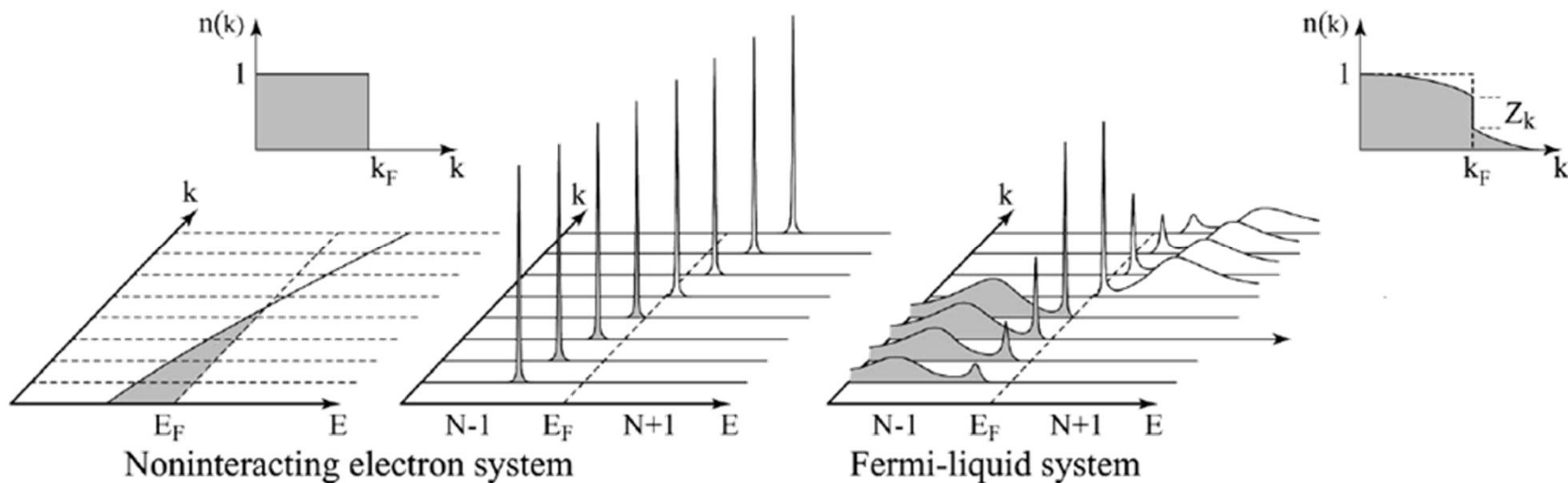
The Volume Photoemission (VOLPE) spectrometer at ESRF  
(G. Panaccione, M. Sacchi, et al.)



# Photoemission

A. Damascelli et al., Rev. Mod. Phys 75, 473 (2003)

One-electron removal and addition spectra in a crystal

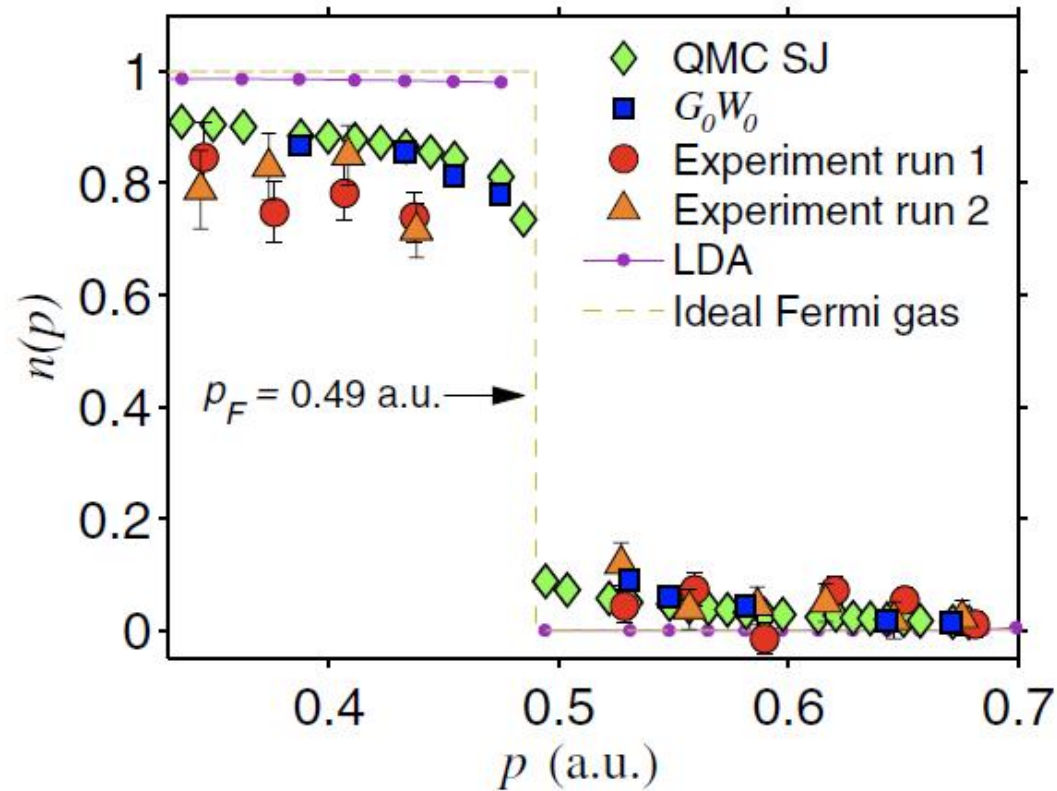


$$\text{PES} \propto \sum_{f,i} \left| M_{f,i}^{\mathbf{p}} \right|^2 A(\mathbf{p}, E) \delta(E_K + E_m^{N-1} - E_i^N - \omega_1)$$

Spectral function



# Quasiparticle renormalisation factor



For Na ( $r_s = 3.99$ ),  
experimental

$$Z_{k_F} = 0.58 \pm 0.07$$

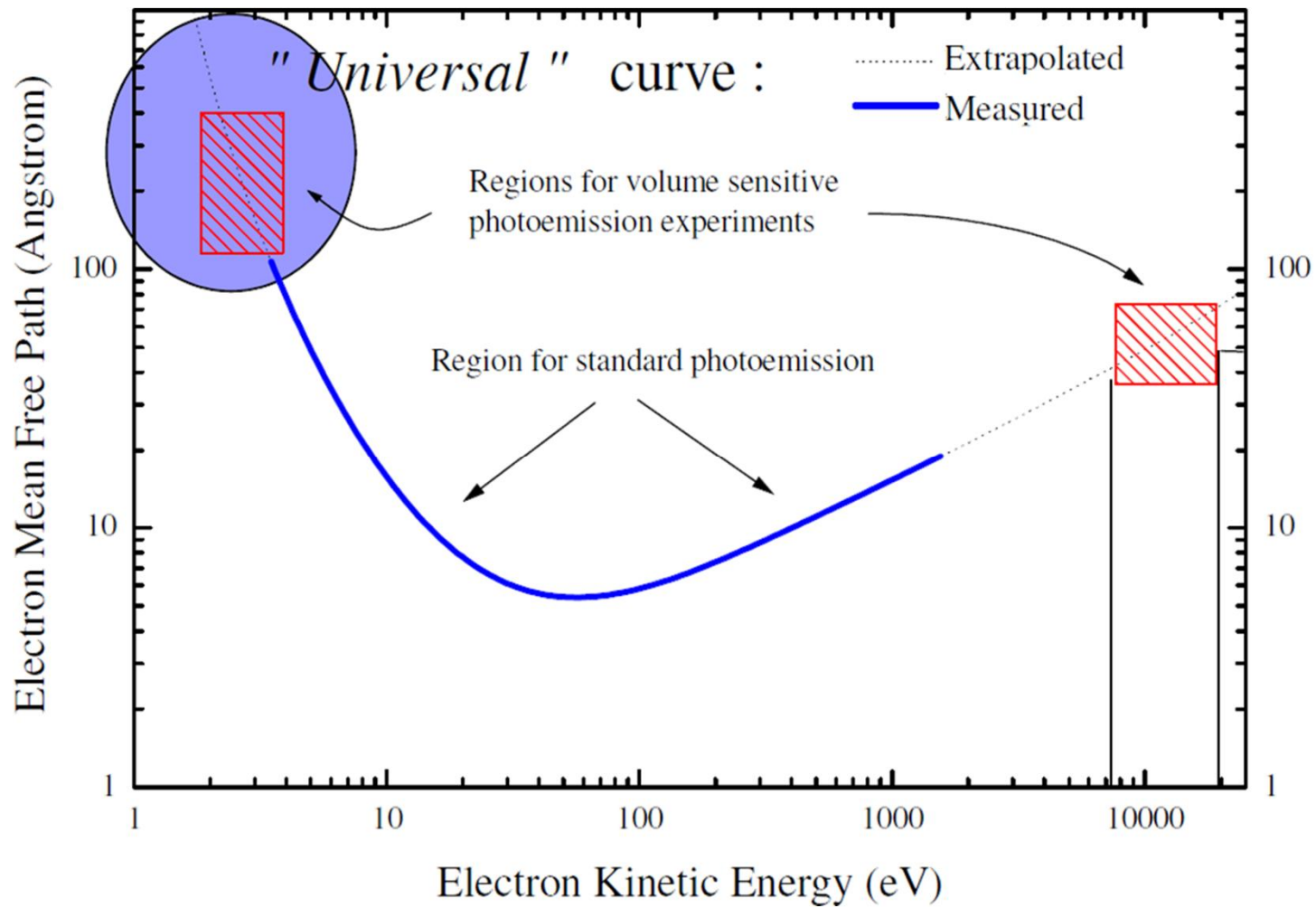
Method: Compton  
spectroscopy

S. Huotari, J. A. Soininen, T. Pylkkänen, K. Hämäläinen, A. Issolah, A. Titov, J. McMinis, J. Kim, K. Esler, D. M. Ceperley, M. Holzmann, V. Olevano, Phys. Rev. Lett. 105, 086403 (2010)





# Bulk-sensitive photoemission

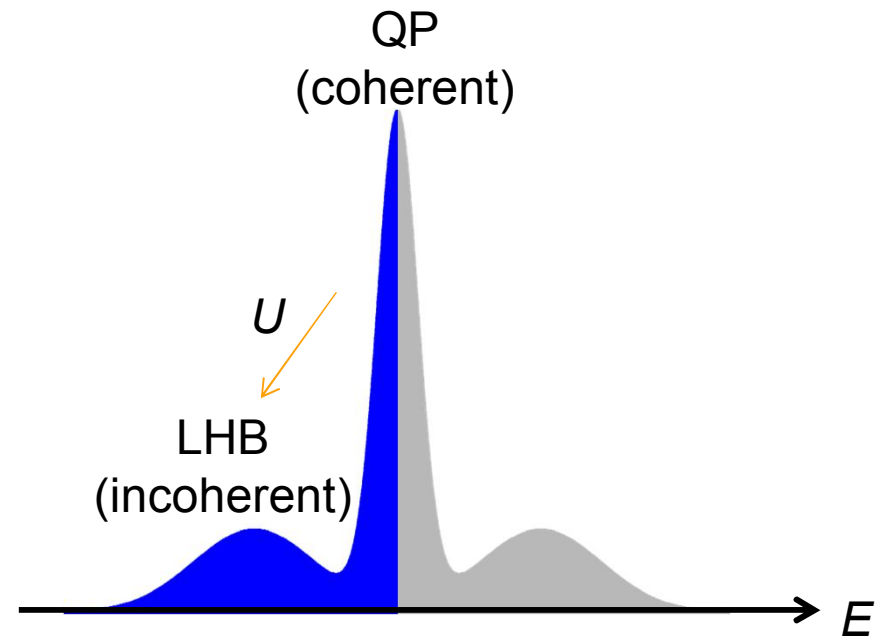
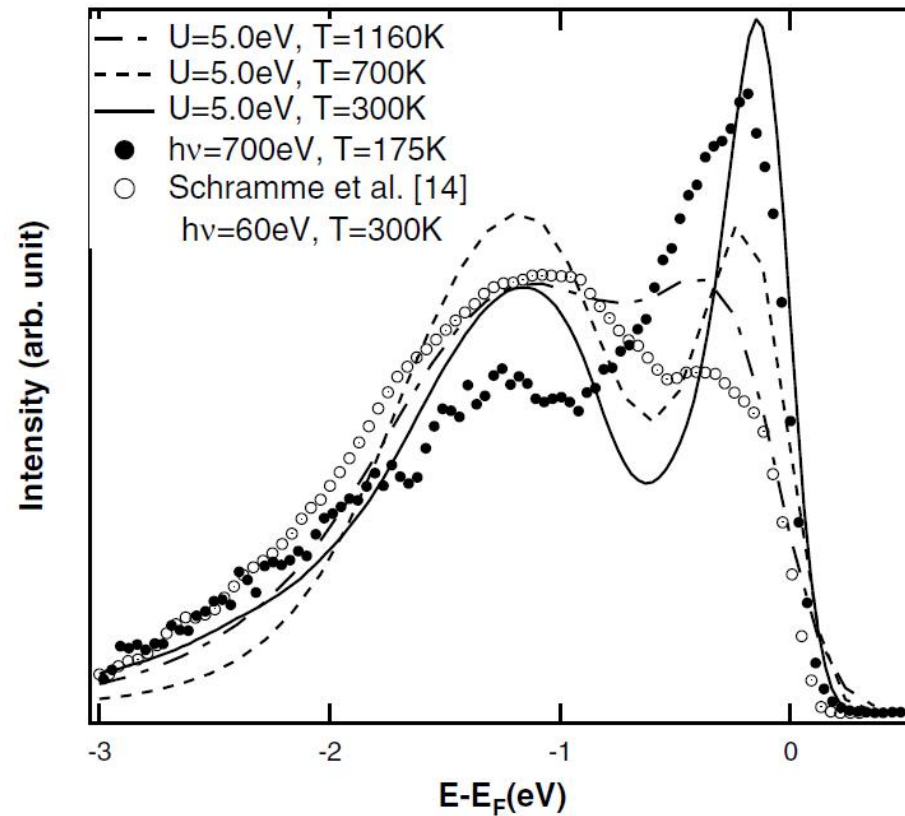




# Bulk-sensitive photoemission

The Mott-Hubbard insulator  $V_2O_3$

S.K. Mo et al., PRL 90, 186403 (2003)

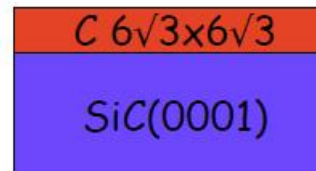
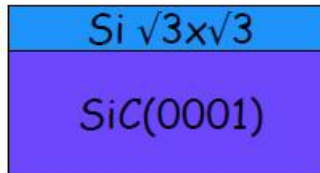
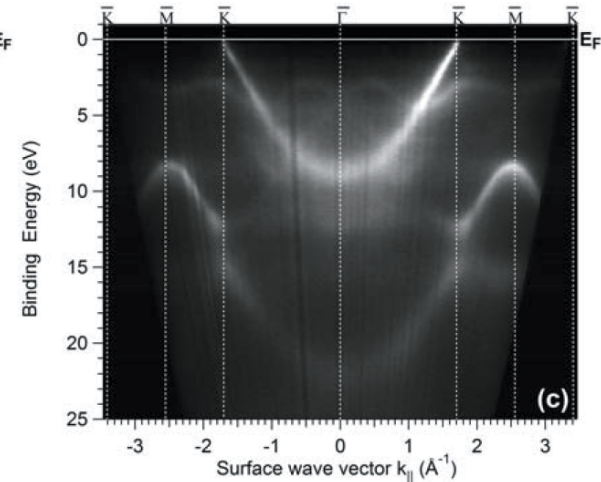
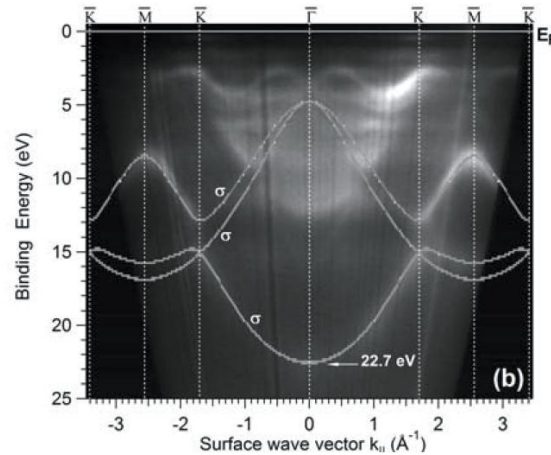
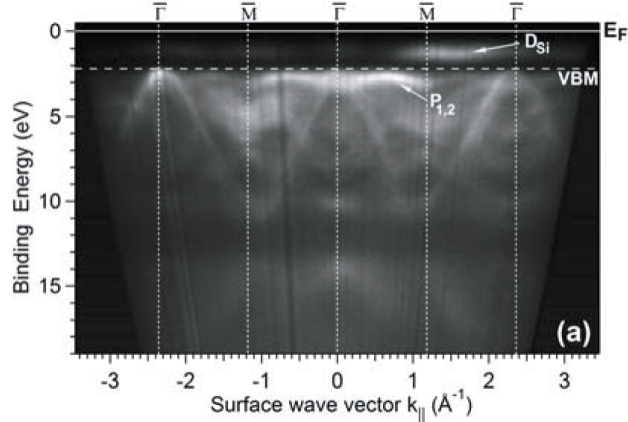


Half-filled one-band Hubbard model

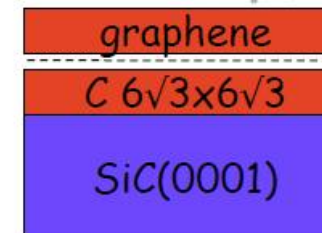
$U$  = on-site Coulomb repulsion



# Band mapping by ARPES



$sp^2$ -bonded  $p_z$  hybridized with SiC;  $\pi$  band not developed



$sp^2$ -bonded  $p_z$  derived band, van der Waals-bonded to  $6\sqrt{3}$  layer

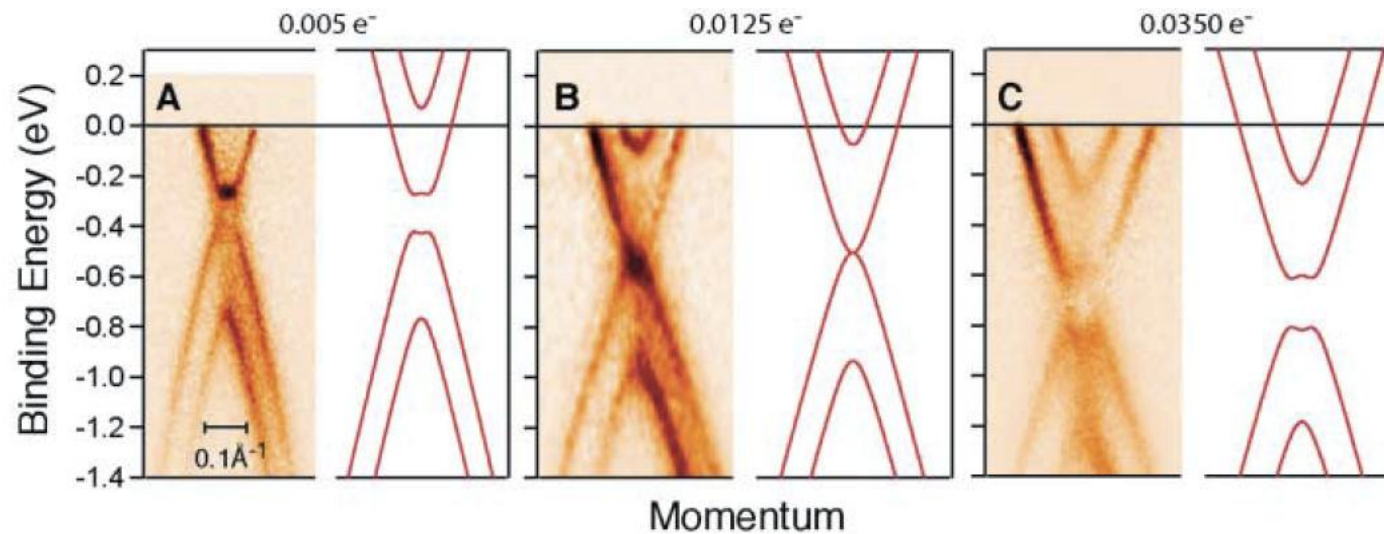
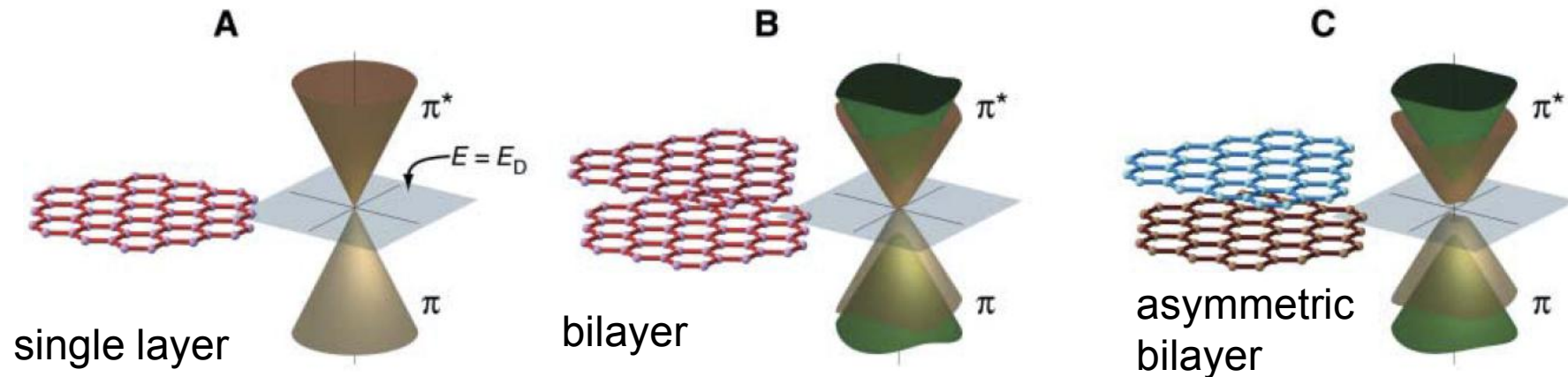
K. V. Emtsev et al., <http://arxiv.org/abs/cond-mat/0609383>

Credits: from a talk by K.Horn et al.

[www.uv.es/wsetld/archivos/Tuesday/WS10-Horn.pdf](http://www.uv.es/wsetld/archivos/Tuesday/WS10-Horn.pdf)



# Controlling the Electronic Structure of Bilayer Graphene



T. Ohta et al., Science 313, 951 (2006)





# Helsinki Electronic Structure and IXS Group



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J. Koskelo, J. Niskanen,  
A.-P. Honkanen

- **ESRF:**  
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