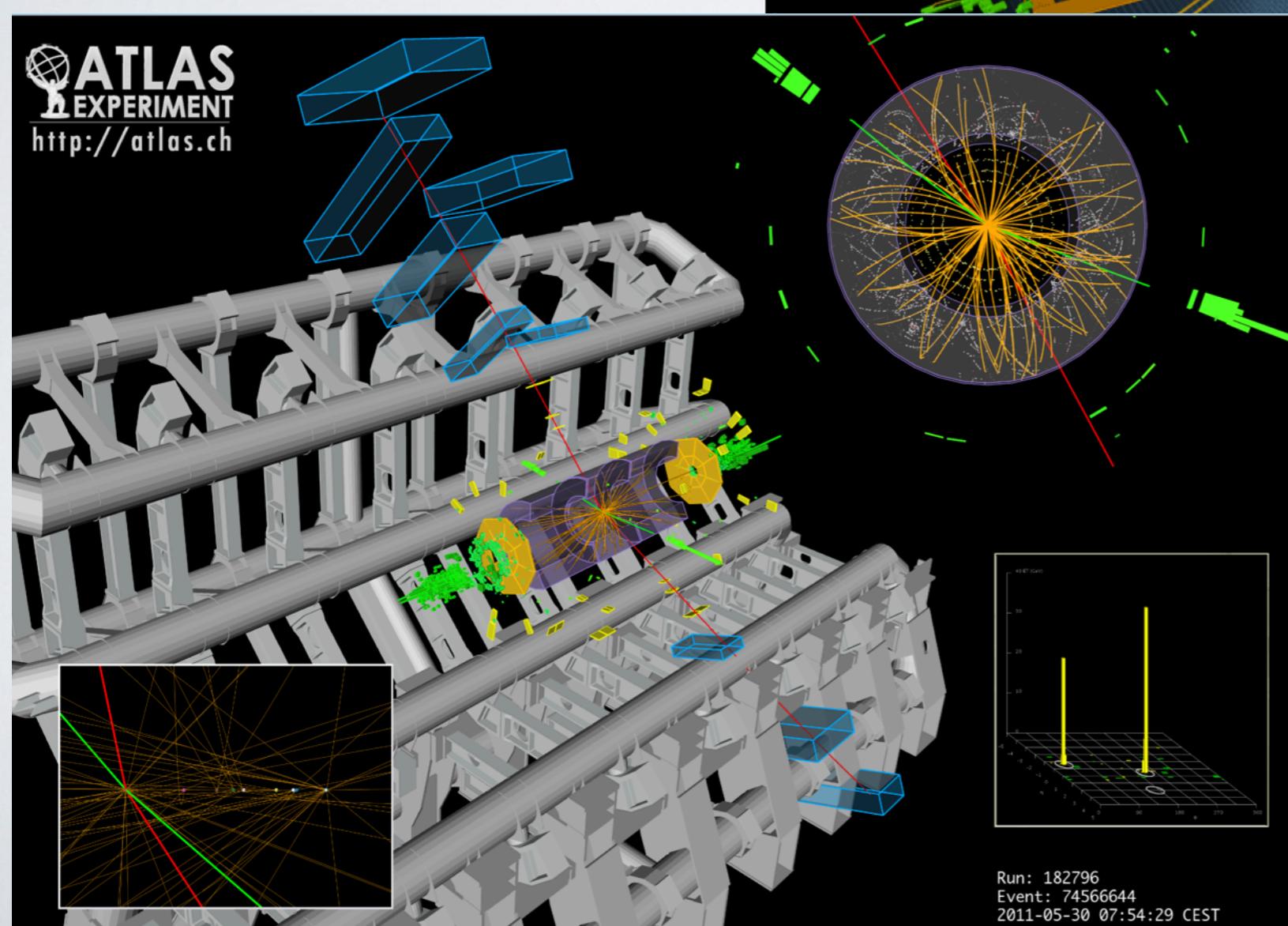
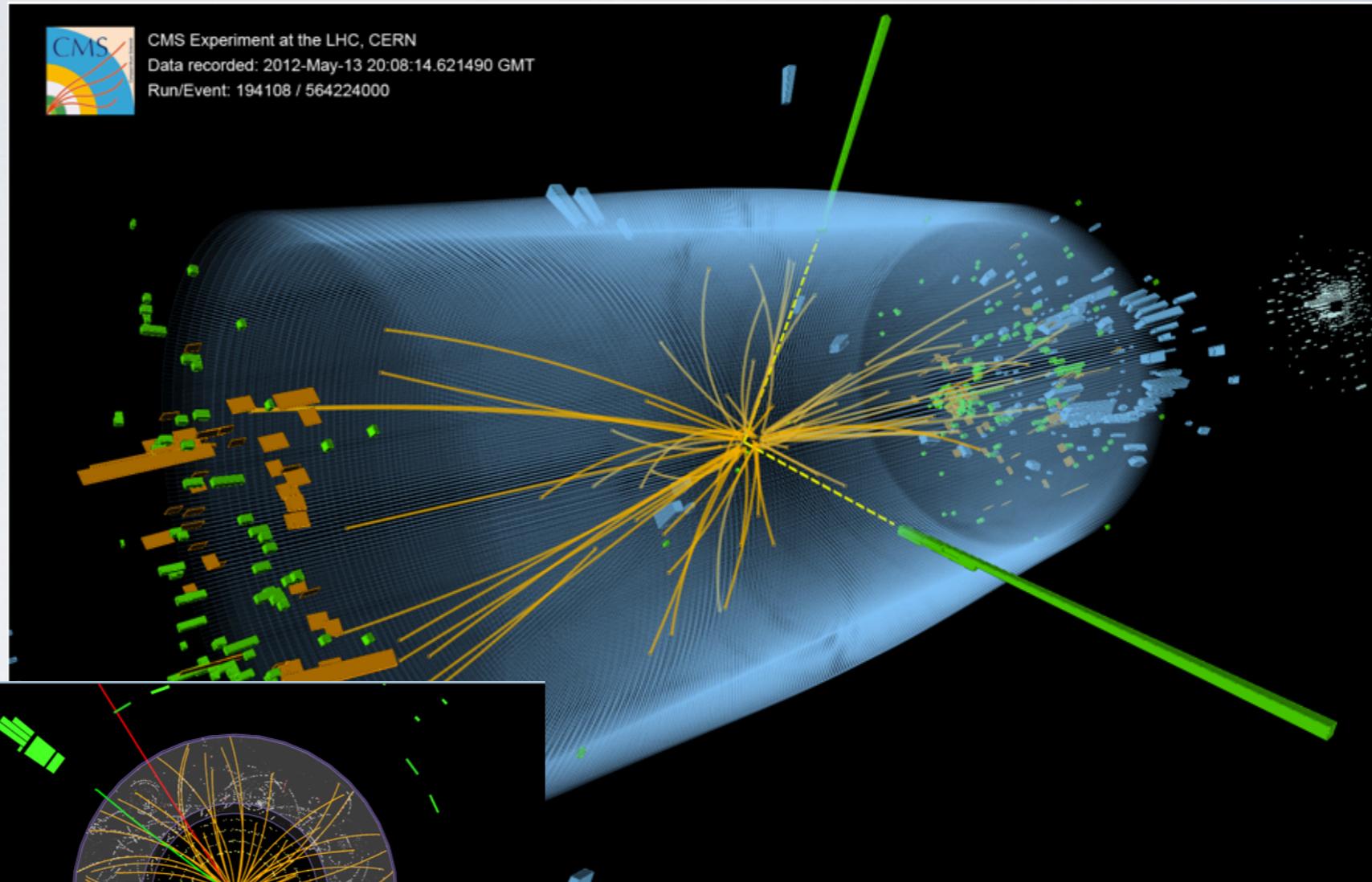


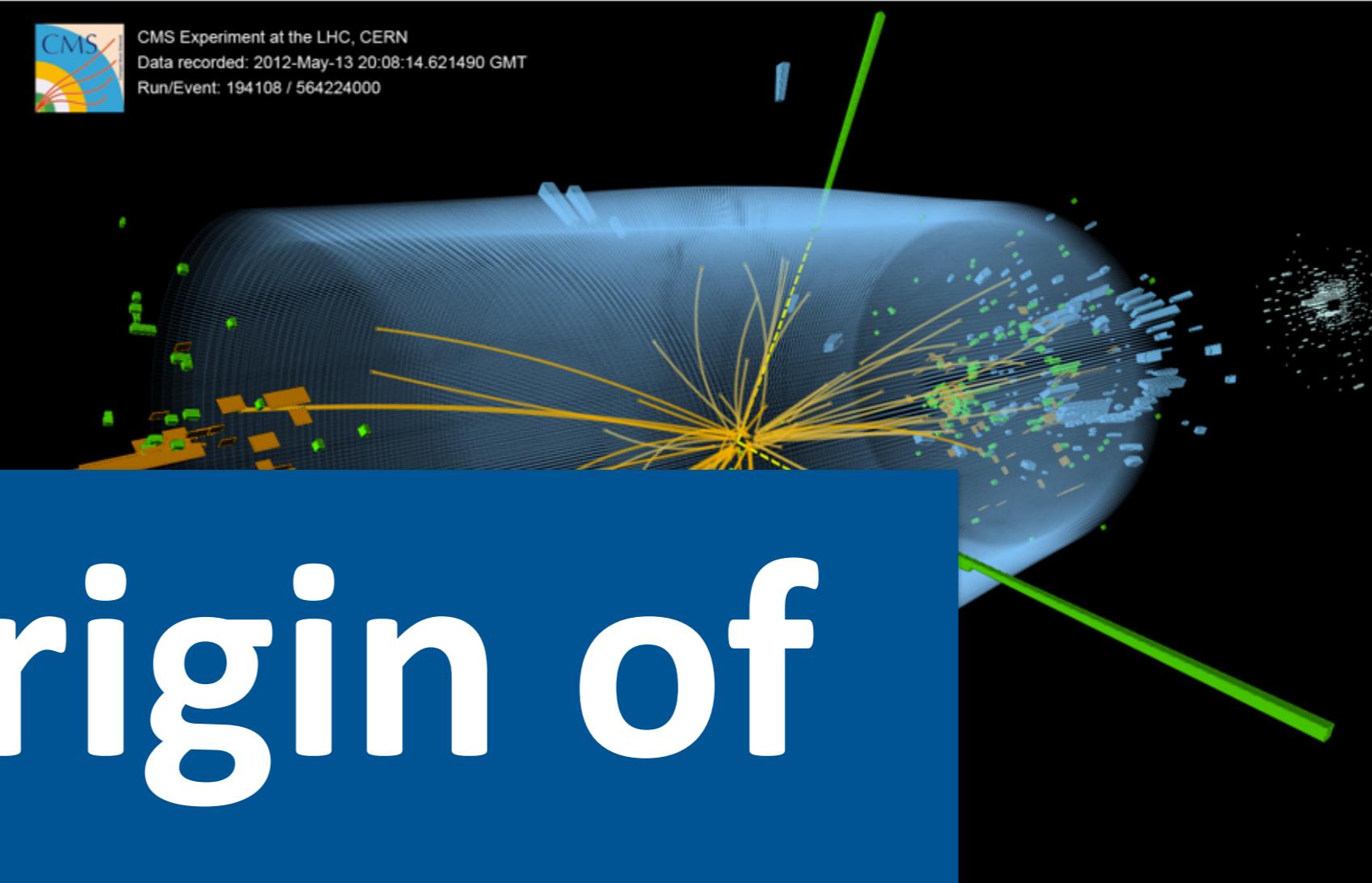
# DYNAMICAL HIGGS

**Luca Merlo**

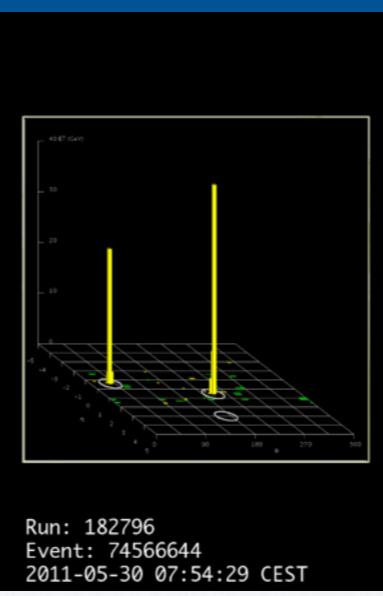
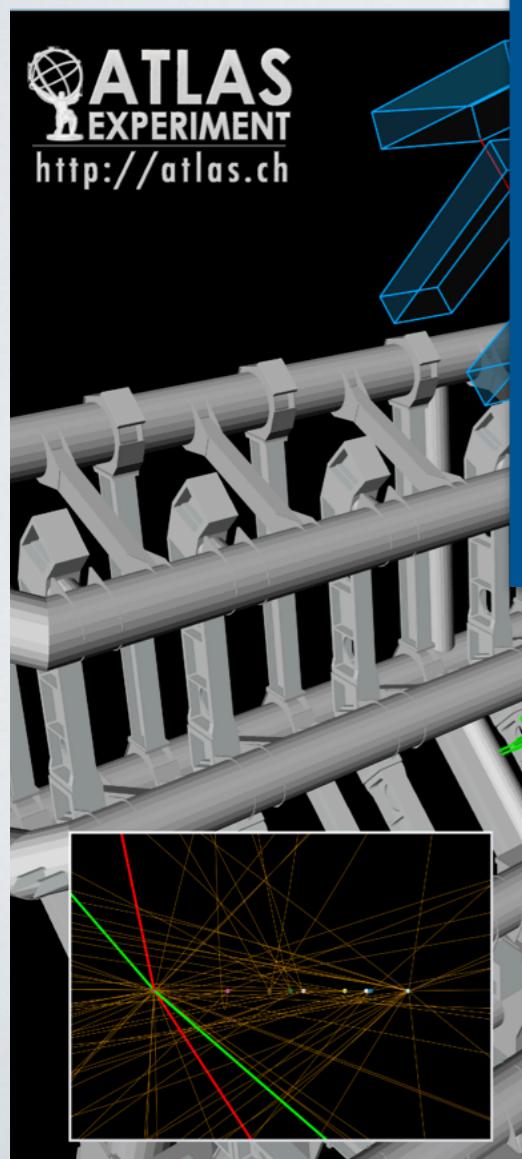


**January 30th 2014, Benasque, Spain**





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- Alternatively, this resonance could be related to a **strong dynamics** at the scale  $\Lambda_s \sim \mathcal{O}(\text{TeV})$
- **Technicolor:** only the usual 3 GBs are accounted for, but no light scalar particle is present.
- **Composite Higgs:** a larger global symmetry is considered and the SM scalar particle arises as a (massless) GB. In this case the resonance corresponds to a composite object.

# Content

- SM Higgs and d=6 linear effective Lagrangian
- A dynamical Higgs (composite state):
  - The Appelquist-Longhitano-Feruglio basis (no Higgs)
  - The bosonic basis for a light dynamical  $h$
- Disentangling a dynamical Higgs from an elementary one

# The d=6 linear effective Lagrangian

- With no evidence of specific beyond SM theories, NP effects above the TeV scale can be parametrised by writing the **Linear Effective Lagrangian** including up to d=6 operators in terms of the **Higgs doublet**:

$$\mathcal{L}_{\text{linear}} = \mathcal{L}_{SM} + \sum_i \frac{f_i}{\Lambda^2} \mathcal{O}_i + \text{higher orders}$$

with  $\Lambda$  ( $\geq$  few TeV) the NP scale.

- Once restricting only to the **bosonic sector**, the effective Lagrangian is built using the SM gauge fields strengths  $G_{\mu\nu}$ ,  $W_{\mu\nu}$  and  $B_{\mu\nu}$ , and the Higgs doublet  $\Phi$  (plus covariant derivatives).

# The d=6 linear Lagrangian: HISZ

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$$\begin{aligned}\mathcal{L}_{SM} = & -\frac{1}{4}W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4}B_{\mu\nu} B^{\mu\nu} - \frac{1}{4}G_{\mu\nu}^a G^{a\mu\nu} - V(h) \\ & + (D_\mu \Phi)^\dagger (D^\mu \Phi) + i\bar{Q} \not{D} Q + i\bar{L} \not{D} L \\ & - (\bar{Q}_L \Phi \mathcal{Y}_D D_R + \text{h.c.}) - (\bar{Q}_L \tilde{\Phi} \mathcal{Y}_U U_R + \text{h.c.}) \\ & - (\bar{L}_L \Phi \mathcal{Y}_L L_R + \text{h.c.})\end{aligned}$$

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These operators describe pure gauge, gauge- $h$  and pure- $h$  interactions and several **correlations** among observables are predicted: i.e. triple gauge couplings vs. HVV couplings. **SMOKING GUNS!!!**

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**10 parameters**

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[Longhitano, PRD22 (1980)]

$$\mathbf{M}(x) \equiv \sqrt{2} \begin{pmatrix} \tilde{\Phi}(x) & \Phi(x) \end{pmatrix}$$

$$V(\mathbf{M}) = \frac{1}{4} \lambda \left( \frac{1}{2} \text{Tr}[\mathbf{M}^\dagger \mathbf{M}] + \frac{\mu^2}{\lambda} \right)^2$$

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- When  $\mathbf{M}$  develops VEV  $\langle \mathbf{M}^\dagger \mathbf{M} \rangle = v^2 \mathbf{1}$

$O(4) \rightarrow SU(2)_V$  custodial symmetry

$SU(2)_L \times U(1)_Y \rightarrow U(1)_{em}$

# The non-linear $\sigma$ -model notation

- Thinking at a very **heavy Higgs particle**, all the remaining d.o.f. are the longitudinal components of the gauge bosons and are described by

$$\mathbf{U}(x) \equiv \mathbf{M}(x)/v = e^{i\sigma_a \pi^a(x)/v}$$

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- Writing the covariant derivative as:

$$\mathbf{D}_\mu \mathbf{U}(x) \equiv \partial_\mu \mathbf{U}(x) + \frac{ig}{2} W_\mu^a(x) \sigma_a \mathbf{U}(x) - \frac{ig'}{2} B_\mu(x) \mathbf{U}(x) \sigma_3$$

we can define the vector and the scalar chiral fields

$$\mathbf{V}_\mu \equiv (\mathbf{D}_\mu \mathbf{U}) \mathbf{U}^\dagger \quad \mathbf{V} \rightarrow L \mathbf{V} L^\dagger$$

$$\mathbf{T} \equiv \mathbf{U} \sigma_3 \mathbf{U}^\dagger \quad \mathbf{T} \rightarrow L \mathbf{T} L^\dagger$$

# The ALF Basis

Making use of these objects, it is possible to construct a basis of independent operators describing all the  $SU(2)_L \times U(1)_Y$  interactions, with no Higgs involved and considering only CP-even structures:

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$\downarrow$

$W, Z$  masses  
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$\downarrow$

Yukawa terms

- $- (\bar{Q}_L \Phi \mathcal{Y}_D D_R + \text{h.c.})$
- $- (\bar{Q}_L \tilde{\Phi} \mathcal{Y}_U U_R + \text{h.c.})$
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$W, Z$  masses  
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 $(D_\mu \Phi)^\dagger (D^\mu \Phi)$

custodial breaking  $Z$  mass contribution

$$\mathcal{O}_{\Phi,1} = (D_\mu \Phi)^\dagger \Phi \Phi^\dagger (D^\mu \Phi)$$

**d=6**

$$-1.7 \times 10^{-3} < \Delta\rho \equiv c_T < 1.9 \times 10^{-3}$$

$$\mathcal{L}_{ALF}^{p=4} = -\frac{1}{4}W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}G_{\mu\nu}^a G^{a\mu\nu} + \sum c_i \mathcal{A}_i$$

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$$\mathcal{A}_1 = g g' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu})$$

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$$\mathcal{A}_3 = i g \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu])$$

$$\mathcal{A}_4 = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2$$

$$\mathcal{A}_5 = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2$$

$$\mathcal{A}_6 = g^2 (\text{Tr}(\mathbf{T} W^{\mu\nu}))^2$$

$$\mathcal{A}_7 = i g \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu])$$

$$\mathcal{A}_8 = g \epsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda})$$

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[Appelquist&Bernard, Phys. Rev. D22 (1980) 200]

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$$\begin{aligned}\mathcal{A}_{12} &= \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \\ \mathcal{A}_{13} &= \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \\ \mathcal{A}_{14} &= \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu)\end{aligned}$$

**If  $\mathbf{m}_f=0$  then these operators are not independent from the others**

[Feruglio, Int.J.Mod.Phys. A8 (1993) 4937–4972]

$$\mathcal{L}_{ALF}^{p=4} = -\frac{1}{4}W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4}B_{\mu\nu} B^{\mu\nu} - \frac{1}{4}G_{\mu\nu}^a G^{a\mu\nu} + \sum c_i \mathcal{A}_i$$

$$\begin{aligned}\mathcal{A}_1 &= g g' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \\ \mathcal{A}_2 &= i g' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \\ \mathcal{A}_3 &= i g \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \\ \mathcal{A}_4 &= (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \\ \mathcal{A}_5 &= (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \\ \mathcal{A}_6 &= g^2 (\text{Tr}(\mathbf{T} W^{\mu\nu}))^2\end{aligned}$$

$$\begin{aligned}\mathcal{A}_7 &= i g \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \\ \mathcal{A}_8 &= g \epsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \\ \mathcal{A}_9 &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \\ \mathcal{A}_{10} &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \\ \mathcal{A}_{11} &= (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2\end{aligned}$$

[Appelquist&Bernard, Phys. Rev. D22 (1980) 200]

[Phys. Rev. D22 (1980) 1166]

[Phys. B188 (1981) 118]

[Phys. Rev. D48 (1993) 3235–3241]

**14(11) + 1**

**parameters**

$$\mathcal{A}_{12} = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2)$$

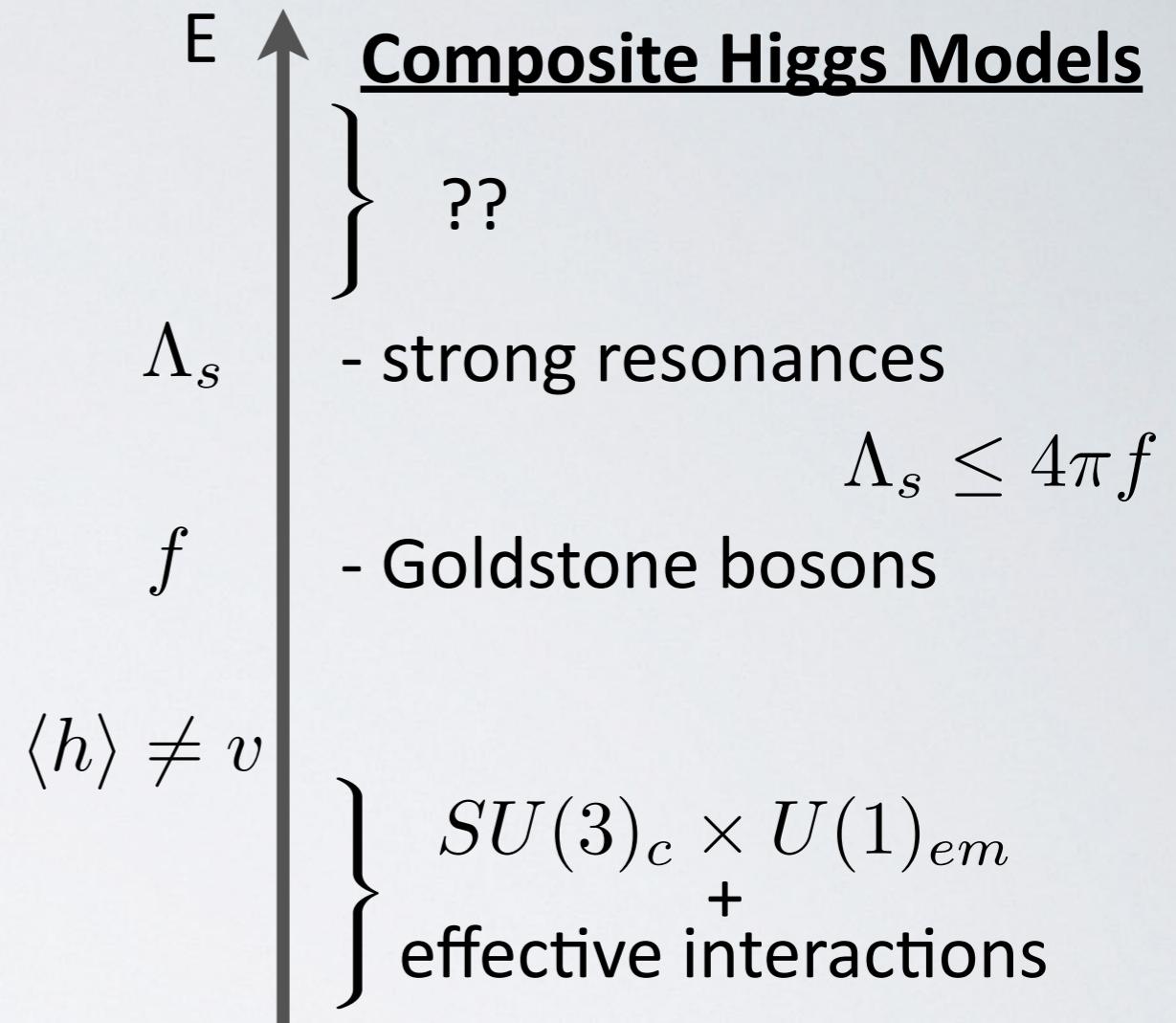
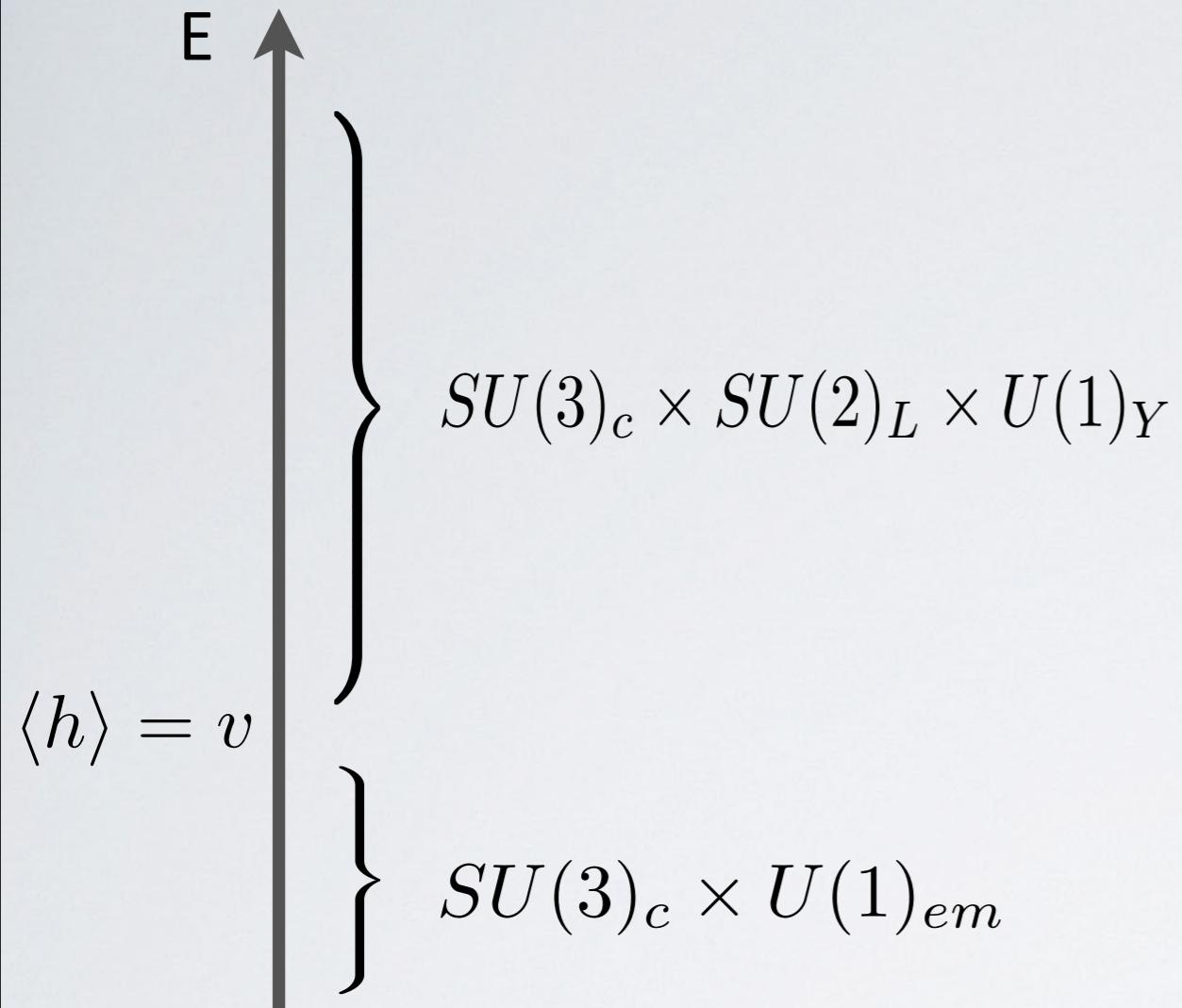
$$\mathcal{A}_{13} = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu)$$

$$\mathcal{A}_{14} = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu)$$

**If  $m_f=0$  then these operators are not independent from the others**

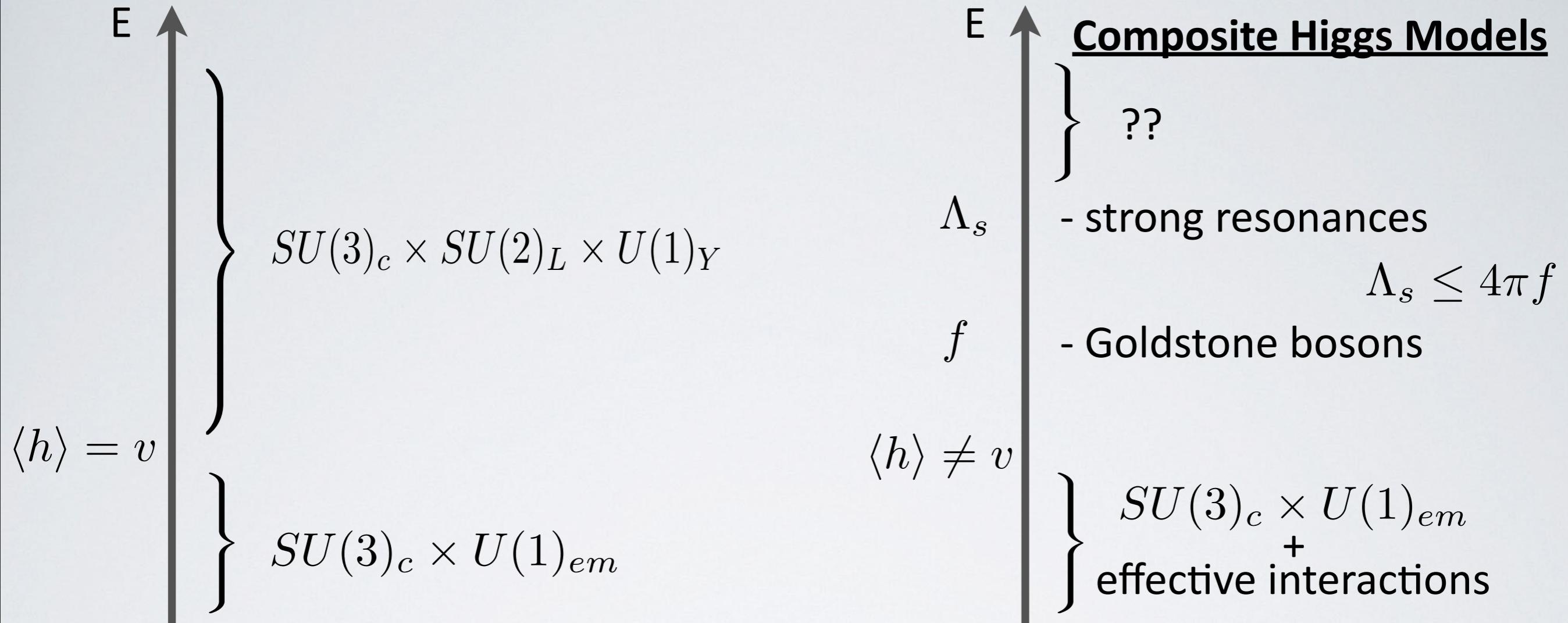
[Feruglio, Int.J.Mod.Phys. A8 (1993) 4937–4972]

# What with a physical Higgs?!



[Georgi & Kaplan, 1984;  
Dimopoulos, Georgi & Kaplan 1984;  
Banks, 1984;  
Galison, Georgi, & Kaplan, 1984;  
Dugan, Georgi & Kaplan 1985;  
Agashe, Contino & Pomarol 2005;  
Gripaios, Pomarol, Riva & Serra 2009;  
...]

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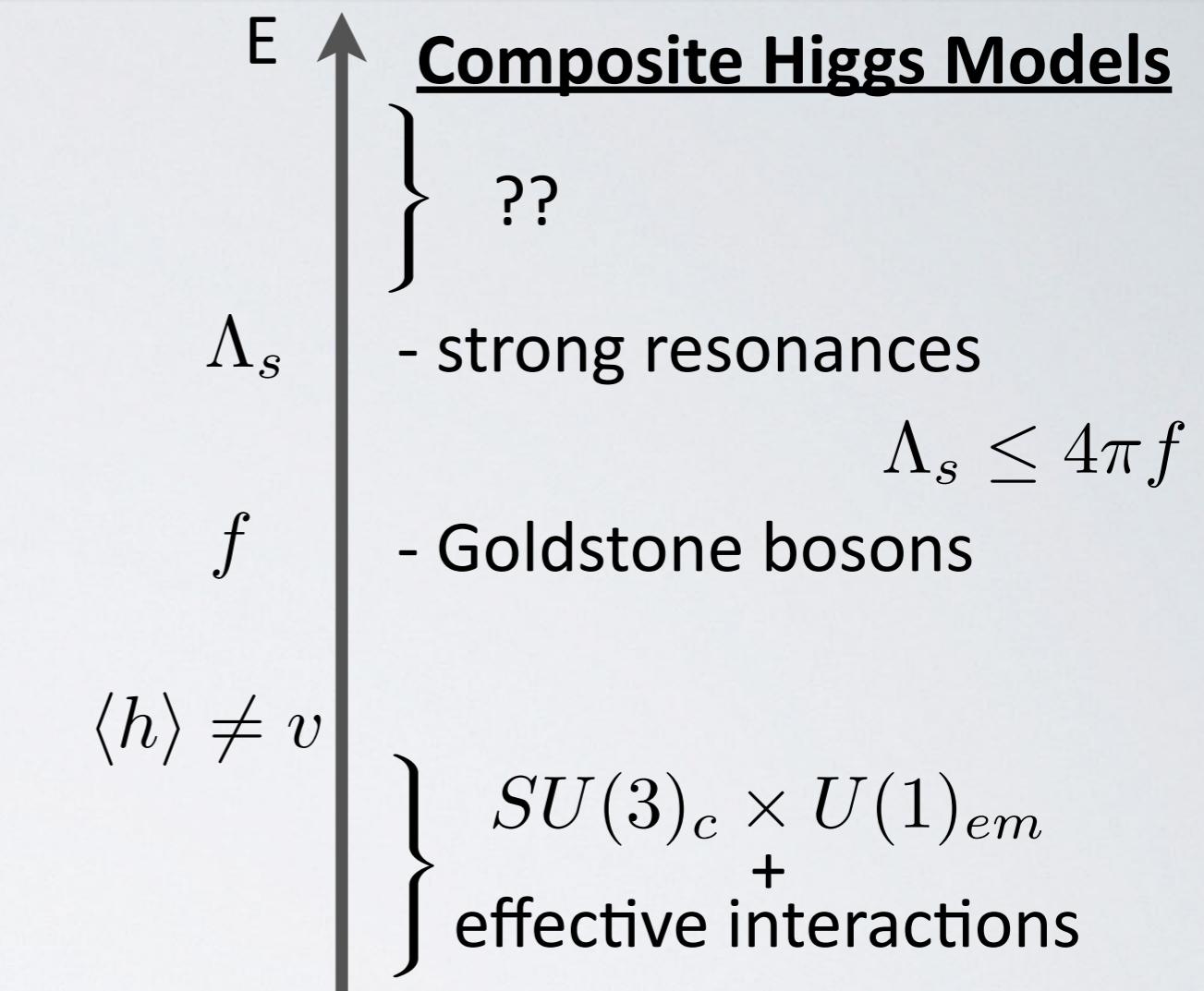
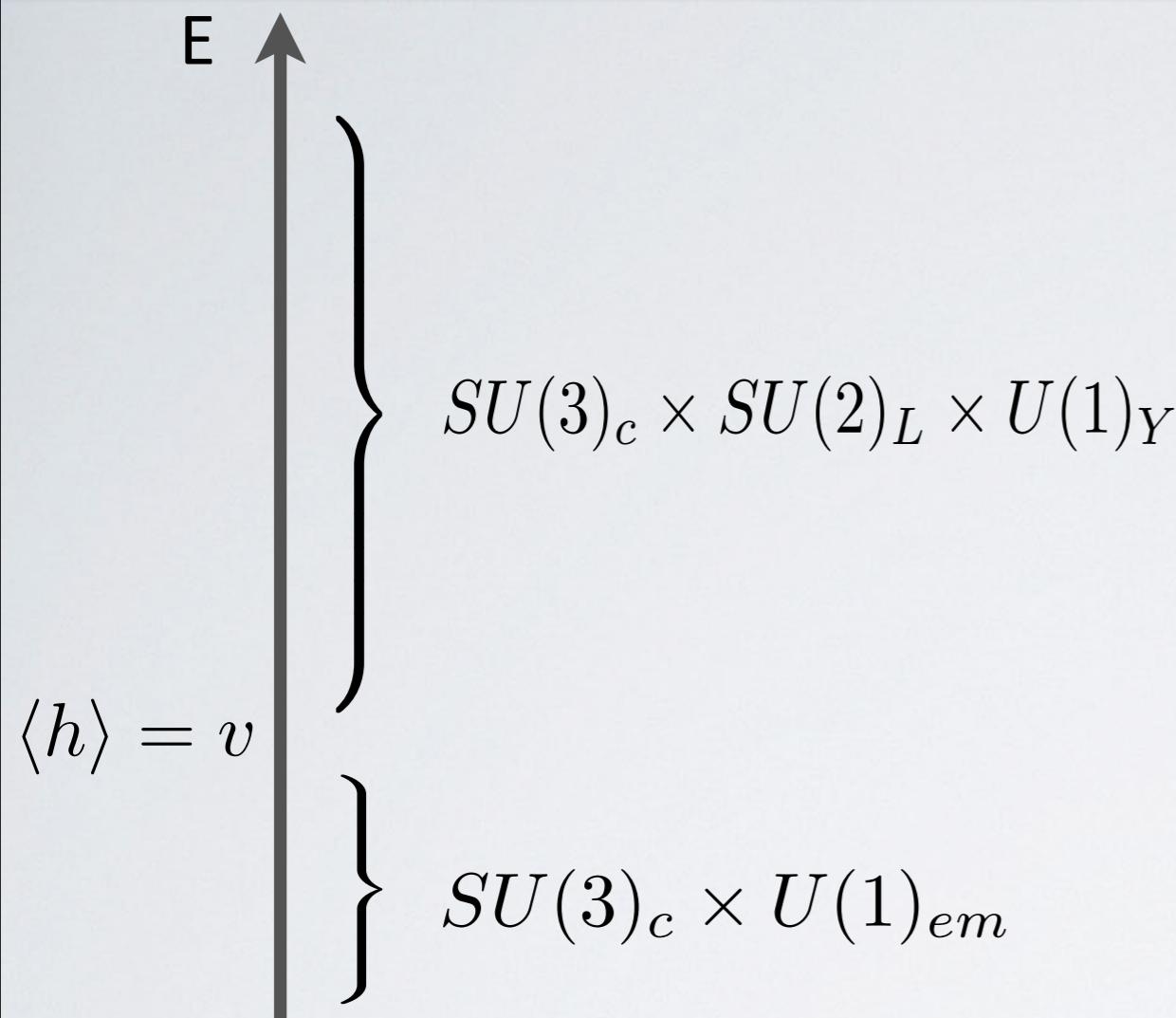


Higher order operators are suppressed by:

$f$  for extra Goldstone leg (Goldstone-Higgs included)

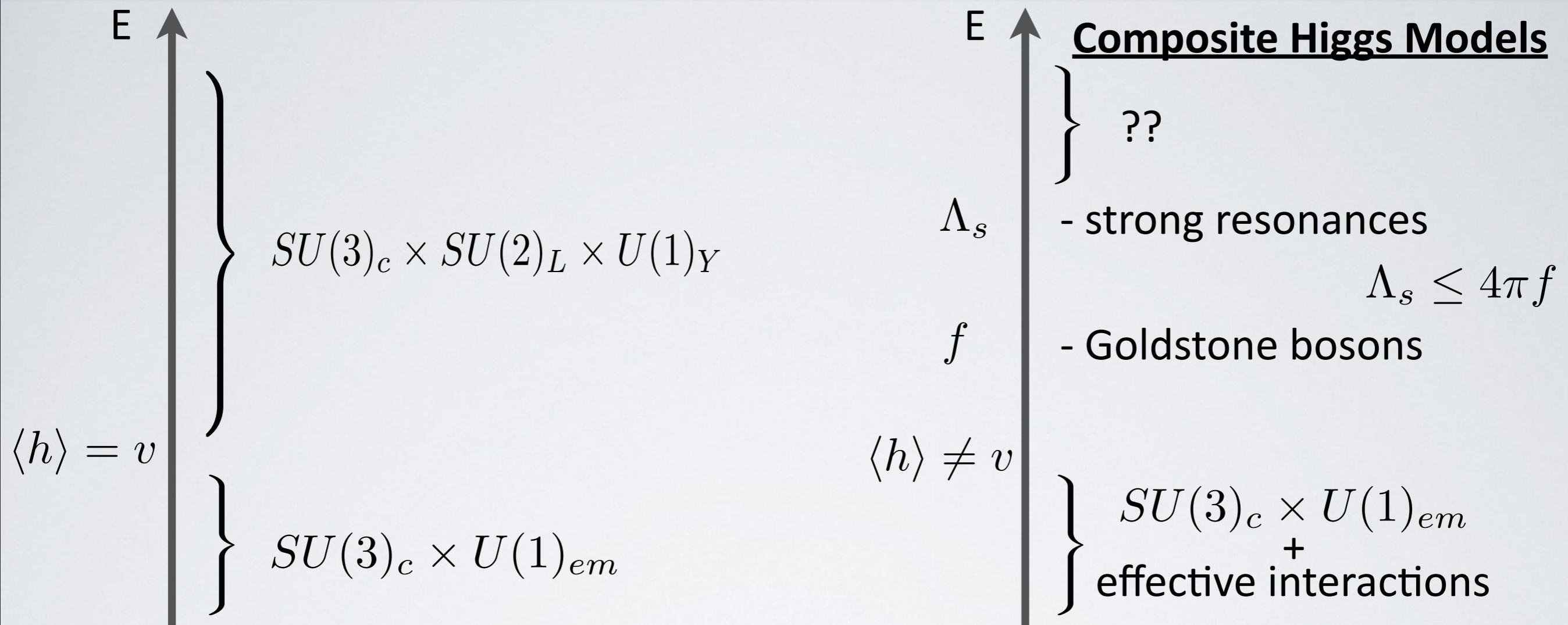
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  - $f$  for extra Goldstone leg (Goldstone-Higgs included)
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- The degree of non-linearity is described by  $\xi \equiv (v/f)^2$

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- Higher order operators are suppressed by:
  - $f$  for extra Goldstone leg (Goldstone-Higgs included)
  - $\Lambda_s$  for extra derivatives and gauge field strength [Manohar&Georgi, 1984]
- The degree of non-linearity is described by  $\xi \equiv (v/f)^2$
- Special limit: SM corresponds to  $\langle h \rangle \equiv v$ ,  $\Lambda_s, f \gg v$ ,  $\xi \rightarrow 0$

The low-energy effective Lagrangian is constructed by means of:

$$\begin{cases} \mathbf{U}(x) = e^{i\sigma_a \pi^a(x)/v} \\ \mathbf{T} \equiv \mathbf{U}\sigma_3\mathbf{U}^\dagger & \mathbf{V}_\mu \equiv (\mathbf{D}_\mu \mathbf{U}) \mathbf{U}^\dagger \end{cases} \quad \begin{cases} h \\ \partial_\mu h \end{cases}$$

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- The GBs are in the Higgs doublet  $\Phi$
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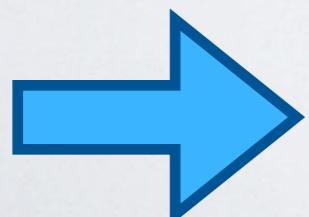
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**The dimension of the leading low-energy operators differs for a purely linear and a non-linear regime**

# The (Dynamical) Chiral Lagrangian

First time the complete pure-gauge & gauge- $h$  basis

[Alonso, Gavela, LM, Rigolin & Yepes, Phys.Lett. **B722** (2013) 330-335]

$$\mathcal{L}_{\text{chiral}} = \mathcal{L}_0 + \Delta\mathcal{L}$$

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$$\mathcal{L}_{\text{chiral}} = \mathcal{L}_0 + \Delta\mathcal{L}$$

$$\begin{aligned}\mathcal{L}_0 = & \frac{1}{2}(\partial_\mu h)(\partial^\mu h) - \frac{1}{4}W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4}B_{\mu\nu} B^{\mu\nu} - \frac{1}{4}G_{\mu\nu}^a G^{a\mu\nu} - V(h) \\ & - \frac{(v+h)^2}{4} \text{Tr}[\mathbf{V}_\mu \mathbf{V}^\mu] + i\bar{Q} \not{D} Q + i\bar{L} \not{D} L \\ & - \frac{v+s_Y h}{\sqrt{2}} (\bar{Q}_L \mathbf{U} \gamma_Q Q_R + \text{h.c.}) - \frac{v+s_Y h}{\sqrt{2}} (\bar{L}_L \mathbf{U} \gamma_L L_R + \text{h.c.}) ,\end{aligned}$$

$s_Y$  accounts for a possible negative sign in the  $h$ -fermion couplings.

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$$\Delta\mathcal{L} = c_B \mathcal{P}_B(h) + c_W \mathcal{P}_W(h) + c_G \mathcal{P}_G(h) + c_C \mathcal{P}_C(h) + c_T \mathcal{P}_T(h) + \sum c_i \mathcal{P}_i(h)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h)$$

$$\mathcal{P}_{17}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_{18}(h) = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_{19}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{F}_i(h) \equiv g(h, f)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

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## BLUE

in the limit  $\mathcal{F}_i(h) = 1$  they reduce to the AL basis (plus non-physical contributions to the kinetic terms and W and Z masses)

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

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$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

**GREEN**

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

in the limit  $\mathcal{F}_i(h) = 1$  they reduce to the gauge-Goldstone Feruglio operators

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

**RED**

new Higgs couplings in the ALF basis, and new operators with derivatives of  $h$  (few of them already present in Azatov, Contino & Galloway (2012))

$$\mathcal{F}_T(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T}\mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_{17}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_{18}(h) = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

$$\mathcal{P}_{19}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{F}_i(h) \equiv g(h, f)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h)$$

$$\mathcal{P}_{17}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_{18}(h) = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_{19}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{F}_i(h) \equiv g(h, f)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_{17}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_{18}(h) = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

$$\mathcal{P}_{19}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{F}_i(h) \equiv g(h, f)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu})$$

$$V_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu])$$

$$, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu])$$

$$V^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu)$$

$${}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu$$

$$(\mu)) {}^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{F}_i(h) \equiv g(h, f)$$

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parameters

# The $\mathcal{F}_i(h)$ Functions

[Brivio,Corbett,Eboli,Gavela,Gonzalez-Fraile,Gonzalez-Garcia,LM&Rigolin, 1311.1823]

The functions  $\mathcal{F}_i(h) \equiv g(h, f)$  are generic functions of  $h/f$  (and can be derived only once a fundamental model is chosen). It is common to write,

$$\mathcal{F}_i(h) = 1 + 2\alpha_i \frac{h}{v} + \beta_i \frac{h^2}{v^2} + \dots$$

with  $\alpha_i, \beta_i$  generic functions of  $\xi \equiv v^2/f^2$ .

# The $\mathcal{F}_i(h)$ Functions

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$$\mathcal{F}_i(h) = 1 + 2\alpha_i \frac{h}{v} + \beta_i \frac{h^2}{v^2} + \dots$$

with  $\alpha_i, \beta_i$  generic functions of  $\xi \equiv v^2/f^2$ .

If we consider the SM as a reference, the combinations  $c_i \mathcal{F}_i(h)$  become:

$$\begin{aligned} \frac{f_{BW}}{f^2} \mathcal{O}_{BW} &= \frac{f_{BW}}{f^2} \Phi^\dagger \hat{B}_{\mu\nu} \hat{W}^{\mu\nu} \Phi & \Phi(x) &= \frac{v+h}{\sqrt{2}} \mathbf{U} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ &= f_{BW} \frac{gg'}{8} B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \left( \frac{v+h}{f} \right)^2 \\ &= f_{BW} \xi \frac{gg'}{8} B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \left( 1 + \frac{h}{v} \right)^2 \\ &= c_1 gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h) = c_1 \mathcal{P}_1(h) \end{aligned}$$

with  $c_1 = \frac{f_{BW}}{8} \xi$        $\alpha_1 = 1$        $\beta_1 = 1$

# Connection with the Linear Basis

We can repeat the previous exercise and see the connection among the bases:

$$\mathcal{O}_{BB}/f^2 = \frac{\xi}{2}\mathcal{P}_B(h)$$

$$\mathcal{O}_{GG}/f^2 = -\frac{2\xi}{g_s^2}\mathcal{P}_G(h)$$

$$\mathcal{O}_B/f^2 = \frac{\xi}{16}\mathcal{P}_2(h) + \frac{\xi}{8}\mathcal{P}_4(h)$$

$$\mathcal{O}_{\Phi,1}/f^2 = \frac{\xi}{2}\mathcal{P}_H(h) - \frac{\xi}{4}\mathcal{F}(h)\mathcal{P}_T(h)$$

$$\mathcal{O}_{\Phi,4}/f^2 = \frac{\xi}{2}\mathcal{P}_H(h) + \frac{\xi}{2}\mathcal{F}(h)\mathcal{P}_C(h)$$

$$\mathcal{O}_{\square\Phi}/f^2 = \frac{\xi}{2}\mathcal{P}_{\square H}(h) + \frac{\xi}{8}\mathcal{P}_6(h) + \frac{\xi}{4}\mathcal{P}_7(h) - \xi\mathcal{P}_8(h) - \frac{\xi}{4}\mathcal{P}_9(h) - \frac{\xi}{2}\mathcal{P}_{10}(h)$$

$$\mathcal{O}_{WW}/f^2 = \frac{\xi}{2}\mathcal{P}_W(h)$$

$$\mathcal{O}_{BW}/f^2 = \frac{\xi}{8}\mathcal{P}_1(h)$$

$$\mathcal{O}_W/f^2 = \frac{\xi}{8}\mathcal{P}_3(h) - \frac{\xi}{4}\mathcal{P}_5(h)$$

$$\mathcal{O}_{\Phi,2}/f^2 = \xi\mathcal{P}_H(h)$$

$$\text{with } \mathcal{F}(h) = 1 + 2\frac{h}{v} + \frac{h^2}{v^2}$$

We added two pure- $h$  operators (only the first was previously considered by Buchalla,Cata,&Krause (2013)):

$$\mathcal{P}_H(h) = \frac{1}{2}(\partial_\mu h)(\partial^\mu h)\mathcal{F}_H(h)$$

$$\mathcal{P}_{\square H} = \frac{1}{v^2}(\partial_\mu \partial^\mu h)^2 \mathcal{F}_{\square H}(h)$$

$$\begin{aligned}
\mathcal{P}_C(h) &= -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h) & \mathcal{P}_{12}(h) &= g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h) \\
\mathcal{P}_T(h) &= \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h) & \mathcal{P}_{13}(h) &= ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h) \\
\mathcal{P}_B(h) &= -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h) & \mathcal{P}_{14}(h) &= g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h) \\
\mathcal{P}_W(h) &= -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h) & \mathcal{P}_{15}(h) &= \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h) \\
\mathcal{P}_G(h) &= -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h) & \mathcal{P}_{16}(h) &= \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h) \\
\mathcal{P}_1(h) &= gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h) & \mathcal{P}_{17}(h) &= ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h) \\
\mathcal{P}_2(h) &= ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h) & \mathcal{P}_{18}(h) &= \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h) \\
\mathcal{P}_3(h) &= ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h) & \mathcal{P}_{19}(h) &= \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h) \\
\mathcal{P}_4(h) &= ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h) & \mathcal{P}_{20}(h) &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h) \\
\mathcal{P}_5(h) &= ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h) & \mathcal{P}_{21}(h) &= (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h) \\
\mathcal{P}_6(h) &= (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h) & \mathcal{P}_{22}(h) &= \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h) \\
\mathcal{P}_7(h) &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h) & \mathcal{P}_{23}(h) &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h) \\
\mathcal{P}_8(h) &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h) & \mathcal{P}_{24}(h) &= \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h) \\
\mathcal{P}_9(h) &= \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h) & \mathcal{P}_{25}(h) &= (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h) \\
\mathcal{P}_{10}(h) &= \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h) & \mathcal{P}_{26}(h) &= (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h) \\
\mathcal{P}_{11}(h) &= (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h) & \mathcal{P}_H(h) &= \frac{1}{2} (\partial_\mu h) (\partial^\mu h) \mathcal{F}_H(h) \\
&& \mathcal{P}_{\square H} &= \frac{1}{v^2} (\partial_\mu \partial^\mu h)^2 \mathcal{F}_{\square H}(h)
\end{aligned}$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{W}^{\mu\nu}) \mathcal{F}_1(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

**GREEN**

have siblings of d=6 and then are weighted by  $\xi$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{P}_H(h) = \frac{1}{2} (\partial_\mu h) (\partial^\mu h) \mathcal{F}_H(h)$$

$$\mathcal{P}_{\square H} = \frac{1}{v^2} (\partial_\mu \partial^\mu h)^2 \mathcal{F}_{\square H}(h)$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

**BLUE**

have siblings of d=8 and then are weighted by  $\xi^2$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T}[\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

$$\mathcal{P}_6(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu))^2 \mathcal{F}_6(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_8(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \partial^\mu \mathcal{F}_8(h) \partial^\nu \mathcal{F}'_8(h)$$

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T}[\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_{17}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_{18}(h) = \text{Tr}(\mathbf{T}[\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

$$\mathcal{P}_{19}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{P}_H(h) = \frac{1}{2} (\partial_\mu h) (\partial^\mu h) \mathcal{F}_H(h)$$

$$\mathcal{P}_{\square H} = \frac{1}{v^2} (\partial_\mu \partial^\mu h)^2 \mathcal{F}_{\square H}(h)$$

$$\mathcal{P}_C(h) = -\frac{v^2}{4} \text{Tr}(\mathbf{V}^\mu \mathbf{V}_\mu) \mathcal{F}_C(h)$$

$$\mathcal{P}_T(h) = \frac{v^2}{4} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \mathcal{F}_T(h)$$

$$\mathcal{P}_B(h) = -\frac{g'^2}{4} B_{\mu\nu} B^{\mu\nu} \mathcal{F}_B(h)$$

$$\mathcal{P}_W(h) = -\frac{g^2}{4} W_{\mu\nu}^a W^{a\mu\nu} \mathcal{F}_W(h)$$

$$\mathcal{P}_G(h) = -\frac{g_s^2}{4} G_{\mu\nu}^a G^{a\mu\nu} \mathcal{F}_G(h)$$

$$\mathcal{P}_1(h) = gg' B_{\mu\nu} \text{Tr}(\mathbf{T} W^{\mu\nu}) \mathcal{F}_1(h)$$

$$\mathcal{P}_2(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_2(h)$$

$$\mathcal{P}_3(h) = ig \text{Tr}(W_{\mu\nu} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_3(h)$$

$$\mathcal{P}_4(h) = ig' B_{\mu\nu} \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_4(h)$$

$$\mathcal{P}_5(h) = ig \text{Tr}(W_{\mu\nu} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_5(h)$$

**RED**

have siblings of d=12 and then are weighted by  $\xi^4$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{11}(h) = (\text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu))^2 \mathcal{F}_{11}(h)$$

$$\mathcal{P}_{12}(h) = g^2 (\text{Tr}(\mathbf{T} W_{\mu\nu}))^2 \mathcal{F}_{12}(h)$$

$$\mathcal{P}_{13}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} [\mathbf{V}^\mu, \mathbf{V}^\nu]) \mathcal{F}_{13}(h)$$

$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_{17}(h) = ig \text{Tr}(\mathbf{T} W_{\mu\nu}) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{17}(h)$$

$$\mathcal{P}_{18}(h) = \text{Tr}(\mathbf{T} [\mathbf{V}_\mu, \mathbf{V}_\nu]) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{18}(h)$$

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$$\mathcal{P}_{20}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \mathcal{F}_{20}(h) \partial^\nu \mathcal{F}'_{20}(h)$$

$$\mathcal{P}_{21}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \mathcal{F}_{21}(h) \partial^\nu \mathcal{F}'_{21}(h)$$

$$\mathcal{P}_{22}(h) = \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\mu \mathcal{F}_{22}(h) \partial^\nu \mathcal{F}'_{22}(h)$$

$$\mathcal{P}_{23}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) (\text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{23}(h)$$

$$\mathcal{P}_{24}(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}_\nu) \text{Tr}(\mathbf{T} \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{24}(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

$$\mathcal{P}_{26}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu))^2 \mathcal{F}_{26}(h)$$

$$\mathcal{P}_H(h) = \frac{1}{2} (\partial_\mu h) (\partial^\mu h) \mathcal{F}_H(h)$$

$$\mathcal{P}_{\square H} = \frac{1}{v^2} (\partial_\mu \partial^\mu h)^2 \mathcal{F}_{\square H}(h)$$

# Disentangling a Dynamical Higgs I

[Brivio,Corbett,Eboli,Gavela,Gonzalez-Fraile,Gonzalez-Garcia,LM&Rigolin, 1311.1823]

Correlations present in the linear basis are absent in the chiral basis

$$\mathcal{O}_B/f^2 = \frac{\xi}{16}\mathcal{P}_2(h) + \frac{\xi}{8}\mathcal{P}_4(h) \quad (\text{similar for } \mathcal{O}_W)$$

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$$\begin{aligned} \mathcal{O}_B = & \frac{ieg^2}{8} A_{\mu\nu} W^{-\mu} W^{+\nu} (v+h)^2 - \frac{ie^2 g}{8 \cos \theta_W} Z_{\mu\nu} W^{-\mu} W^{+\nu} (v+h)^2 \\ & - \frac{eg}{4 \cos \theta_W} A_{\mu\nu} Z^\mu \partial^\nu h (v+h) + \frac{e^2}{4 \cos^2 \theta_W} Z_{\mu\nu} Z^\mu \partial^\nu h (v+h) \end{aligned}$$

$$\mathcal{P}_2(h) = 2ieg^2 A_{\mu\nu} W^{-\mu} W^{+\nu} \mathcal{F}_2(h) - 2 \frac{ie^2 g}{\cos \theta_W} Z_{\mu\nu} W^{-\mu} W^{+\nu} \mathcal{F}_2(h)$$

$$\mathcal{P}_4(h) = - \frac{eg}{\cos \theta_W} A_{\mu\nu} Z^\mu \partial^\nu \mathcal{F}_4(h) + \frac{e^2}{\cos^2 \theta_W} Z_{\mu\nu} Z^\mu \partial^\nu \mathcal{F}_4(h)$$

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$$\mathcal{P}_2(h) = 2ieg^2 A_{\mu\nu} W^{-\mu} W^{+\nu} \mathcal{F}_2(h) - 2 \frac{ie^2 g}{\cos \theta_W} Z_{\mu\nu} W^{-\mu} W^{+\nu} \mathcal{F}_2(h)$$

$$\mathcal{P}_4(h) = -\frac{eg}{\cos \theta_W} A_{\mu\nu} Z^\mu \partial^\nu \mathcal{F}_4(h) + \frac{e^2}{\cos^2 \theta_W} Z_{\mu\nu} Z^\mu \partial^\nu \mathcal{F}_4(h)$$

due to the decorrelation in the  $\mathcal{F}_i(h)$  functions: i.e.

$$\begin{aligned} \gamma - W - W - h & \leftrightarrow \gamma - W - W \\ Z - W - W - h & \leftrightarrow Z - W - W \end{aligned}$$

$$\mathcal{F}_i(h) \equiv g(h, f)$$

# Disentangling a Dynamical Higgs I

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Correlations present in the linear basis are absent in the chiral basis

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$$\begin{aligned} \mathcal{O}_B = & \frac{ieg^2}{8} A_{\mu\nu} W^{-\mu} W^{+\nu} (v+h)^2 - \frac{ie^2 g}{8 \cos \theta_W} Z_{\mu\nu} W^{-\mu} W^{+\nu} (v+h)^2 \\ & - \frac{eg}{4 \cos \theta_W} A_{\mu\nu} Z^\mu \partial^\nu h (v+h) + \frac{e^2}{4 \cos^2 \theta_W} Z_{\mu\nu} Z^\mu \partial^\nu h (v+h) \end{aligned}$$

$$\mathcal{P}_2(h) = 2ieg^2 A_{\mu\nu} W^{-\mu} W^{+\nu} \mathcal{F}_2(h) - 2 \frac{ie^2 g}{\cos \theta_W} Z_{\mu\nu} W^{-\mu} W^{+\nu} \mathcal{F}_2(h)$$

$$\mathcal{P}_4(h) = -\frac{eg}{\cos \theta_W} A_{\mu\nu} Z^\mu \partial^\nu \mathcal{F}_4(h) + \frac{e^2}{\cos^2 \theta_W} Z_{\mu\nu} Z^\mu \partial^\nu \mathcal{F}_4(h)$$

due to the nature of the chiral operators (different  $c_i$  coefficients): i.e.

$$\gamma - W - W \leftrightarrow \gamma - Z - h$$

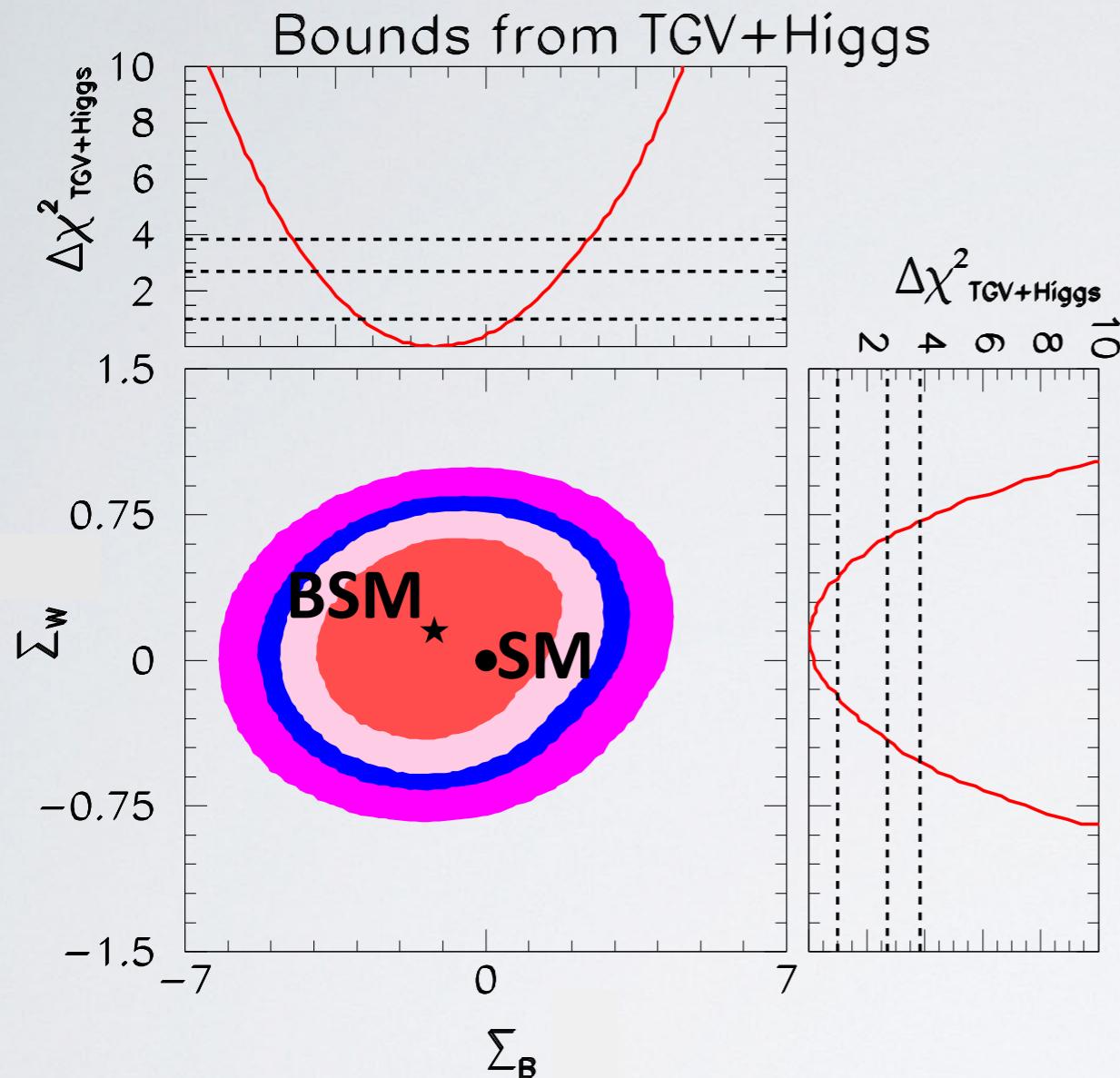
$$Z - W - W \leftrightarrow Z - Z - h$$

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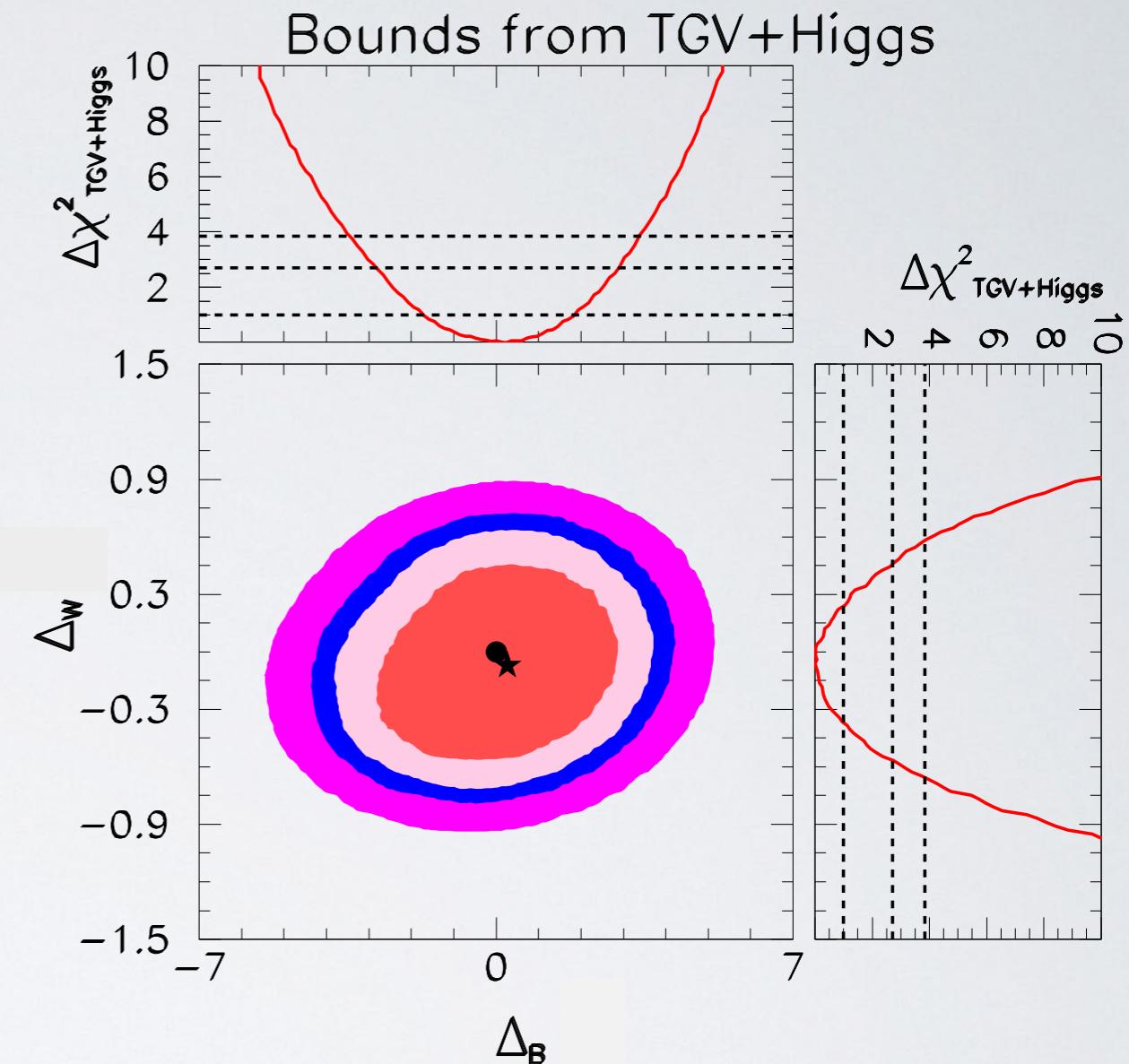
# Disentangling a Dynamical Higgs I

[Brivio,Corbett,Eboli,Gavela,Gonzalez-Fraile,Gonzalez-Garcia,LM&Rigolin, 1311.1823]



$$\Sigma_B = 4(2c_2 + a_4) \rightarrow f_B \xi$$

$$\Sigma_W = 2(2c_3 - a_5) \rightarrow f_W \xi$$

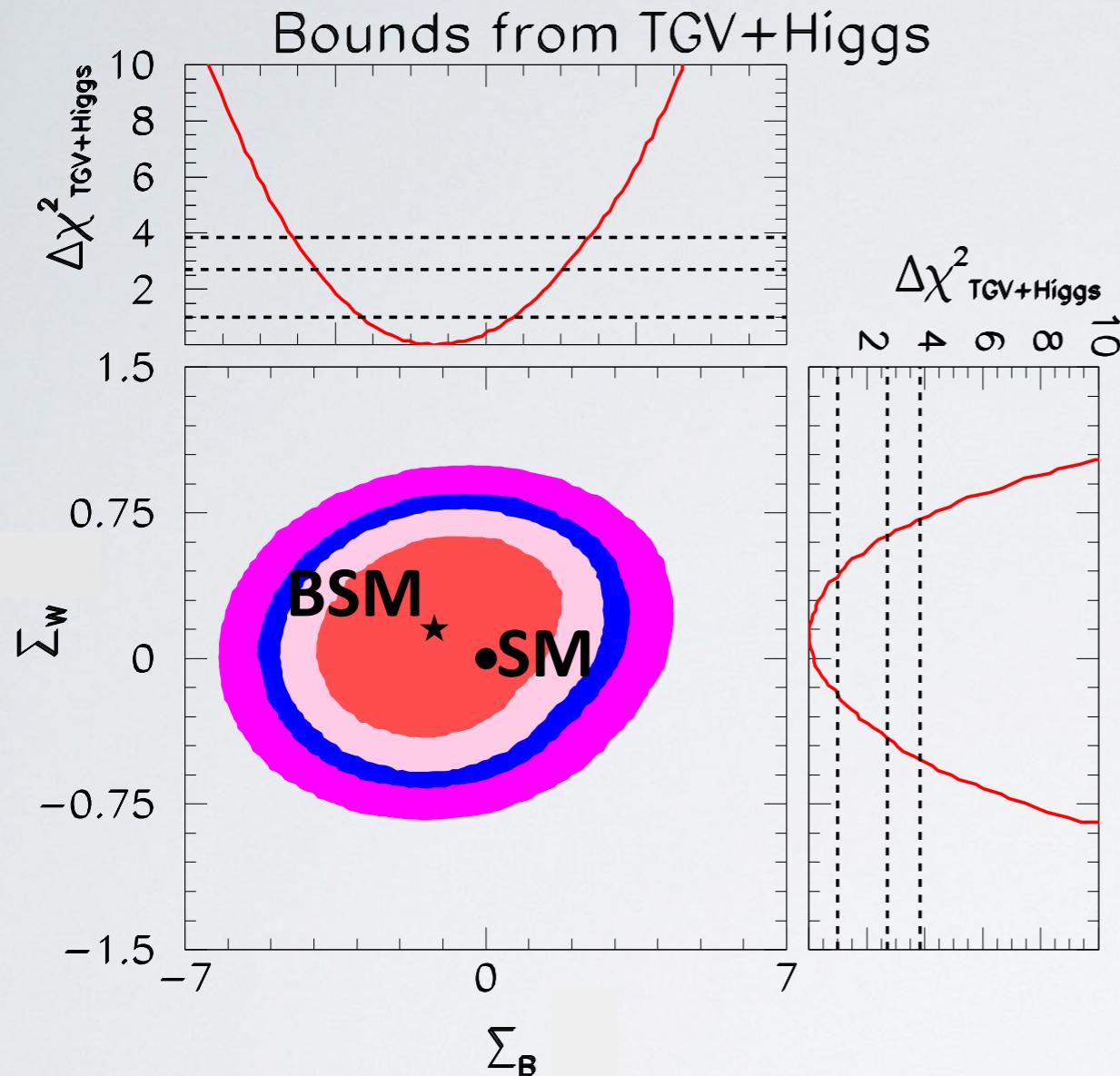


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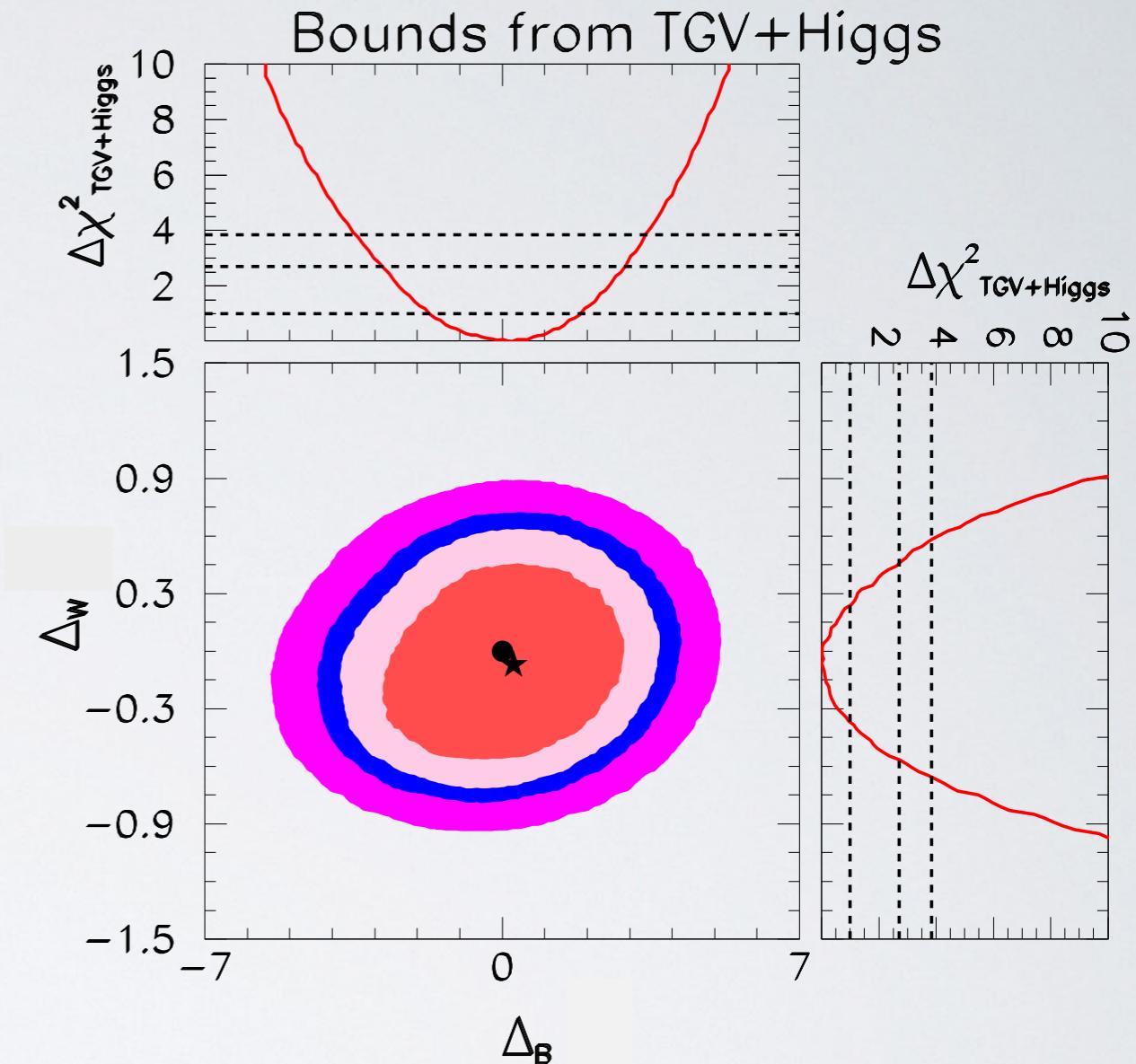
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Need of more precision for: - discovering BSM physics with TGV and HVV  
- disentangling dynamical from elementary

# Disentangling a Dynamical Higgs II

Specific “relevant” signals are expected in the chiral basis,  
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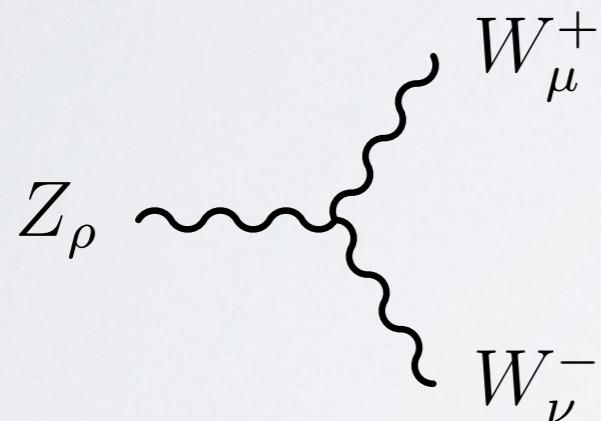
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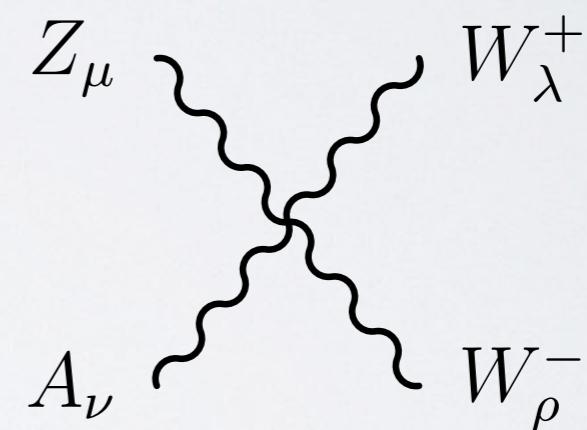
$$\mathcal{P}_{14}(h) = g \varepsilon^{\mu\nu\rho\lambda} \text{Tr}(\mathbf{T}\mathbf{V}_\mu) \text{Tr}(\mathbf{V}_\nu W_{\rho\lambda}) \mathcal{F}_{14}(h)$$

C and P odd, but CP even

$$\varepsilon^{\mu\nu\rho\lambda} \partial_\mu W_\nu^+ W_\rho^- Z_\lambda \mathcal{F}_{14}(h)$$



$$\varepsilon^{\mu\nu\rho\lambda} Z_\mu A_\nu W_\rho^- W_\lambda^+ \mathcal{F}_{14}(h)$$



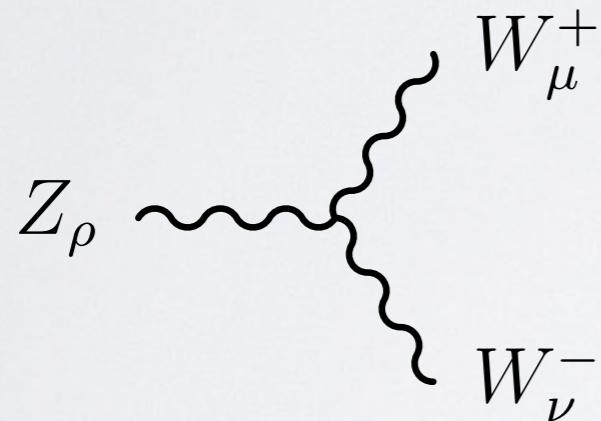
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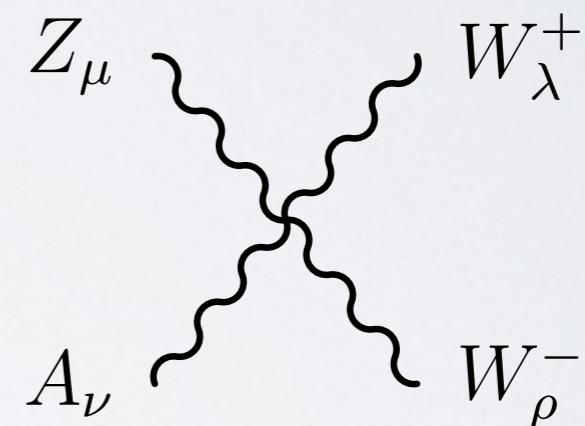
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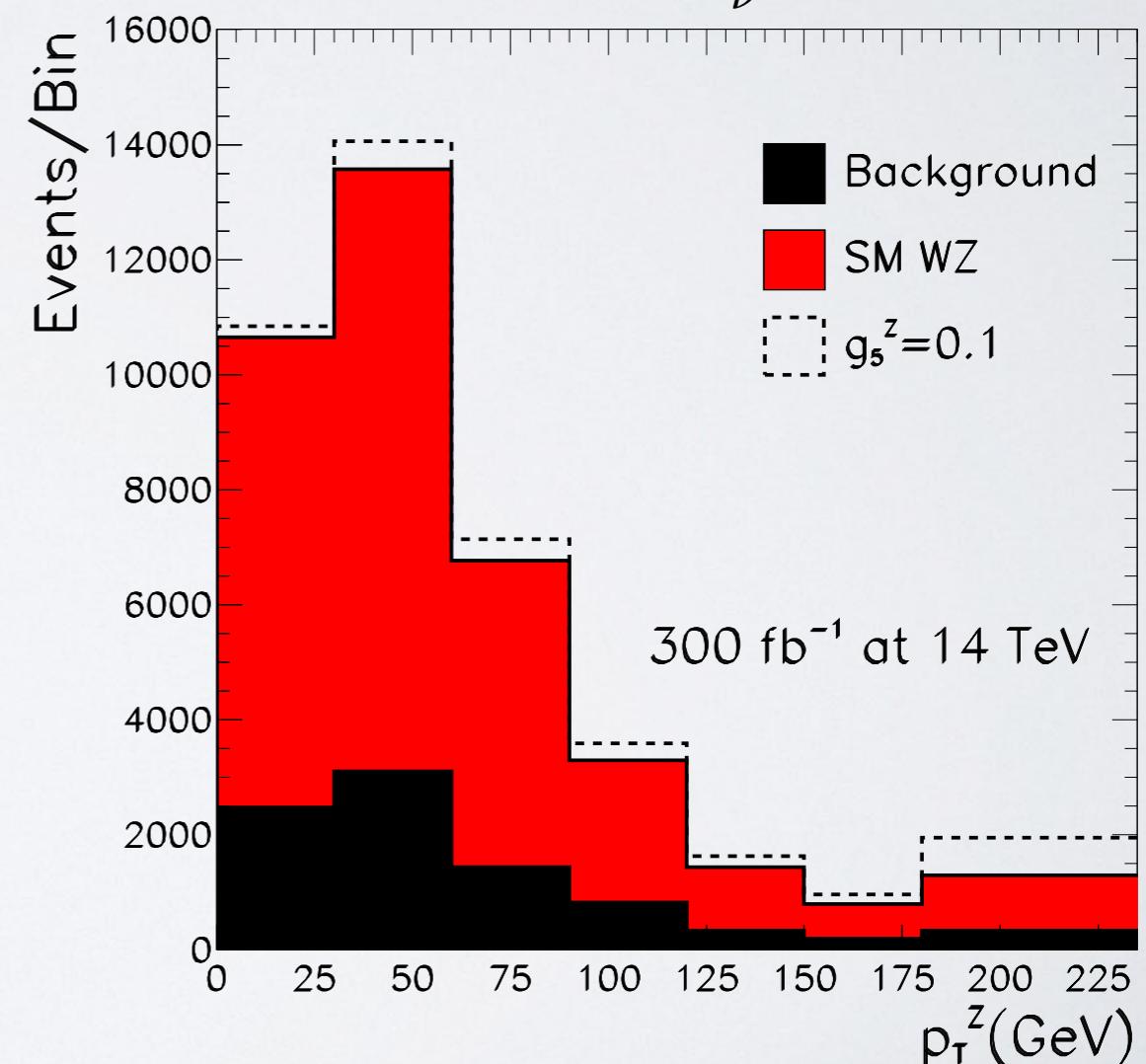
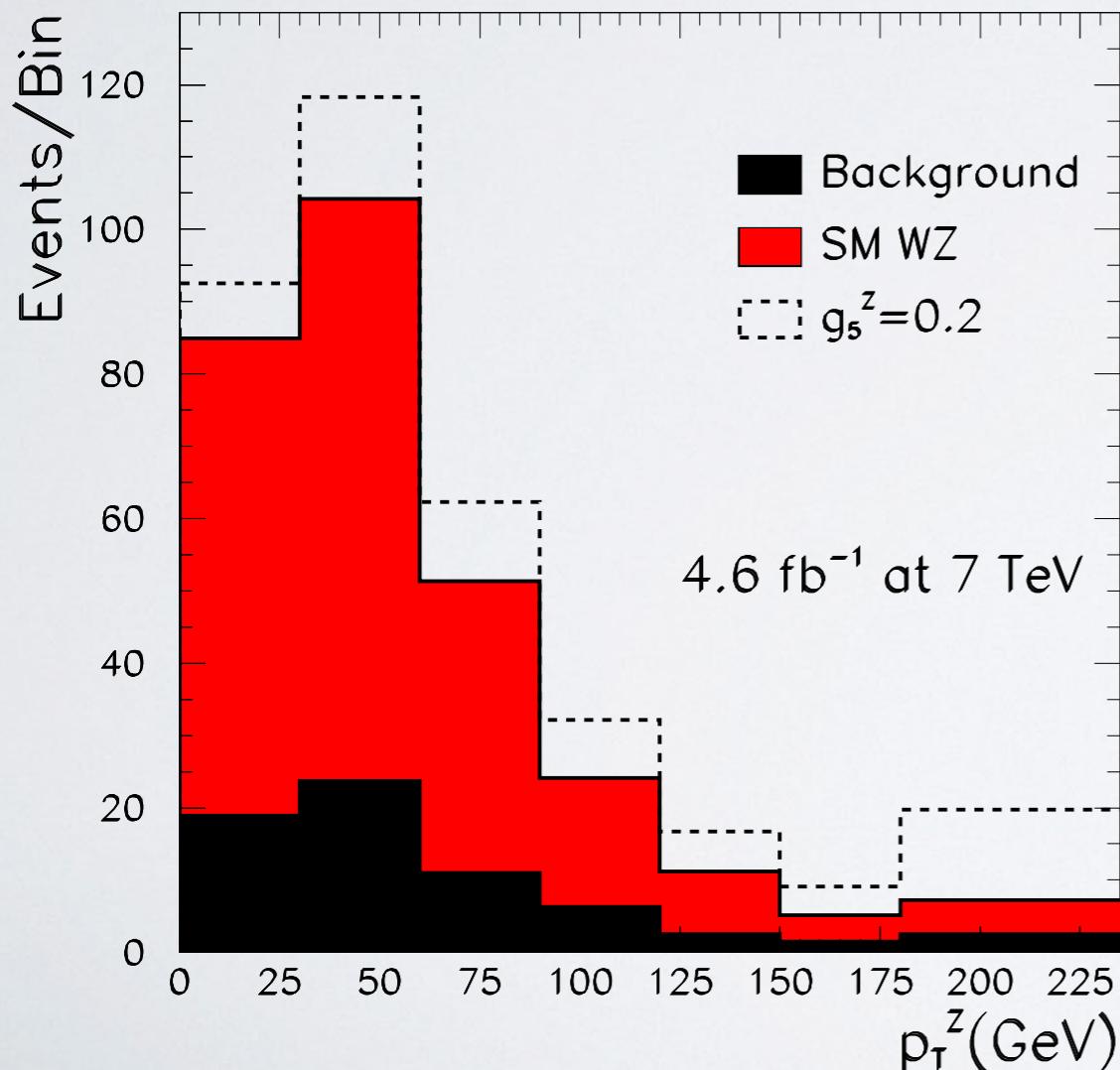
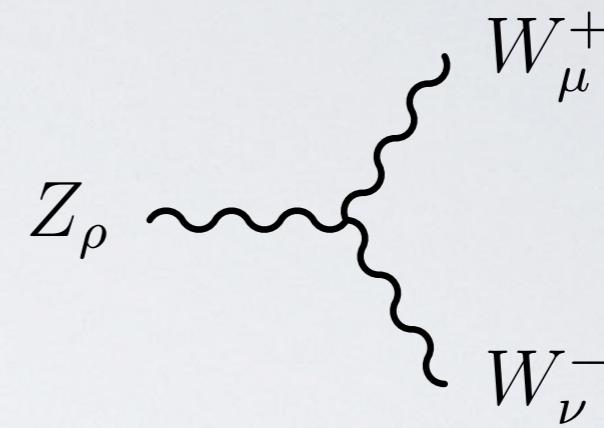
The interactions of this operator are described in the linear regime by an operator with  $d=8$  and therefore a signal at collider would be an indication in favour of the chiral EW realisation, wrt the linear one.

# Disentangling a Dynamical Higgs II

[Brivio,Corbett,Eboli,Gavela,Gonzalez-Fraile,Gonzalez-Garcia,LM&Rigolin, 1311.1823]

Simulation of what can be seen at LHC (7+8 TeV, 7+8+14 TeV) for  $g_5^Z$

$$\varepsilon^{\mu\nu\rho\lambda} \partial_\mu W_\nu^+ W_\rho^- Z_\lambda \mathcal{F}_{14}(h)$$



number of expected events (WZ production) with respect to the  $Z$   $p_T$

■ Present results, mainly from LEP II (WW pairs and single W production) and radiative corrections to Z physics

	Measurement ( $\pm 68\%$ CL region)	95% CL region	
Experiment	$g_5^Z$	$g_5^Z$	$c_{14}$
OPAL	$-0.04^{+0.13}_{-0.12}$	[-0.28, 0.21]	[-0.16, 0.12]
L3	$0.00^{+0.13}_{-0.13}$	[-0.21, 0.20]	[-0.12, 0.11]
ALEPH	$-0.064^{+0.13}_{-0.13}$	[-0.317, 0.19]	[-0.18, 0.11]

90% CL region from indirect bounds	$g_5^Z$ : [-0.08, 0.04]	$c_{14}$ : [-0.04, 0.02]
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■ Expected sensitivity on  $g_5^Z$  at the LHC (7+8 TeV and 7+8+14 TeV)

	68% CL range		95% CL range	
Data sets used	Counting $p_T^Z > 90$ GeV	$p_T^Z$ binned analysis	Counting $p_T^Z > 90$ GeV	$p_T^Z$ binned analysis
7+8 TeV (4.64+19.6 $\text{fb}^{-1}$ )	(-0.066, 0.058)	(-0.057, 0.050)	(-0.091, 0.083)	(-0.080, 0.072)
7+8+14 TeV (4.64+19.6+300 $\text{fb}^{-1}$ )	(-0.030, 0.022)	(-0.024, 0.019)	(-0.040, 0.032)	(-0.033, 0.028)

**LHC7+8 could have already a sensitivity that competes with the present bounds**

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  - Specific “relevant” signals are expected in the chiral basis, but not in the linear one, and vice versa
- Need of more precision to disentangle a dynamical Higgs with TGV+HVV
- A dedicated study on  $g_5^Z$  with LHC data could have already something to say about the presence of BSM physics and on the nature of  $h$ !!!

Thank you

# Backup

$$\begin{aligned}
\mathcal{L}_{\text{SILH}} = & \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{c_T}{2f^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) \left( H^\dagger \overleftrightarrow{D}_\mu H \right) \\
& - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3 + \left( \frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.} \right) \\
& + \frac{ic_W g}{2m_\rho^2} \left( H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i + \frac{ic_B g'}{2m_\rho^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu}) \\
& + \frac{ic_{HW} g}{16\pi^2 f^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{ic_{HB} g'}{16\pi^2 f^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\
& + \frac{c_\gamma g'^2}{16\pi^2 f^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{16\pi^2 f^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}
\end{aligned}$$

Alonso,Jenkins,Manohar & Trott, 1312.2014  
advocates that the SILH Lagrangian has been used not consistently in several recent papers

$$\mathcal{O}_g^{\text{SILH}} \equiv \mathcal{O}_{GG}$$

$$\mathcal{O}_B^{\text{SILH}} \equiv 2\mathcal{O}_B + \mathcal{O}_{BW} + \mathcal{O}_{BB}$$

$$\mathcal{O}_{HW}^{\text{SILH}} \equiv \mathcal{O}_W$$

$$\mathcal{O}_T^{\text{SILH}} \equiv \mathcal{O}_{\Phi,2} - 2\mathcal{O}_{\Phi,1}$$

$$\mathcal{O}_6^{\text{SILH}} \equiv \mathcal{O}_{\Phi,3}$$

$$\mathcal{O}_\gamma^{\text{SILH}} \equiv \mathcal{O}_{BB}$$

$$\mathcal{O}_W^{\text{SILH}} \equiv 2\mathcal{O}_W + \mathcal{O}_{BW} + \mathcal{O}_{WW}$$

$$\mathcal{O}_{HB}^{\text{SILH}} \equiv \mathcal{O}_B$$

$$\mathcal{O}_H^{\text{SILH}} \equiv \mathcal{O}_{\Phi,2}$$

$$\mathcal{O}_y^{\text{SILH}} \equiv 2\mathcal{O}_{\Phi,2} + 2\mathcal{O}_{\Phi,4} - (\Phi^\dagger \Phi) \Phi^\dagger \frac{\delta V(h)}{\delta \Phi^\dagger}$$

The SILH Lagrangian is just a linear Lagrangian, alternative to the HISZ one.

$$\begin{aligned}\mathcal{L}_{\text{SILH}} = & \frac{c_H}{2f^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{c_T}{2f^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) \left( H^\dagger \overleftrightarrow{D}_\mu H \right) \\ & - \frac{c_6 \lambda}{f^2} (H^\dagger H)^3 + \left( \frac{c_y y_f}{f^2} H^\dagger H \bar{f}_L H f_R + \text{h.c.} \right) \\ & + \frac{i c_W g}{2m_\rho^2} \left( H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i + \frac{i c_B g'}{2m_\rho^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu}) \\ & + \frac{i c_{HW} g}{16\pi^2 f^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{i c_{HB} g'}{16\pi^2 f^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ & + \frac{c_\gamma g'^2}{16\pi^2 f^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{c_g g_S^2}{16\pi^2 f^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}\end{aligned}$$

$$\begin{array}{lll} \mathcal{O}_g^{\text{SILH}} = \frac{v^2}{2g_s^2} \mathcal{P}_G & \mathcal{O}_\gamma^{\text{SILH}} = \frac{v^2}{2} \mathcal{P}_B & \mathcal{O}_W^{\text{SILH}} = \frac{v^2}{4} (\mathcal{P}_3 - 2\mathcal{P}_5) + \frac{v^2}{8} \mathcal{P}_1 + \frac{v^2}{2} \mathcal{P}_W \\ \mathcal{O}_B^{\text{SILH}} = \frac{v^2}{8} (\mathcal{P}_2 + 2\mathcal{P}_4) + \frac{v^2}{8} \mathcal{P}_1 + \frac{v^2}{2} \mathcal{P}_B & \mathcal{O}_{HB}^{\text{SILH}} = \frac{v^2}{16} (\mathcal{P}_2 + 2\mathcal{P}_4) & \mathcal{O}_{HW}^{\text{SILH}} = \frac{v^2}{8} (\mathcal{P}_3 - 2\mathcal{P}_5) \\ \mathcal{O}_T^{\text{SILH}} = \frac{v^2}{2} \mathcal{F}(h) \mathcal{P}_T & \mathcal{O}_H^{\text{SILH}} = v^2 \mathcal{P}_H & \mathcal{O}_y^{\text{SILH}} = 3v^2 \mathcal{P}_H + v^2 \mathcal{F}(h) \mathcal{P}_C - \frac{(v+h)^3}{2} \frac{\delta V(h)}{\delta h} \end{array}$$

# Other Effective Chiral Lagrangian

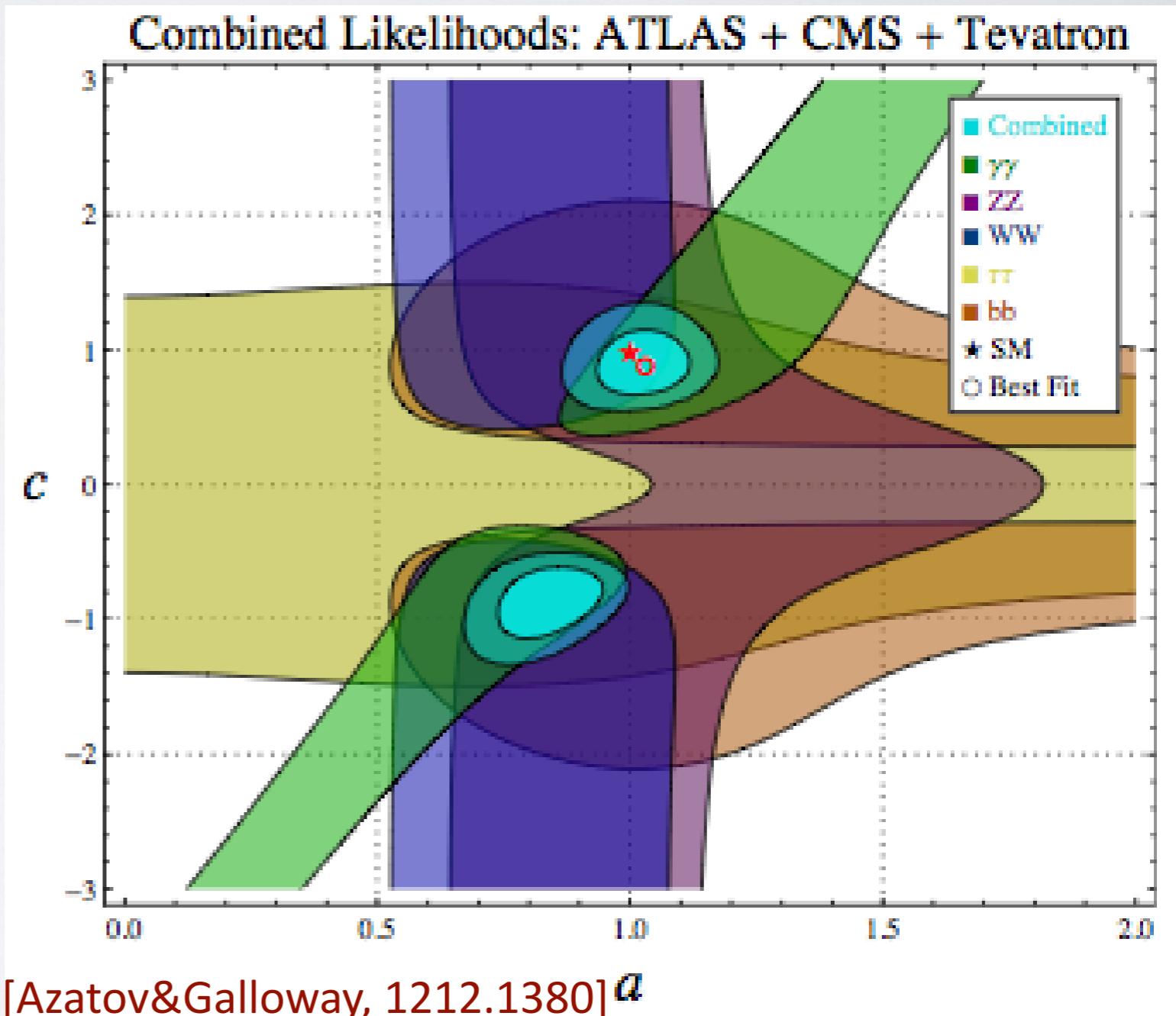
$$\mathcal{L} \supset -\frac{v^2}{4} \text{Tr} (\mathbf{V}_\mu \mathbf{V}^\mu) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \frac{v}{\sqrt{2}} (\bar{Q}_L \mathbf{U} \gamma Q_R + \text{h.c.}) \left( 1 + c \frac{h}{v} \right)$$

$$a = 1 + c_C(\alpha_C - 1)$$

$$b = 1 + c_C(\beta_C - 1)$$

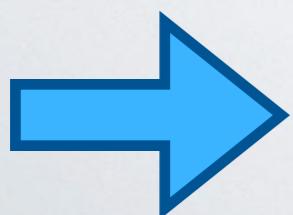
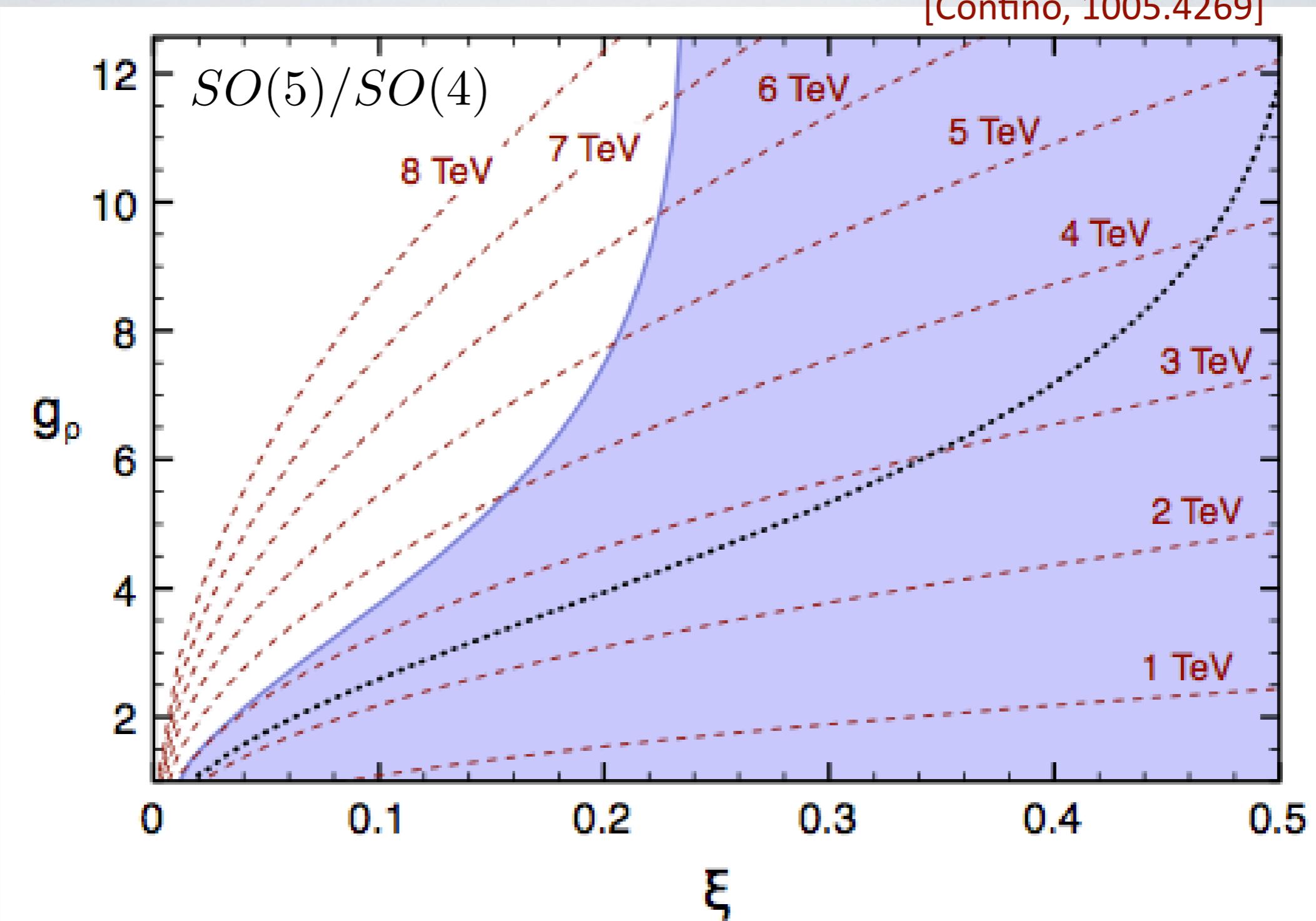
$$c = 1 + c_Y(2\alpha_Y - 1)$$

$c_C$  and  $c_Y$  have a dependence on  $\xi$



# The parameter $\xi$

[Contino, 1005.4269]



In the general effective approach,  $\xi$  could be even larger than 0.2, but a specific UV completion is necessary.

$$\mathcal{P}_9(h) = \text{Tr}((\mathcal{D}_\mu \mathbf{V}^\mu)^2) \mathcal{F}_9(h)$$

$$\mathcal{P}_{10}(h) = \text{Tr}(\mathbf{V}_\nu \mathcal{D}_\mu \mathbf{V}^\mu) \partial^\nu \mathcal{F}_{10}(h)$$

$$\mathcal{P}_{15}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathcal{D}_\nu \mathbf{V}^\nu) \mathcal{F}_{15}(h)$$

$$\mathcal{P}_{16}(h) = \text{Tr}([\mathbf{T}, \mathbf{V}_\nu] \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}^\nu) \mathcal{F}_{16}(h)$$

$$\mathcal{P}_{19}(h) = \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \text{Tr}(\mathbf{T} \mathbf{V}_\nu) \partial^\nu \mathcal{F}_{19}(h)$$

$$\mathcal{P}_7(h) = \text{Tr}(\mathbf{V}_\mu \mathbf{V}^\mu) \partial_\nu \partial^\nu \mathcal{F}_7(h)$$

$$\mathcal{P}_{25}(h) = (\text{Tr}(\mathbf{T} \mathbf{V}_\mu))^2 \partial_\nu \partial^\nu \mathcal{F}_{25}(h)$$

**If  $m_f=0$  then these operators are not independent from the others**

$$\frac{iv}{\sqrt{2}} \text{Tr}(\sigma^j \mathcal{D}_\mu \mathbf{V}^\mu) \left(1 + \frac{h}{v}\right)^2 = \frac{v + s_Y h}{v} (i \bar{Q}_L \sigma^j \mathbf{U} \mathcal{Y}_Q Q_R + i \bar{L}_L \sigma^j \mathbf{U} \mathcal{Y}_L L_R + \text{h.c.})$$

$$- \frac{iv}{\sqrt{2}} \text{Tr}(\sigma^j \mathbf{V}_\mu) \partial^\mu \left(1 + \frac{h}{v}\right)^2$$

$$\frac{iv}{\sqrt{2}} \text{Tr}(\mathbf{T} \mathcal{D}_\mu \mathbf{V}^\mu) \left(1 + \frac{h}{v}\right)^2 = \frac{v + s_Y h}{v} (i \bar{Q}_L \mathbf{T} \mathbf{U} \mathcal{Y}_Q Q_R + i \bar{L}_L \mathbf{T} \mathbf{U} \mathcal{Y}_L L_R + \text{h.c.})$$

$$- \frac{iv}{\sqrt{2}} \text{Tr}(\mathbf{T} \mathbf{V}_\mu) \partial^\mu \left(1 + \frac{h}{v}\right)^2$$

$$\square h = -\frac{\delta V(h)}{\delta h} - \frac{v + h}{2} \text{Tr}[\mathbf{V}_\mu \mathbf{V}^\mu] - \frac{s_Y}{\sqrt{2}} (\bar{Q}_L \mathbf{U} \mathcal{Y}_Q Q_R + \bar{L}_L \mathbf{U} \mathcal{Y}_L L_R + \text{h.c.})$$

# Triple Gauge Vertices

$$\mathcal{L}_{WWV} = -ig_{WWV} \left\{ g_1^V \left( W_{\mu\nu}^+ W^{-\mu} V^\nu - W_\mu^+ V_\nu W^{-\mu\nu} \right) + \kappa_V W_\mu^+ W_\nu^- V^{\mu\nu} \right.$$

$$\left. - ig_5^V \epsilon^{\mu\nu\rho\sigma} \left( W_\mu^+ \partial_\rho W_\nu^- - W_\nu^- \partial_\rho W_\mu^+ \right) V_\sigma + g_6^V \left( \partial_\mu W^{+\mu} W^{-\nu} - \partial_\mu W^{-\mu} W^{+\nu} \right) V_\nu \right\}$$

$$V \equiv \{\gamma, Z\} \text{ and } g_{WW\gamma} \equiv e = g \sin \theta_W, \quad g_{WWZ} = g \cos \theta_W$$

The SM values are:  $g_1^Z = \kappa_\gamma = \kappa_Z = 1$  and  $g_5^Z = g_6^\gamma = g_6^Z = 0$

	Coeff. $\times e^2/s_\theta^2$	Chiral $\times \xi$		$\times \xi^2$	Linear $\times v^2/\Lambda^2$
$\Delta \kappa_\gamma$	1	$-2c_1 + 2c_2 + c_3$		$-4c_{12} + 2c_{13}$	$\frac{1}{8}(f_W + f_B - 2f_{BW})$
$\Delta g_6^\gamma$	1	$-c_9$		—	$\frac{1}{4}f_{\square\Phi}$
$\Delta g_1^Z$	$\frac{1}{c_\theta^2}$	$\frac{s_{2\theta}^2}{4e^2 c_{2\theta}} c_T + \frac{2s_\theta^2}{c_{2\theta}} c_1 + c_3$		—	$\frac{1}{8}f_W + \frac{s_\theta^2}{4c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2}{16e^2 c_{2\theta}} f_{\Phi,1}$
$\Delta \kappa_Z$	1	$\frac{s_\theta^2}{e^2 c_{2\theta}} c_T + \frac{4s_\theta^2}{c_{2\theta}} c_1 - \frac{2s_\theta^2}{c_\theta^2} c_2 + c_3$		$-4c_{12} + 2c_{13}$	$\frac{1}{8}f_W - \frac{s_\theta^2}{8c_\theta^2} f_B + \frac{s_\theta^2}{2c_{2\theta}} f_{BW} - \frac{s_\theta^2}{4e^2 c_{2\theta}} f_{\Phi,1}$
$\Delta g_5^Z$	$\frac{1}{c_\theta^2}$	—		$c_{14}$	—
$\Delta g_6^Z$	$\frac{1}{c_\theta^2}$	$s_\theta^2 c_9$		$-c_{16}$	$-\frac{s_\theta^2}{4} f_{\square\Phi}$

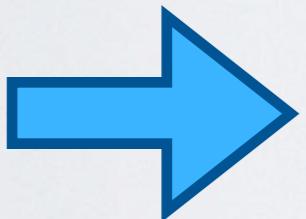
From the table, we can read out two correlations:

$$\Delta\kappa_Z + \frac{s_\theta^2}{c_\theta^2} \Delta\kappa_\gamma - \Delta g_1^Z = \frac{16e^2}{s_\theta^2} (2c_{12} - c_{13}) \xi^2 ,$$

$$\Delta g_6^\gamma + \frac{c_\theta^2}{s_\theta^2} \Delta g_6^Z = -\frac{e^2}{s_\theta^4} c_{16} \xi^2 ,$$

The RHS is vanishing, once considering:

- d=6 linear effective basis
- chiral basis truncated to  $\xi$ -weighted operators



No possibility of distinguishing a dynamical Higgs from an elementary Higgs if  $\xi \ll 1$ , considering only TGV.

# Higgs-Vector-Vector Vertices

$$\begin{aligned}
\mathcal{L}_{\text{HVV}} \equiv & g_{Hgg} G_{\mu\nu}^a G^{a\mu\nu} h + g_{H\gamma\gamma} A_{\mu\nu} A^{\mu\nu} h + g_{HZ\gamma}^{(1)} A_{\mu\nu} Z^\mu \partial^\nu h + g_{HZ\gamma}^{(2)} A_{\mu\nu} Z^{\mu\nu} h \\
& + g_{HZZ}^{(1)} Z_{\mu\nu} Z^\mu \partial^\nu h + g_{HZZ}^{(2)} Z_{\mu\nu} Z^{\mu\nu} h + g_{HZZ}^{(3)} Z_\mu Z^\mu h + g_{HZZ}^{(4)} Z_\mu Z^\mu \square h \\
& + g_{HZZ}^{(5)} \partial_\mu Z^\mu Z_\nu \partial^\nu h + g_{HZZ}^{(6)} \partial_\mu Z^\mu \partial_\nu Z^\nu h \\
& + g_{HWW}^{(1)} (W_{\mu\nu}^+ W^{-\mu} \partial^\nu h + \text{h.c.}) + g_{HWW}^{(2)} W_{\mu\nu}^+ W^{-\mu\nu} h + g_{HWW}^{(3)} W_\mu^+ W^{-\mu} h \\
& + g_{HWW}^{(4)} W_\mu^+ W^{-\mu} \square h + g_{HWW}^{(5)} (\partial_\mu W^{+\mu} W_\nu^- \partial^\nu h + \text{h.c.}) + g_{HWW}^{(6)} \partial_\mu W^{+\mu} \partial_\nu W^{-\nu} h
\end{aligned}$$

where  $V_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu$  with  $V = \{A, Z, W, G\}$

Writing the couplings as

$$g_i^{(j)} \simeq g_i^{(j)SM} + \Delta g_i^{(j)}$$

the only non-vanishing SM contributions are given by

$$g_{HZZ}^{(3)SM} = \frac{m_Z^2}{v}, \quad g_{HWW}^{(3)SM} = \frac{2m_Z^2 \cos \theta_W^2}{v}$$

	Coeff. $\times e^2/4v$	Chiral $\times \xi$	$\times \xi^2$	Linear $\times v^2/\Lambda^2$
$\Delta g_{Hgg}$	$\frac{g_s^2}{e^2}$	$-2a_G$	—	$-4f_{GG}$
$\Delta g_{H\gamma\gamma}$	1	$-2(a_B + a_W) + 8a_1$	$8a_{12}$	$-(f_{BB} + f_{WW}) + f_{BW}$
$\Delta g_{HZ\gamma}^{(1)}$	$\frac{1}{s_{2\theta}}$	$-8(a_5 + 2a_4)$	$-16a_{17}$	$2(f_W - f_B)$
$\Delta g_{HZ\gamma}^{(2)}$	$\frac{c_\theta}{s_\theta}$	$4\frac{s_\theta^2}{c_\theta^2}a_B - 4a_W + 8\frac{c_{2\theta}}{c_\theta^2}a_1$	$16a_{12}$	$2\frac{s_\theta^2}{c_\theta^2}f_{BB} - 2f_{WW} + \frac{c_{2\theta}}{c_\theta^2}f_{BW}$
$\Delta g_{HZZ}^{(1)}$	$\frac{1}{c_\theta^2}$	$-4\frac{c_\theta^2}{s_\theta^2}a_5 + 8a_4$	$-8\frac{c_\theta^2}{s_\theta^2}a_{17}$	$\frac{c_\theta^2}{s_\theta^2}f_W + f_B$
$\Delta g_{HZZ}^{(2)}$	$-\frac{c_\theta^2}{s_\theta^2}$	$2\frac{s_\theta^4}{c_\theta^4}a_B + 2a_W + 8\frac{s_\theta^2}{c_\theta^2}a_1$	$-8a_{12}$	$\frac{s_\theta^4}{c_\theta^4}f_{BB} + f_{WW} + \frac{s_\theta^2}{c_\theta^2}f_{BW}$
$\Delta g_{HZZ}^{(3)}$	$\frac{m_Z^2}{e^2}$	$-2c_H + 2(2a_C - c_C) - 8(a_T - c_T)$	—	$f_{\Phi,1} + 2f_{\Phi,4} - 2f_{\Phi,2}$
$\Delta g_{HZZ}^{(4)}$	$-\frac{1}{s_{2\theta}^2}$	$16a_7$	$32a_{25}$	$4f_{\square\Phi}$
$\Delta g_{HZZ}^{(5)}$	$-\frac{1}{s_{2\theta}^2}$	$16a_{10}$	$32a_{19}$	$-8f_{\square\Phi}$
$\Delta g_{HZZ}^{(6)}$	$-\frac{1}{s_{2\theta}^2}$	$16a_9$	$32a_{15}$	$-4f_{\square\Phi}$
$\Delta g_{HWW}^{(1)}$	$\frac{1}{s_\theta^2}$	$-4a_5$	—	$f_W$
$\Delta g_{HWW}^{(2)}$	$\frac{1}{s_\theta^2}$	$-4a_W$	—	$-2f_{WW}$
$\Delta g_{HWW}^{(3)}$	$\frac{m_Z^2 c_\theta^2}{e^2}$	$-4c_H + 4(2a_C - c_C) + \frac{32e^2}{c_{2\theta}}c_1 + \frac{16c_\theta^2}{c_{2\theta}}c_T$	$-\frac{32e^2}{s_\theta^2}c_{12}$	$\frac{-2(3c_\theta^2 - s_\theta^2)}{c_{2\theta}}f_{\Phi,1} + 4f_{\Phi,4} - 4f_{\Phi,2} + \frac{4e^2}{c_{2\theta}}f_{BW}$
$\Delta g_{HWW}^{(4)}$	$-\frac{1}{s_\theta^2}$	$8a_7$	—	$2f_{\square\Phi}$
$\Delta g_{HWW}^{(5)}$	$-\frac{1}{s_\theta^2}$	$4a_{10}$	—	$-2f_{\square\Phi}$
$\Delta g_{HWW}^{(6)}$	$-\frac{1}{s_\theta^2}$	$8a_9$	—	$-2f_{\square\Phi}$

From the table, we can read out several correlations:

$$g_{HWW}^{(1)} - c_\theta^2 g_{HZZ}^{(1)} - c_\theta s_\theta g_{HZ\gamma}^{(1)} = \frac{2e^2}{vs_\theta^2} a_{17} \xi^2,$$

$$2c_\theta^2 g_{HZZ}^{(2)} + 2s_\theta c_\theta g_{HZ\gamma}^{(2)} + 2s_\theta^2 g_{H\gamma\gamma}^{(2)} - g_{HWW}^{(2)} = \frac{4e^2}{vs_\theta^2} a_{12} \xi^2.$$

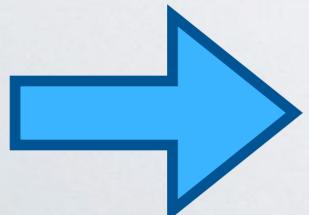
$$\Delta g_{HZZ}^{(4)} - \frac{1}{2c_\theta^2} \Delta g_{HWW}^{(4)} = -\frac{8e^2}{vs_{2\theta}^2} a_{25} \xi^2$$

$$\Delta g_{HZZ}^{(5)} - \frac{1}{c_\theta^2} \Delta g_{HWW}^{(5)} = -\frac{8e^2}{vs_{2\theta}^2} a_{19} \xi^2$$

$$\Delta g_{HZZ}^{(6)} - \frac{1}{2c_\theta^2} \Delta g_{HWW}^{(6)} = -\frac{8e^2}{vs_{2\theta}^2} a_{15} \xi^2$$

The RHS is vanishing, once considering:

- d=6 linear effective basis
- chiral basis truncated to  $\xi$ -weighted operators



No possibility of distinguishing a dynamical Higgs from an elementary Higgs if  $\xi \ll 1$ , considering only HVV.

Comparing TGV and HVV, a correlation arises that holds only for the d=6 linear effective basis. In particular, it does not hold for the chiral basis even considering only  $\xi$ -weighted operators.

$$\Delta\kappa_Z - \Delta g_1^Z = \frac{v s_\theta}{2 c_\theta} \left[ (c_\theta^2 - s_\theta^2) \left( g_{HZ\gamma}^{(1)} + 2g_{HZ\gamma}^{(2)} \right) + 2s_\theta c_\theta \left( 2g_{H\gamma\gamma} - g_{HZZ}^{(1)} - 2g_{HZZ}^{(2)} \right) \right]$$

Deviations from this correlations indicate that d=6 linear description is not satisfactory:

- d=8 becomes import
- the non-linear description is mode adequate
- or...

# Quartic Gauge Vertices

$$\begin{aligned} \mathcal{L}_{4X} \equiv g^2 & \left\{ g_{ZZ}^{(1)} (Z_\mu Z^\mu)^2 + g_{WW}^{(1)} W_\mu^+ W^{+\mu} W_\nu^- W^{-\nu} - g_{WW}^{(2)} (W_\mu^+ W^{-\mu})^2 \right. \\ & + g_{VV'}^{(3)} W^{+\mu} W^{-\nu} (V_\mu V'_\nu + V'_\mu V_\nu) - g_{VV'}^{(4)} W_\nu^+ W^{-\nu} V^\mu V'_\mu \\ & \left. + ig_{VV'}^{(5)} \varepsilon^{\mu\nu\rho\sigma} W_\mu^+ W_\nu^- V_\rho V'_\sigma \right\}, \end{aligned}$$

where  $VV' = \{\gamma\gamma, \gamma Z, ZZ\}$

The only non-vanishing SM contributions are given by

$$\begin{array}{llll} g_{WW}^{(1)SM} = \frac{1}{2} & g_{WW}^{(2)SM} = \frac{1}{2} & g_{ZZ}^{(3)SM} = \frac{\cos^2 \theta_W}{2} & g_{\gamma\gamma}^{(3)SM} = \frac{\sin^2 \theta_W}{2} \\ g_{Z\gamma}^{(3)SM} = \frac{\sin 2\theta_W}{2} & g_{ZZ}^{(4)SM} = \cos^2 \theta_W & g_{\gamma\gamma}^{(4)SM} = \sin^2 \theta_W & g_{Z\gamma}^{(4)SM} = \sin 2\theta_W \end{array}$$

	Coeff. $\times e^2/4s_\theta^2$	Chiral $\times \xi$	$\times \xi^2$	Linear $\times v^2/\Lambda^2$
$\Delta g_{WW}^{(1)}$	1	$\frac{s_{2\theta}^2}{e^2 c_{2\theta}} c_T + \frac{8s_\theta^2}{c_{2\theta}} c_1 + 4c_3$	$2c_{11} - 16c_{12} + 8c_{13}$	$\frac{f_W}{2} + \frac{s_\theta^2}{c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2}{4c_{2\theta}e^2} f_{\Phi 1}$
$\Delta g_{WW}^{(2)}$	1	$\frac{s_{2\theta}^2}{e^2 c_{2\theta}} c_T + \frac{8s_\theta^2}{c_{2\theta}} c_1 + 4c_3 - 4c_6$	$-2c_{11} - 16c_{12} + 8c_{13}$	$\frac{f_W}{2} + \frac{s_\theta^2}{c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2}{4c_{2\theta}e^2} f_{\Phi 1} - \frac{1}{2} f_{\square\Phi}$
$\Delta g_{ZZ}^{(1)}$	$\frac{1}{c_\theta^4}$	$c_6$	$c_{11} + 2c_{23} + 2c_{24} + 4c_{26}\xi^2$	$\frac{1}{8} f_{\square\Phi}$
$\Delta g_{ZZ}^{(3)}$	$\frac{1}{c_\theta^2}$	$\frac{s_{2\theta}^2 c_\theta^2}{e^2 c_{2\theta}} c_T + \frac{2s_{2\theta}^2}{c_{2\theta}} c_1 + 4c_\theta^2 c_3 - 2s_\theta^4 c_9$	$2c_{11} + 4s_\theta^2 c_{16} + 2c_{24}$	$\frac{f_W c_\theta^2}{2} + \frac{s_{2\theta}^2}{4c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2 c_\theta^2}{4e^2 c_{2\theta}} f_{\Phi 1} + \frac{s_\theta^4}{2} f_{\square\Phi}$
$\Delta g_{ZZ}^{(4)}$	$\frac{1}{c_\theta^2}$	$\frac{2s_{2\theta}^2 c_\theta^2}{e^2 c_{2\theta}} c_T + \frac{4s_{2\theta}^2}{c_{2\theta}} c_1 + 8c_\theta^2 c_3 - 4c_6$	$-4c_{23}$	$f_W c_\theta^2 + 2\frac{s_{2\theta}^2}{4c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2 c_\theta^2}{2e^2 c_{2\theta}} f_{\Phi 1} - \frac{1}{2} f_{\square\Phi}$
$\Delta g_{\gamma\gamma}^{(3)}$	$s_\theta^2$	$-2c_9$	—	$\frac{1}{2} f_{\square\Phi}$
$\Delta g_{\gamma Z}^{(3)}$	$\frac{s_\theta}{c_\theta}$	$\frac{s_{2\theta}^2}{e^2 c_{2\theta}} c_T + \frac{8s_\theta^2}{c_{2\theta}} c_1 + 4c_3 + 4s_\theta^2 c_9$	$-4c_{16}$	$\frac{f_W}{2} + \frac{s_\theta^2}{c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2}{4c_{2\theta}e^2} f_{\Phi 1} - s_\theta^2 f_{\square\Phi}$
$\Delta g_{\gamma Z}^{(4)}$	$\frac{s_\theta}{c_\theta}$	$\frac{2s_{2\theta}^2}{e^2 c_{2\theta}} c_T + \frac{16s_\theta^2}{c_{2\theta}} c_1 + 8c_3$	—	$f_W + 2\frac{s_\theta^2}{c_{2\theta}} f_{BW} - \frac{s_{2\theta}^2}{2c_{2\theta}e^2} f_{\Phi 1}$
$\Delta g_{\gamma Z}^{(5)}$	$\frac{s_\theta}{c_\theta}$	—	$8c_{14}$	—

# Other constraints on the parameters



From EWPD, we can constrain 2 parameters: S and T parameters

$$-4.7 \times 10^{-3} \leq c_1 \leq 4 \times 10^{-3} \quad \text{and} \quad -2 \times 10^{-3} \leq c_T \leq 1.7 \times 10^{-3}$$



From TGV and HVV, we can constrain other 8 parameters: at 90% C.L.

	Set A	Set B
$a_G (\cdot 10^{-3})$	$s_Y = +1: [-1.8, 2.1] \cup [6.5, 10]$ $s_Y = -1: [-9.9, -6.5] \cup [-2.1, 1.8]$	$s_Y = +1: [-0.78, 2.4] \cup [6.5, 12]$ $s_Y = -1: [-12, -6.5] \cup [-2.3, 0.75]$
$a_4$		$[-0.47, 0.14]$
$a_5$		$[-0.33, 0.17]$
$a_W$		$[-0.12, 0.51]$
$a_B$		$[-0.50, 0.21]$
$c_H$	$[-0.66, 0.66]$	$[-1.1, 0.49]$
$c_2$		$[-0.12, 0.076]$
$c_3$		$[-0.064, 0.079]$

$$\text{Set A : } a_G, a_4, a_5, a_B, a_W, c_H, 2a_C - c_C = 0 \quad \text{HVV} = \text{Hff}$$

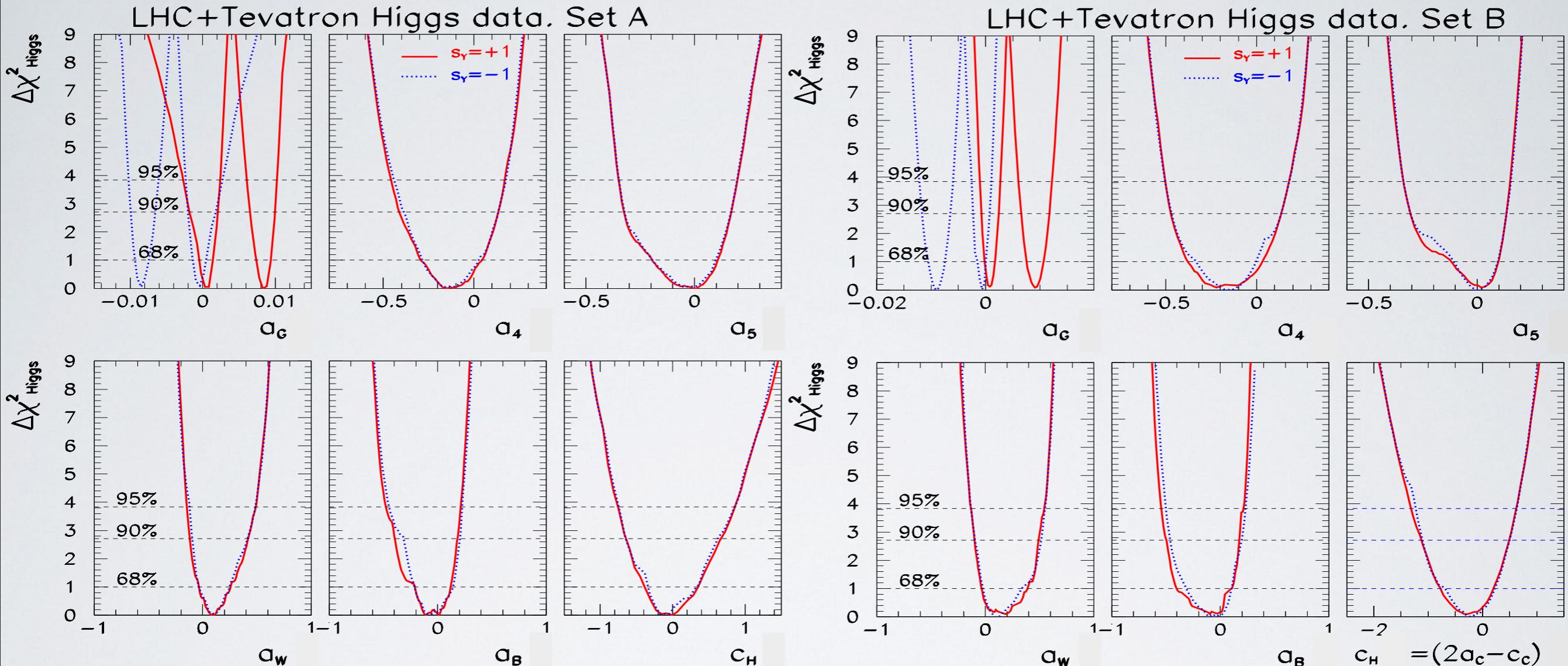
$$\text{Set B : } a_G, a_4, a_5, a_B, a_W, c_H = 2a_C - c_C \quad \text{HVV} \neq \text{Hff}$$

Set A :  $a_G, a_4, a_5, a_B, a_W, c_H, 2a_C - c_C = 0$

$\text{HV}\bar{V} = \text{Hff}$

Set B :  $a_G, a_4, a_5, a_B, a_W, c_H = 2a_C - c_C$

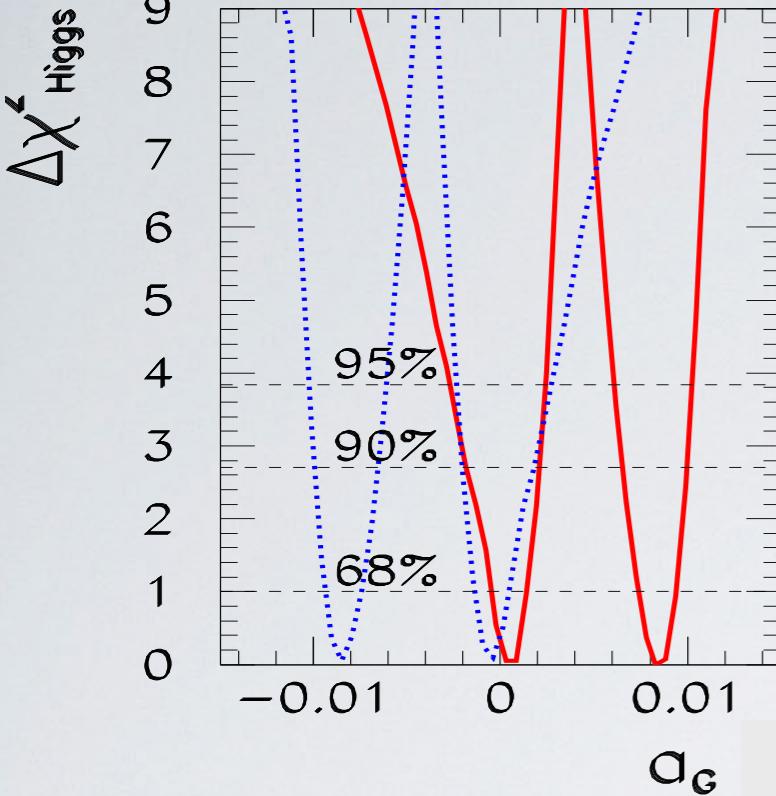
$\text{HV}\bar{V} \neq \text{Hff}$



$$|\chi^2_{\min, A} - \chi^2_{\min, B}| < 0.5$$

**Data:** Tevatron D0 and CDF Collaborations and LHC, CMS, and ATLAS Collaborations at 7 TeV and 8 TeV for final states  $\gamma\gamma$ ,  $W^+W^-$ ,  $ZZ$ ,  $Z\gamma$ ,  $b\bar{b}$ , and  $\tau\tau$

## LHC+Tevatron



From EWPD on the quartic gauge couplings, we get

coupling	90% CL allowed region
$c_6$	$[-0.23, 0.26]$
$c_{11}$	$[-0.094, 0.10]$
$c_{23}$	$[-0.092, 0.10]$
$c_{24}$	$[-0.012, 0.013]$
$c_{26}$	$[-0.0061, 0.0068]$

# Disentangling a Dynamical Higgs II

The simulation for LHC (7 TeV, 14 TeV) has been done taking cuts and precautions:

- Focused on WZ production, considering leptonic decays of W and Z (background)

$$pp \rightarrow \ell'^{\pm} \ell^+ \ell^- E^{\text{miss}} \quad \ell^{(\prime)} = e \text{ or } \mu$$

- Main background: SM production of WZ pairs; W and Z production with jets; ZZ production with one Z in leptons with one charged in missing E, the other in tt pair.

- Detection efficiencies rescaled to the one by ATLAS for TGV  $\Delta K_Z$ ,  $g_1^Z$ ,  $\lambda_Z$ .

- We closely follow the TGV analysis performed by ATLAS (cuts on transverse momentum and pseudorapidity).

- The cross section in the presence of an anomalous  $g_5^Z$  is then given by

$$\sigma = \sigma_{\text{bck}} + \sigma_{SM} + \sigma_{\text{int}} g_5^Z + \sigma_{\text{ano}} (g_5^Z)^2$$

In the SM, Zff and Wff contain a CP odd component. The amplitude for any subprocess  $q\bar{q} \rightarrow WZ$  contains SM contributions that are both C and P odd and that interfere with the contribution from the anomalous.

Data sets used	68% CL range		95% CL range	
	Counting $p_T^Z > 90$ GeV	$p_T^Z$ binned analysis	Counting $p_T^Z > 90$ GeV	$p_T^Z$ binned analysis
7+8 TeV (4.64+19.6 $\text{fb}^{-1}$ )	(-0.066, 0.058)	(-0.057, 0.050)	(-0.091, 0.083)	(-0.080, 0.072)
7+8+14 TeV (4.64+19.6+300 $\text{fb}^{-1}$ )	(-0.030, 0.022)	(-0.024, 0.019)	(-0.040, 0.032)	(-0.033, 0.028)

### ■ Counting $p_T^Z > 90$ GeV

Simple even counting analysis, assuming that the observed events are SM and looking for values of  $g_5^Z$  inside the 68% and 95% CL allowed regions. The restriction to  $p_T^Z > 90$  GeV increases the sensitivity.

### ■ $p_T^Z$ binned analysis

Simple  $\chi^2$  based on the contents of the different  $p_T^Z$  distributions with no cuts.  
Same conditions of the previous method.