



# Introduction to Octopus: a real-space (TD)DFT code

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TDDFT 2012, Benasque

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<sup>1</sup>Filling in for Xavier Andrade (Harvard).

## Time-dependent Kohn-Sham equation

$$i\frac{\partial}{\partial t}\varphi_n(\mathbf{r}, t) = -\nabla^2\varphi_n + V_{\text{eff}}[\rho](\mathbf{r}, t)\varphi_n(\mathbf{r}, t)$$
$$\rho(\mathbf{r}, t) = \sum_n \varphi_n^*(\mathbf{r}, t)\varphi_n(\mathbf{r}, t)$$

- Solve the equations numerically.
- Represent functions and other objects.
- Calculate derivatives and integrals.

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How to construct pseudo-potentials in Kohn-Sham-DFT codes

$$V = V_{\text{core}} + \sum_{lm} |l m\rangle (V_l - V_{\text{core}}) \langle l m|$$

# Pseudo-potentials

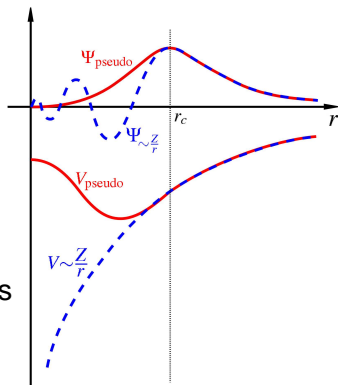
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  - Reduce to a finite number.
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  - Point distribution:
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- Finite region of the space: *Box*

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  - Uniformly spaced grid.
  - Irregular spacing between points to capture singularities.
  - Non-uniform grids also possible.
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# Boundary conditions

- For finite systems, functions go to zero.
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- Other BCs are possible: periodic, zero derivative, open.

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# Boundary conditions

- Optimize the shape of the box to minimize the number of points needed.
- Available box shapes:
  - Minimum box: union of spheres around each atom.
  - Rectangular
  - Truncated octahedron
  - Spherical (e.g. `mpgsl`)

- Optimize the shape of the box to minimize the number of points needed.
- Available box shapes:
  - Minimum box: union of spheres around each atom.
  - Sphere.
  - Cylinder.
  - Parallelepiped.
  - Arbitrary (e.g. 2D image!)

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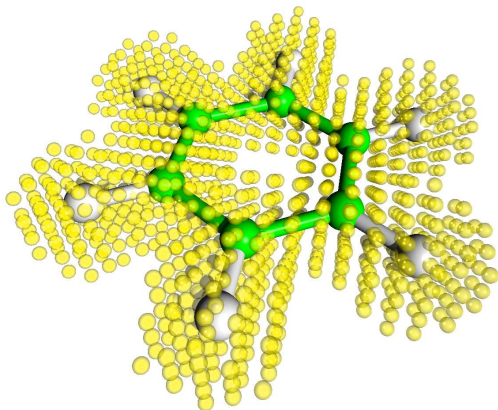
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# Example: benzene molecule in minimal box



# Real-space grid characteristics

- Natural boundary conditions for different problems:  
zero, one, two, or three periodic dimensions for molecules, wires, sheets, and solids.
- Representation used for calculating  $V_{xc}[\rho]$  even with other bases.
- Can systematically improve discretization quality:
  - Increase the spacing (the increasing the number of grid points)
  - Decrease the spacing (the increasing the number of grid points)
- Orthogonal “basis set”.
- Unbiased, independent of atomic positions (no Pulay forces).
- Problems:

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# Derivatives

- **Derivative at a point: sum over neighboring points.**
- The coefficients  $c_{ij}$  depend on the mesh and number of points used: *the stencil*.
- General form for Laplacian:

$$\nabla^2 f(n_x h, n_y h) = \sum_i^n \sum_j^n \frac{c_{ij}}{h} f(n_x h + ih, n_y h + jh)$$

- Compare definition of derivative:

$$f'(x_0) = \lim_{h \rightarrow 0} \frac{f(x_0 + h) - f(x_0)}{\Delta x}$$

- More points  $\rightarrow$  more precision.
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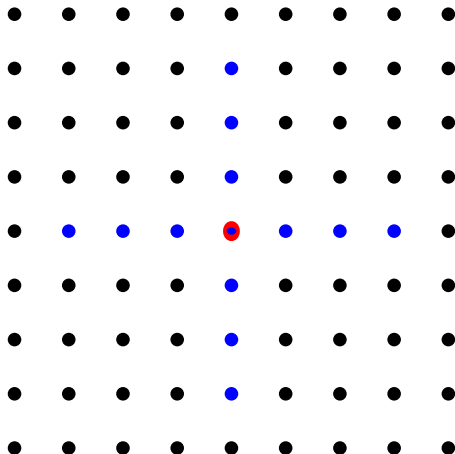
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# Example of stencil for Laplacian

Symmetric third-order in 2D.



## Trapezoidal rule

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- What we want to solve:

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- Solve for eigenstates at fixed  $V_{\text{eff}}$ , then update  $\rho$  and  $V_{\text{eff}}$ .

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- The Hamiltonian becomes a finite-size matrix.

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- We minimize (using conjugate gradient or other method):

Rayleigh-Ritz quotient

$$\epsilon(\psi) = \frac{\langle \psi | H | \psi \rangle}{\langle \psi | \psi \rangle}$$

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# Time-propagation

- Given an initial condition, solve the:

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# Absorption spectra from time-propagation

- Start from the ground state, with a 'kick.'

## Time-dependent potential

$$V(\mathbf{r}, t) = \kappa \delta(t) \quad \Rightarrow \quad \psi \rightarrow \psi e^{i\mathbf{k} \cdot \mathbf{r}}$$

- Time-propagate and get the dipole  $d(t)$  as a function of time.

$$\psi(\mathbf{r}, t) = \frac{1}{\Omega} \int d\mathbf{k} \psi(\mathbf{k}) e^{i\mathbf{k} \cdot \mathbf{r} - i\epsilon(\mathbf{k})t}$$

Apply the dipole operator

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## Polarizability tensor

$$\alpha_{ij}(\omega) = -\frac{1}{\kappa_i} \int dt e^{i\omega t} d_j(t)$$

## Absorption cross section

$$\sigma(\omega) = \frac{4\pi\omega}{c} \Im[\alpha(\omega)]$$

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$$\sigma(\omega) = \frac{4\pi\omega}{c} \Im[\alpha(\omega)]$$

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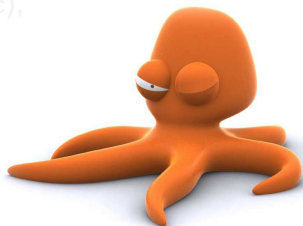
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Two papers on the Octopus code:

- A. Castro, H. Appel, Micael Oliveira, C.A. Rozzi, X. Andrade, F. Lorenzen, M.A.L. Marques, E.K.U. Gross, and A. Rubio, “octopus: a tool for the application of time-dependent density functional theory,” *Phys. Stat. Sol. B* **243**, 2465-2488 (2006).
- M.A.L. Marques, Alberto Castro, George F. Bertsch, and Angel Rubio, “octopus: a first-principles tool for excited electron-ion dynamics,” *Comput. Phys. Commun.* **151**, 60-78 (2003).



# Pulpo a feira (pulpo a la gallega)

The origin of the name Octopus. (Recipe available in code.)



- **Ground-state DFT.**
- Time-propagation.
- Molecular dynamics (Ehrenfest, Born-Oppenheimer, Car-Parrinello).
- Casida linear response.
- Sternheimer linear response for electromagnetic response, phonons, Van der Waals coefficients.
- Optimal control theory.
- Real-time quantum transport.
- (Other experimental features.)

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# Parallelization

- Parallelization in domains:

- Each processor handles points in a region of space.
- Points in the boundaries of each region must be copied to other nodes.
- Integrals are performed locally and summed over all domains.
- Efficient and scalable scheme.

- Parallelization in states:

- Parallelization in k-points/spin.
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- Scales to thousands of processors.

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- Xavier Andrade (Harvard)
- Heiko Appel (Fritz-Haber Institut)
- Alberto Castro (BIFI, Zaragoza)
- Miguel Marques (Université Lyon I)
- Danilo Nitsche (Freie Universität Berlin)
- Fernando Nogueira (Universidade de Coimbra)
- Micael Oliveira (Universidade de Coimbra)
- Carlo Andrea Rozzi (Università di Modena e Reggio Emilia)
- Angel Rubio (UPV San Sebastián and FHI)
- David Strubbe (University of California, Berkeley; LBNL)

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# The tutorial<sup>4</sup>

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- Optimizing grid parameters.
- Visualization.
- Time-propagation with a laser.
- Optical spectrum from time-propagation.
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Have fun!

