

# Unsolved problems in Gravitational Waves

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University of Birmingham

*Unsolved problems in Astrophysics and Cosmology  
Centro de Ciencias de Benasque Pedro Pascual 14th - 18th February 2011*



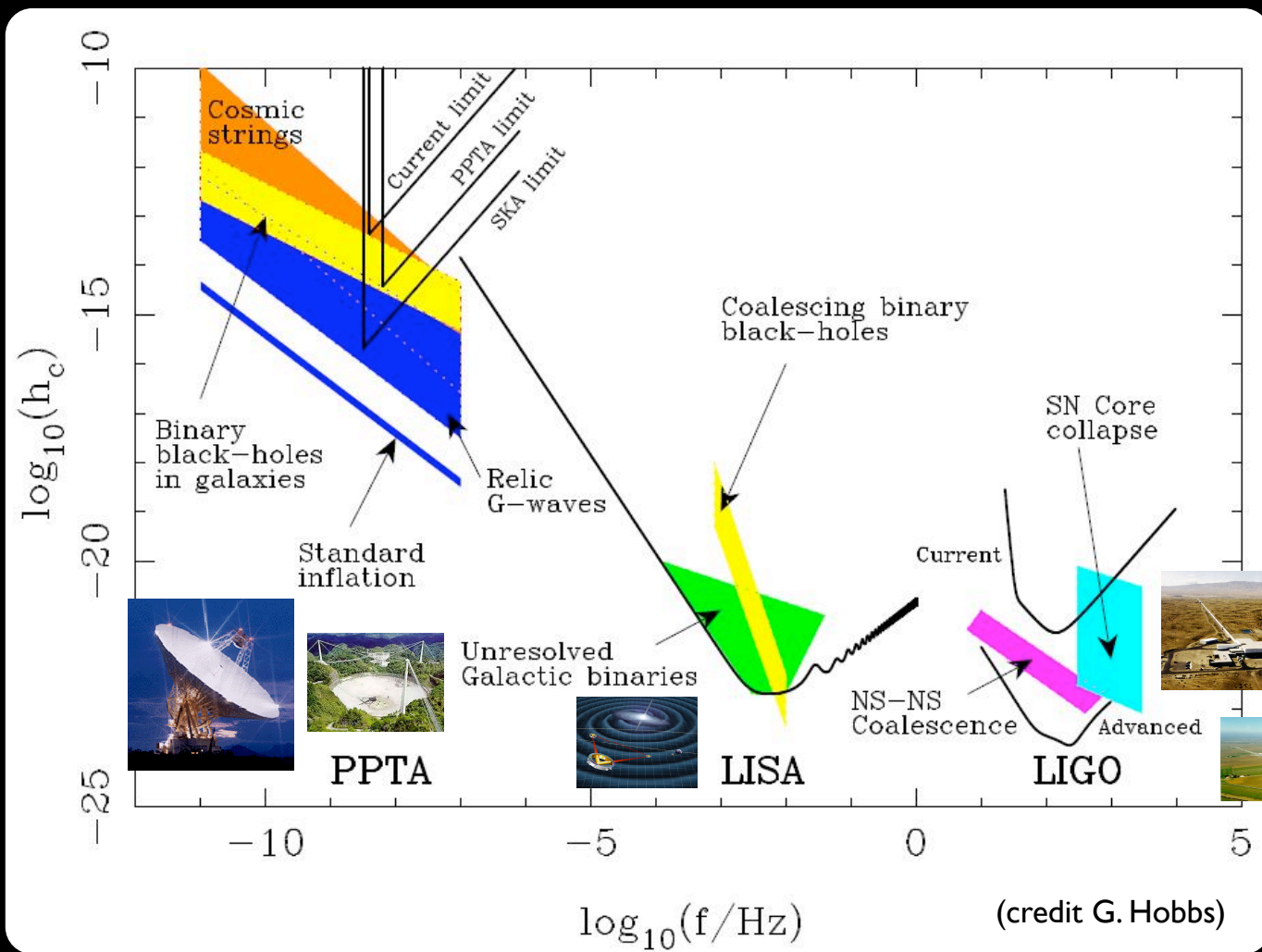
# I. GW unsolved problems: No *direct* detection (yet)



I. GW unsolved problems:  
No *direct* detection (yet)  
Is it expected?

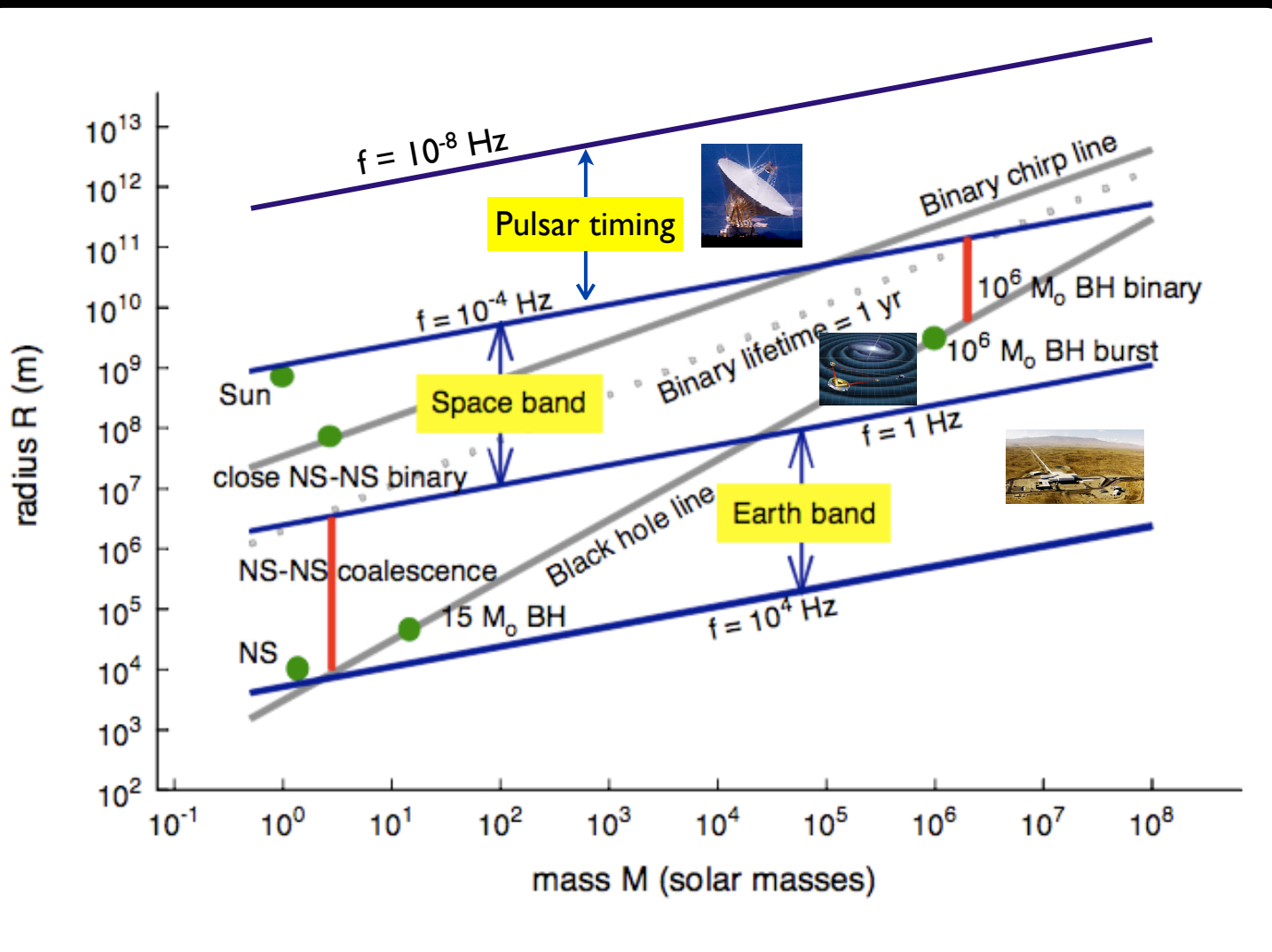


# GW spectrum





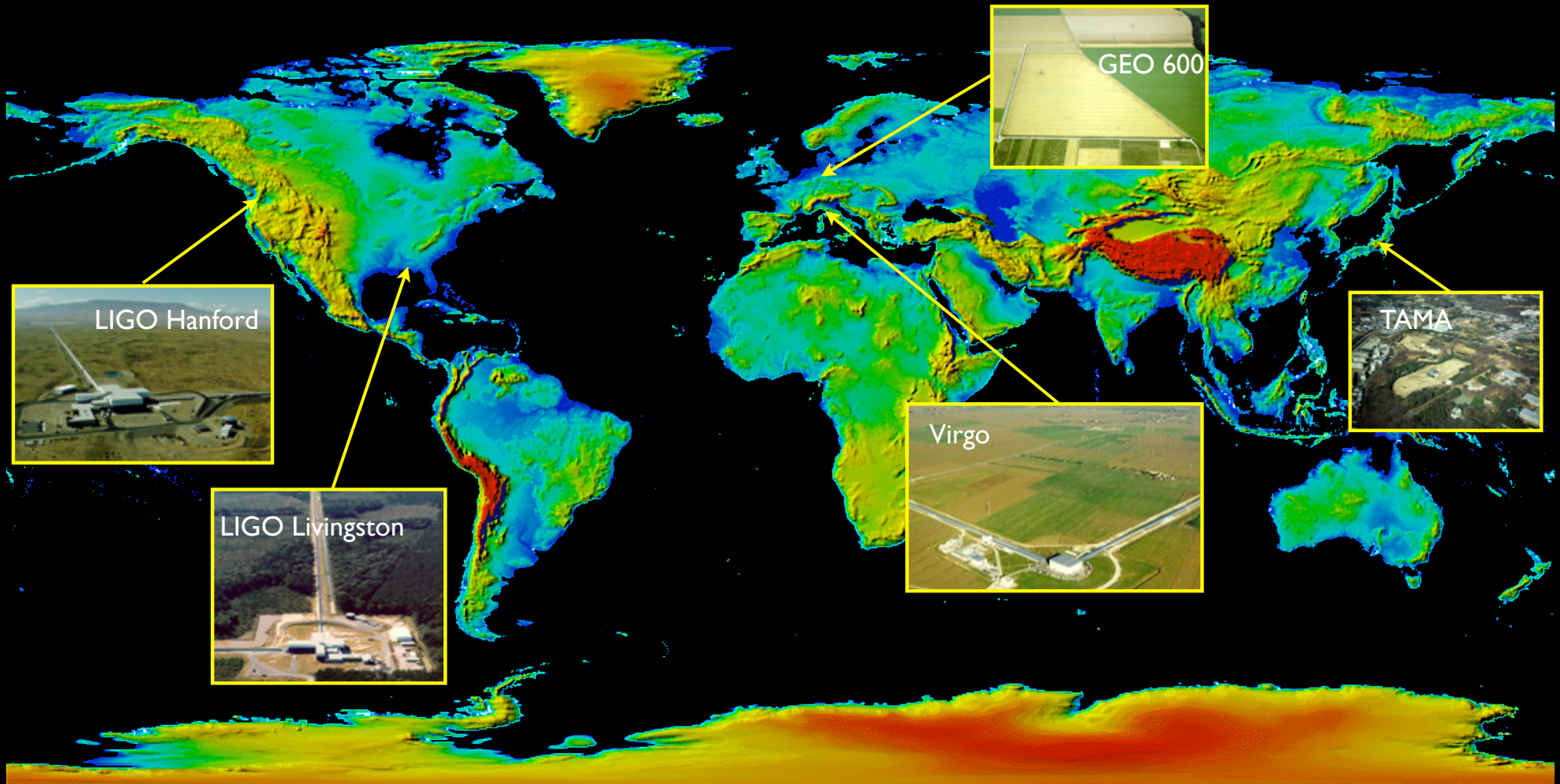
# Black holes and GWs



(Schutz)

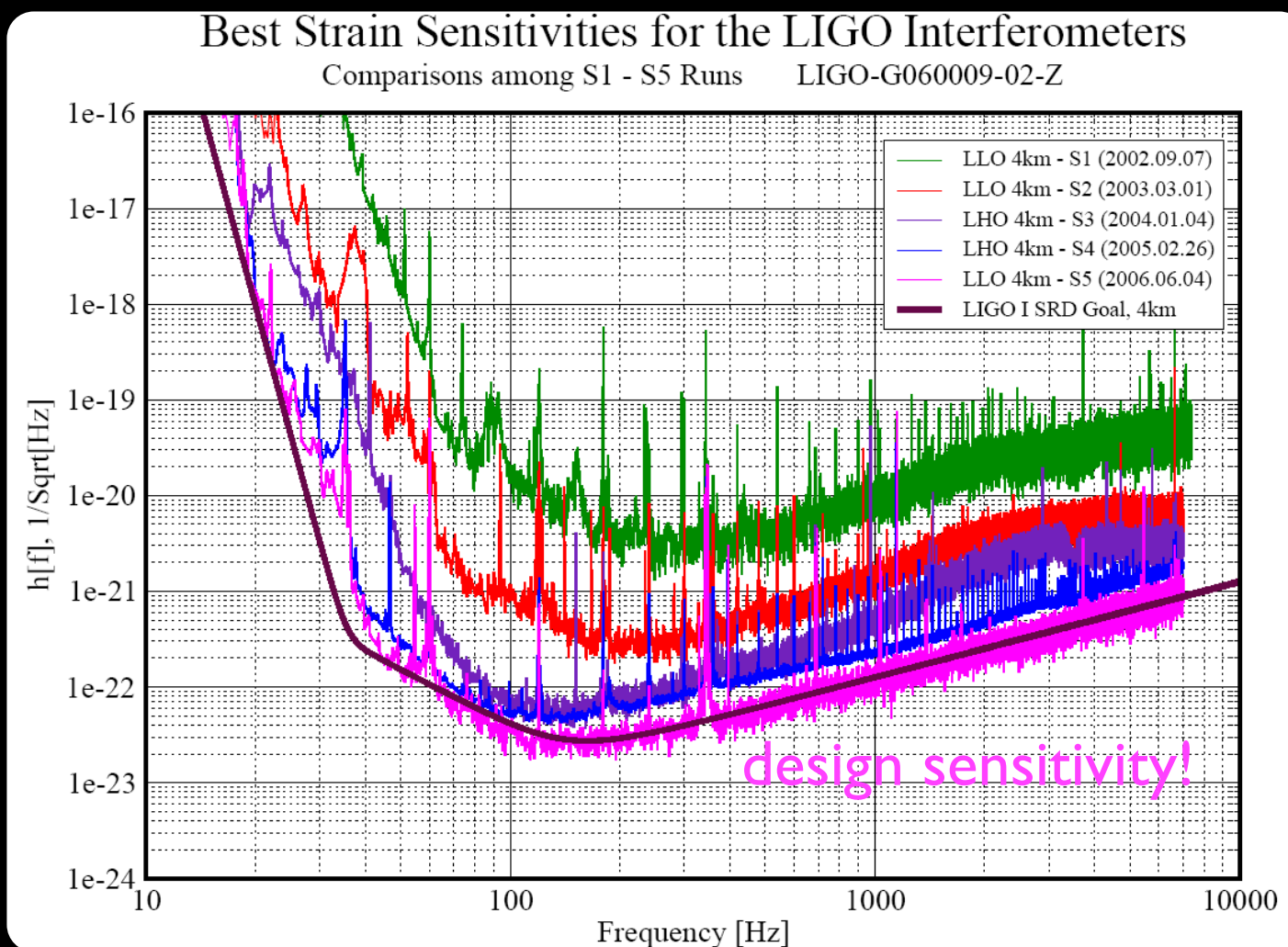


# The global network of laser interferometers





# Evolution of LIGO sensitivity

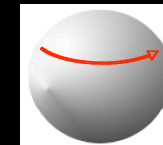
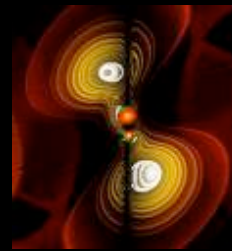




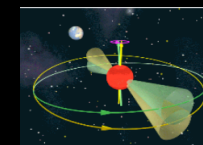
# Science targets of on-going searches



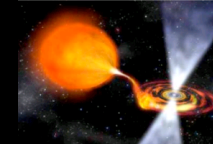
- Coalescing binaries
  - NS/BH binary systems
- Un-modeled bursts
  - e.g. supernovae, gamma-ray bursts
- Continuous waves
  - e.g. rotating neutron stars
- Stochastic signals
  - e.g. backgrounds from the early universe, foreground radiation from astrophysical sources



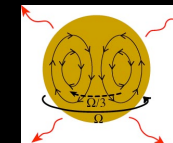
"Mountain" on neutron star



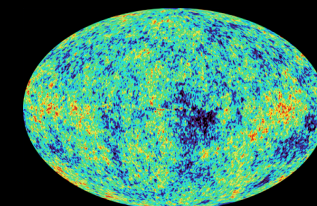
Wobbling neutron star



Accreting neutron star



R-modes

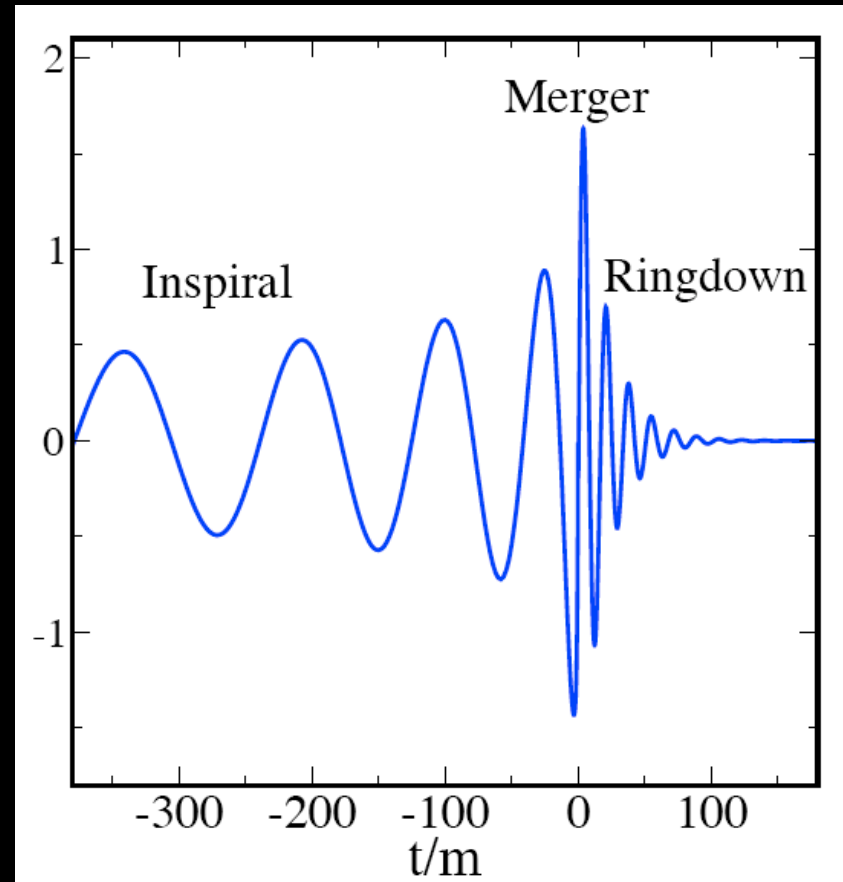
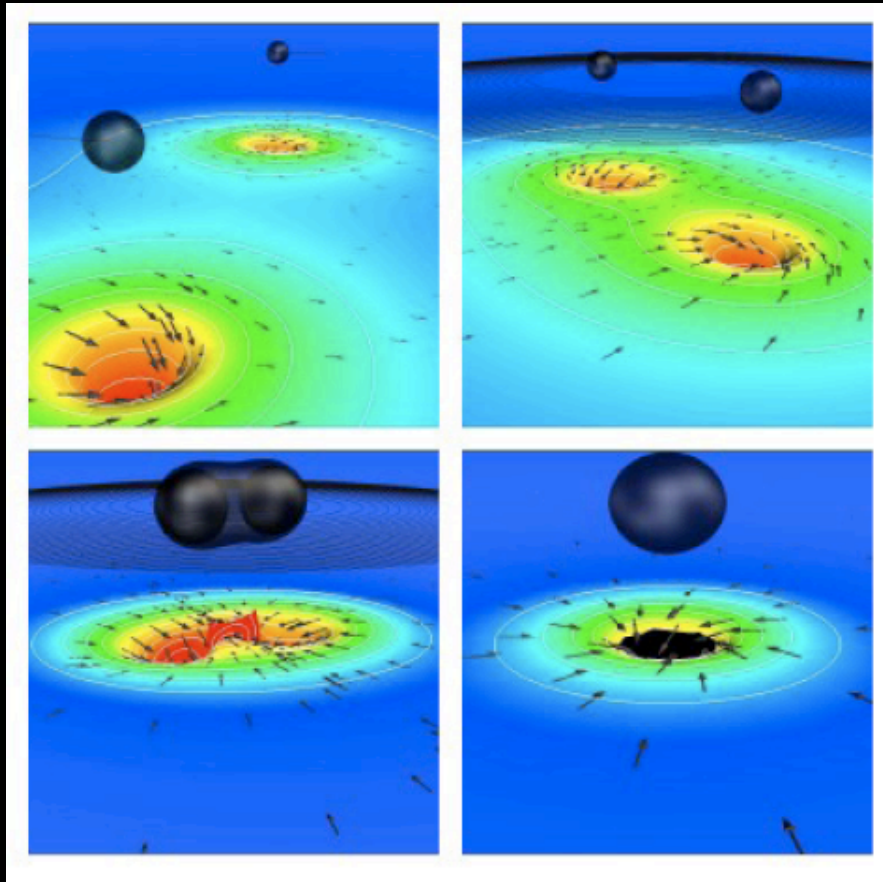


Analog from cosmic microwave background -- WMAP 2003





# Coalescing binaries



SpeC code



# GWs from binary systems

$$h(t) \sim \text{angles} \times \frac{\mathcal{M}^{5/3} f(t)^{2/3}}{D_L} \cos \Phi(t; m_{1,2}, S_{1,2})$$

“chirp” mass →  $\mathcal{M}$   
frequency →  $f(t)$   
masses →  $m_{1,2}$   
spins →  $S_{1,2}$   
sky location  
orbit orientation → angles  
luminosity distance →  $D_L$

- Demographics of neutron star and black holes: masses, spins, 3D distribution in the universe
- Star formation history, mass function
- Dynamics in star clusters
- Cosmography (binary systems are standard candles): independent measure of luminosity distance, cosmological parameters
- Maps of the strongly non-linear dynamics
- Tests of general relativity
- Joint observations with X/γ-ray, optical, neutrino,... telescopes: full details about the physical processes at work



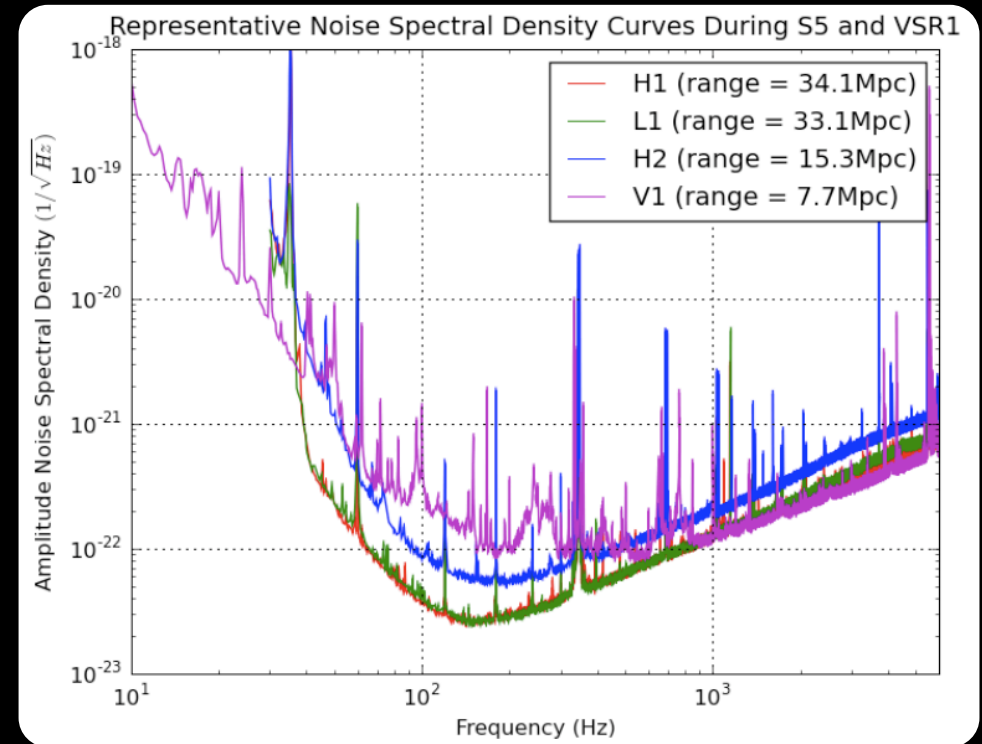
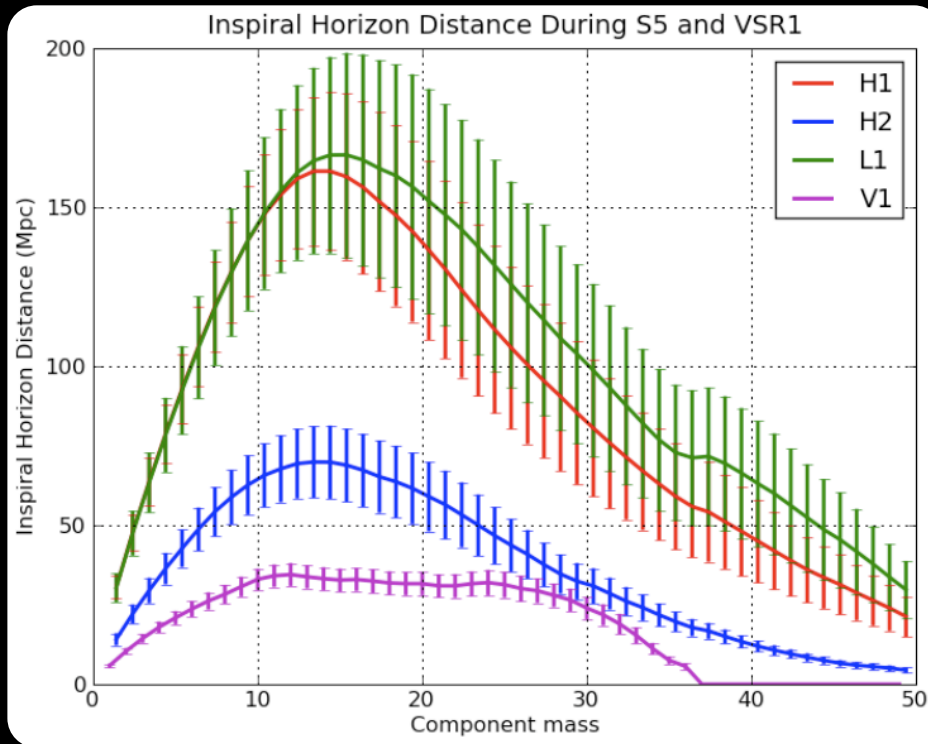
# Measured signal: strain

$$h(t) = F_+(\alpha, \delta, \psi) h_+(t) + F_x(\alpha, \delta, \psi) h_x(t)$$

- Polarization amplitudes  $h_+(t)$  and  $h_x(t)$  contain full information about the physics
- Unknown parameters (9 for non-spinning binary systems, 15 for general spins, 17 if also eccentricity is present)
  - Masses (2 parameters)
  - Source location in the sky (2 parameters)
  - Orbital plane orientation (2 parameters)
  - Luminosity distance
  - Time and phase at coalescence (2 parameters)
  - Spins (6 parameters)
  - Eccentricity (2 parameters)



# How far could LIGO/Virgo see during S5/VSR1?



- LIGO S5: November 2005 - October 2007
- One year of data at design sensitivity in triple coincidence
- VIRGO VSR1: last 5 months of the run



# Detection rate

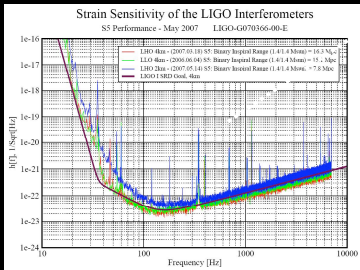
## Detection Rate

$$\dot{N} = R \times N_G$$

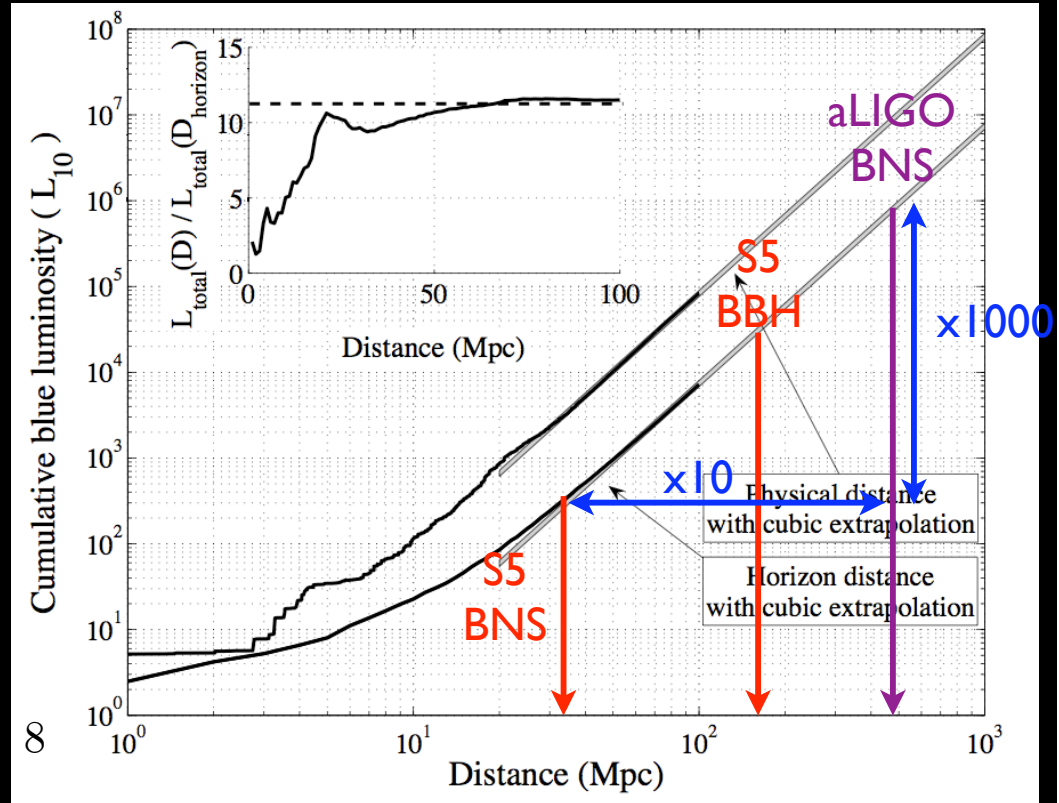
number of galaxies accessible by a search in  $L_{10}$ 's

coalescence rate per galaxy

$$\text{SNR}^2 = \int_{f_{\text{low}}}^{f_{\text{isco}}} \frac{|\tilde{h}(f)|^2}{S_n(f)} df$$



$$\tilde{h}(f) \propto \frac{\mathcal{M}^{5/6}}{D_L} f^{-7/6}$$



$$N_G(L_{10}) = \frac{4\pi}{3} D_{\text{hor}}^3 \times \left( \frac{1}{2.26} \right)^3 \times 0.02 \times L_{10} / \text{Mpc}^3$$

average over sky and orientation



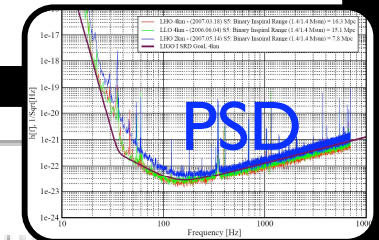
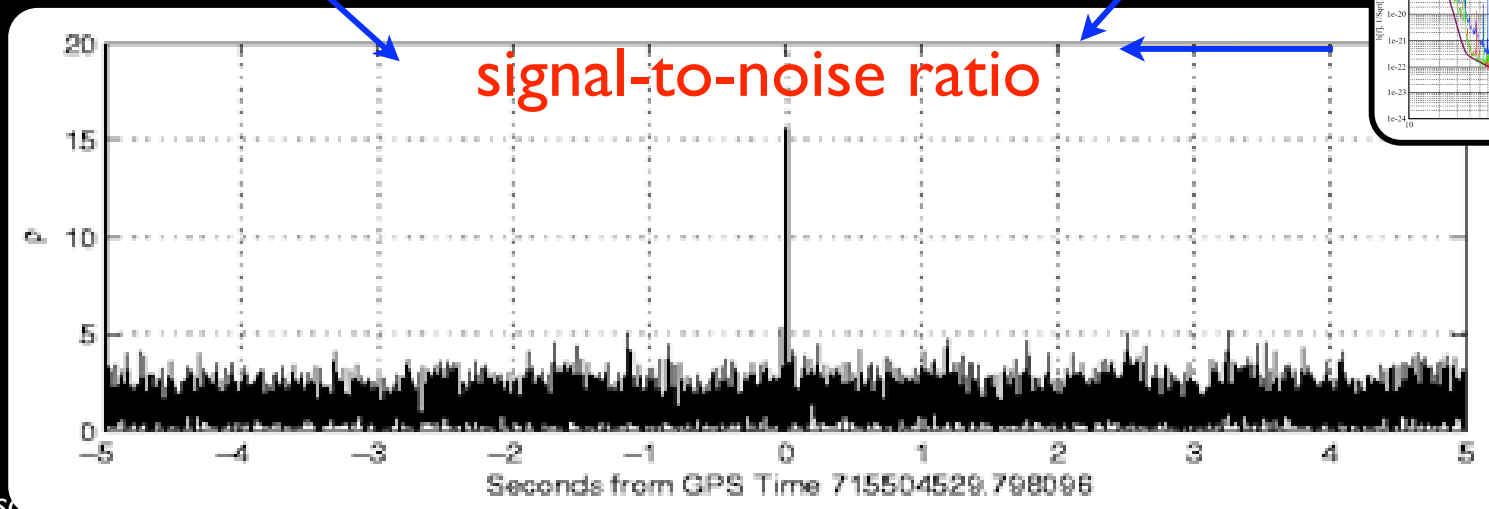
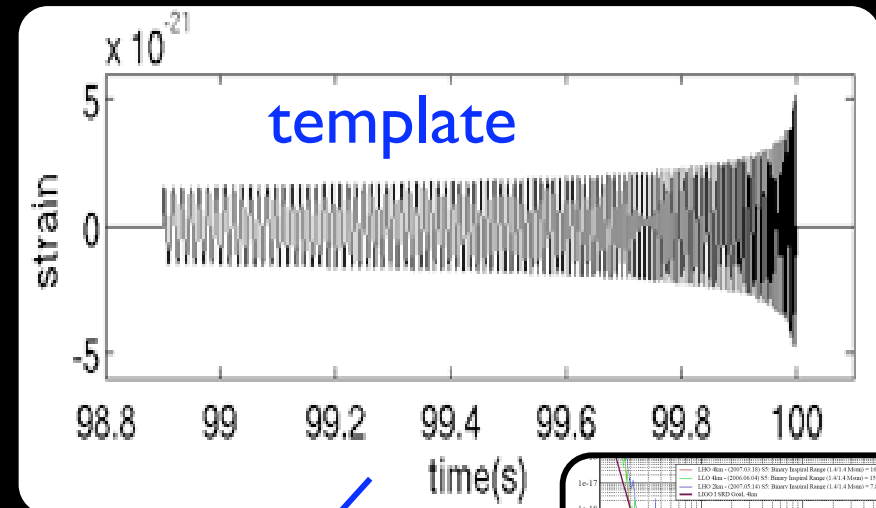
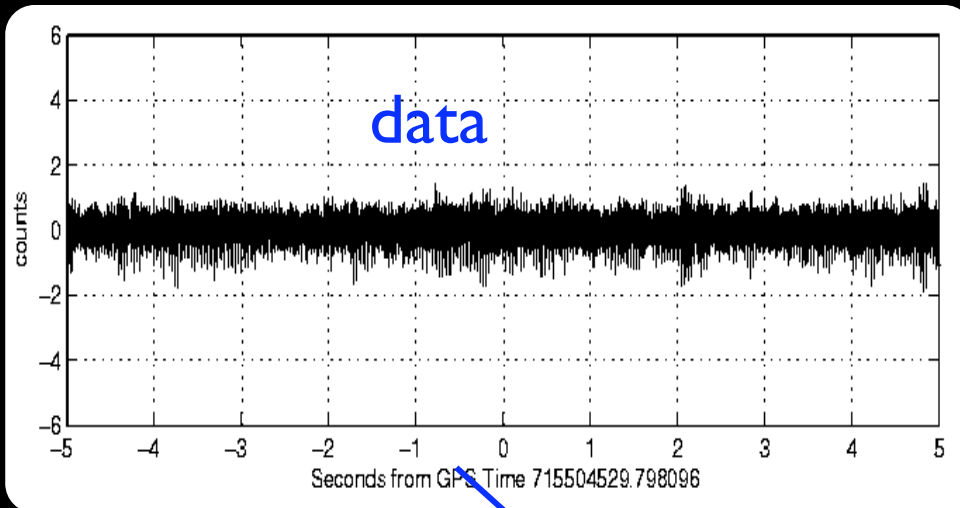
# Expected detection rates

IFO	Source <sup>a</sup>	$\dot{N}_{\text{low}}$ yr <sup>-1</sup>	$\dot{N}_{\text{re}}$ yr <sup>-1</sup>	$\dot{N}_{\text{high}}$ yr <sup>-1</sup>	$\dot{N}_{\text{max}}$ yr <sup>-1</sup>
Initial	NS-NS	$2 \times 10^{-4}$	0.02	0.2	0.6
	NS-BH	$7 \times 10^{-5}$	0.004	0.1	
	BH-BH	$2 \times 10^{-4}$	0.007	0.5	
	IMRI into IMBH			$< 0.001^b$	$0.01^c$
	IMBH-IMBH			$10^{-4d}$	$10^{-3e}$
Advanced	NS-NS	0.4	40	400	1000
	NS-BH	0.2	10	300	
	BH-BH	0.4	20	1000	
	IMRI into IMBH			$10^b$	$300^c$
	IMBH-IMBH			$0.1^d$	$1^e$

Abadie et al. (LSC and Virgo), CQG 27, 173001 (2010)



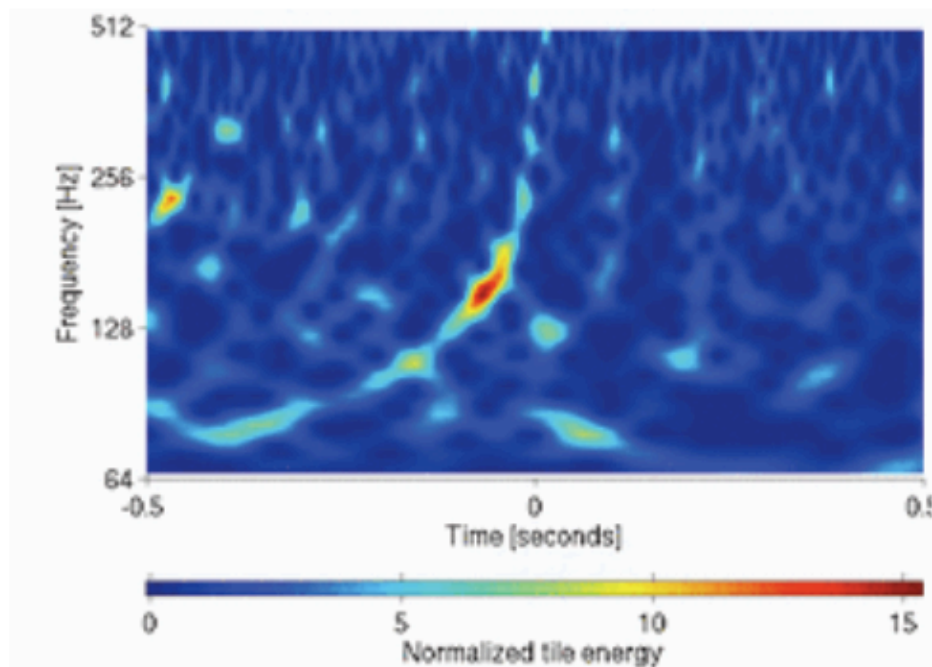
# Searching for binaries: matched-filtering



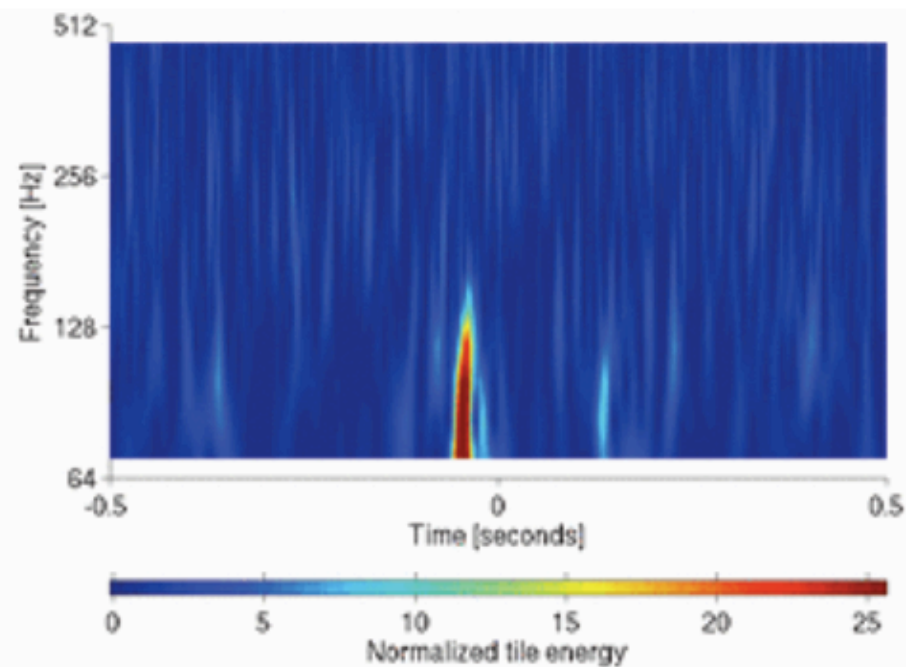


# Examples of “signals”

## Hardware injection



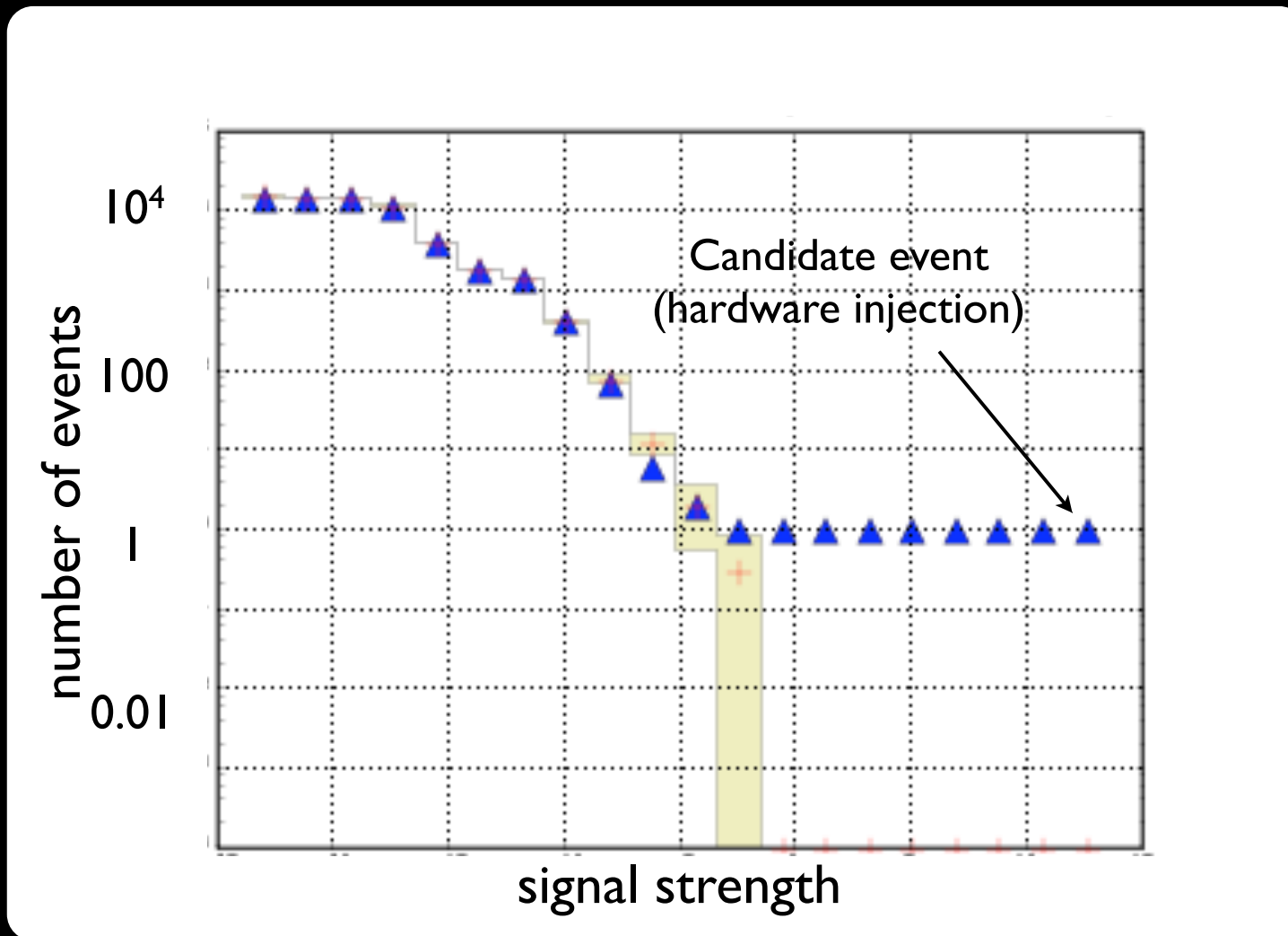
## Instrumental artifact







# How a detection candidate shows up





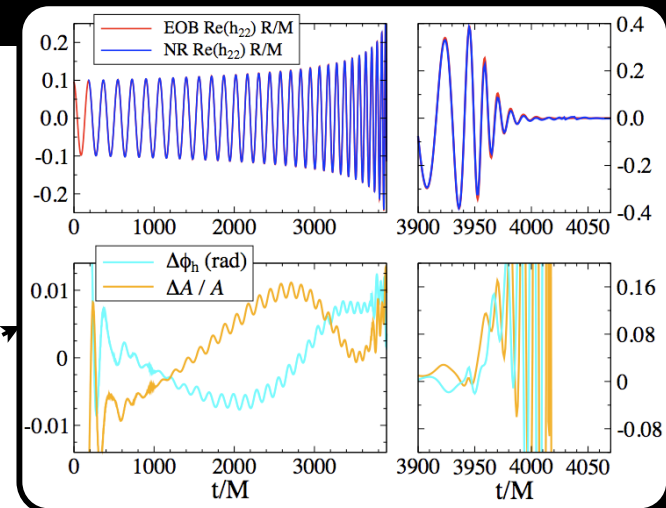
# Mass search area

post-Newtonian approx. of inspiral

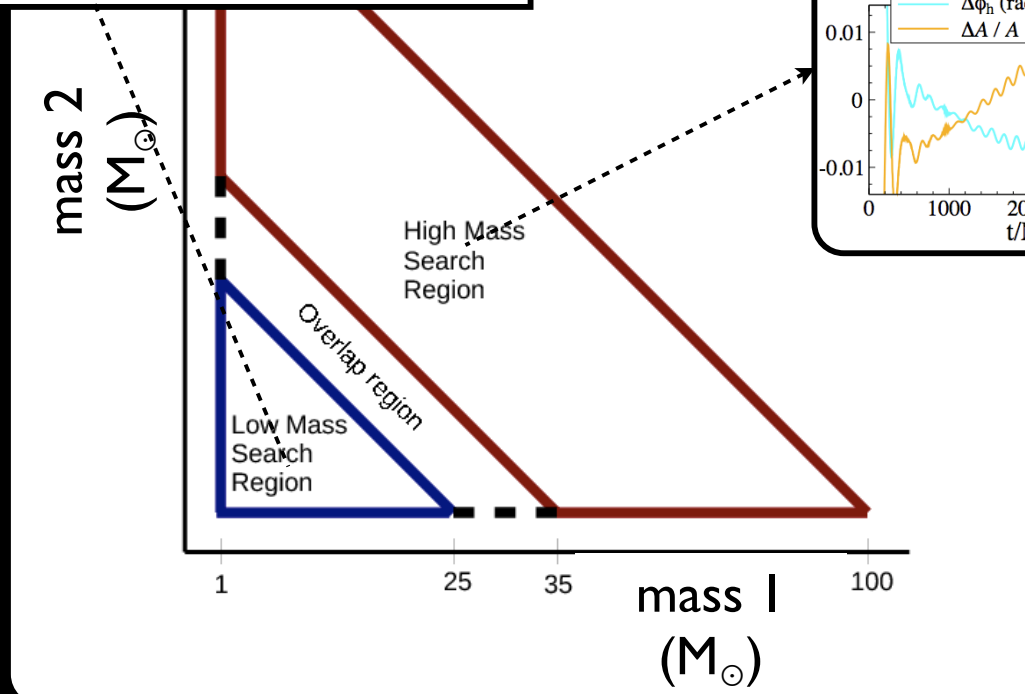
$$\begin{aligned} \phi = & -\frac{x^{-5/2}}{32\nu} \left\{ 1 + \left( \frac{3715}{1008} + \frac{55}{12}\nu \right) x - 10\pi x^{3/2} + \left( \frac{15293365}{1016064} + \frac{27145}{1008}\nu + \frac{3085}{144}\nu^2 \right) x^2 \right. \\ & + \left( \frac{38645}{1344} - \frac{65}{16}\nu \right) \pi x^{5/2} \ln\left(\frac{x}{x_0}\right) \\ & + \left[ \frac{12348611926451}{18776862720} - \frac{160}{3}\pi^2 - \frac{1712}{21}C - \frac{856}{21}\ln(16x) \right. \\ & + \left. \left. \left( -\frac{15737765635}{12192768} + \frac{2255}{48}\pi^2 \right) \nu + \frac{76055}{6912}\nu^2 - \frac{127825}{5184}\nu^3 \right] x^3 \right. \\ & \left. + \left( \frac{77096675}{2032128} + \frac{378515}{12096}\nu - \frac{74045}{6048}\nu^2 \right) \pi x^{7/2} + \mathcal{O}\left(\frac{1}{c^8}\right) \right\}, \end{aligned}$$

Blanchet LLR 2006

full inspiral-merger-ringdown waveforms



see Buonanno et al, 2009;  
Ajith et al, 2008



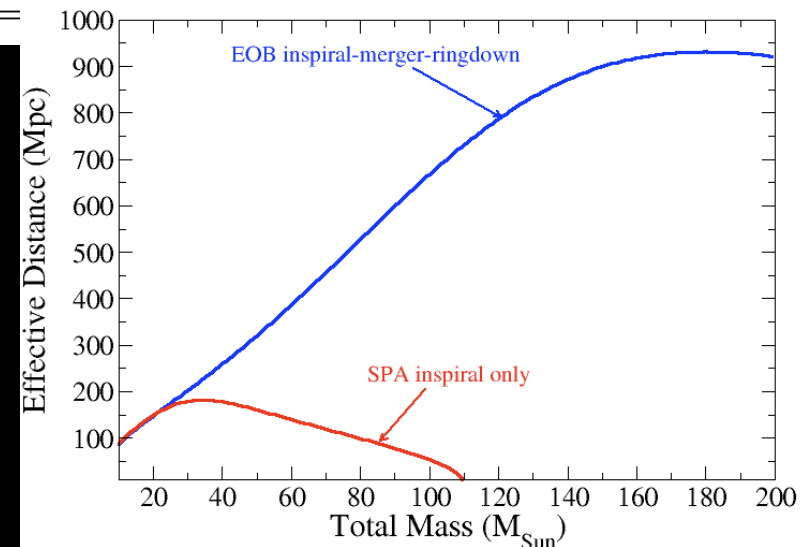


# The two body problem

Number of inspiral wave cycles ( $f > 10\text{Hz}$ )

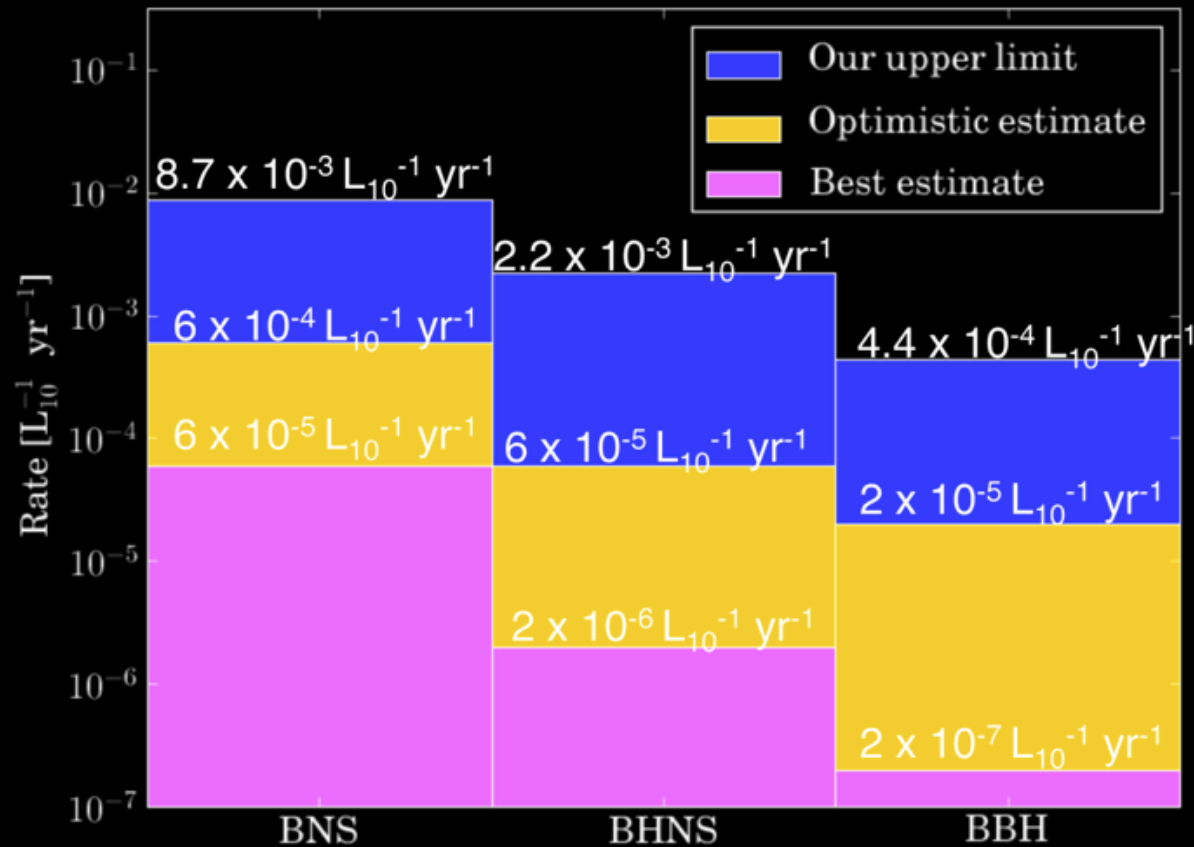
	$2 \times 1.4 M_{\odot}$	$10 M_{\odot} + 1.4 M_{\odot}$	$2 \times 10 M_{\odot}$
Newtonian order	16031	3576	602
1PN	441	213	59
1.5PN (dominant tail)	-211	-181	-51
2PN	9.9	9.8	4.1
2.5PN	-11.7	-20.0	-7.1
3PN	2.6	2.3	2.2
3.5PN	-0.9	-1.8	-0.8

Horizon Distance vs Total Mass





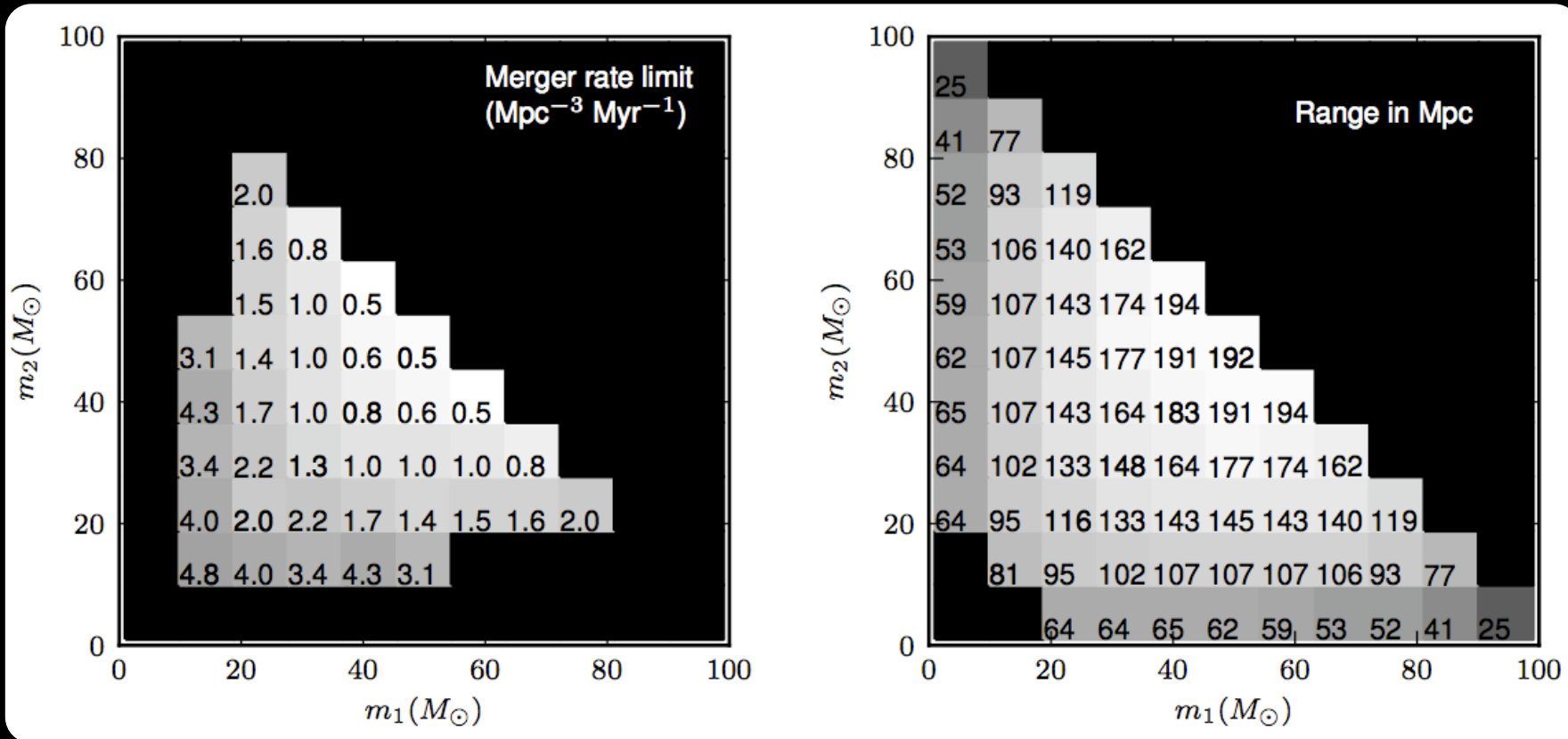
# S5 “low-mass”: Upper-limits



Abadie et al. (LSC and Virgo), PRD 82, 102001 (2010)



# S5 “high-mass”: Upper-limits



Upper-limit a factor  $\sim 10$  higher than optimistic rate



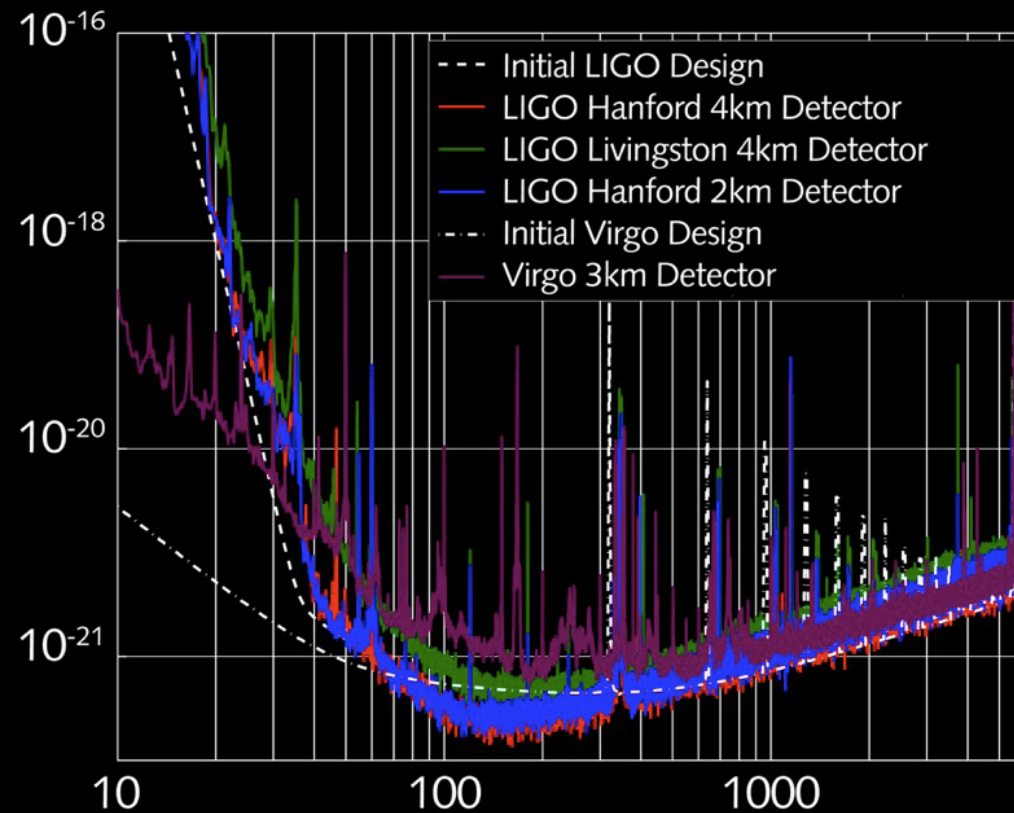
I. GW unsolved problems:  
No *direct* detection (yet)  
Is it expected?  
(Unfortunately) yes



## 2. Any chance of a detection “soon”?



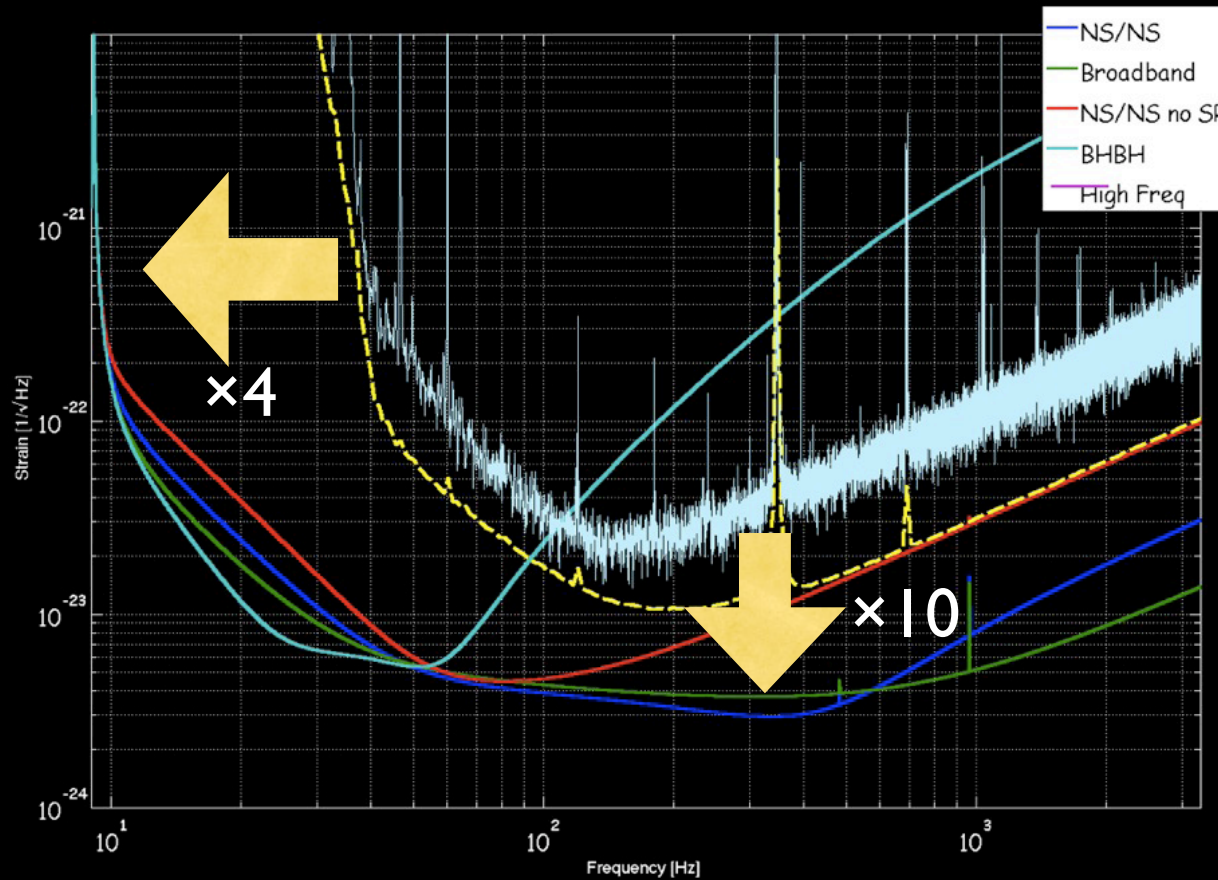
# Beyond design sensitivity: eLIGO/Virgo+ (S6/VSR2/3)







# Advanced LIGO





# Expected detection rates

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Abadie et al. (LSC and Virgo), CQG 27, 173001 (2010)



# LIGO Australia?

Gingin facility



Decision will be made by Oct 2011

# Feel the Universe in Underground

- Detect Gravitational Waves from 200 Mpc Away -

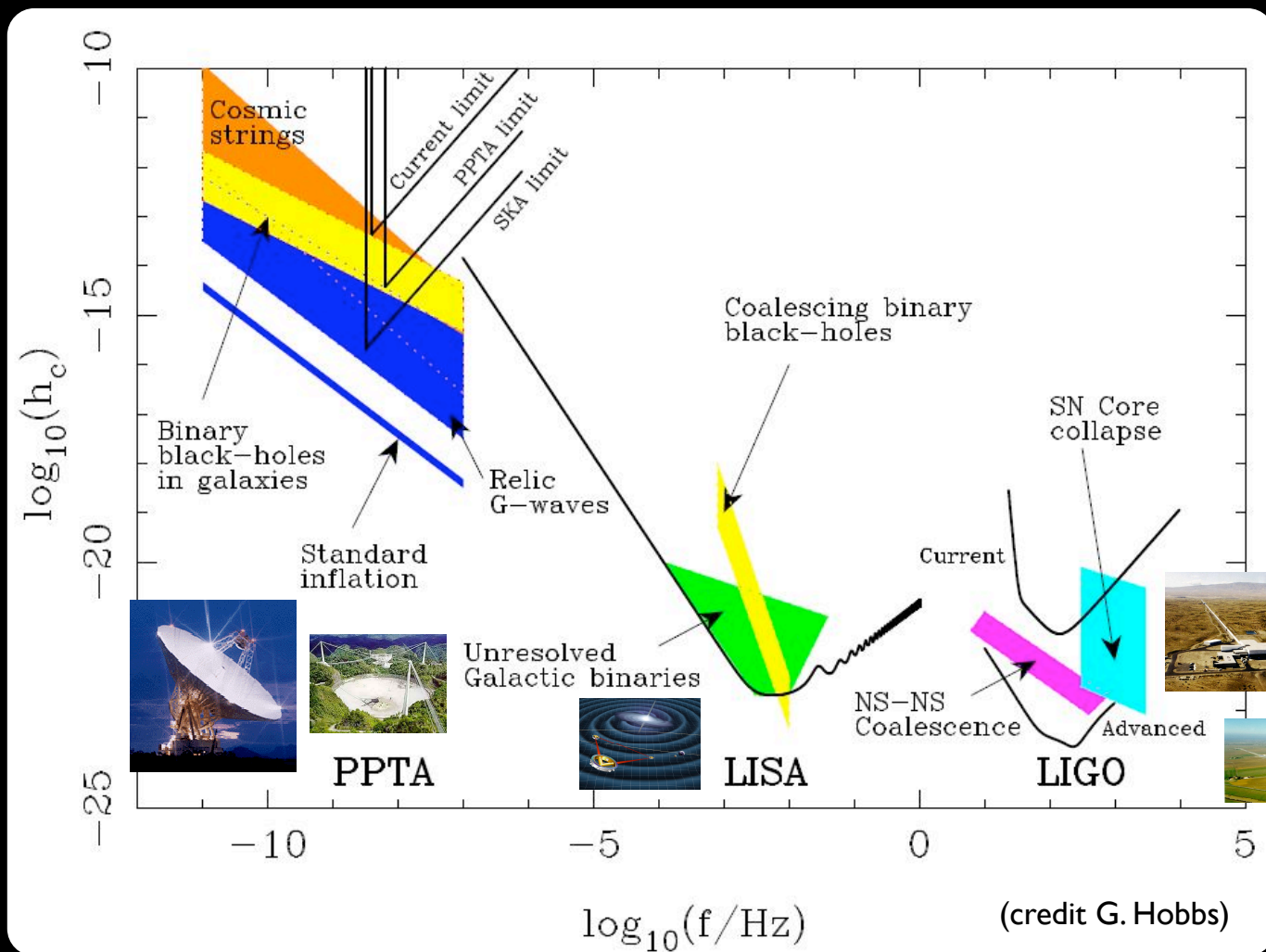
# LCGT

# LCGT



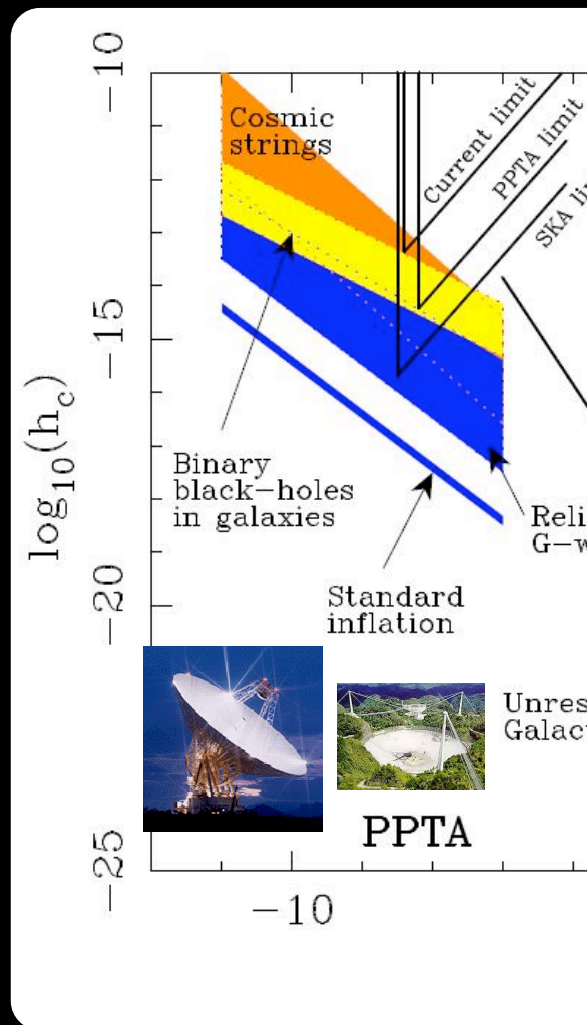


# GW spectrum





# Pulsar Timing Arrays

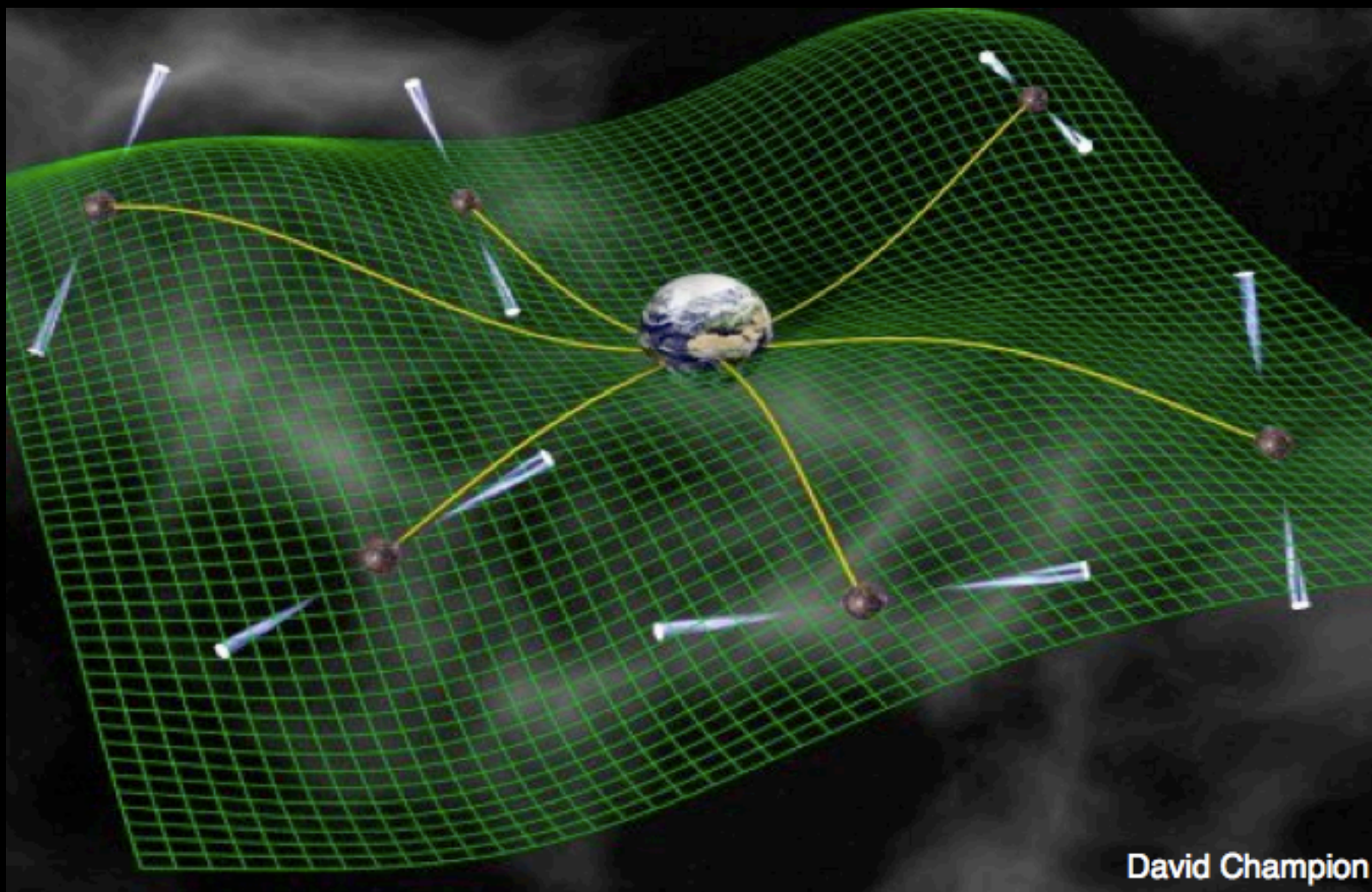


In operation:

- Parkes PTA
- European Pulsar Timing Array (EPTA/LEAP)
- Nanograv



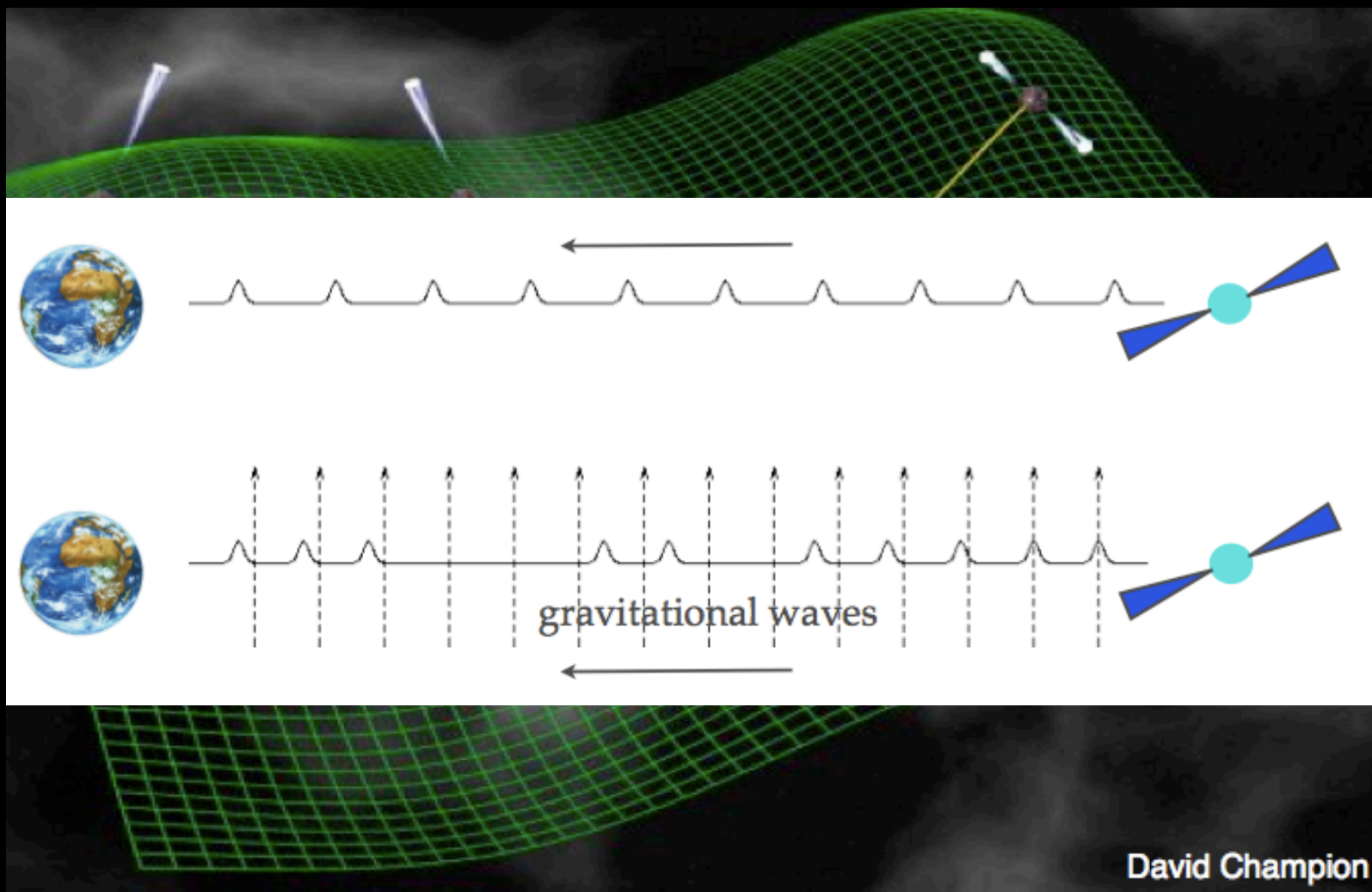
# Pulsar Timing Arrays



David Champion



# Pulsar Timing Arrays







# PTA and 3C 66B

- VLBI measurements of motion of radio core 3C 66B (Sudou et al, 2002). Consistent with super-massive black hole binary with:

$$P = 1.05 \pm 0.03 \text{ yr}$$

$$M \approx 5 \times 10^{10} M_{\odot}$$

$$z = 0.02$$

- Analysis of timing data from a single pulsar (B1855+09) rules out the system at 95% confidence (Jenet et al, 2004)
- See also Lommen and Backer (2001) for proof-of-concept analysis

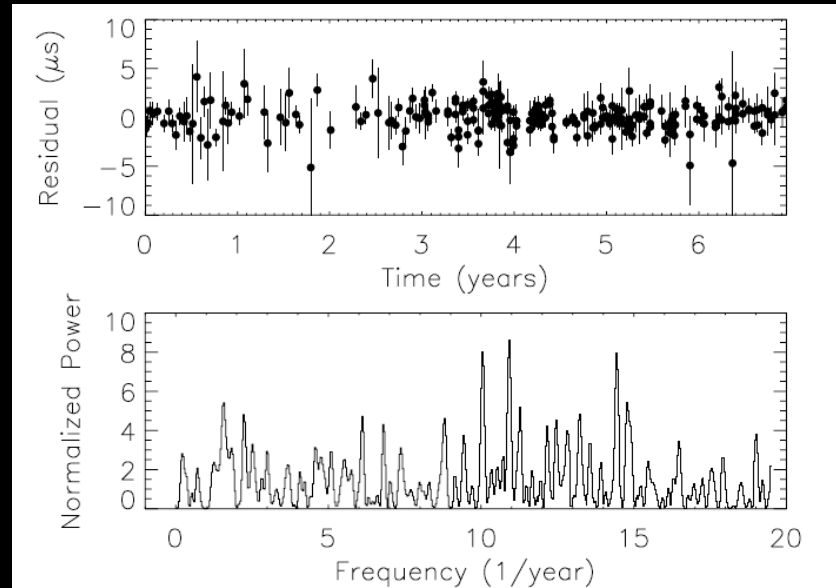


FIG. 2.—*Top*: Timing residuals for PSR B1855+09. *Bottom*: The corresponding normalized Lomb periodogram.

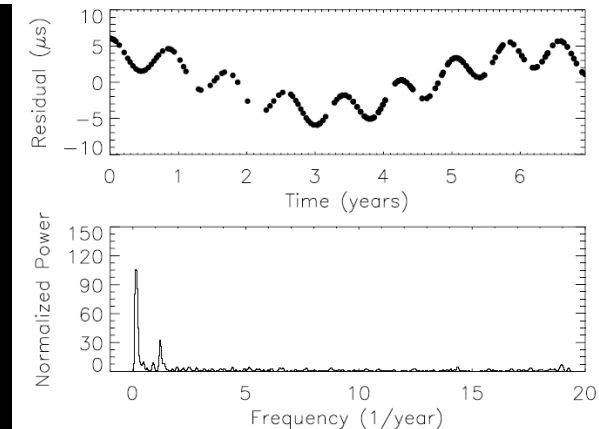


FIG. 1.—*Top*: Theoretical timing residuals induced by G-waves from 3C 66B. The timing points are chosen to coincide with the actual timing residuals of PSR B1855+09. *Bottom*: The corresponding normalized Lomb periodogram.



# What is the sensitivity needed?

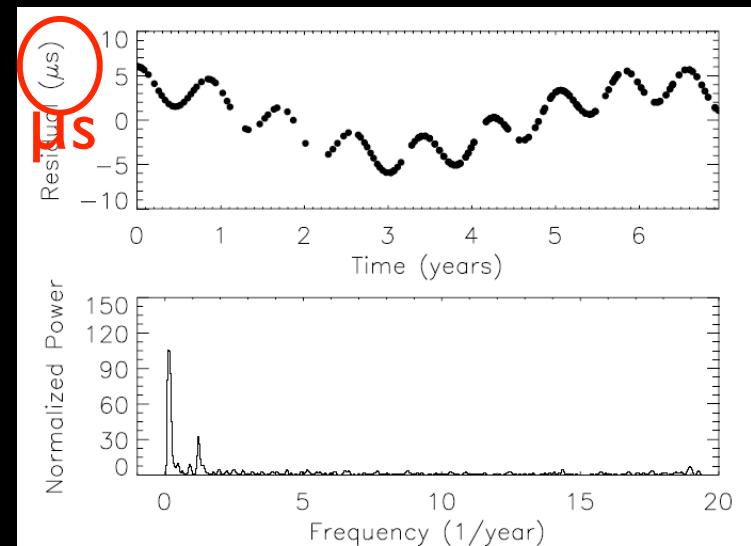
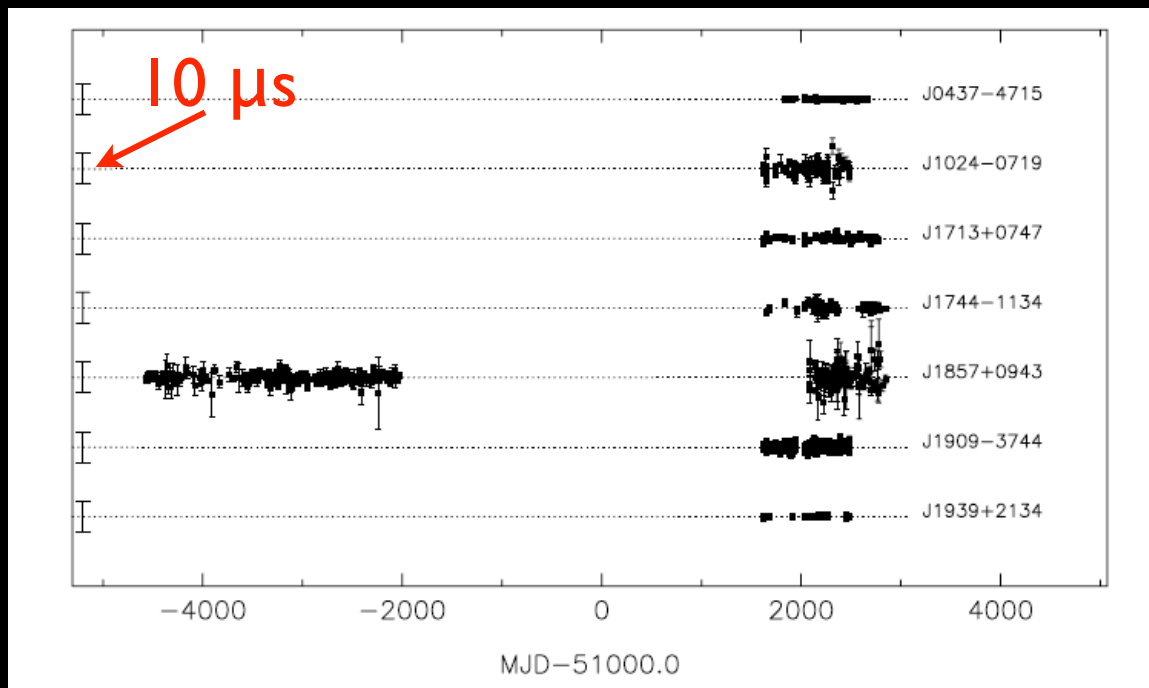


FIG. 1.—*Top*: Theoretical timing residuals induced by G-waves from 3C 66B. The timing points are chosen to coincide with the actual timing residuals of PSR B1855+09. *Bottom*: The corresponding normalized Lomb periodogram.

(Jenet et al, 2004, 2006)

$$r(t) \simeq 26 \left( \frac{\mathcal{M}}{10^9 M_\odot} \right)^{5/3} \left( \frac{D}{100 \text{ Mpc}} \right)^{-1} \left( \frac{f}{5 \times 10^{-8} \text{ Hz}} \right)^{-1/3} \text{ ns}$$

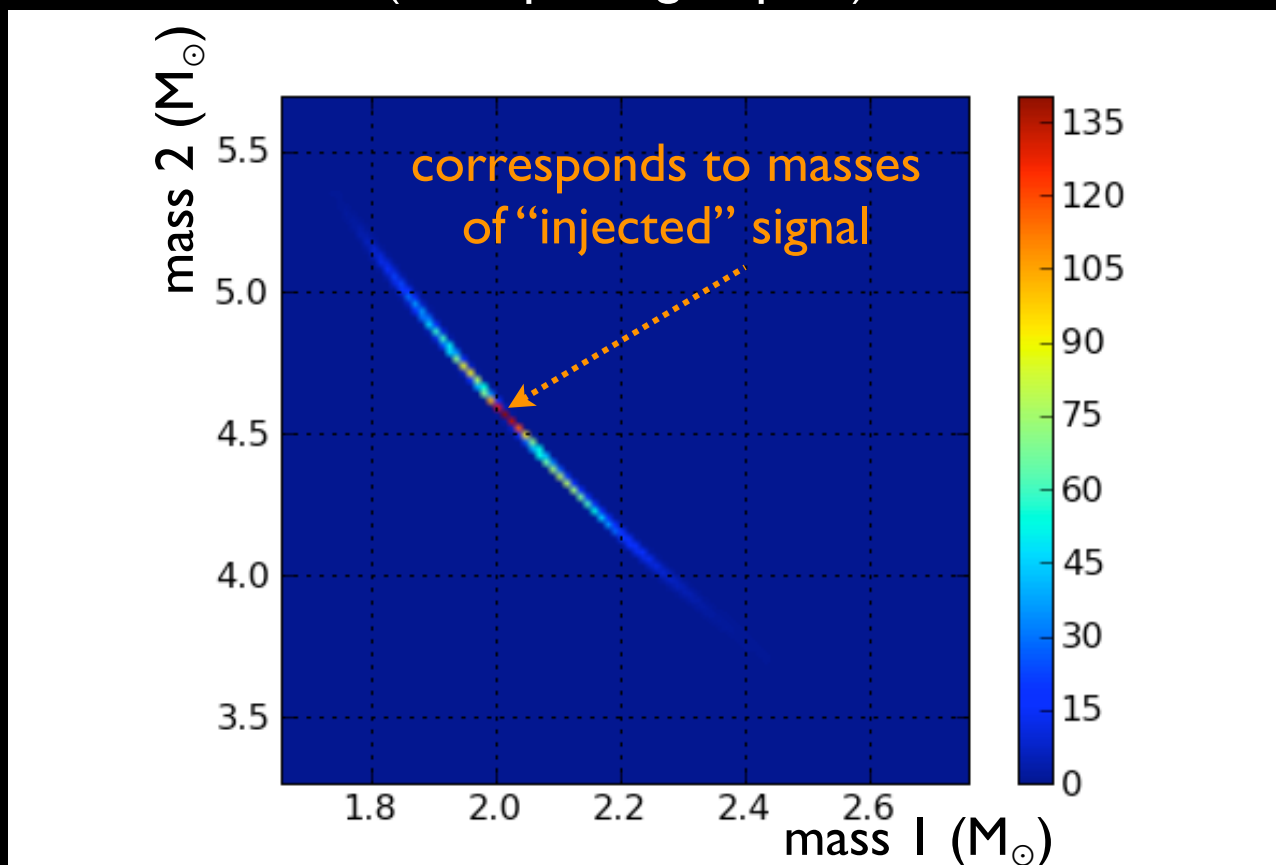


3. Can we do precise astronomy?
- 3a. Are coalescing binaries a new class of standard candles?  
(do we need a new class?)



# e.g.: Measuring masses

Marginalised PDFs over a 9-dimensional parameter space  
(non-spinning inspiral)

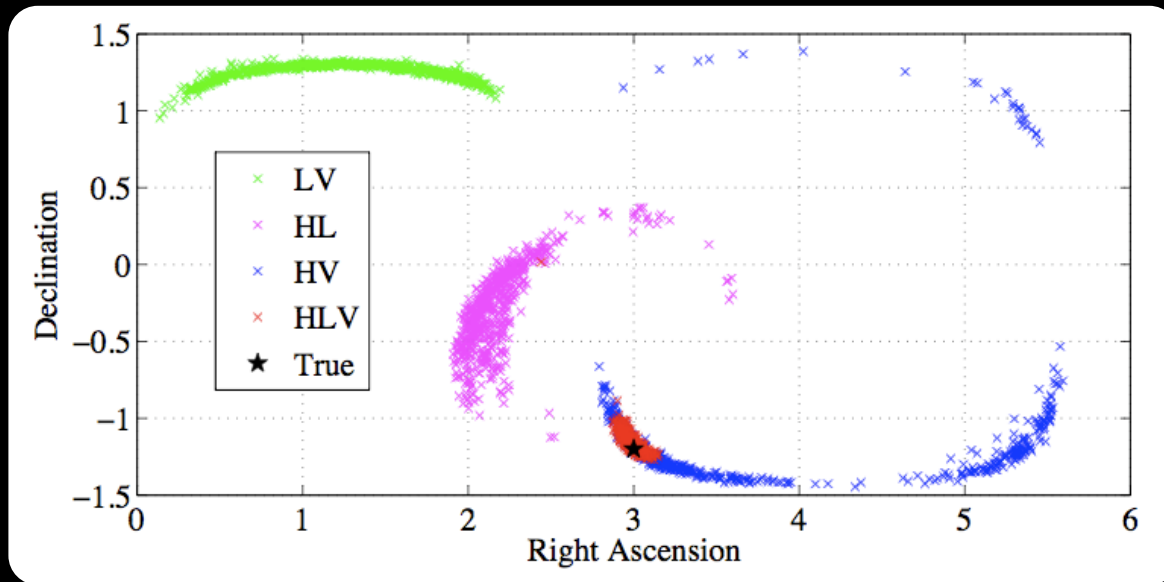


(see e.g. Roever et al, 2007, van der Sluys et al 2008, Veitch and AV 2009)



# Sampling rings in the sky

$$h(t) = F_+(\alpha, \delta, \psi) h_+(t) + F_x(\alpha, \delta, \psi) h_x(t)$$

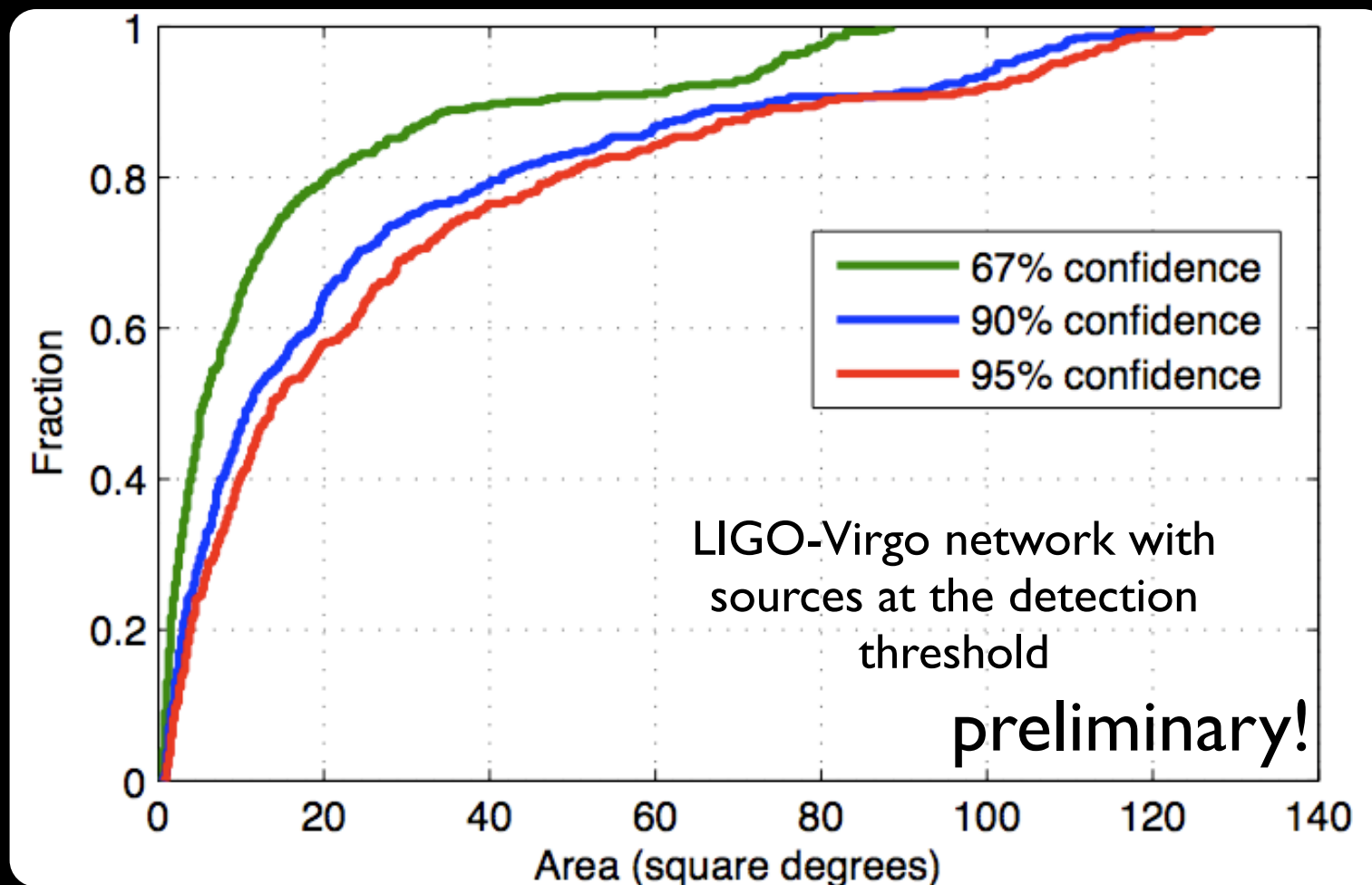


(Veitch & AV 2010)



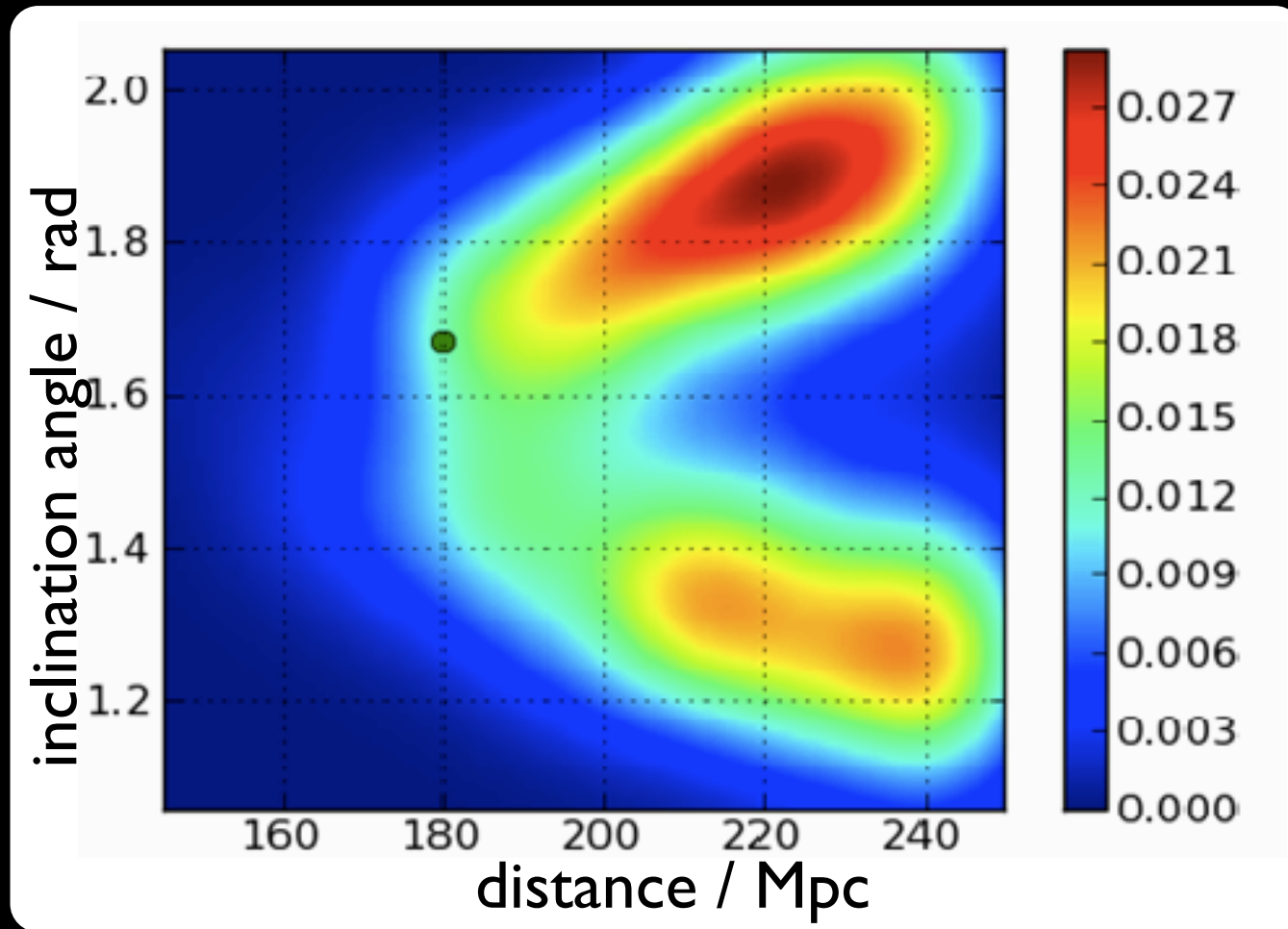


# Locating a source in the sky





# Distance measurements



$$h_+ = \# \frac{(1 + \cos^2 \iota)}{D}$$
$$h_\times = \# \frac{\cos \iota}{D}$$

credit J.Veitch

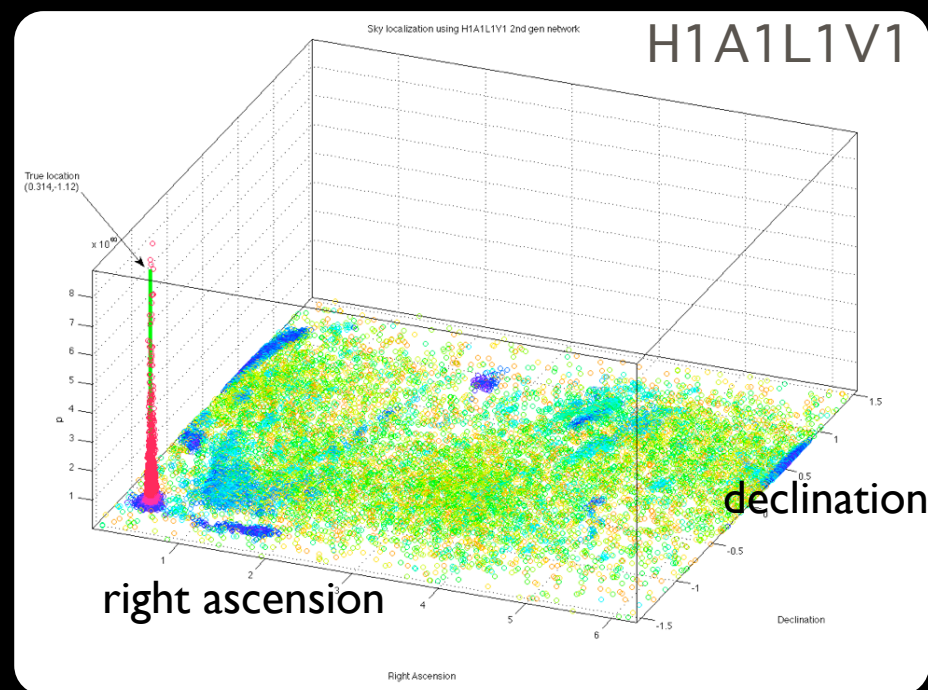
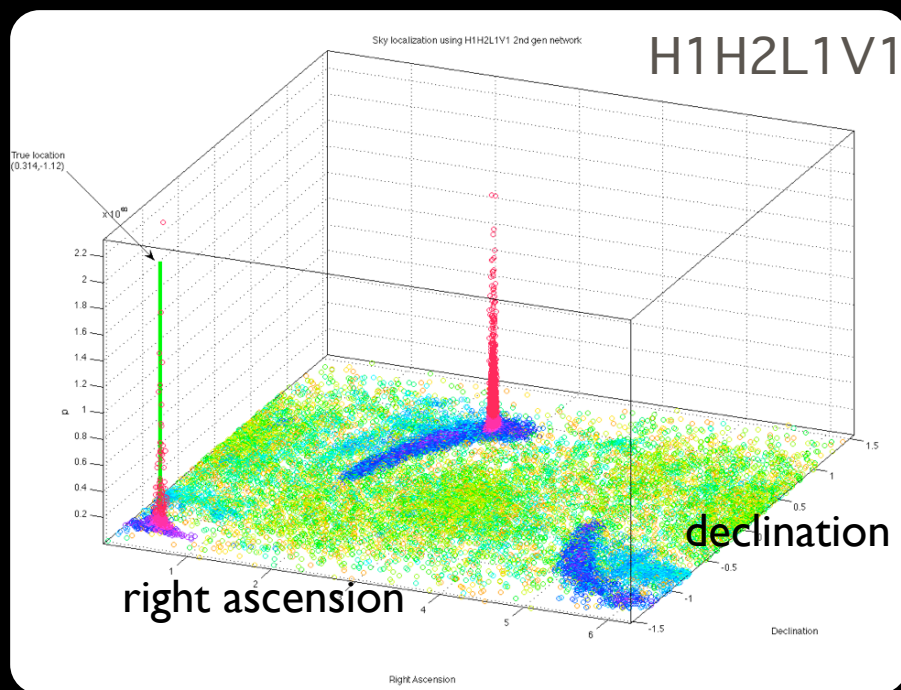


# (One of the) benefits of LIGO Australia



Current network

Current network  
+  
instrument in Australia



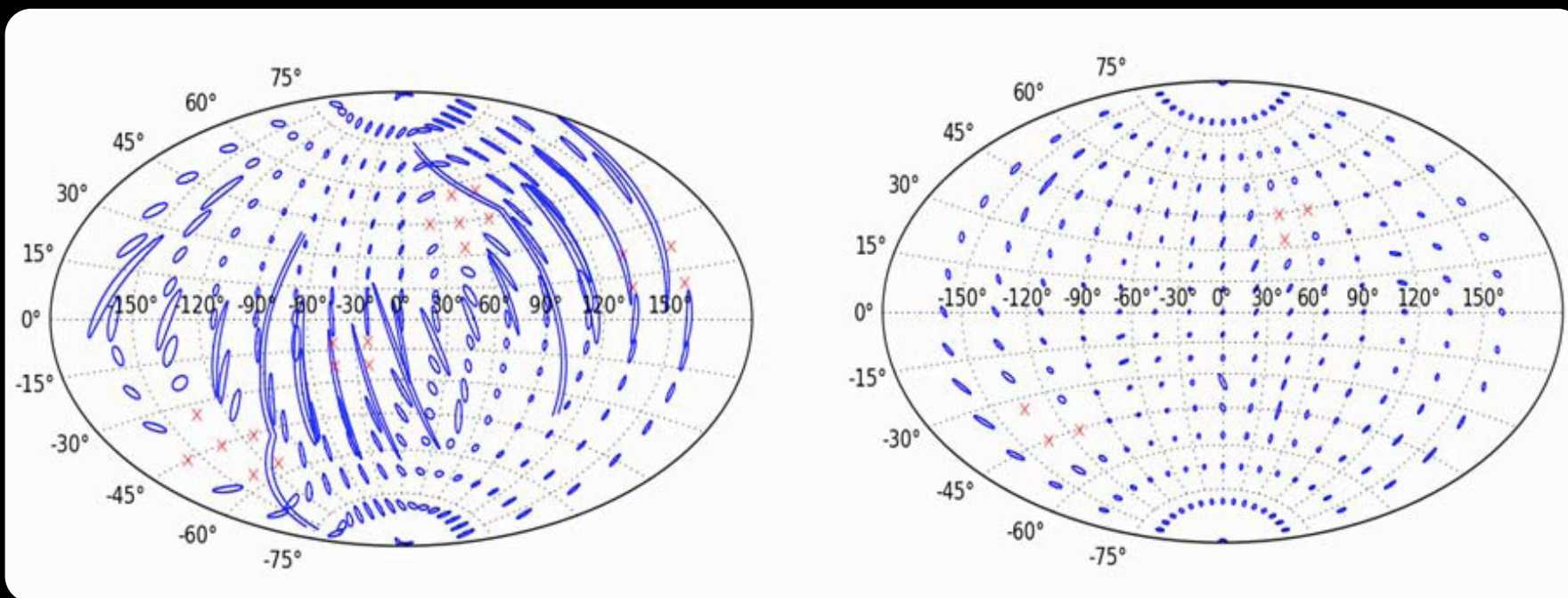




# Sky resolution

Current network

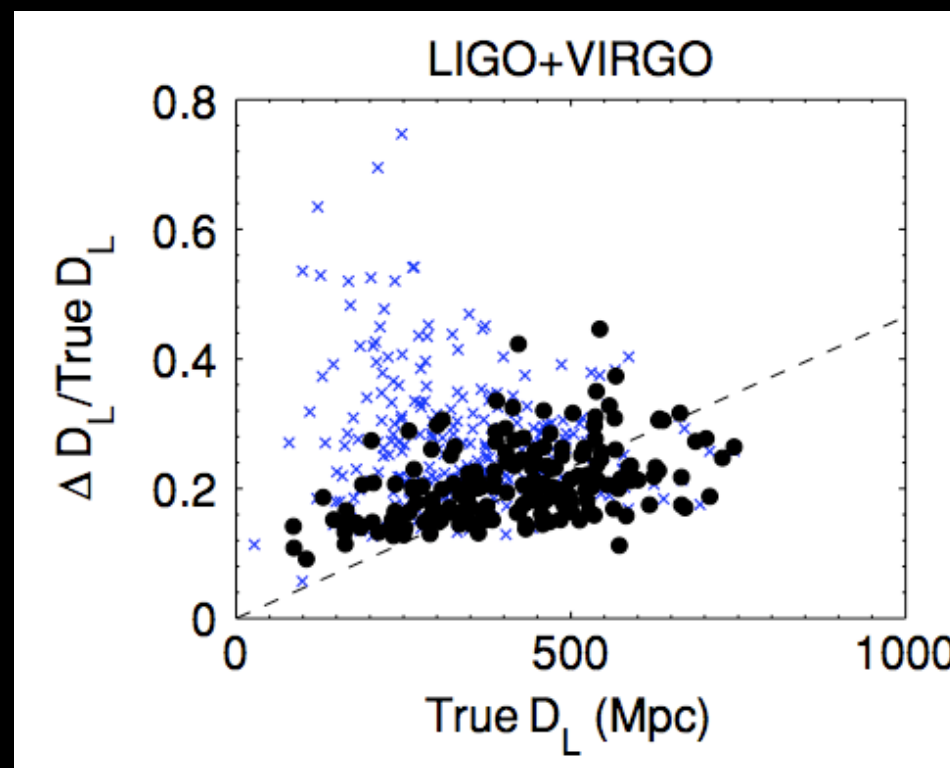
Current network  
+  
instrument in Australia





# Measuring cosmological parameters

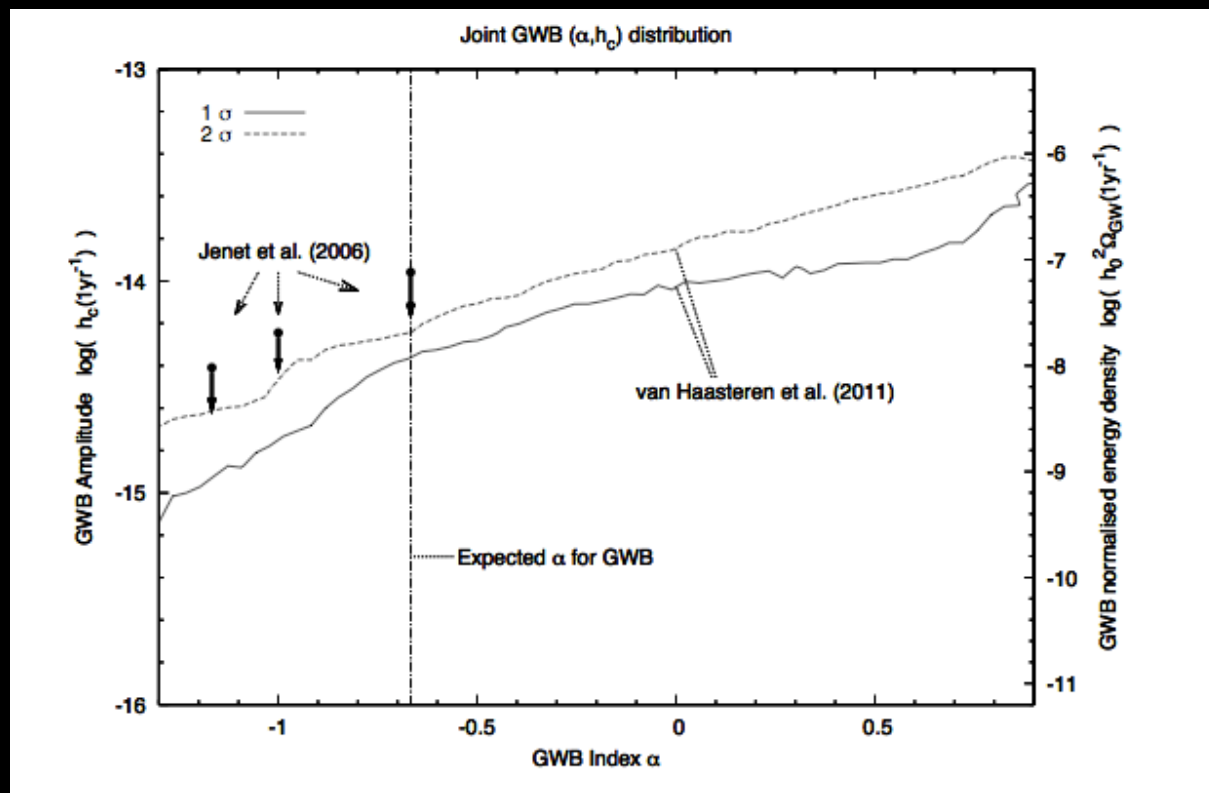
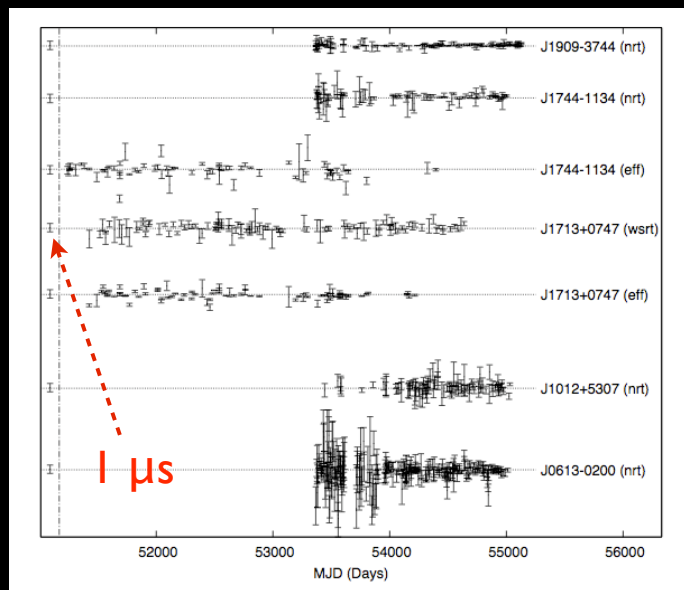
- “Poor” angular resolution may prevent optical identification (i.e. redshift)
- Degeneracies in parameter space may limit accuracy in distance measurements
- Weak lensing may be the ultimate limitation if there is a small number of detections
- Many papers (Hughes, Holz & Co), the issue is not settled



Nissanke et al, 2010



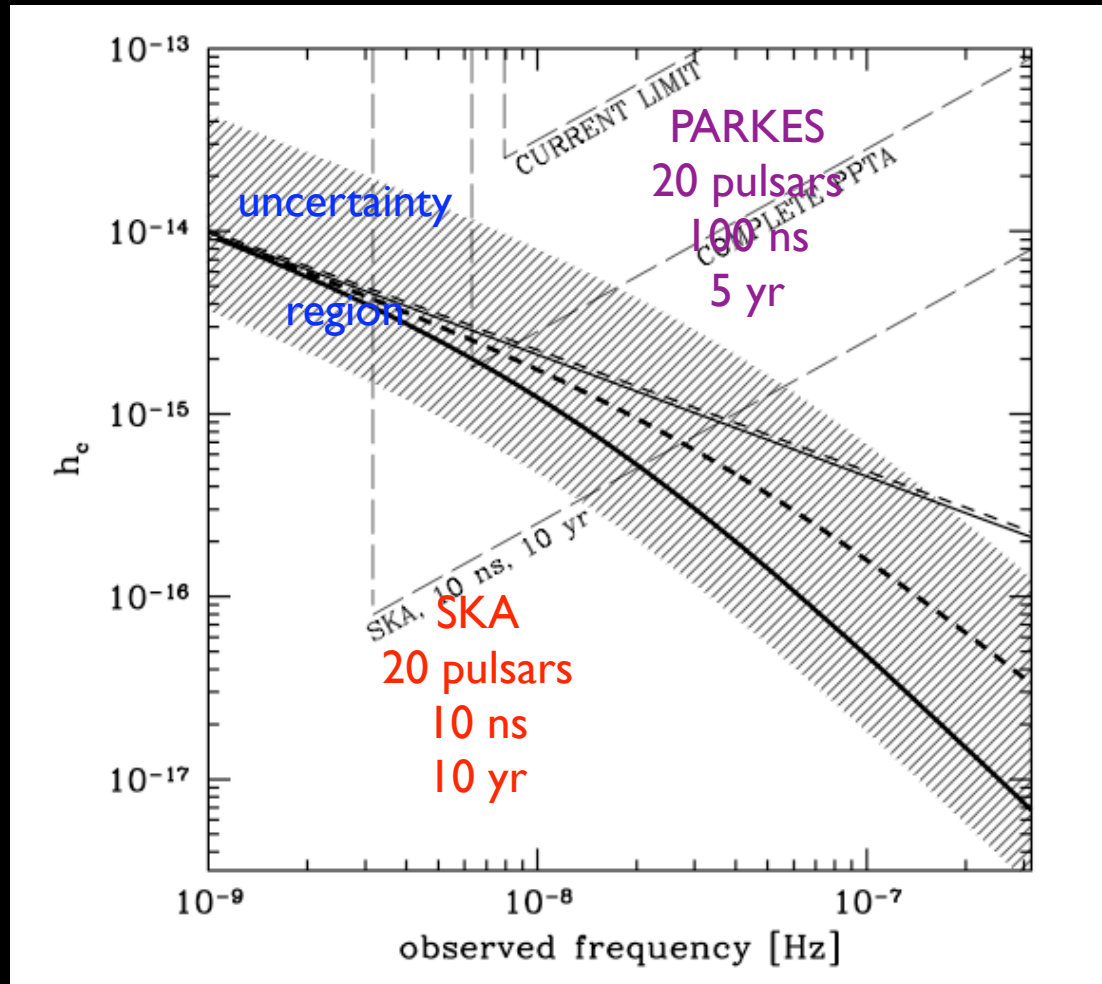
# New upper-limit from EPTA



van Haasteren et al (EPTA), 2010 submitted

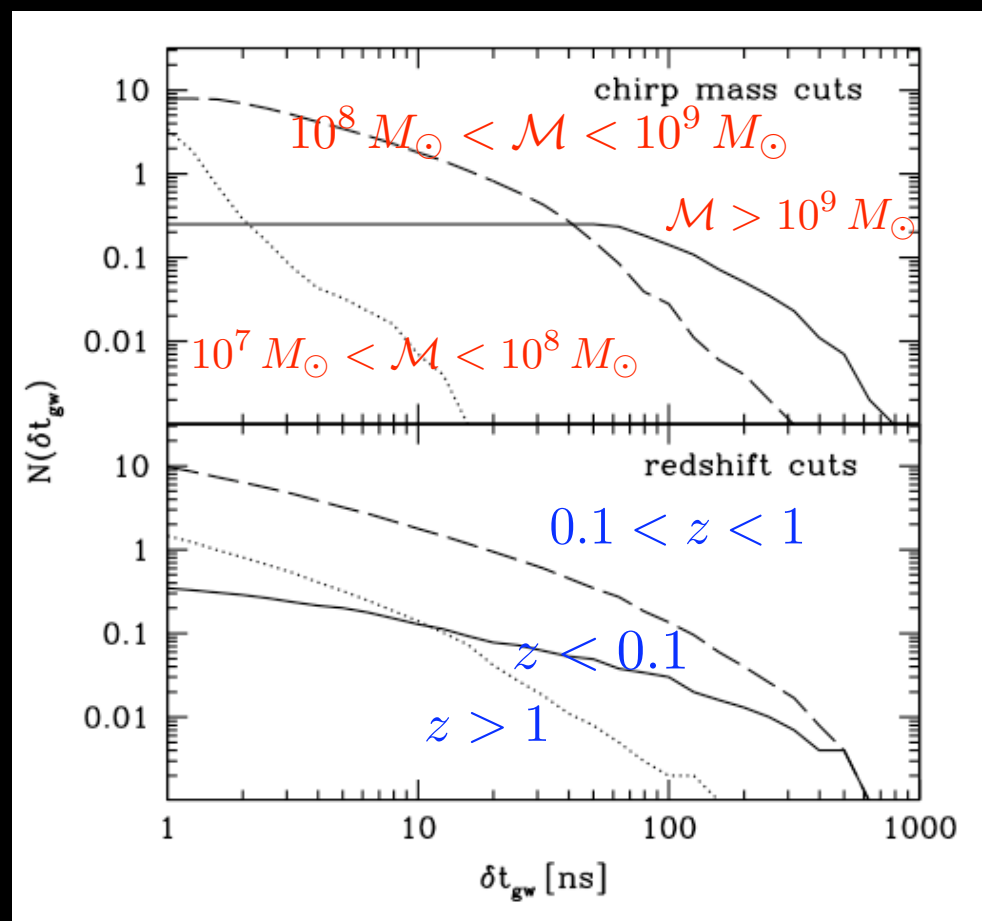


# Observing the foreground from SMBH binaries





# Resolving SMBH binaries

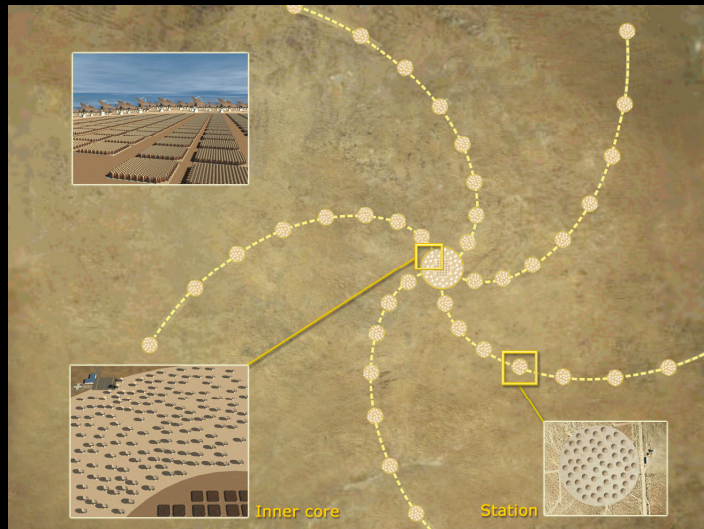


Sesana, AV and Volonteri (2009)

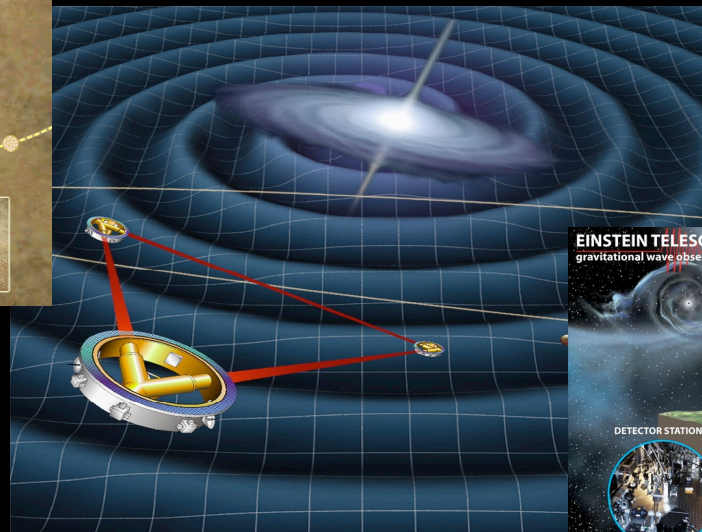


# 2020 - 2030+

## Square Kilometre Array (SKA)



## Laser Interferometer Space Antenna (LISA)



## Einstein gravitational-wave Telescope (ET)



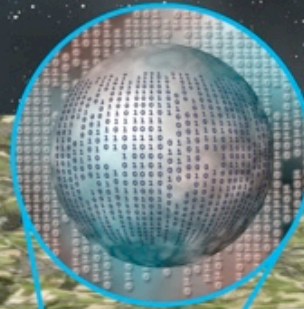
# EINSTEIN TELESCOPE

gravitational wave observatory

CENTRAL FACILITY



COMPUTING CENTRE



DETECTOR STATION



END STATION



Length ~10 km



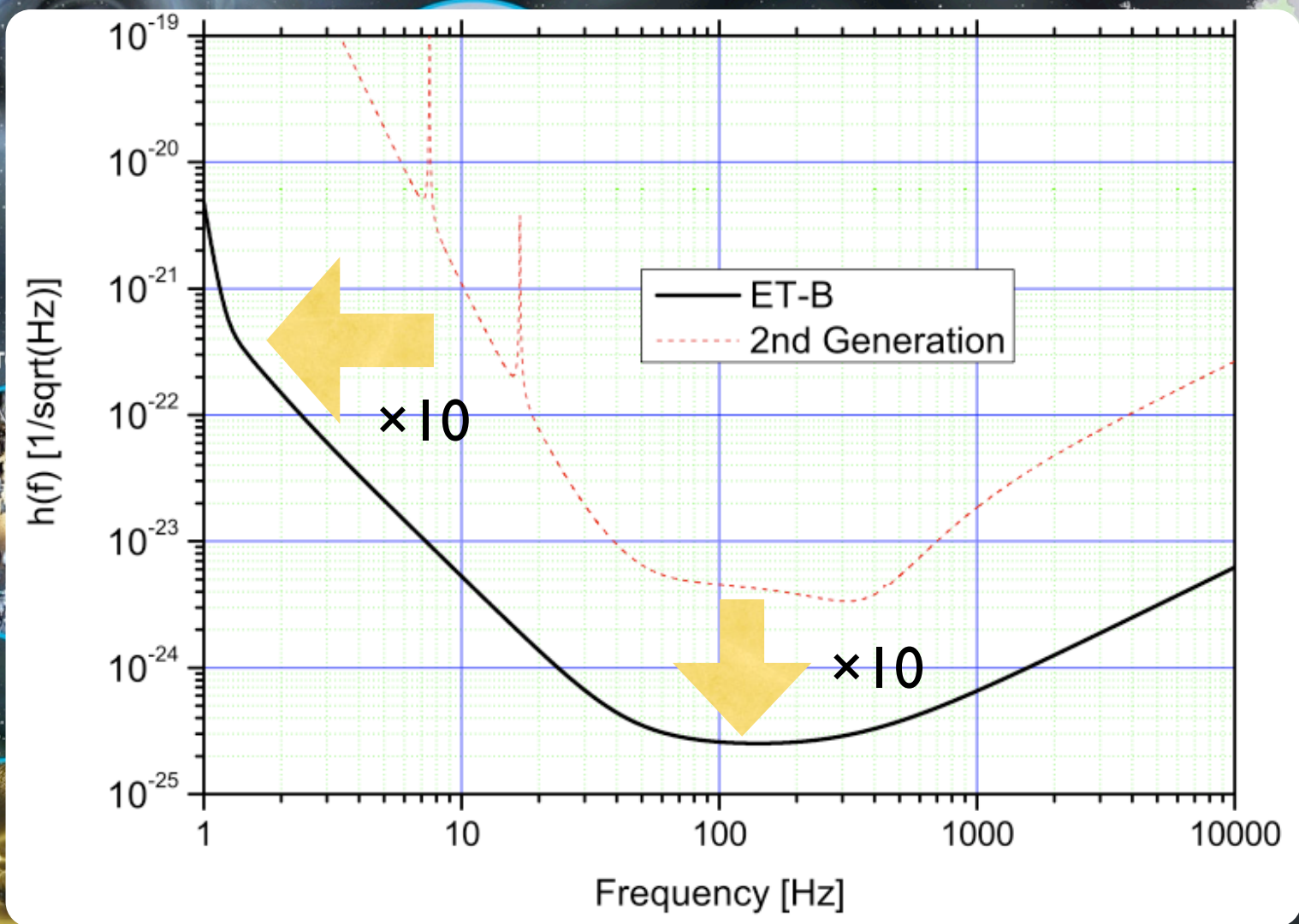
TUNNEL  $\varnothing$  ~5 m

# EINSTEIN TELESCOPE

gravitational wave observatory



CENTRAL FACILITY



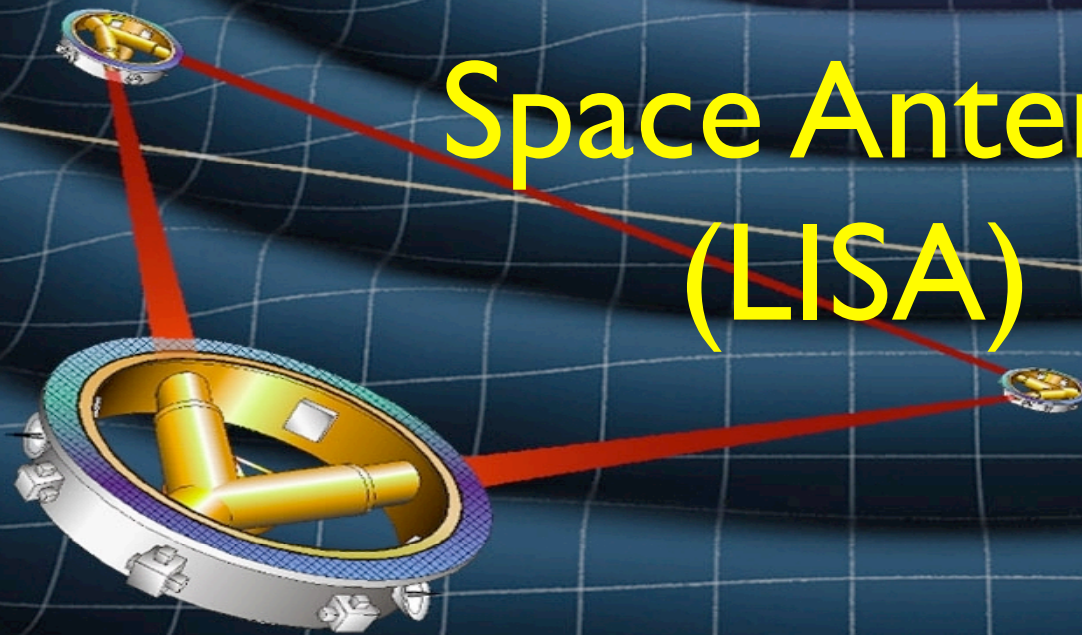
DETECT

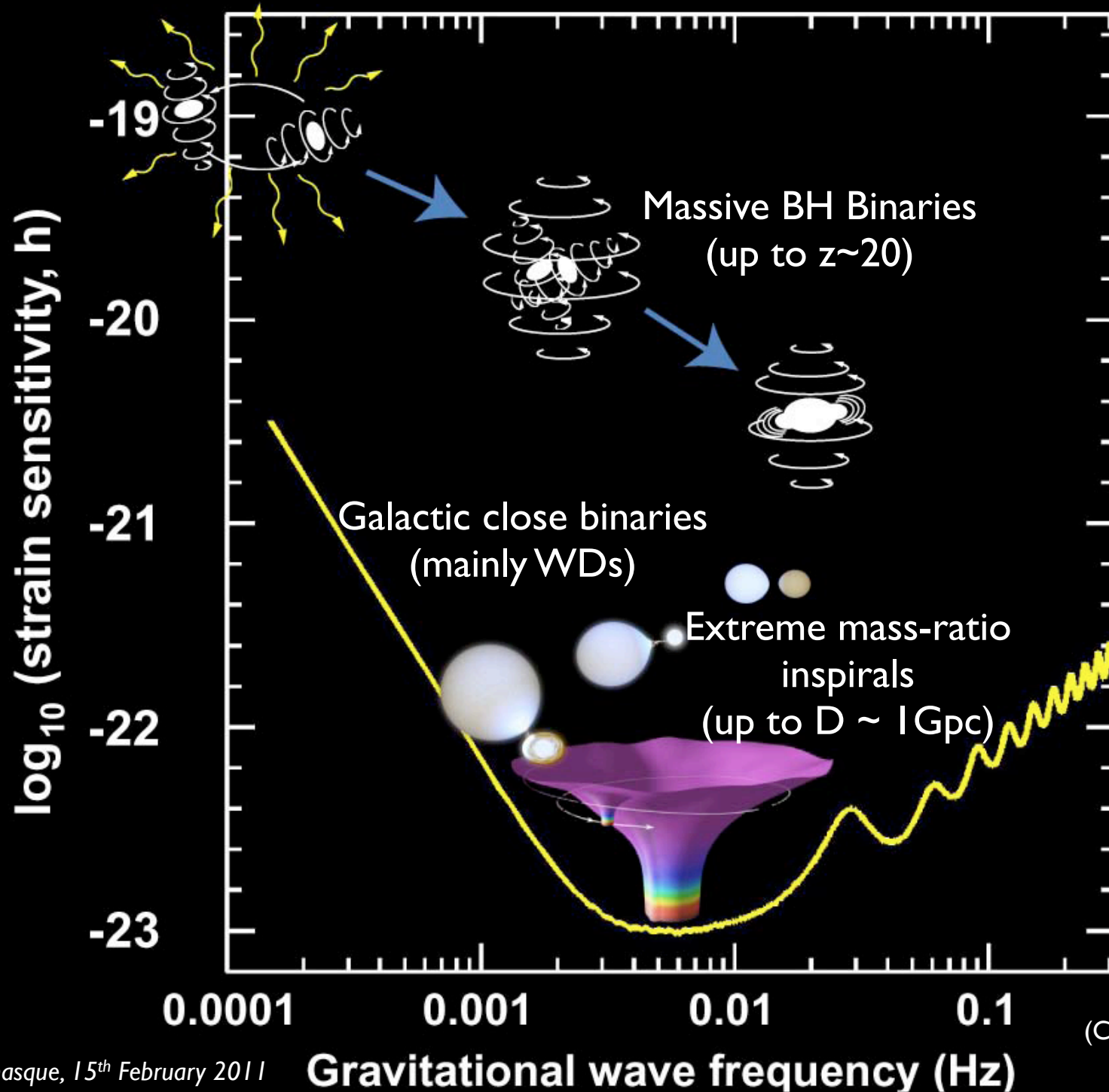
END STATION





# Laser Interferometer Space Antenna (LISA)

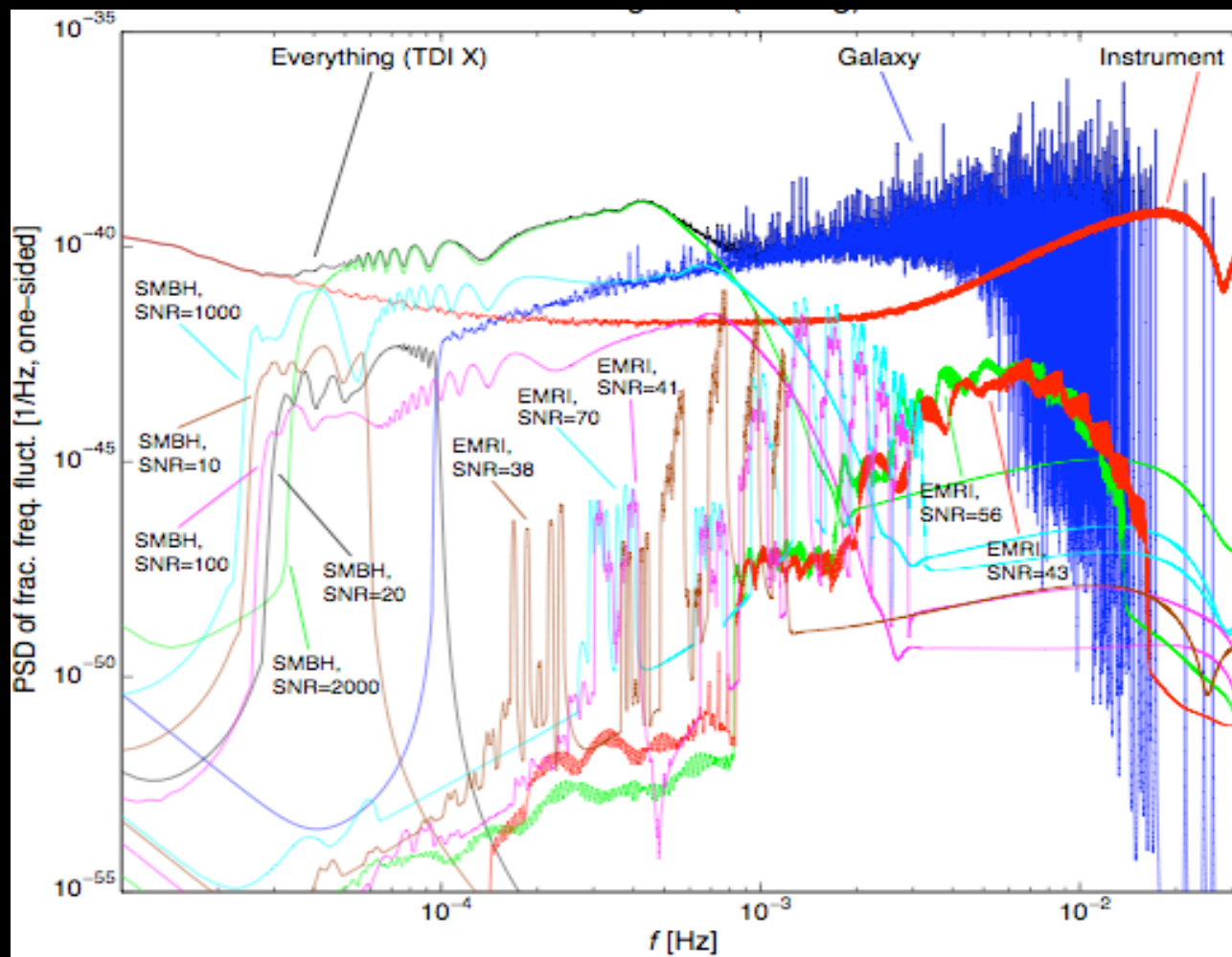




(Courtesy S. Phinney)



# The embarrassment of richness



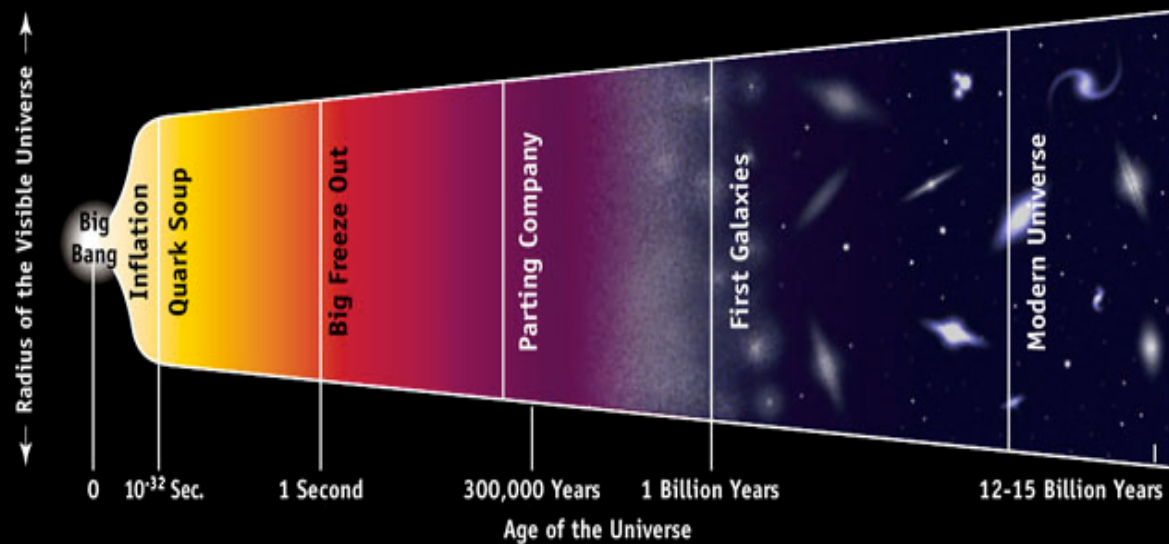
(Courtesy M.Vallisneri)



4. Any chance of *directly* observing relic gravitons?  
(possibly all the way back to an inflationary epoch)

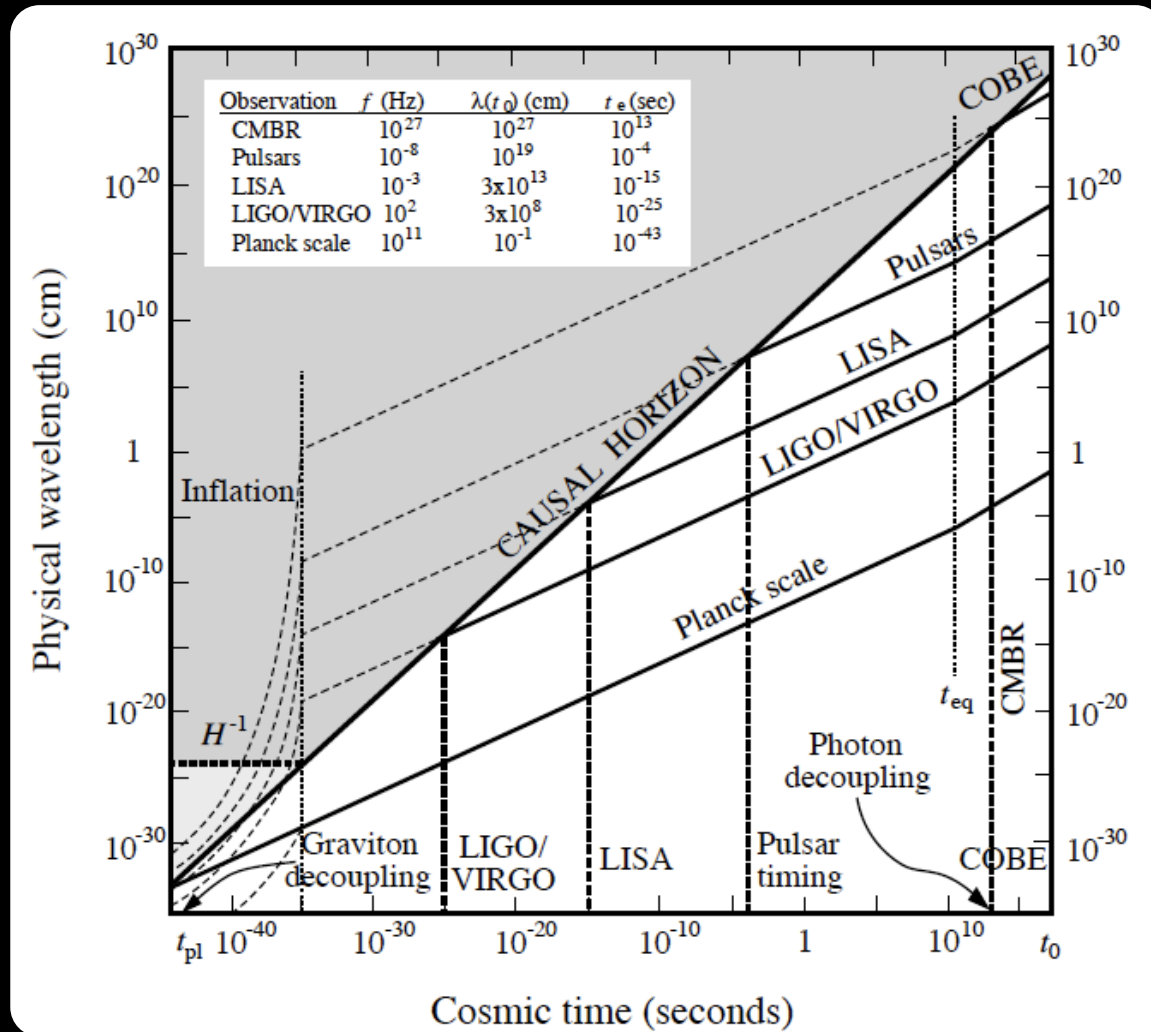


# GW stochastic backgrounds





# GWs and the early universe



(Battye and Shellard, arXiv:9604059)



# Stochastic backgrounds

Spectrum:

$$\Omega_{\text{gw}}(f) = \frac{1}{\rho_c} \frac{d\rho_{\text{gw}}(f)}{d \ln f}$$

Amplitude:

$$S^{1/2}(f) = 5.6 \times 10^{-22} [h_{100}^2 \Omega_{\text{gw}}(f)]^{1/2} \left( \frac{f}{100 \text{ Hz}} \right)^{-3/2} \text{ Hz}^{-1/2}$$



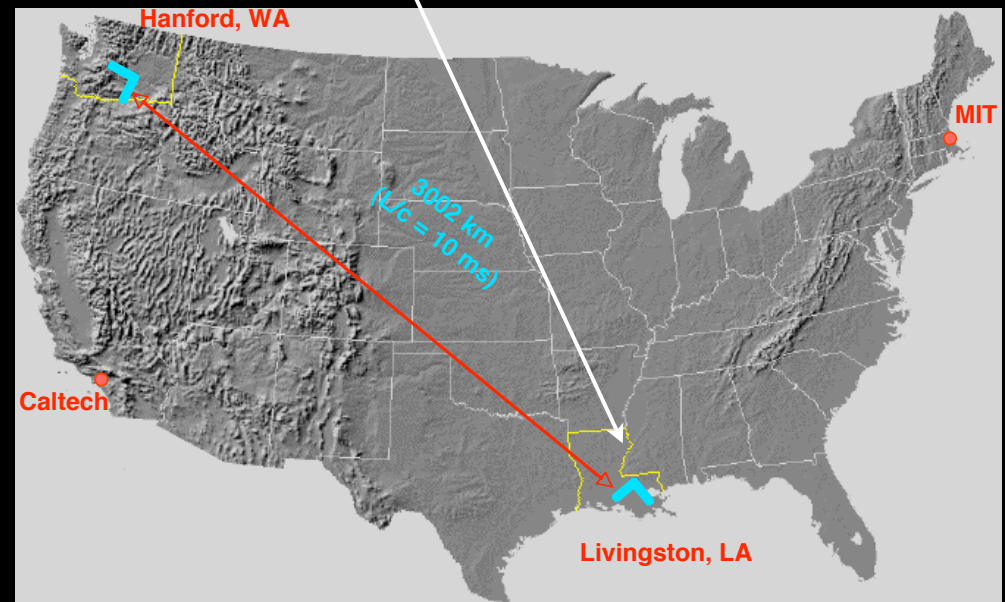
# Search approach

- Cross-correlation between outputs from pairs of instruments

$$\langle \tilde{s}_1^*(f) \tilde{s}_2(f) \rangle = \gamma(f) S_{\text{gw}}(f)$$

- The geometry enters via the overlap reduction function that depends on orientation and separation of the instruments

$$s_1 = n_1 + h_1$$
$$s_2 = n_2 + h_2$$

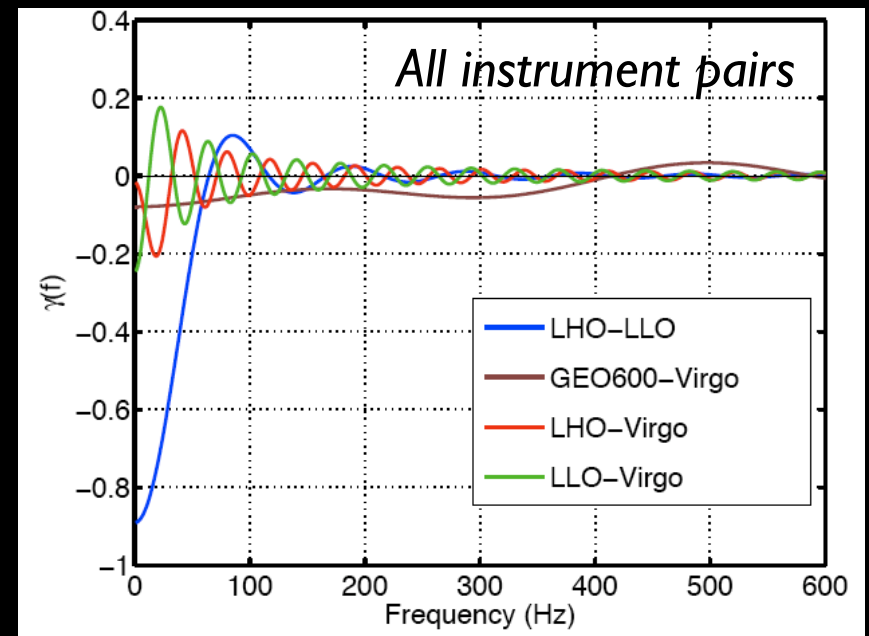
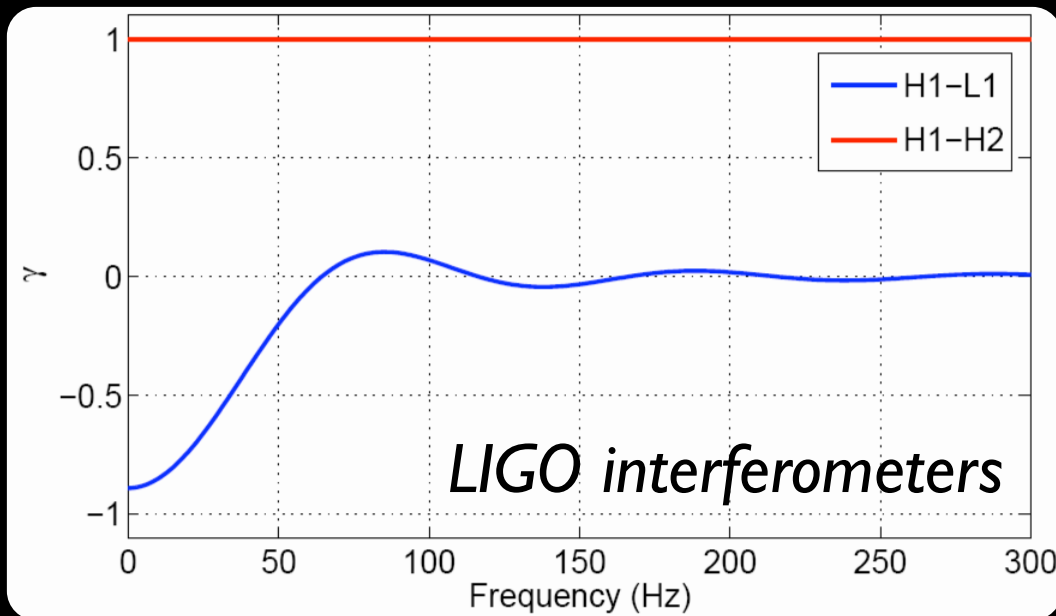






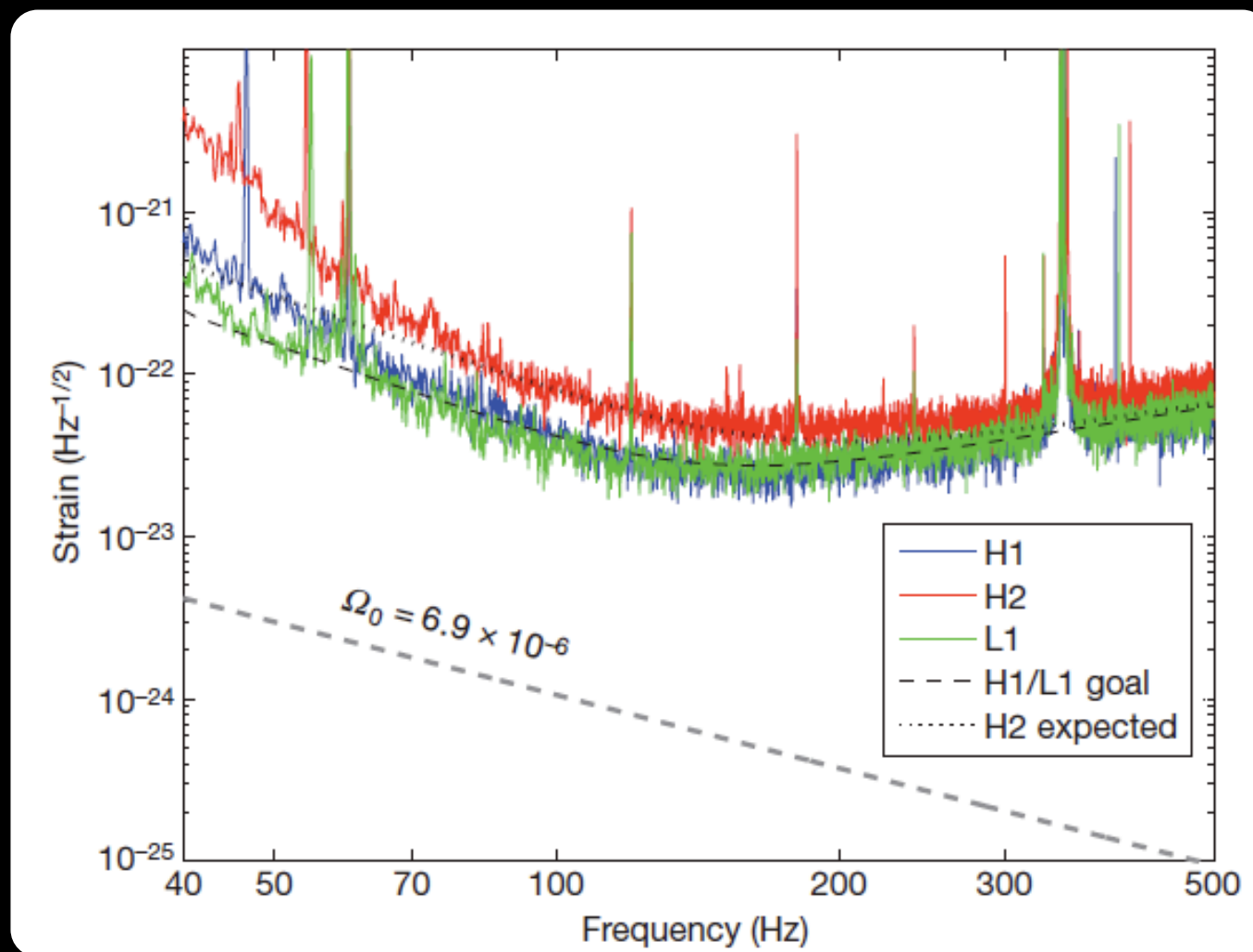
# Geometry: overlap reduction function

$$\gamma(f) \equiv \frac{5}{8\pi} \sum_{A=+, \times} \int_{S^2} d\hat{n} e^{i2\pi f \hat{n} \cdot \Delta \vec{x} / c} F_1^A(\hat{n}) F_2^A(\hat{n})$$
$$F^A(\hat{n}) \equiv \frac{1}{2} e_{ab}^A(\hat{n}) \begin{bmatrix} \hat{l}_1^a \hat{l}_1^b & \\ & -\hat{l}_2^a \hat{l}_2^b \end{bmatrix}$$



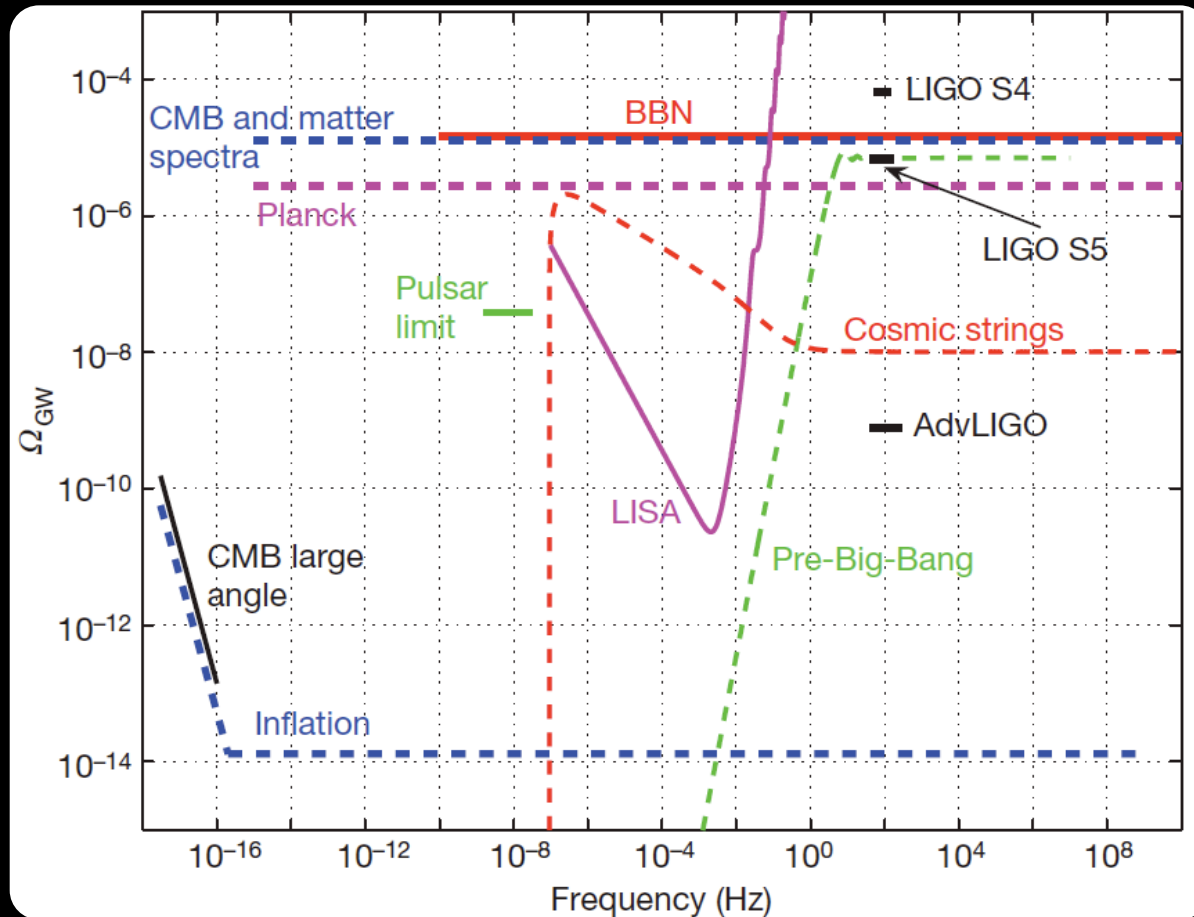


# S5 LIGO sensitivity





# LIGO upper-limit vs nucleosynthesis bound



## Upper-limit

$$41.5\text{Hz} \leq f \leq 161.25\text{Hz}$$

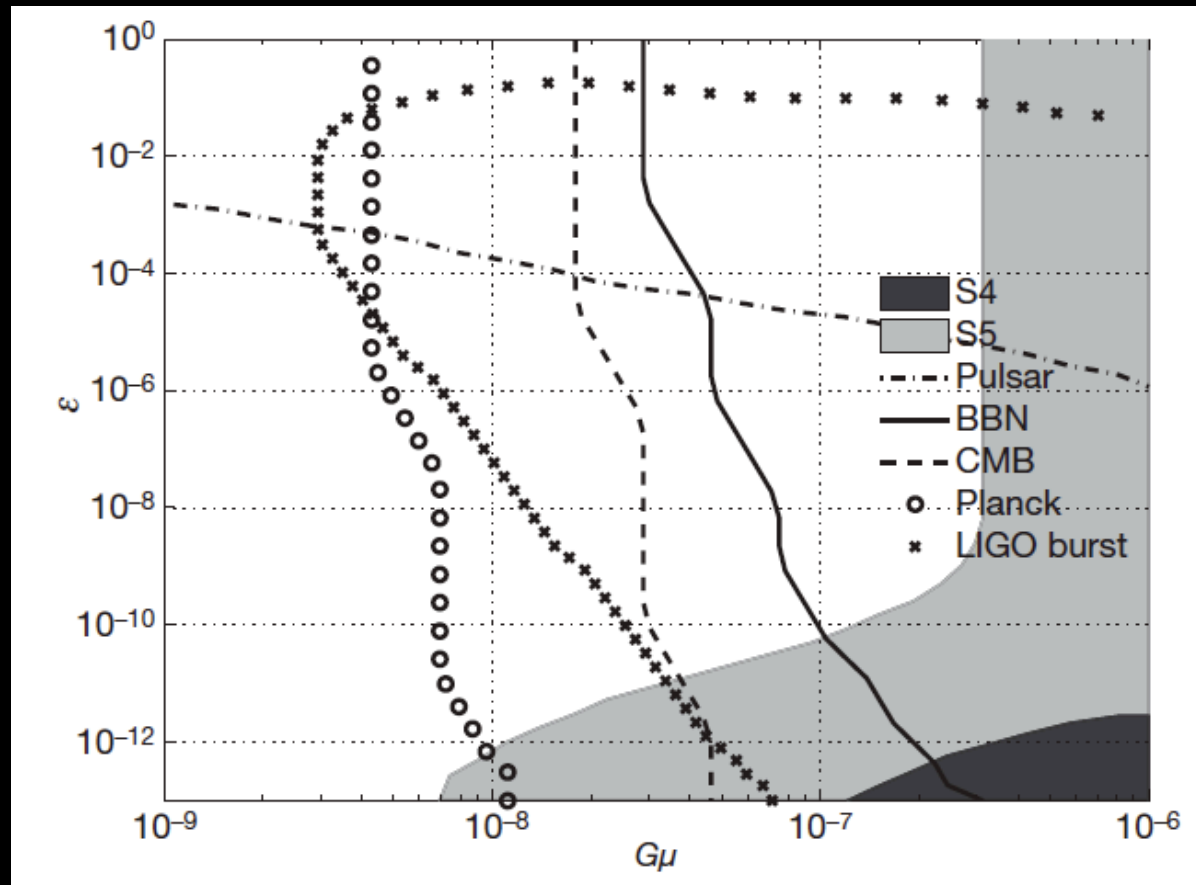
$$\Omega_{\text{GW}}(f) = \Omega_0$$

$$\Omega_0^{95\%} = 6.9 \times 10^{-6}$$

Abbott et al (LSC & Virgo Collaboration),  
Nature **460**, 990 (2009)



# Constraining e.g. string models

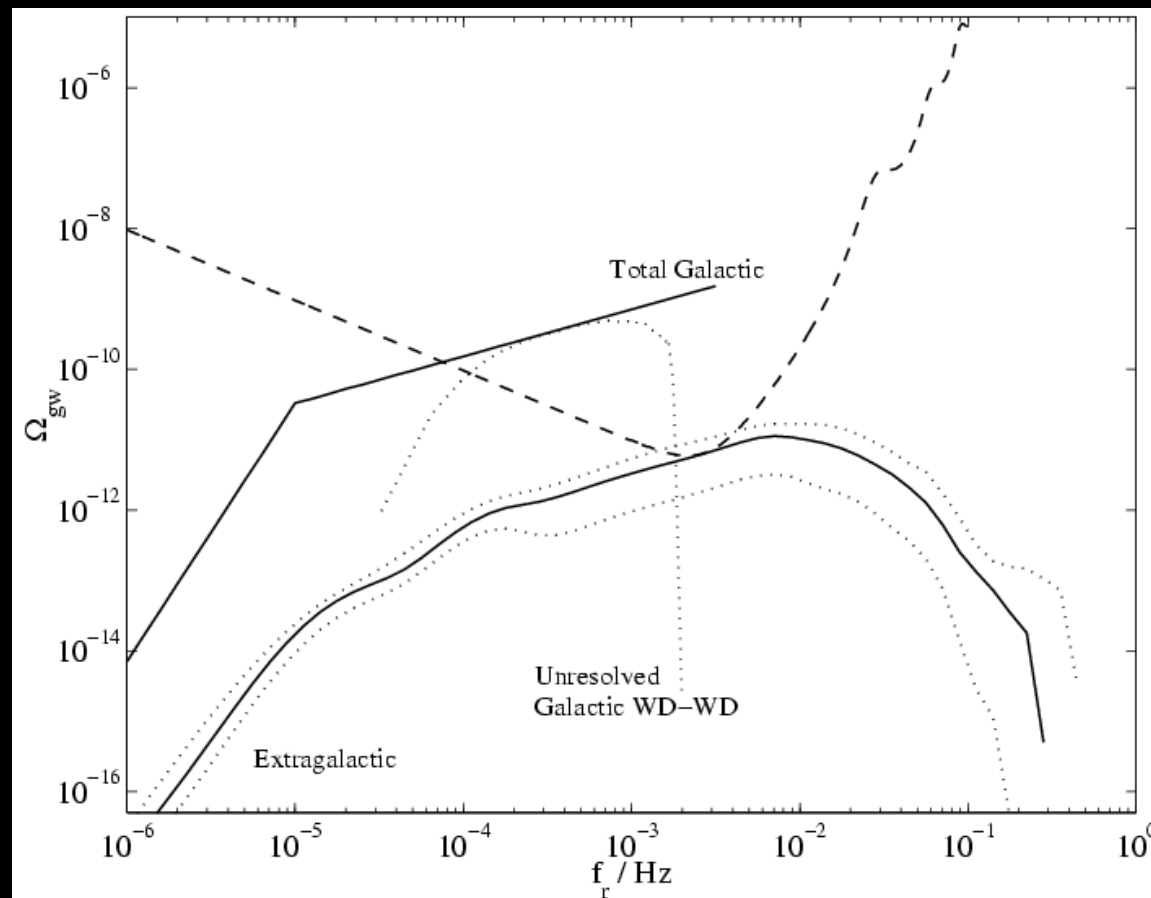


Abbott et al, Nature **460**, 990 (2009)



# Foregrounds

$$S^{1/2}(f) = 5.6 \times 10^{-22} [h_{100}^2 \Omega_{\text{gw}}(f)]^{1/2} \left( \frac{f}{100 \text{ Hz}} \right)^{-3/2} \text{ Hz}^{-1/2}$$



Farmer and Phinney, 2003

# The Big Bang Observer:

Direct detection of gravitational waves from the birth of the Universe  
to the present

**P.I.:** E. S. Phinney

**US Co-Is:** Peter Bender, Saps Buchman, Robert Byer, Neil Cornish, Peter Fritschel, William Folkner, Stephen Merkowitz

**Foreign Co-P/Is:** Karsten Danzmann, Luciano DiFiore, Seiji Kawamura, Bernard Schutz, Alberto Vecchio, Stefano Vitale

**Collaborators:** John Armstrong, Fabrizio Barone, Charles Bennett, Jordan Camp, Joan Centrella, David Chernoff, Adrian Cruise, Curt Cutler, Frank Estabrook, Jens Gundlach, Gerhard Heinzl, Ronald Hellings, Craig Hogan, James Hough, Scott Hughes, Andrew Jaffe, Barry Kent, William Kinney, Alberto Lobo, Nergis Mavalvala, Thomas Prince, Michael Sandford, Bangalore Sathyaprakash, David Shoemaker, Steinn Sigurdsson, Clive Speake, David Spergel, Robin Stebbins, Timothy Sumner, Kip Thorne, Massimo Tinto, Carlo Ungarelli, Henry Ward.

NASA OSS Vision Missions Program, Proposal VM03-0021-0021

## I. Introduction: Primary and Secondary Science Objectives

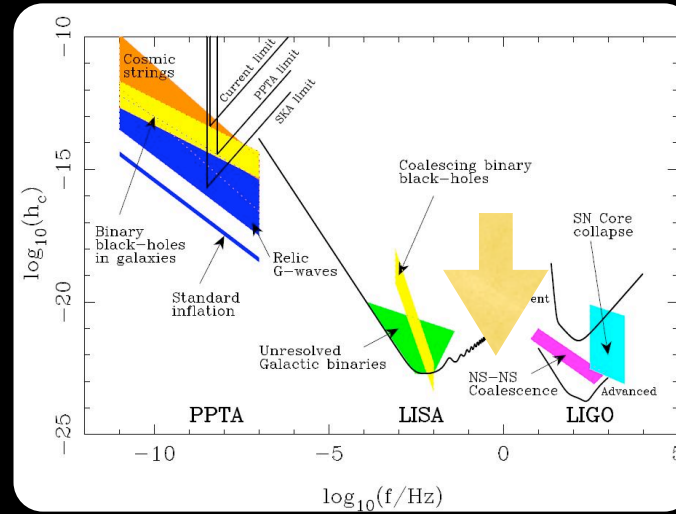
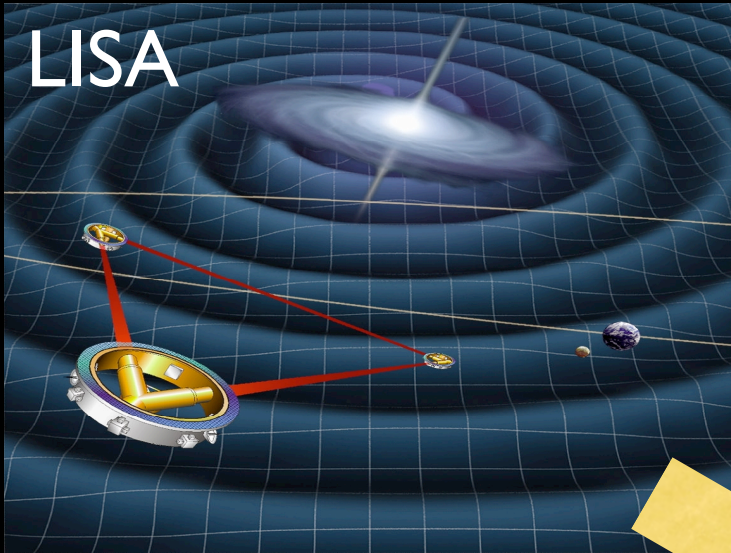
NASA's 2002 SEU Roadmap *Beyond Einstein* highlights three major unanswered questions raised by Einstein's general theory of relativity:

1. *What powered the Big Bang?*
2. *What happens to space, time and matter at the edge of a black hole?*
3. *What is the mysterious dark energy pulling the Universe apart?*

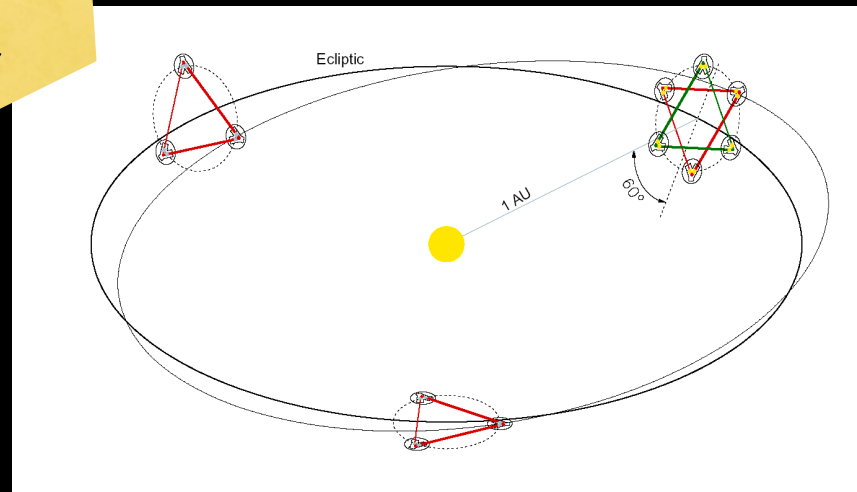
The prime scientific objective of the Big Bang Observer (BBO) mission is the direct detection of relic gravitational waves from inflation. When combined with cosmic microwave background inferences about gravitational waves 17 orders of magnitude lower in frequency,



# Big Bang Observer & DECIGO



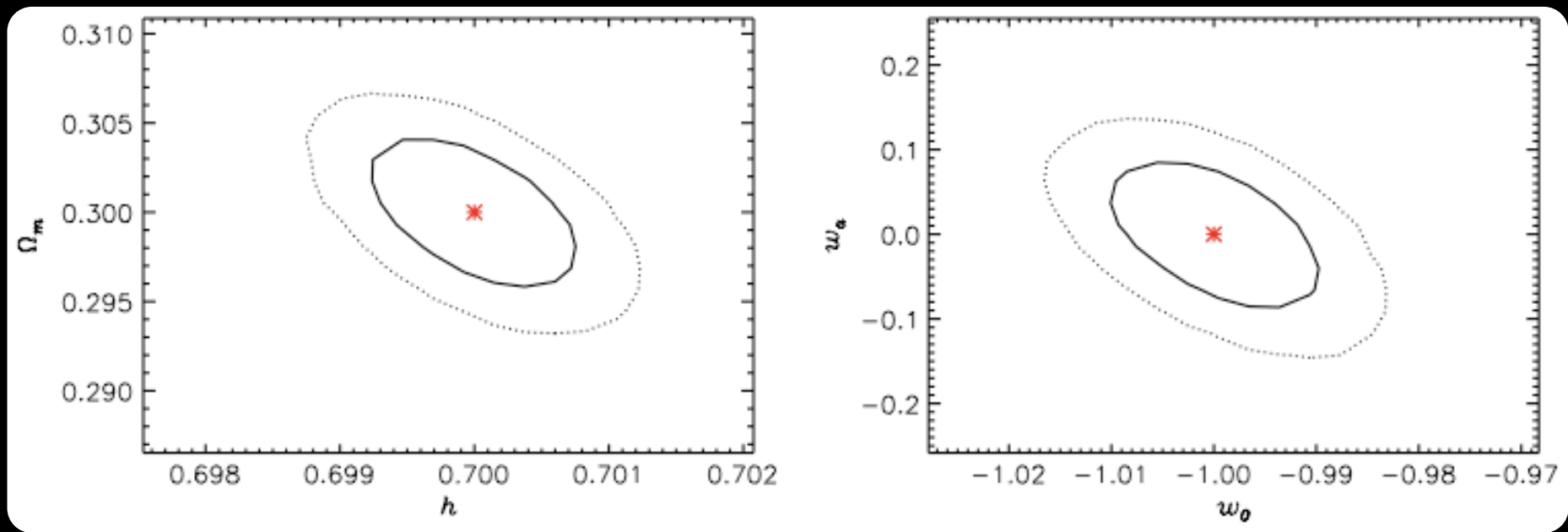
## BBO/DECIGO



- arm-length shorter by  $\sim \times 100$
- peak sensitivity  $\sim 0.1$ - $1$  Hz



# The ultimate dark energy mission?



Cutler and Holz 2009





# To summarise

1. No *direct* detection (yet)
2. Prospects for detecting soon-ish (both from ground and with pulsar timing arrays)?
3. High precision astronomy and cosmography?
4. Is it on the cards to detect gravitational waves emitted by processes in the early universe?