

# EXTRACTING OSCILLATION PARAMETERS FROM NEUTRINO DATA

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# Outline of the course

Introduction

Lecture I: Solar Neutrinos ( $\theta_{12}$ ,  $\Delta m^2_{12}$ )

Lecture II: Atmospheric Neutrinos ( $\theta_{23}$ ,  $\Delta m^2_{23}$ )

Lecture III: Bounds on  $\theta_{13}$  and  $\delta$ ; sterile neutrinos

Lecture IV: Future facilities

FUTURE FACILITIES  
AND THE QUEST  
FOR  $\delta$

# Outline

- Correlations and degeneracies
- Super-Beams
- Neutrino Factory
- Beta-Beams

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- Super-Beams
- Neutrino Factory
- Beta-Beams

I am not covering reactors, although they can be important (see Lecture3).

# The PMNS matrix

The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) mixing matrix is the **leptonic analogous** of the **CKM matrix**

“Atmospheric”  
oscillation

“Solar”  
oscillation

$$U_{PMNS} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_1} & 0 \\ 0 & 0 & e^{i\alpha_2} \end{pmatrix}$$

$$\theta_{23} = 39^\circ - 48^\circ$$

$$\theta_{13} < 11^\circ$$

$$\theta_{12} = 32^\circ - 35^\circ$$

Majorana  
phases

Gonzalez-García and Maltoni '07

# The PMNS matrix

Solar  
parameters:

$$\Delta m_{21}^2 = 7.67^{+0.22}_{-0.21} \begin{pmatrix} +0.67 \\ -0.61 \end{pmatrix} \times 10^{-5} \text{ eV}^2$$

$$\theta_{12} = 34.5 \pm 1.4 \begin{pmatrix} +4.8 \\ -4.0 \end{pmatrix}$$

Atmospheric  
parameters:

$$\Delta m_{31}^2 = \begin{cases} -2.37 \pm 0.15 \begin{pmatrix} +0.43 \\ -0.46 \end{pmatrix} \times 10^{-3} \text{ eV}^2 & \text{(inverted hierarchy),} \\ +2.46 \pm 0.15 \begin{pmatrix} +0.47 \\ -0.42 \end{pmatrix} \times 10^{-3} \text{ eV}^2 & \text{(normal hierarchy),} \end{cases}$$

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Gonzalez-García and Maltoni '08

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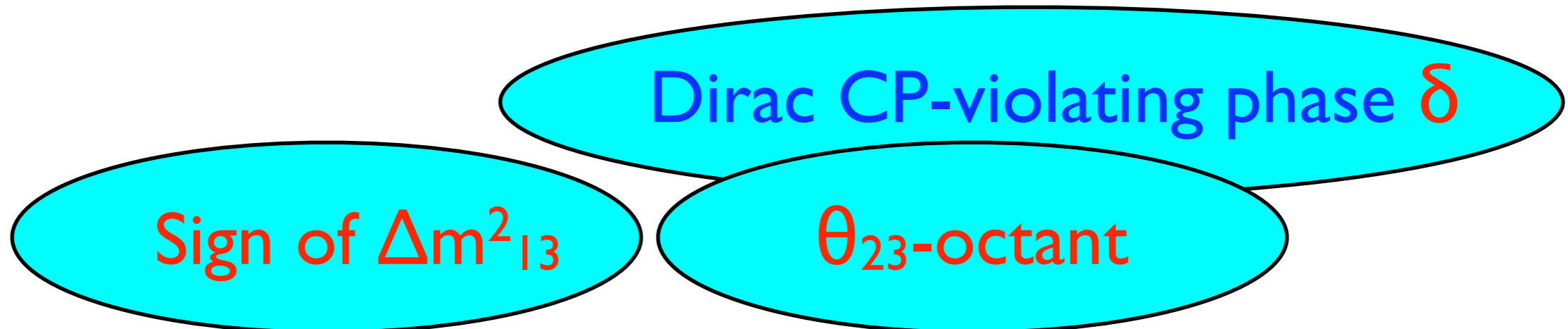
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Unknown parameters (maybe less, by the time of NF):

$$\theta_{13} < 11.5^\circ$$

Dirac CP-violating phase  $\delta$

Sign of  $\Delta m_{13}^2$

$\theta_{23}$ -octant

# CORRELATIONS AND DEGENERACIES

# The Golden Channel

$$P_{e\mu}^{\pm} = X_{\mu}^{\pm} \sin^2 2\theta_{13} + (Y_c^{\pm} \cos\delta \mp Y_s^{\pm} \sin\delta) \sin 2\theta_{13} + Z_{\mu}$$

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$$\left\{ \begin{array}{l} X_{\pm} = \boxed{\sin^2 \theta_{23}} \left( \frac{\Delta_{23}}{\tilde{B}_{\mp}} \right)^2 \sin^2 \left( \frac{\tilde{B}_{\mp} L}{2} \right) \\ Y_{\pm}^c = \boxed{\sin 2\theta_{23}} \sin 2\theta_{12} \frac{\Delta_{12}}{A} \frac{\Delta_{23}}{\tilde{B}_{\mp}} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\tilde{B}_{\mp} L}{2} \right) \boxed{\cos \left( \frac{\Delta_{23} L}{2} \right)} \\ Y_{\pm}^s = \boxed{\sin 2\theta_{23}} \sin 2\theta_{12} \frac{\Delta_{12}}{A} \frac{\Delta_{23}}{\tilde{B}_{\mp}} \sin \left( \frac{AL}{2} \right) \sin \left( \frac{\tilde{B}_{\mp} L}{2} \right) \boxed{\sin \left( \frac{\Delta_{23} L}{2} \right)} \\ Z = \boxed{\cos^2 \theta_{23}} \sin^2 2\theta_{12} \left( \frac{\Delta_{12}}{A} \right)^2 \sin^2 \left( \frac{AL}{2} \right) \end{array} \right.$$

where  $\Delta_{ij} = \Delta m_{ij}^2 / 2E$ ,  $B_{\mp} = |A \mp \Delta_{23}|$  and  $A$  is the matter parameter.

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Strong sensitivity to  $\theta_{13}$

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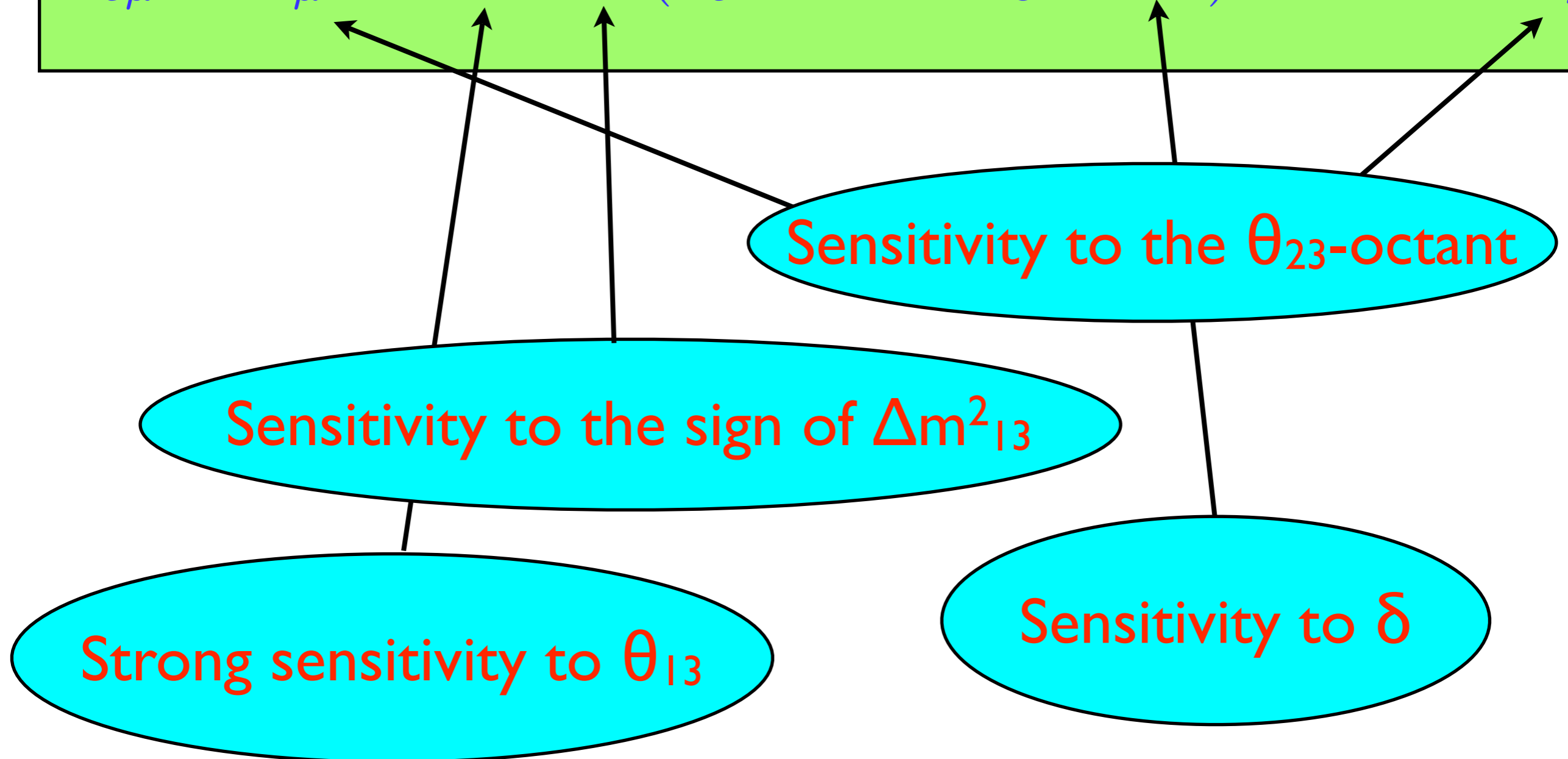
Sensitivity to the sign of  $\Delta m^2_{13}$

Strong sensitivity to  $\theta_{13}$

Sensitivity to  $\delta$

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The price to pay to be  
the “Golden Channel” is:  
**CORRELATIONS**  
and  
**DEGENERACIES**

Strong

$\delta$

octant

# The $(\theta_{13}, \delta)$ correlation

The signal is:

$$N_{\mu}(\bar{\theta}_{13}, \bar{\delta}) = \left\{ \epsilon_{\mu} \otimes \sigma_{\nu_{\mu}} \otimes P_{e\mu}^{+}(\bar{\theta}_{13}, \bar{\delta}) \otimes \Phi_{\nu_{\mu}} \right\}_E^{E+\Delta E}$$

$$N_{\pm}^i(\bar{\theta}_{13}, \bar{\delta}) = N_{\pm}^i(\theta_{13}, \delta)$$

By changing  $(\theta_{13}, \delta)$  accordingly,  
curves are drawn in the  $(\theta_{13}, \delta)$  plane.

# The $(\theta_{13}, \delta)$ correlation (2)

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$$N_{\pm}^i(\bar{\theta}_{13}, \bar{\delta}, \bar{s}_{atm}, \bar{s}_{oct}) = N_{\pm}^i(\theta_{13}, \delta, s_{atm}, s_{oct})$$

where

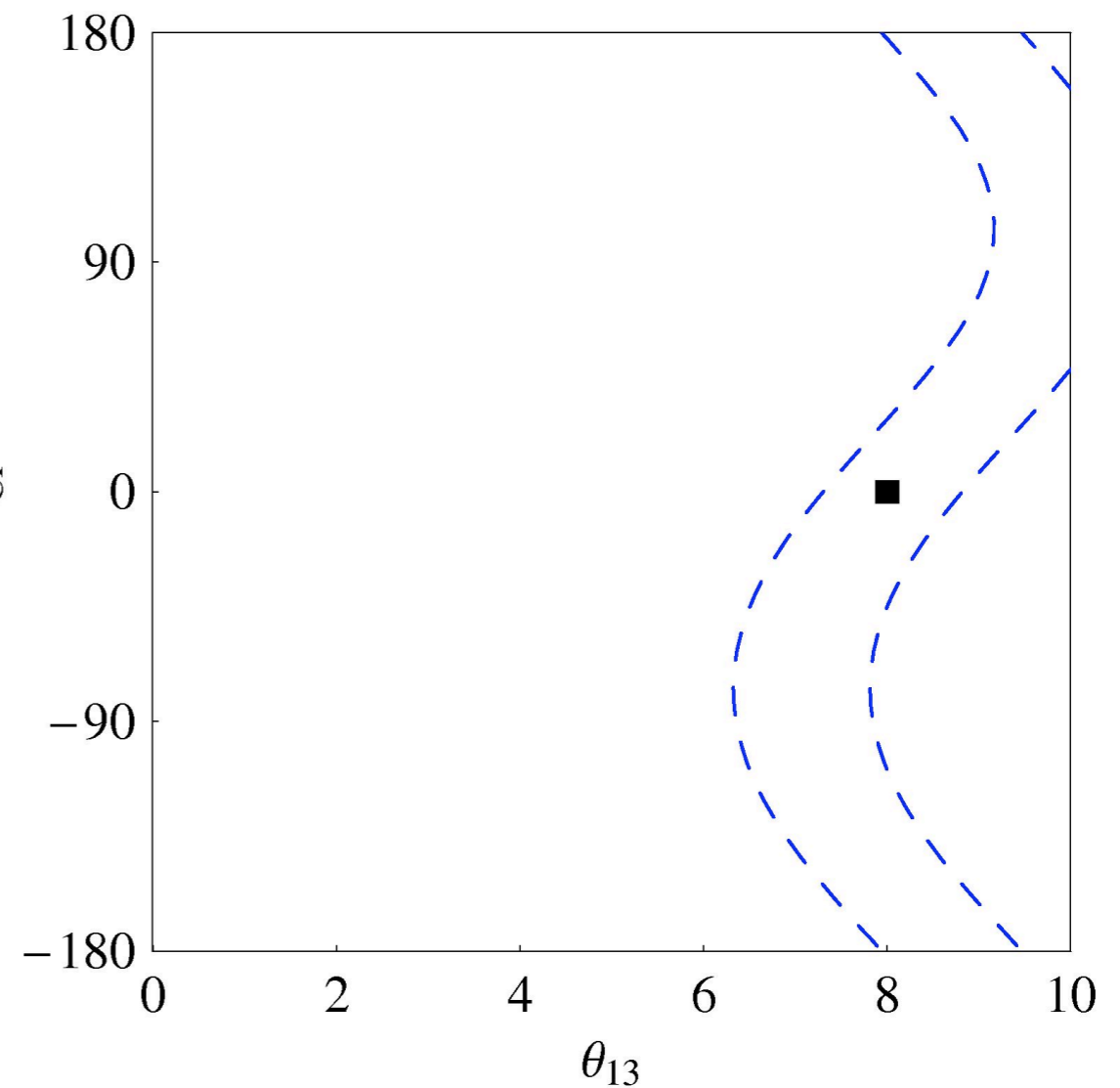
$$\begin{cases} s_{atm} & = \text{sign}(\Delta m_{atm}^2) = \pm 1 \\ s_{oct} & = \text{sign}(\tan 2\theta_{23}) = \pm 1 \end{cases}$$

# Correlations

- Black square = input “true” value
- There is a curve of solutions:  $\theta_{13}$ - $\delta$  correlation

Texto

$\delta_{CP}$



J. Burguet-Castell et al. hep-ph/0103258



# Correlations

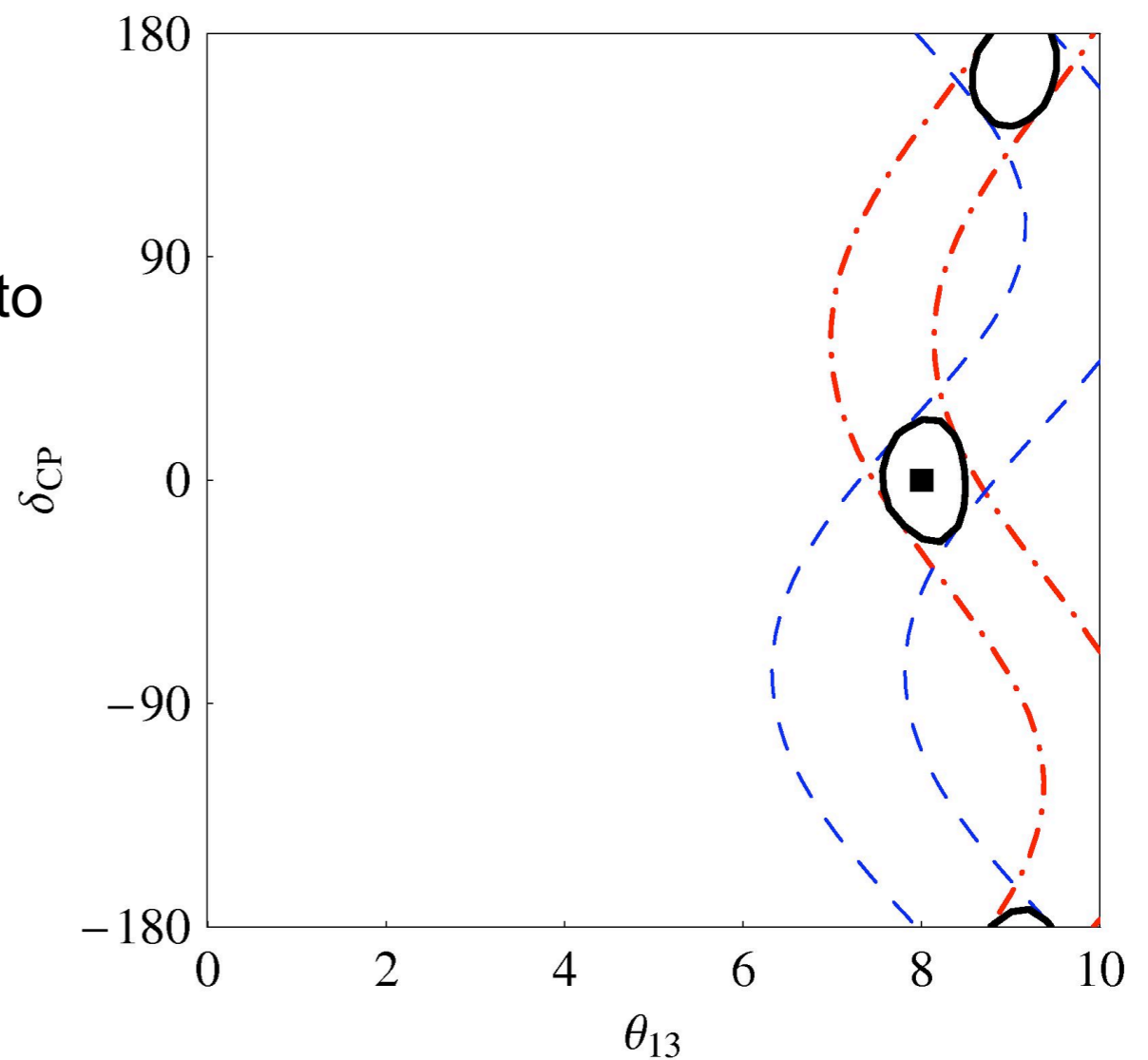
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- If we add antineutrinos the two curves intersect in 2 regions:

The true solution

and

an intrinsic degeneracy

Texto



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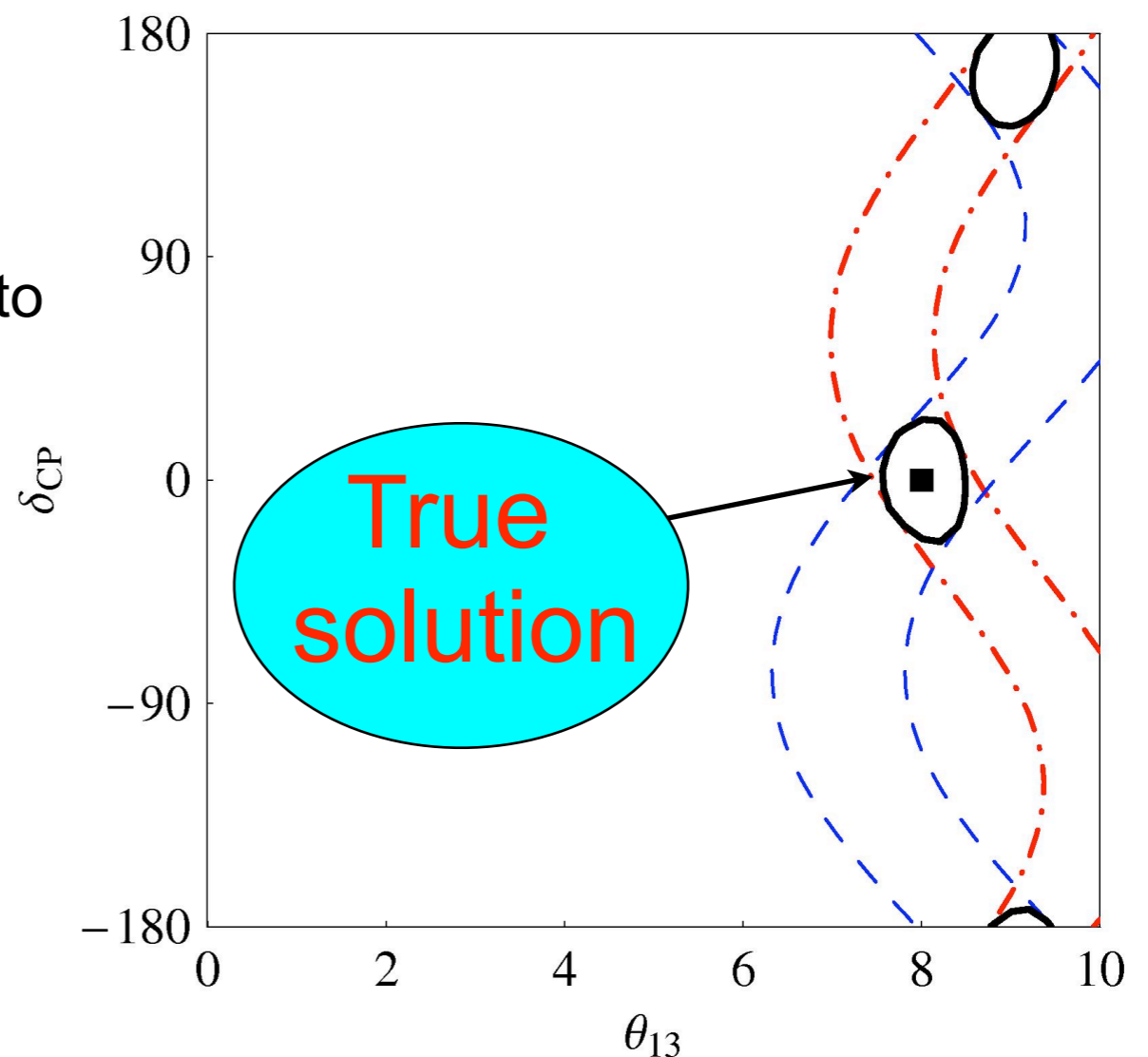
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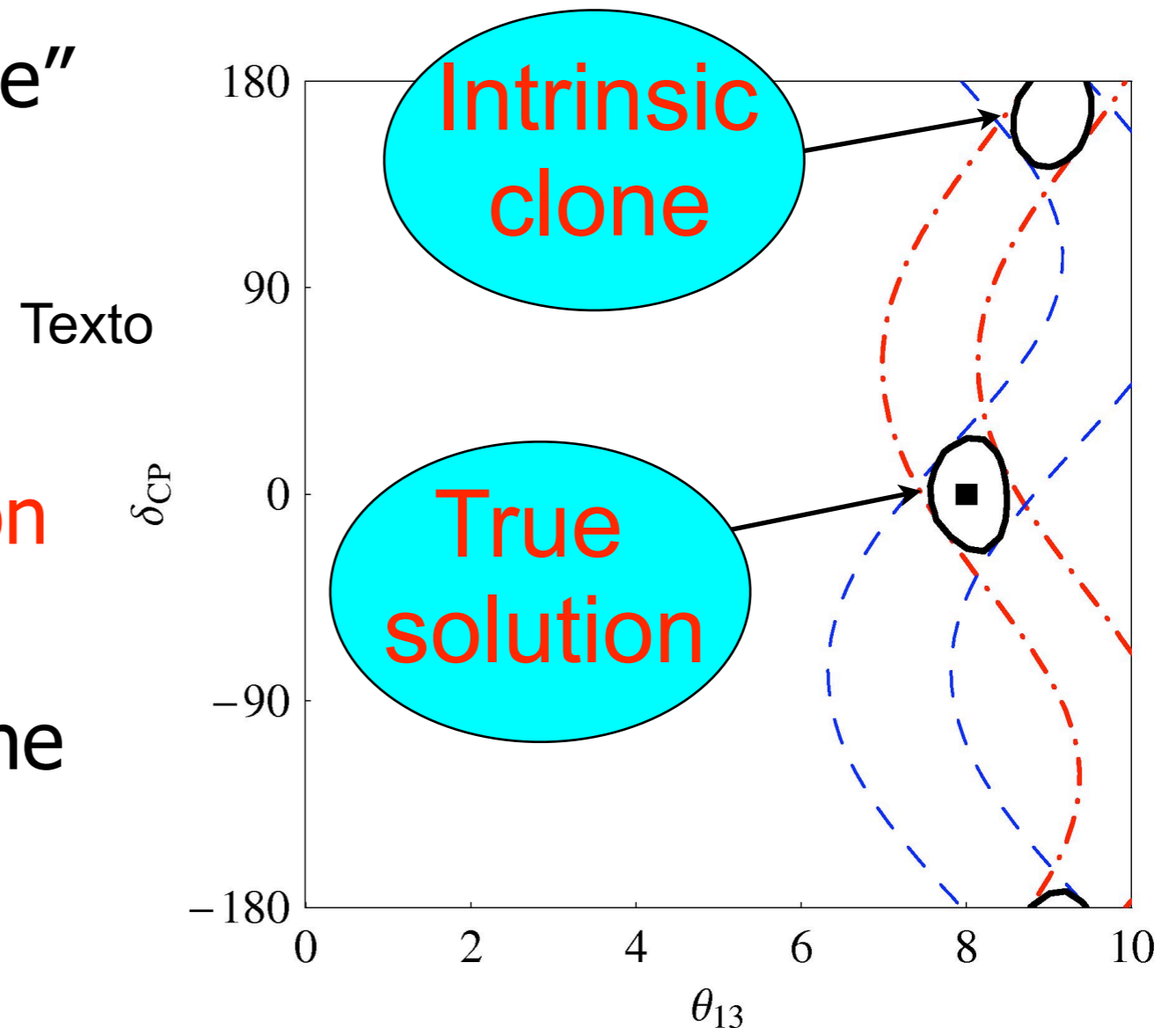
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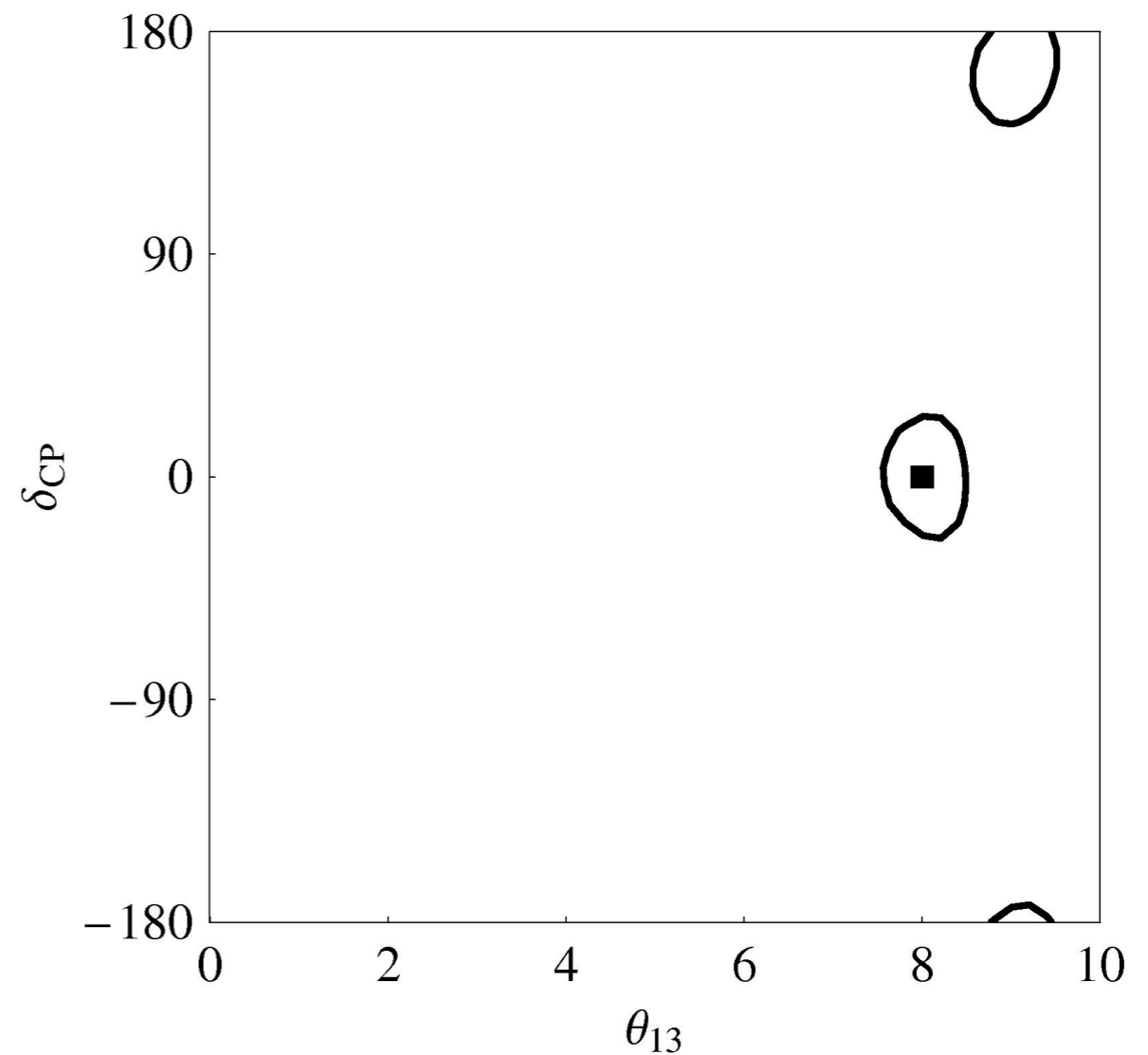
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# Of other degeneracies

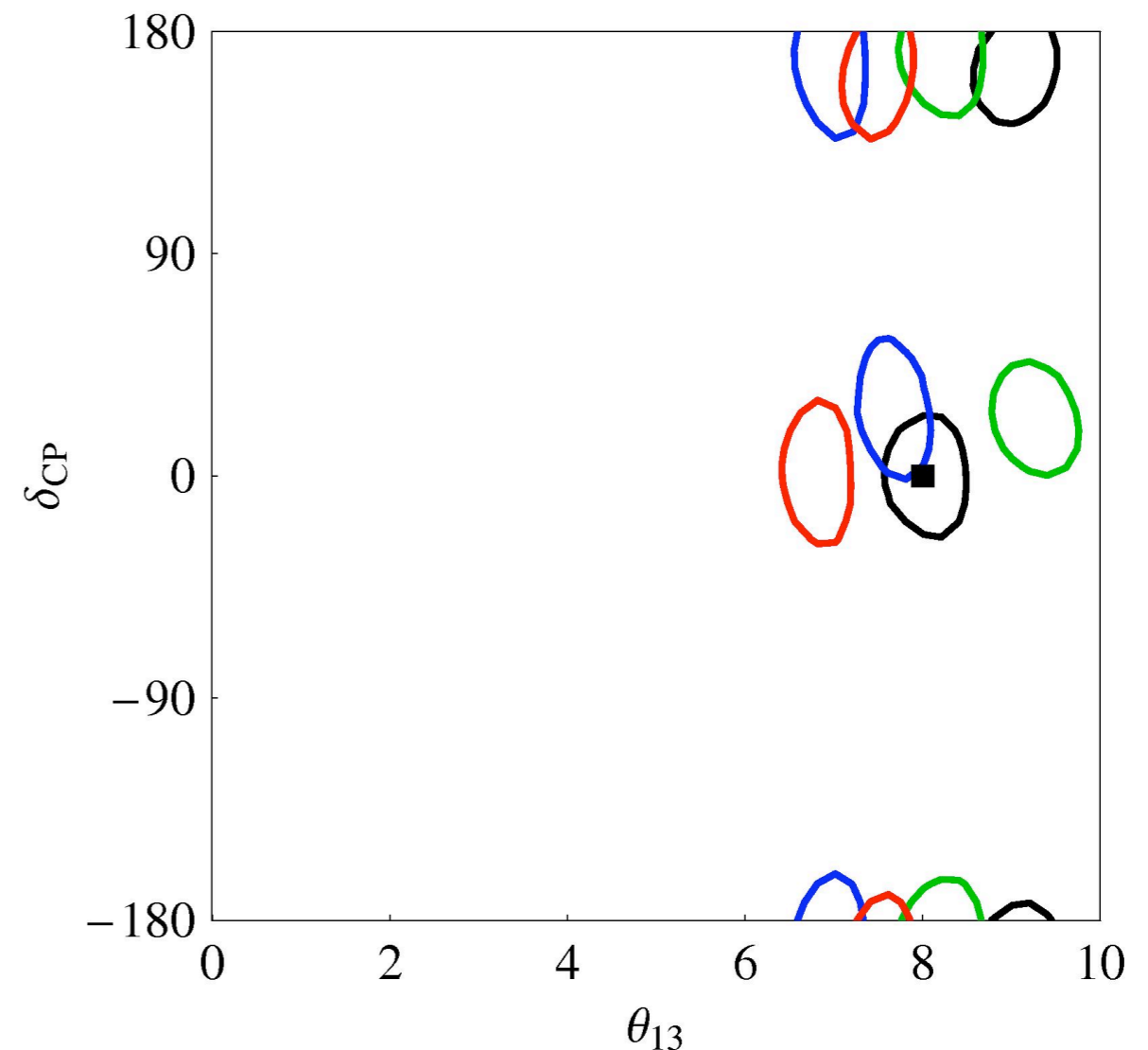
- Two unknown discrete parameters:  $s_{atm}, s_{oct}$
- There are 4 different sets of curves for different choices of  $s_{atm}, s_{oct}$



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- 2 Intersections each

Eightfold degeneracy:  
Intrinsic **sign** **octant** **mixed**

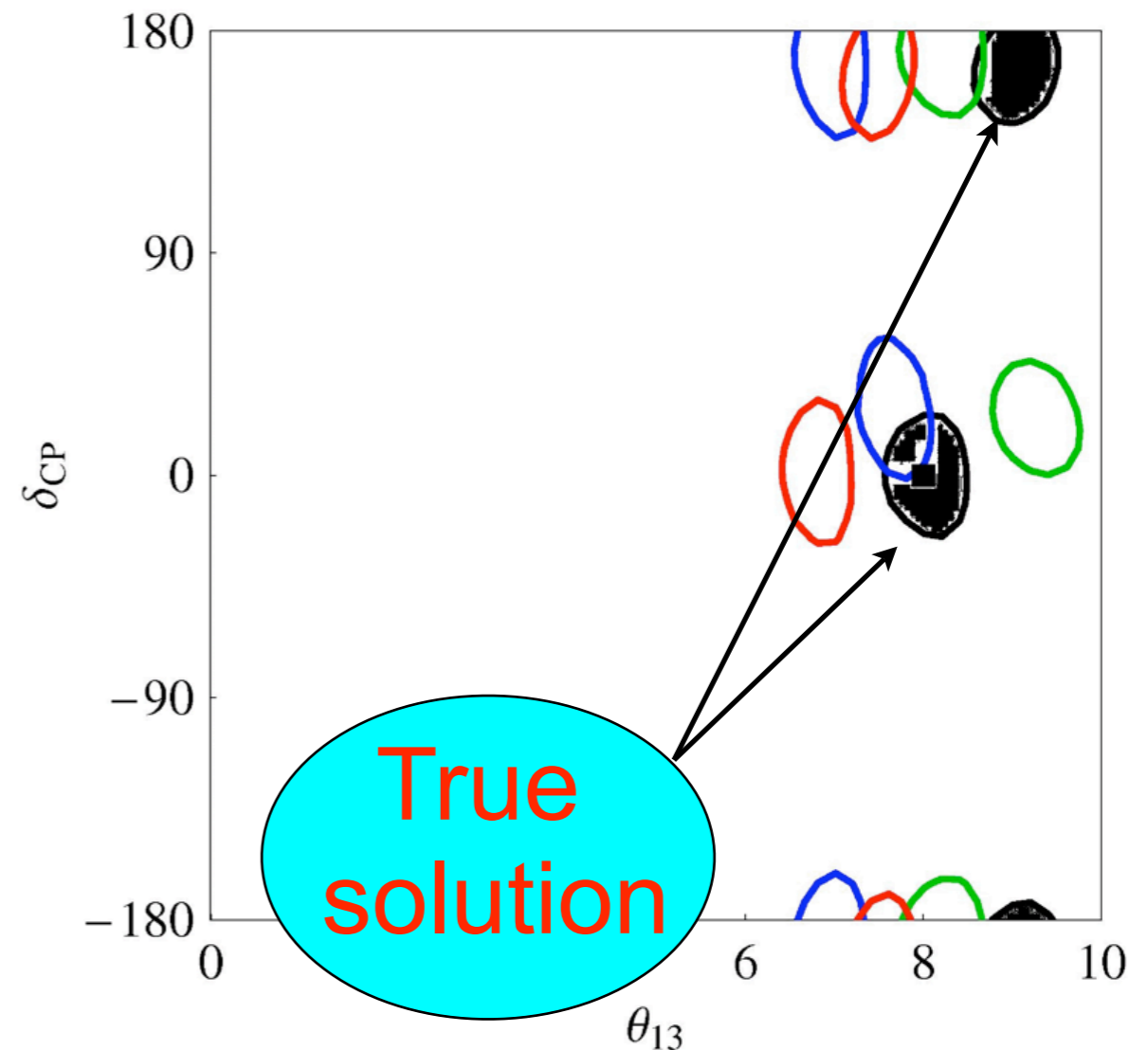


H. Minakata and H. Nunokawa hep-ph/0108085  
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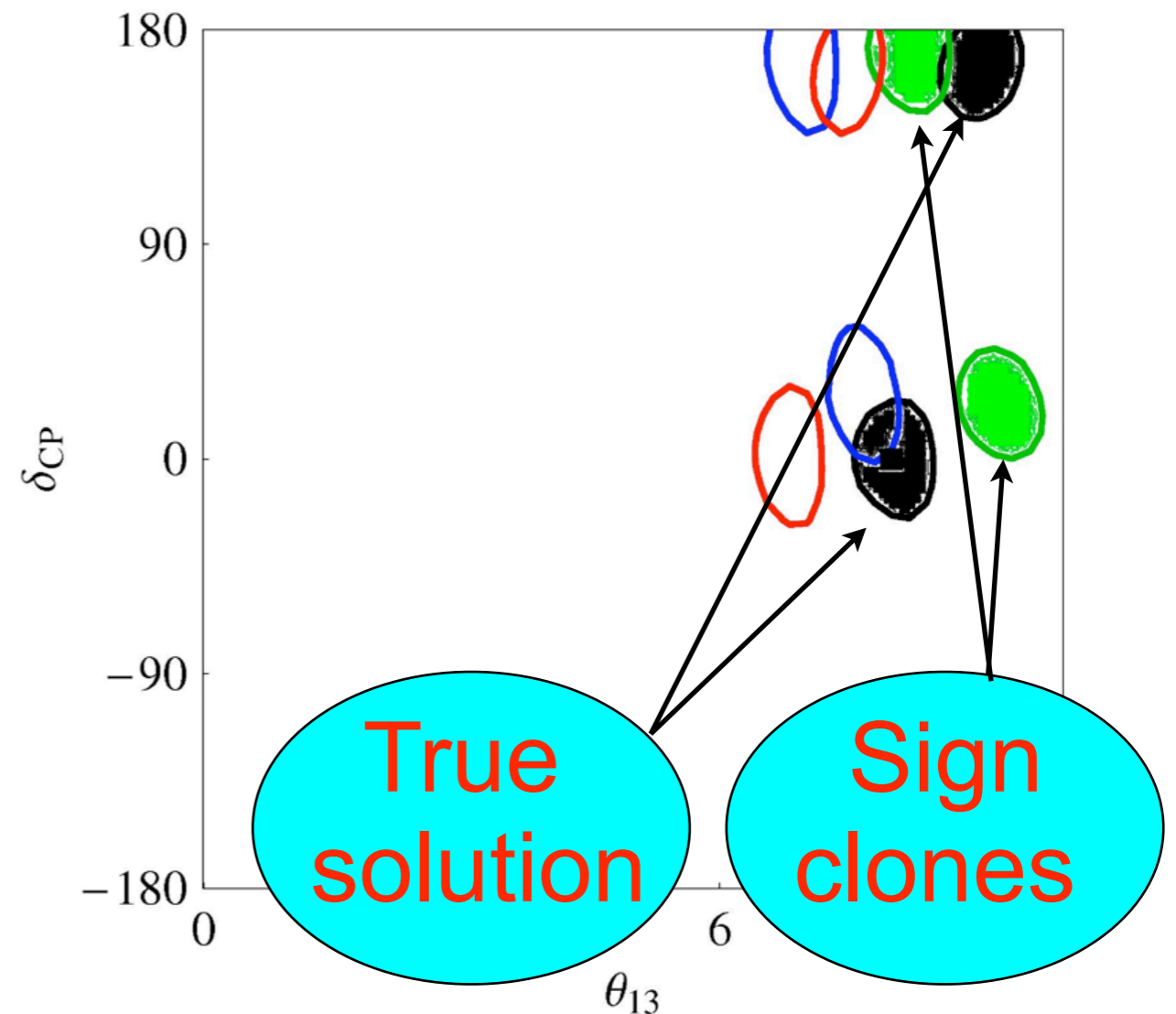


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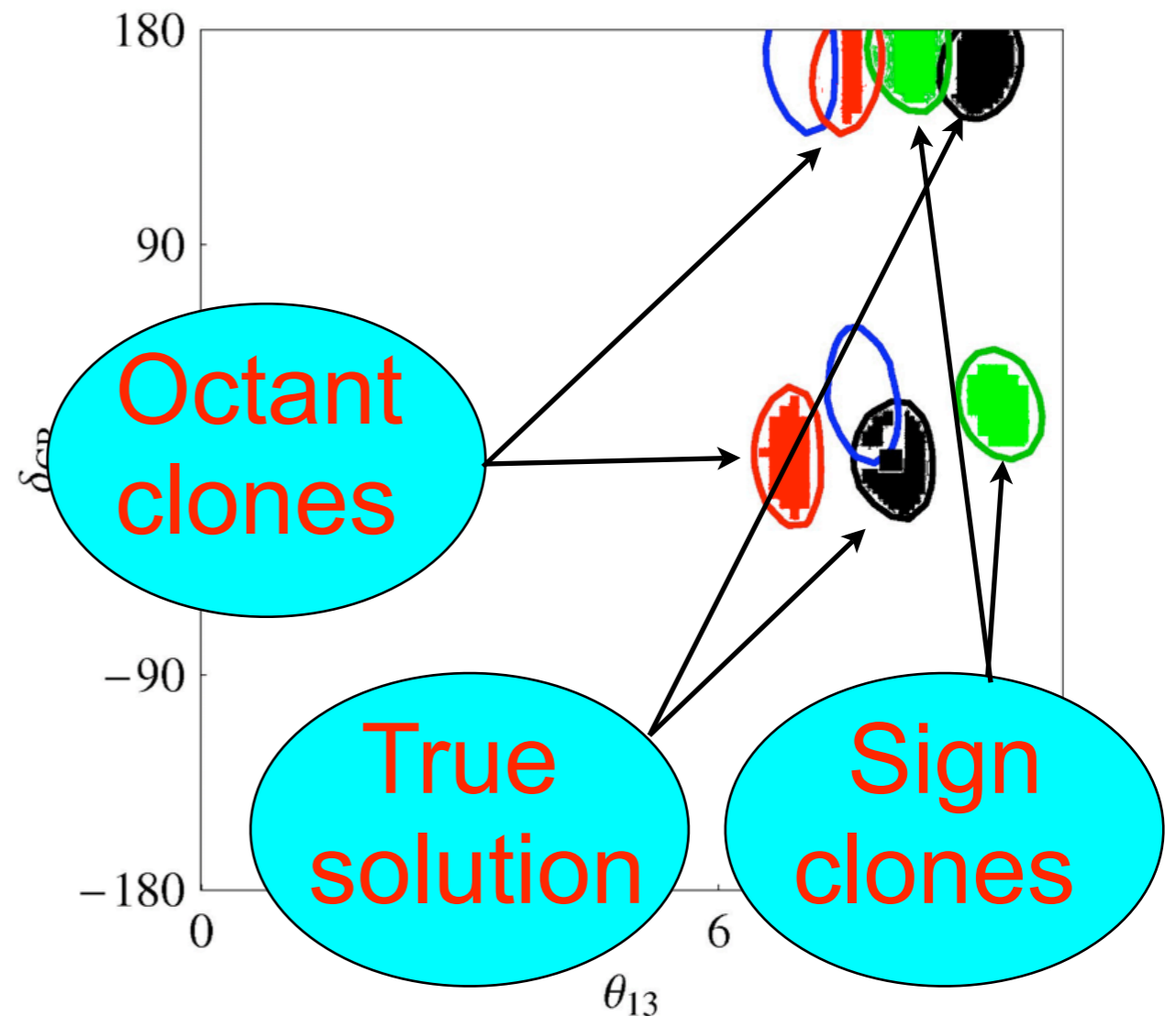


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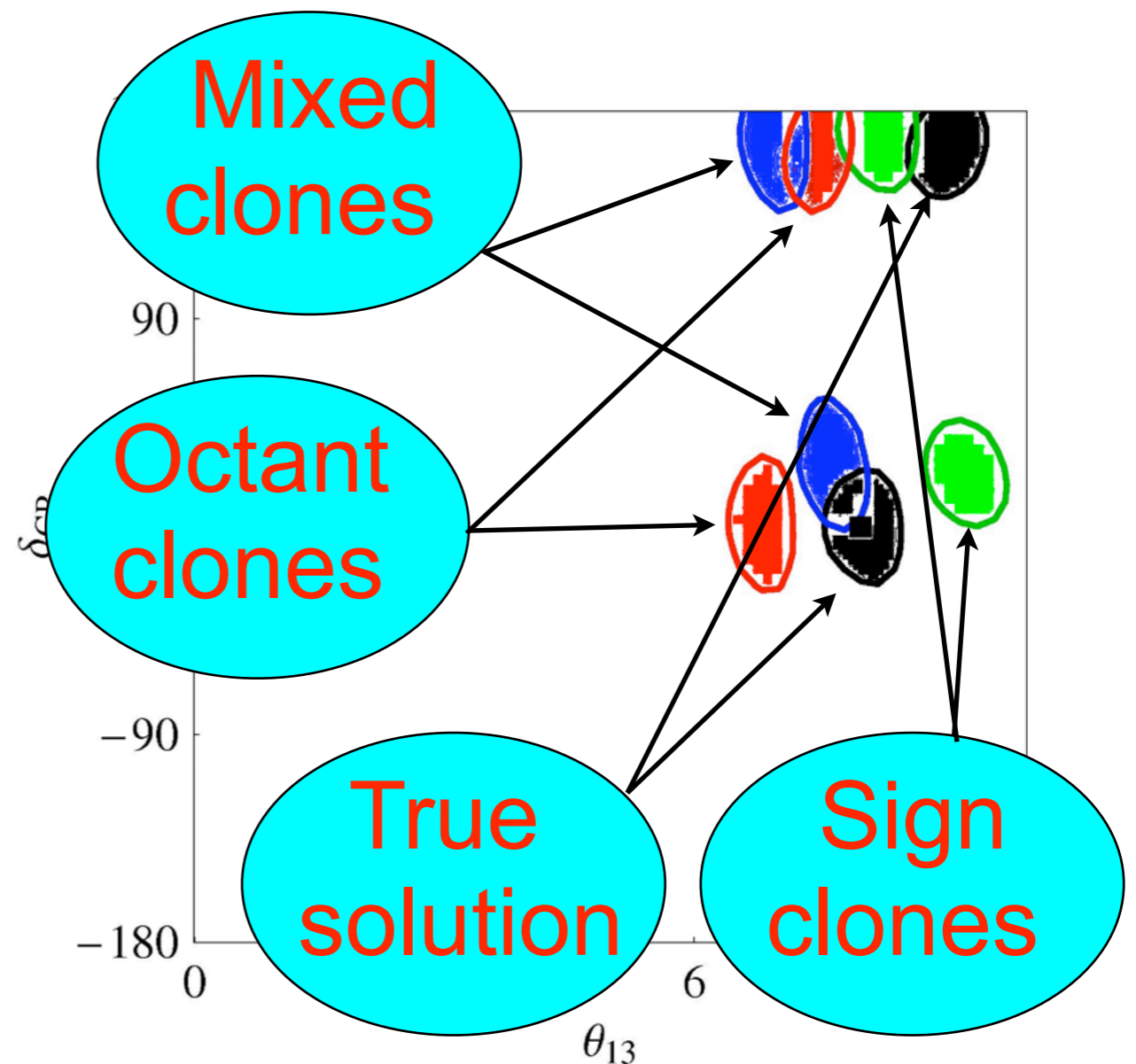
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- The goal: measure at the same time the four parameters that we do not yet know:  $\theta_{13}$ ,  $\delta$ , the sign of  $\Delta m^2_{23}$  and the  $\theta_{23}$ -octant
- To achieve our goal, we must then solve the problem of degeneracies.

# SUPERBEAMS

# Sensitivity bounds by T2K and NOvA

EXP	$\theta_{13}$	$\sin^2(2\theta_{13})$	$\sin^2 \theta_{13}$
Global Fit	10.8°	0.135	0.035
<b>SBEAMS</b>			
T2K-I	2.2°	0.006	0.0015
(JHF)	→ 3.3°	→ 0.013	→ 0.0030
NOνA	2°	0.005	0.0010
(NUMI-OA)	→ 3.5°	→ 0.015	→ 0.0040

$$P_{\mu e} = s_{23}^2 \sin^2(2\theta_{13}) \sin^2 \left[ \frac{\Delta_{atm} L}{2} \right] + \mathcal{O} \left[ \left( \frac{\Delta_{sol}}{\Delta_{atm}} \right) \sin(2\theta_{13}) \cos \delta \right] + \mathcal{O} \left[ \left( \frac{\Delta_{sol}}{\Delta_{atm}} \right) \sin(2\theta_{13}) \sin \delta \right]$$

Sensitivity loss due to  $(\theta_{13} - \delta)$ -correlations

# Around 2012...

After the wave of conventional beams and first generation superbeams, and of high-power reactors experiments, we will know something more on the PMNS matrix:

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Precision measurements of **LEPTONIC MIXING** will start with the next-to-next generation experiments, using SuperBeams or BetaBeams with 1 Mton Water Čerenkov or/and the Neutrino Factory.

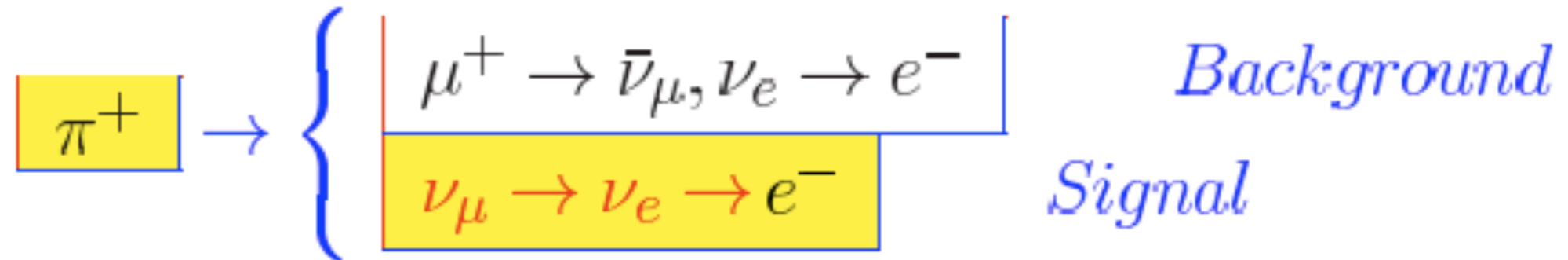


# An intermediate phase?

After T2K and NO $\nu$ A, we will face a forking path:

- ★  $\nu_{\mu} \rightarrow \nu_e$  oscillation has been observed!  
A good option: increase detector mass,  
same source: T2-HK or SPL+UNO  
(really a good option?)
- No signal has been observed:  $\theta_{13} \leq 3^{\circ} - 4^{\circ}$  !  
Go to new sources:  
Neutrino Factory or the Beta-Beam.

# Appearance Signal at a SB



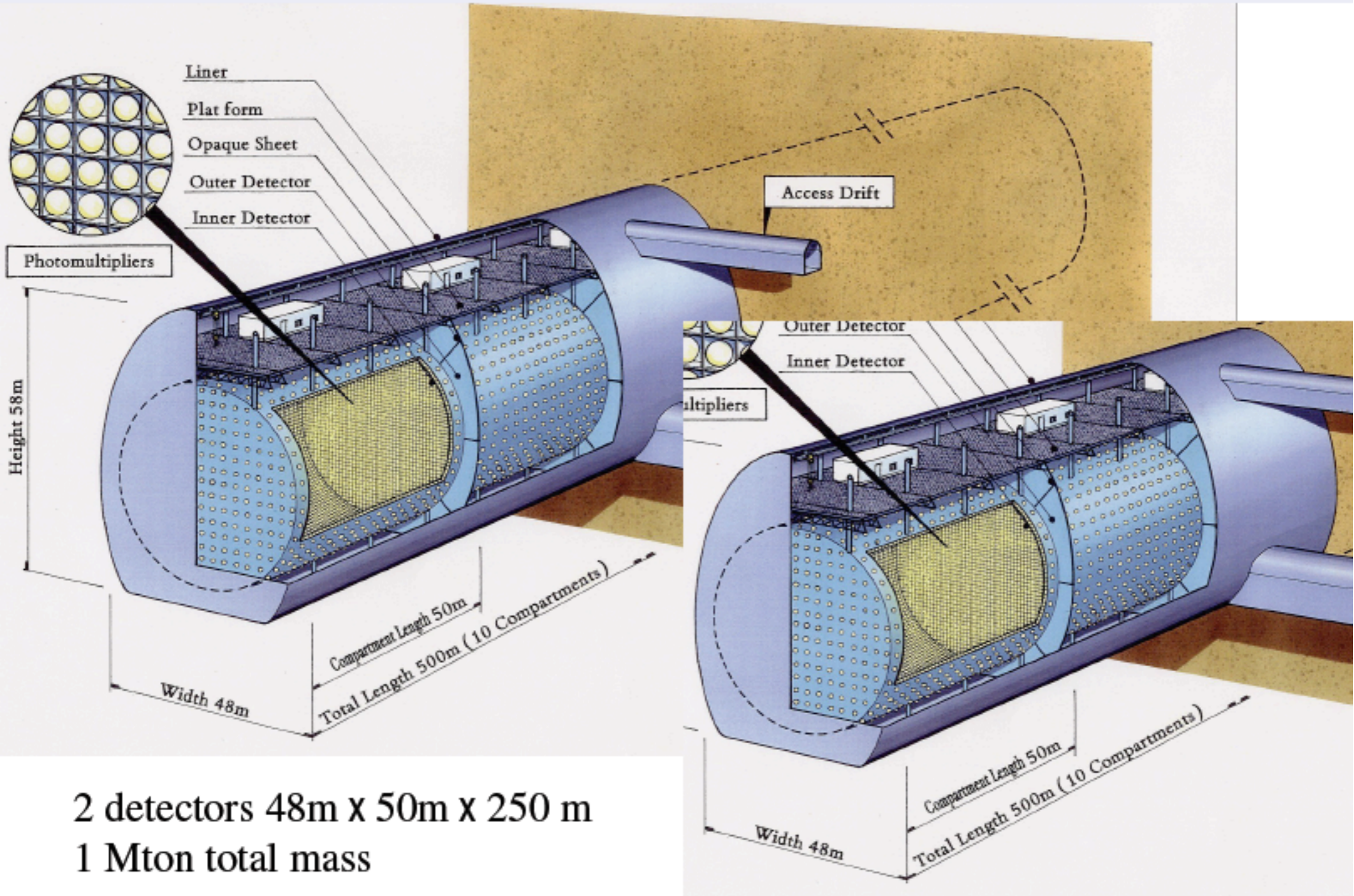
The oscillation probability is

$$P_{\mu e}^\pm \simeq X_\pm \sin^2(2\theta_{13})$$

$$+ Y_\pm \cos\left(\delta \pm \frac{\Delta_{atm} L}{2}\right) \cos\theta_{13} \sin(2\theta_{13})$$

$$+ Z + \dots$$

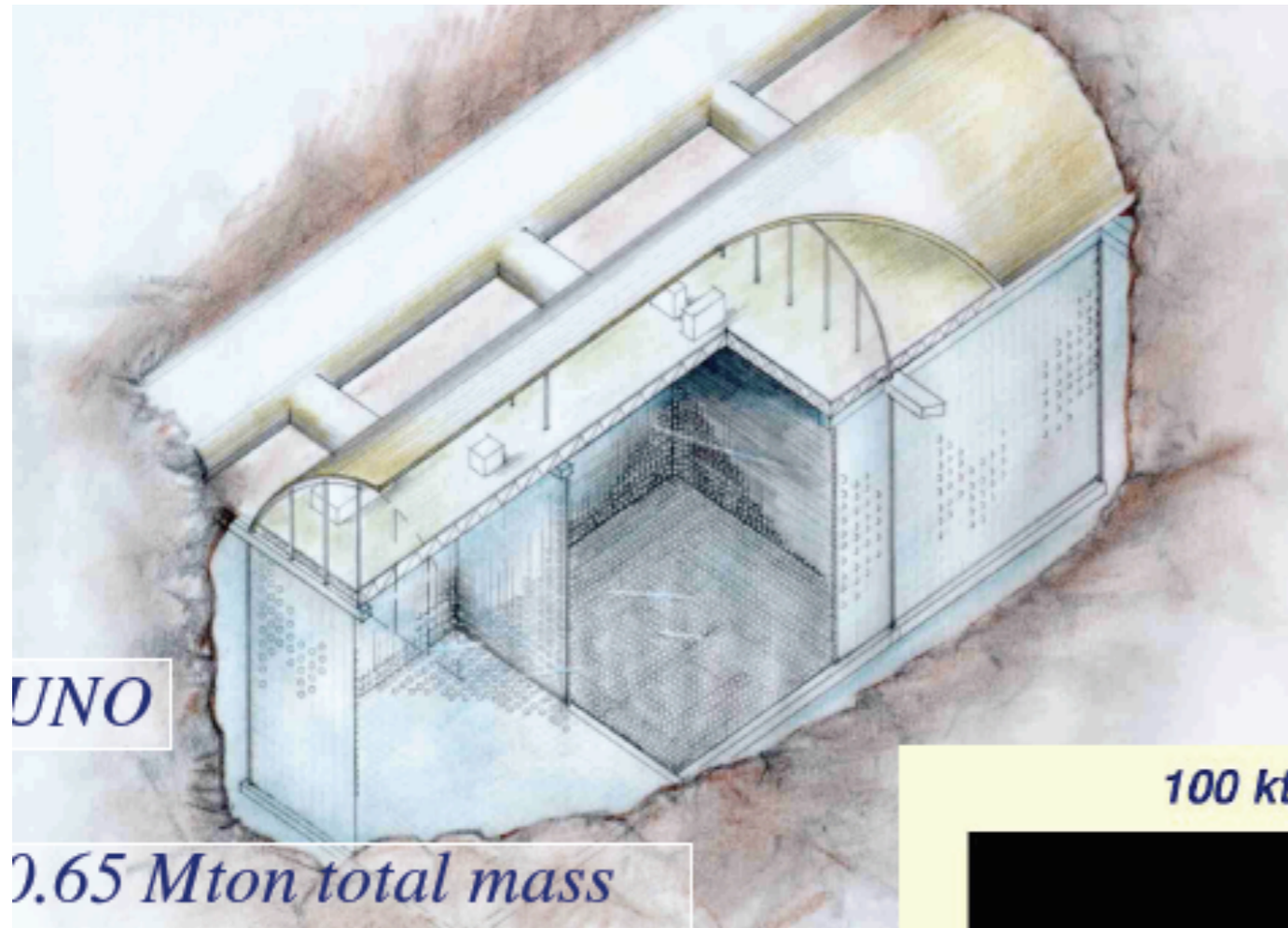
# Hyper-Kamiokande



2 detectors 48m x 50m x 250 m  
1 Mton total mass

# The CERN-Memphys project

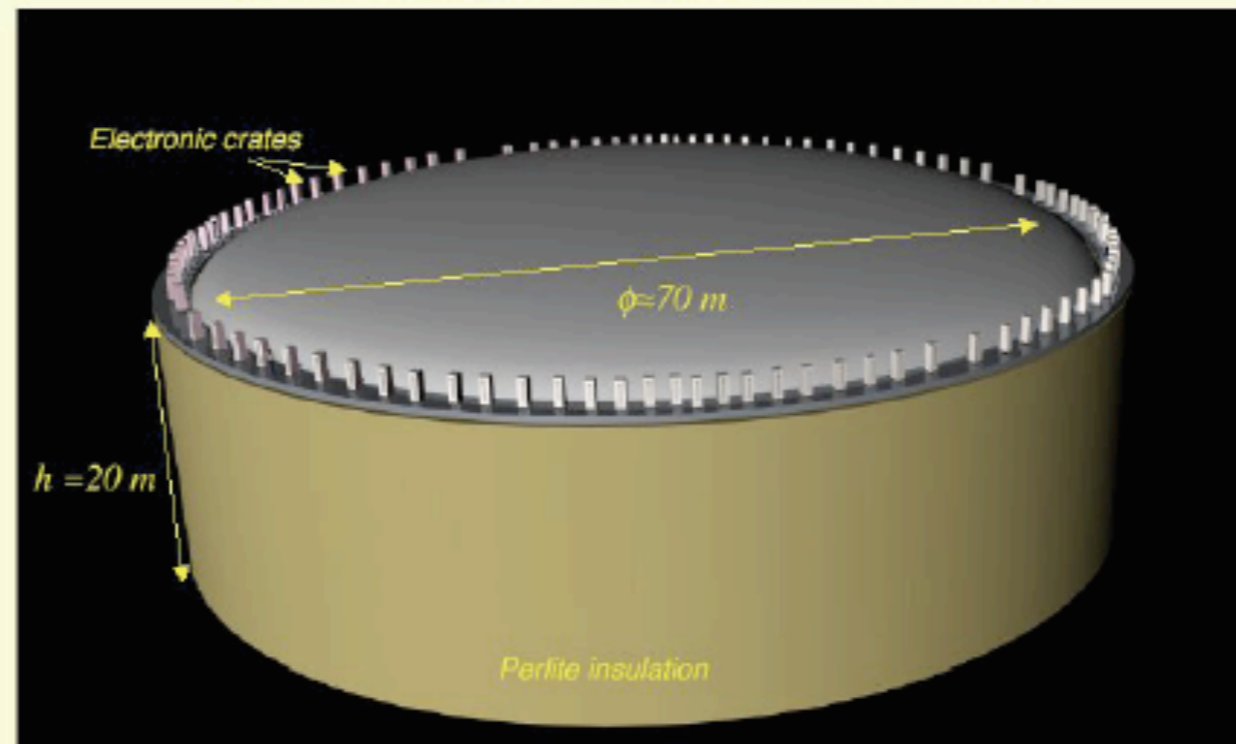
## *Detector options*



UNO

0.65 Mton total mass

### 100 kton liquid Argon TPC detector

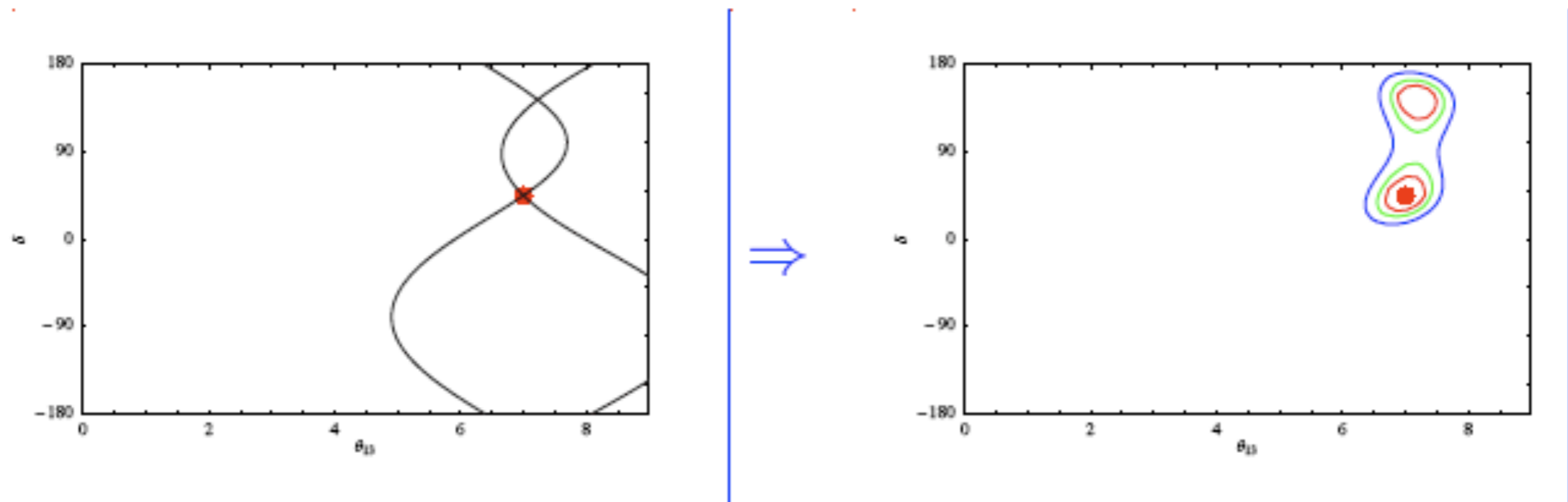


Experiments for CP violation: a giant liquid Argon scintillation, Cerenkov and charge imaging experiment.

A.Rubbia, Proc. II Int. Workshop on Neutrinos in Venice, 2003, hep-ph/0402110

# Degeneracy in $(\theta_{13}, \delta)$ at the SPL

2 years for  $\pi^+$  and 8 years for  $\pi^-$

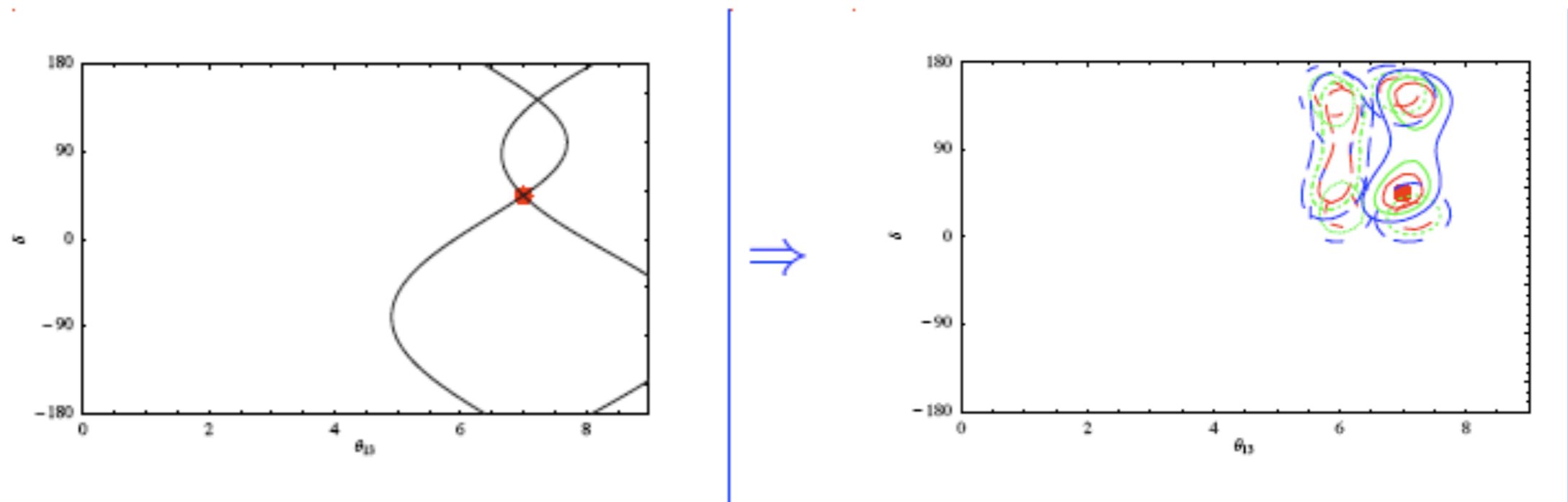


$$L = 130 \text{ Km}, \bar{E}_{\nu\mu} = 0.27 \text{ GeV}, \bar{E}_{\bar{\nu}\mu} = 0.25 \text{ GeV}$$

Input parameters:  $\bar{\theta}_{13} = 7^\circ, \bar{\delta} = 45^\circ$

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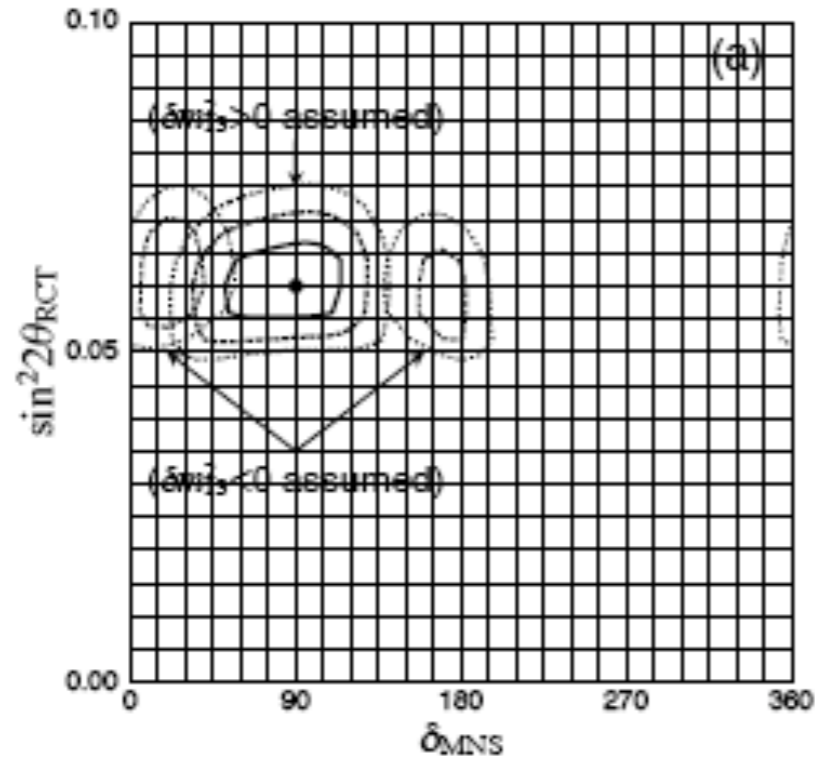


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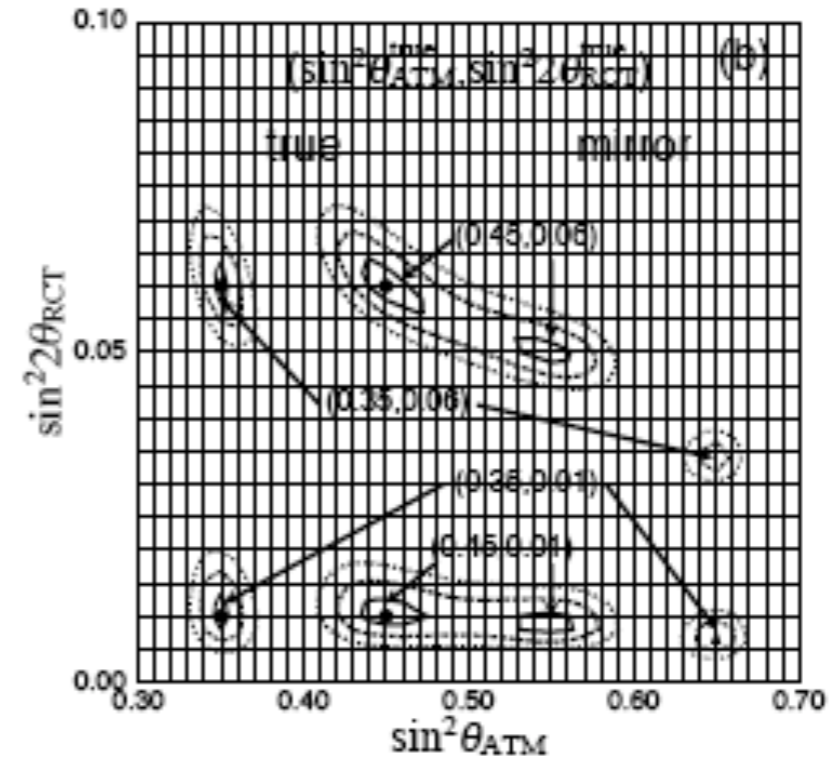
Input parameters:  $\bar{\theta}_{13} = 7^\circ, \bar{\delta} = 45^\circ$

# The same at T2-HK

## The sign degeneracy



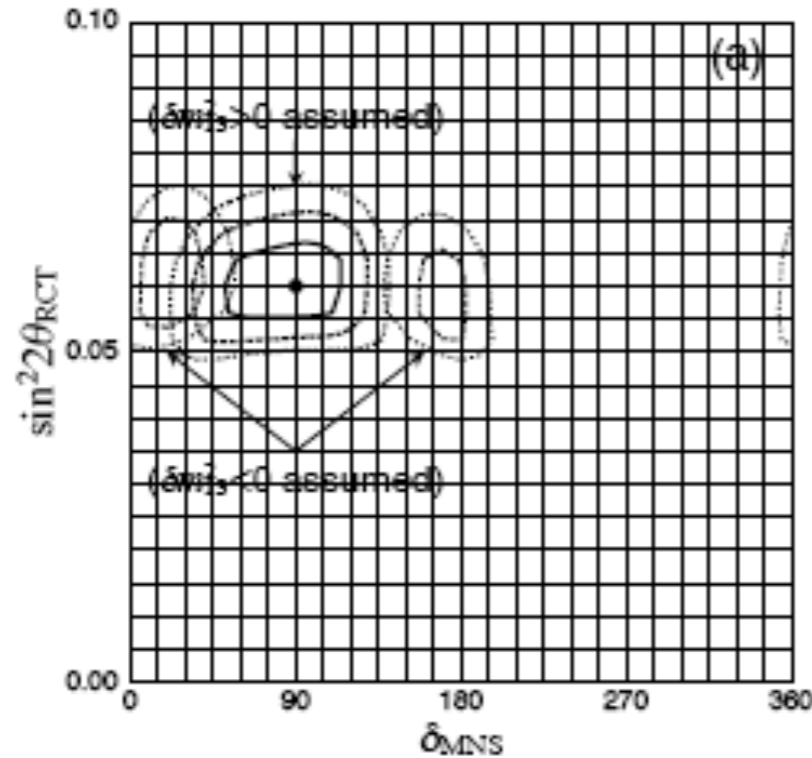
## The octant degeneracy



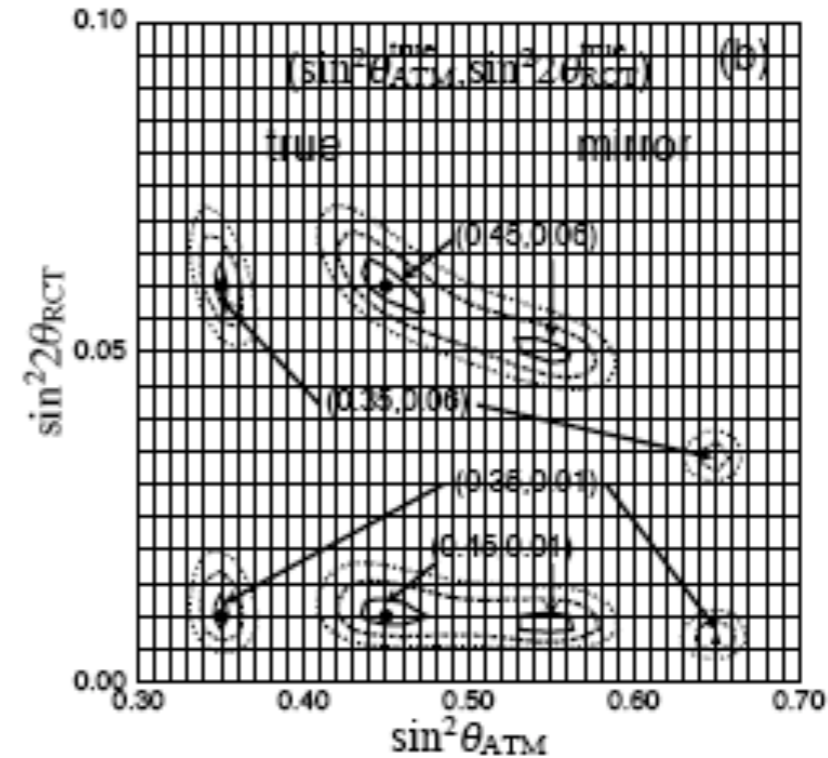
K. Hagiwara, hep-ph/0410229

# The same at T2-HK

## The sign degeneracy



## The octant degeneracy



K. Hagiwara, hep-ph/0410229

The problem: **the sign of  $\Delta m_{23}^2$**  is not measured



## Solving parameter degeneracies with atmospheric data

- The HK detector of T2K-II will also record ATM events. We assume 9 yr of data. When these events are combined with the LBL ones:
  - the **octant degeneracy** is completely solved regardless of the **true octant**;
  - the **hierarchy degeneracy** is solved if **true octant** is the dark one.

- **solid**: LBL only;
- **colored**: LBL + ATM;
- regions at  $2\sigma$ , 99%,  $3\sigma$  CL (2 dof);

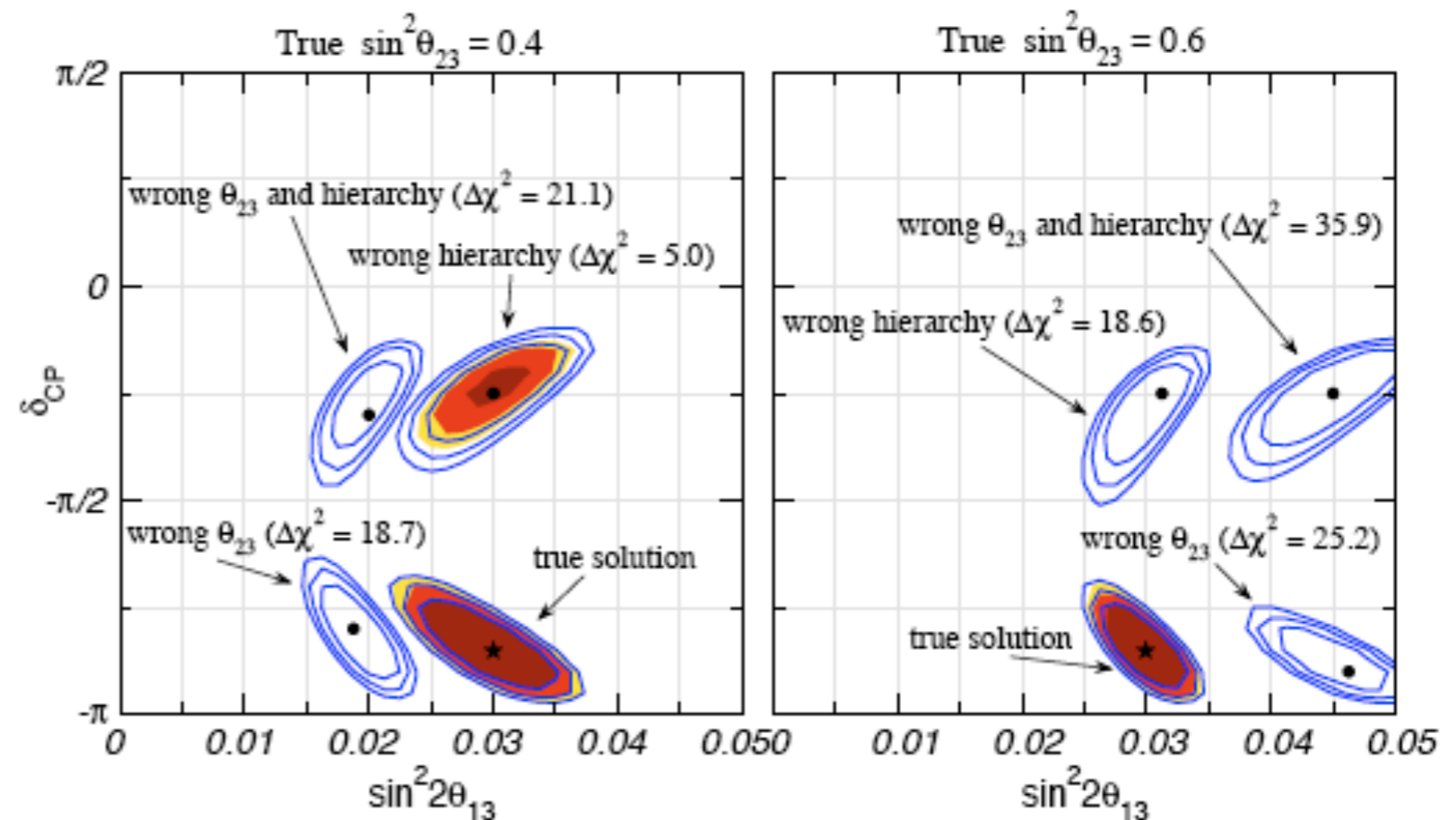
- true values:

$$\delta_{CP} = -0.85\pi,$$

$$\sin^2 \theta_{13} = 0.03,$$

$$\Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2,$$

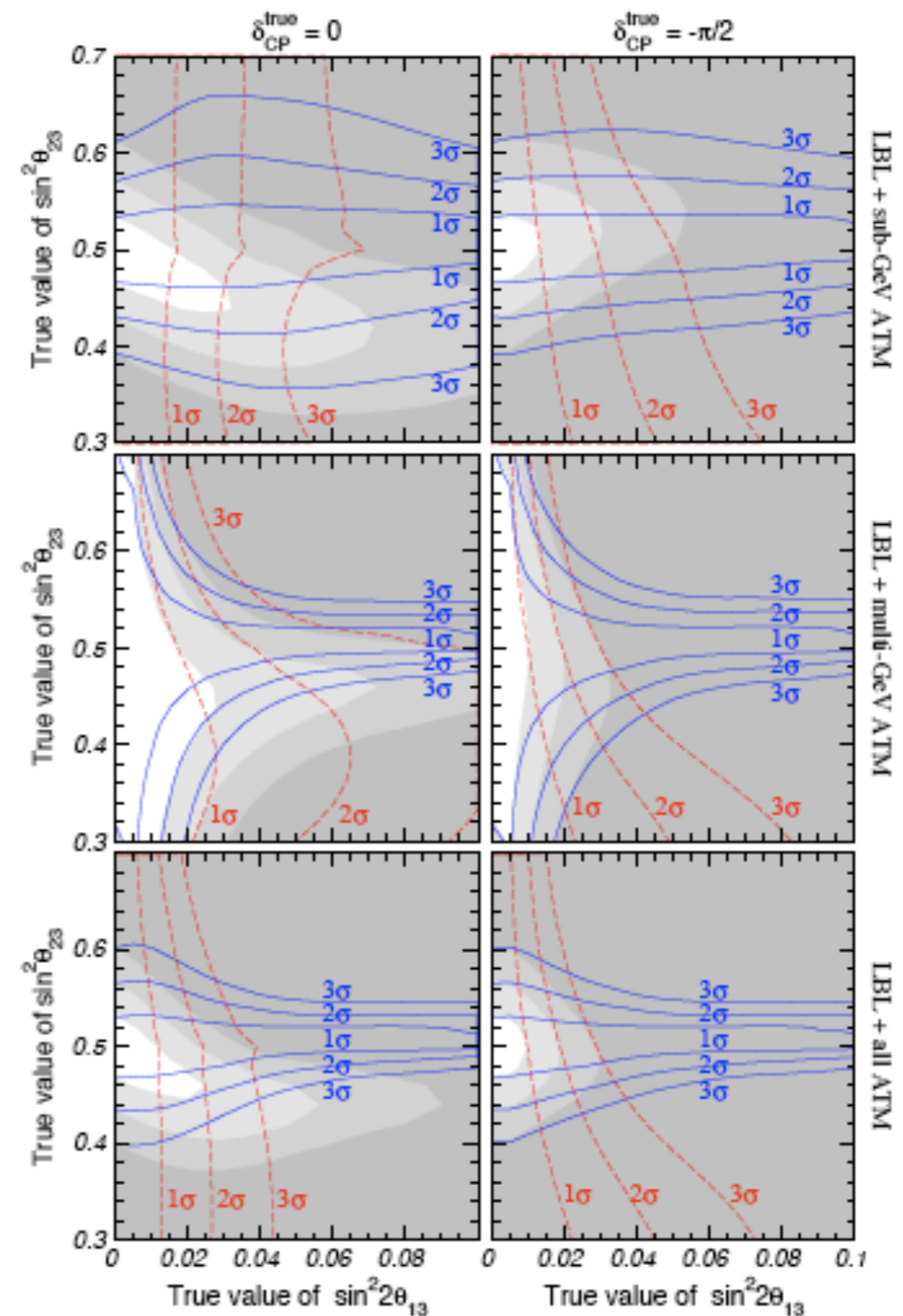
$$\Delta m_{21}^2 = 7.9 \times 10^{-5} \text{ eV}^2.$$



[Huber, MM, Schwetz, PRD 71 (2005) 053006, hep-ph/0501037]

## Resolving parameter degeneracies

- sensitivity to the **octant** (blue lines):
  - given by **sub-GeV** events for  $\theta_{13} \approx 0$ ;
  - given by **multi-GeV** events for  $\theta_{13} \gtrsim 0.04$ ;
  - only mildly dependent on  $\delta_{CP}$ ;
- sensitivity to the **hierarchy** (red lines):
  - dominated by **multi-GeV** for  $\theta_{23} > 45^\circ$ ;
  - **sub-GeV** events relevant if  $\theta_{23} < 45^\circ$ ;
  - strongly depends on  $\delta_{CP}$  in the latter case;
- sensitivity to **octant+hierarchy** (gray regions):
  - mostly given by “sum” of blue and red lines;
  - $\delta_{CP}$  interference terms may be relevant.

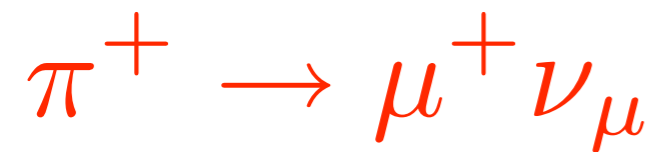


# NEUTRINO FACTORY

# The Neutrino Factory

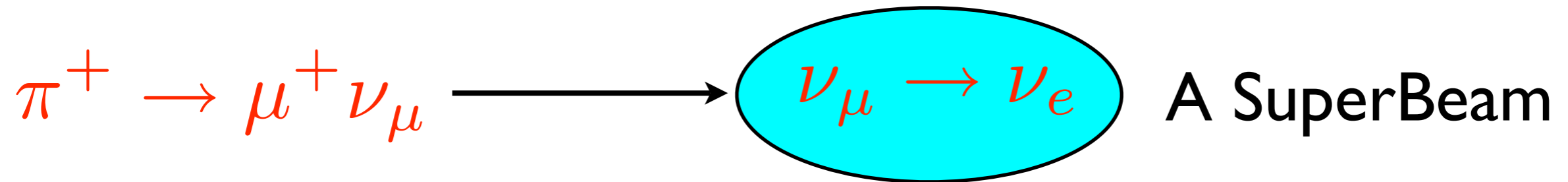
Geer '97  
De Rujula, Gavela  
and Hernandez '98

# The Neutrino Factory



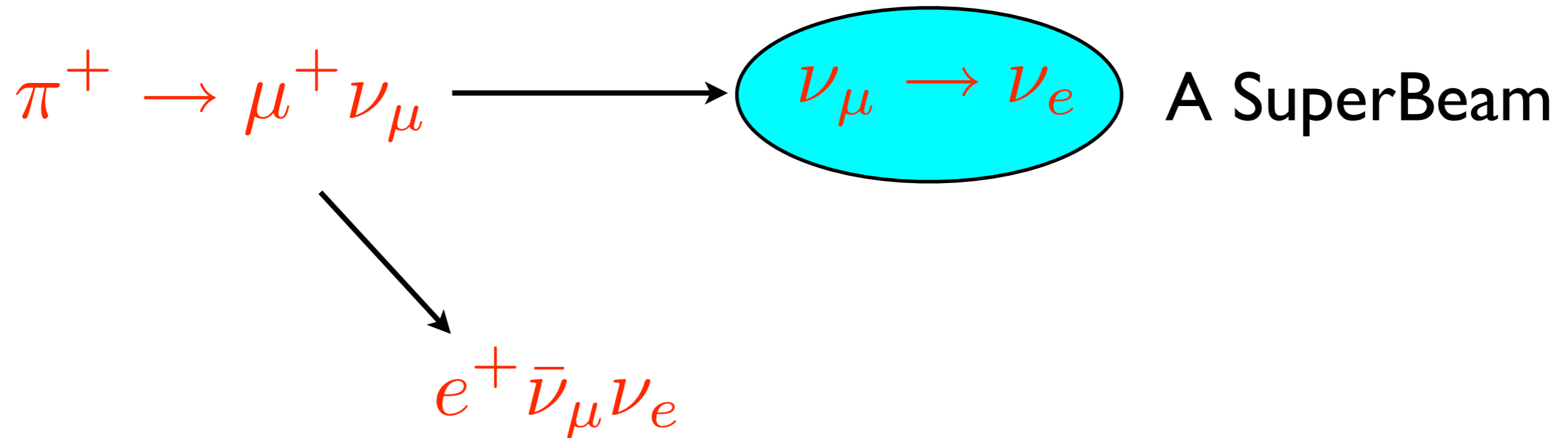
Geer '97  
De Rujula, Gavela  
and Hernandez '98

# The Neutrino Factory



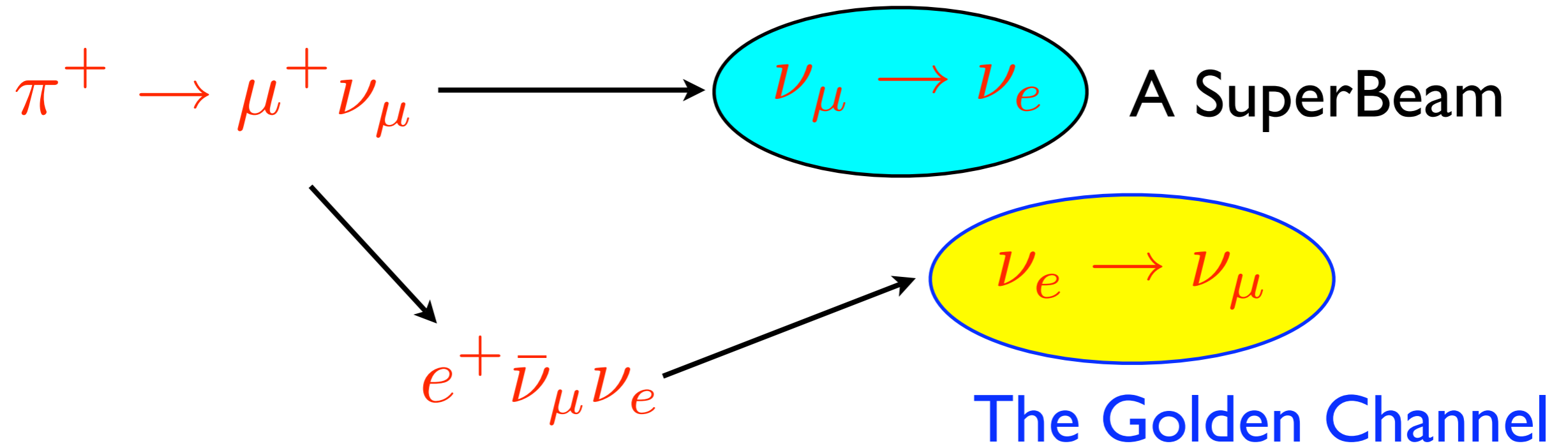
Geer '97  
De Rujula, Gavela  
and Hernandez '98

# The Neutrino Factory



Geer '97  
De Rujula, Gavela  
and Hernandez '98

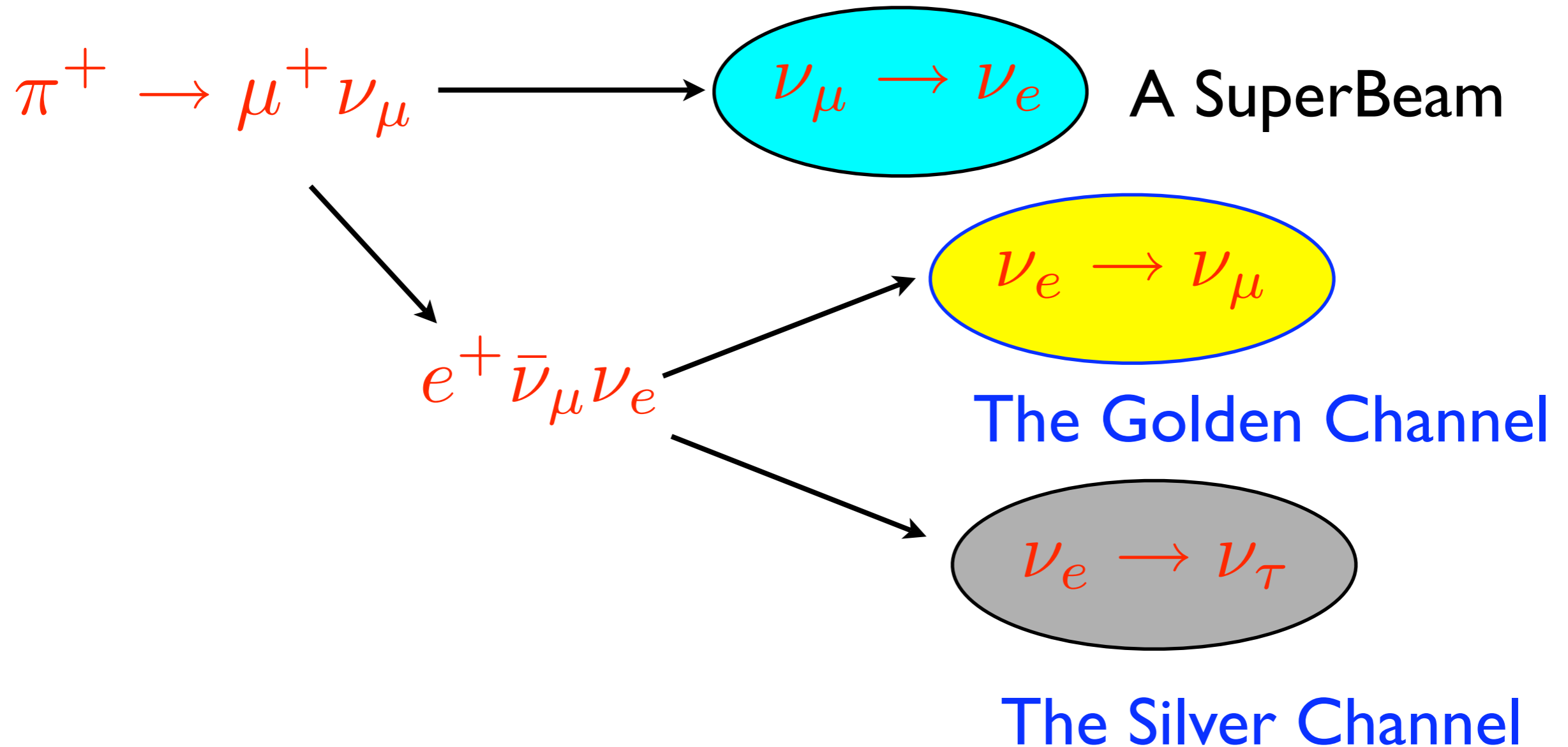
# The Neutrino Factory



Geer '97  
De Rujula, Gavela  
and Hernandez '98

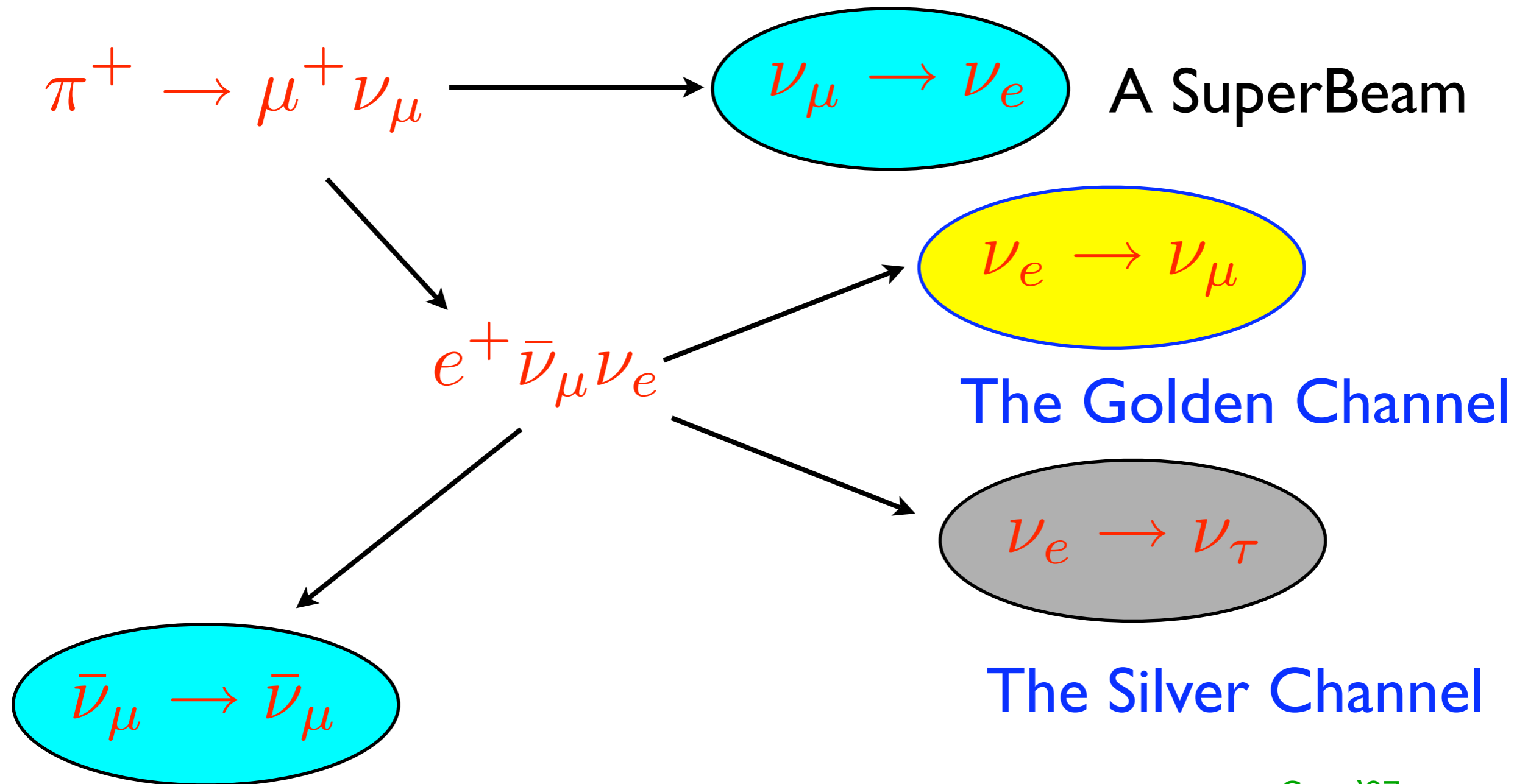


# The Neutrino Factory



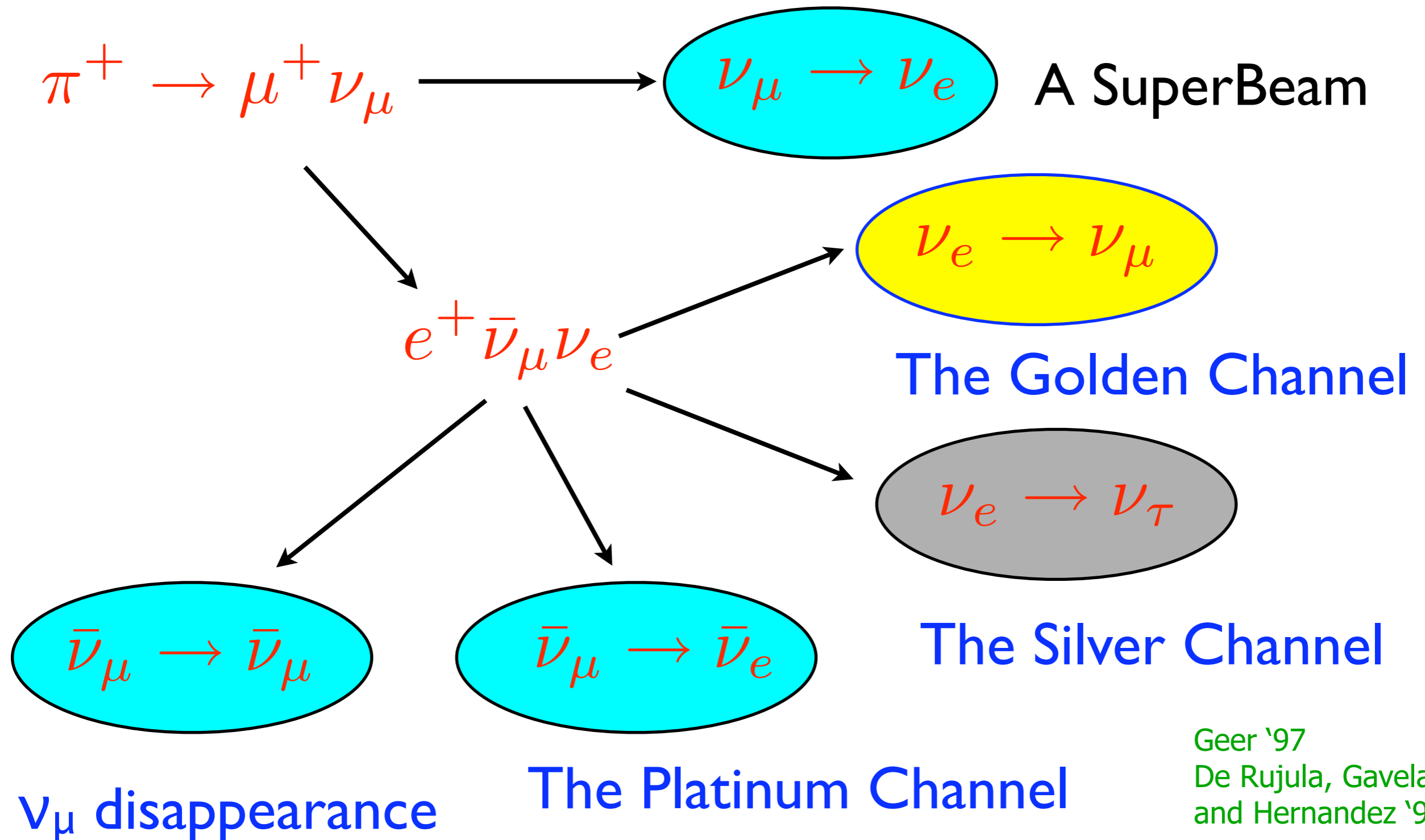
Geer '97  
De Rujula, Gavela  
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# The Neutrino Factory



Geer '97  
De Rujula, Gavela  
and Hernandez '98

# The Neutrino Factory



Geer '97  
De Rujula, Gavela  
and Hernandez '98

# The Neutrino Factory

## Proton Driver

primary beam on production target

## Target, Capture, Decay

### Bunching

Phase Rotation reduce E of bunch

## Cooling

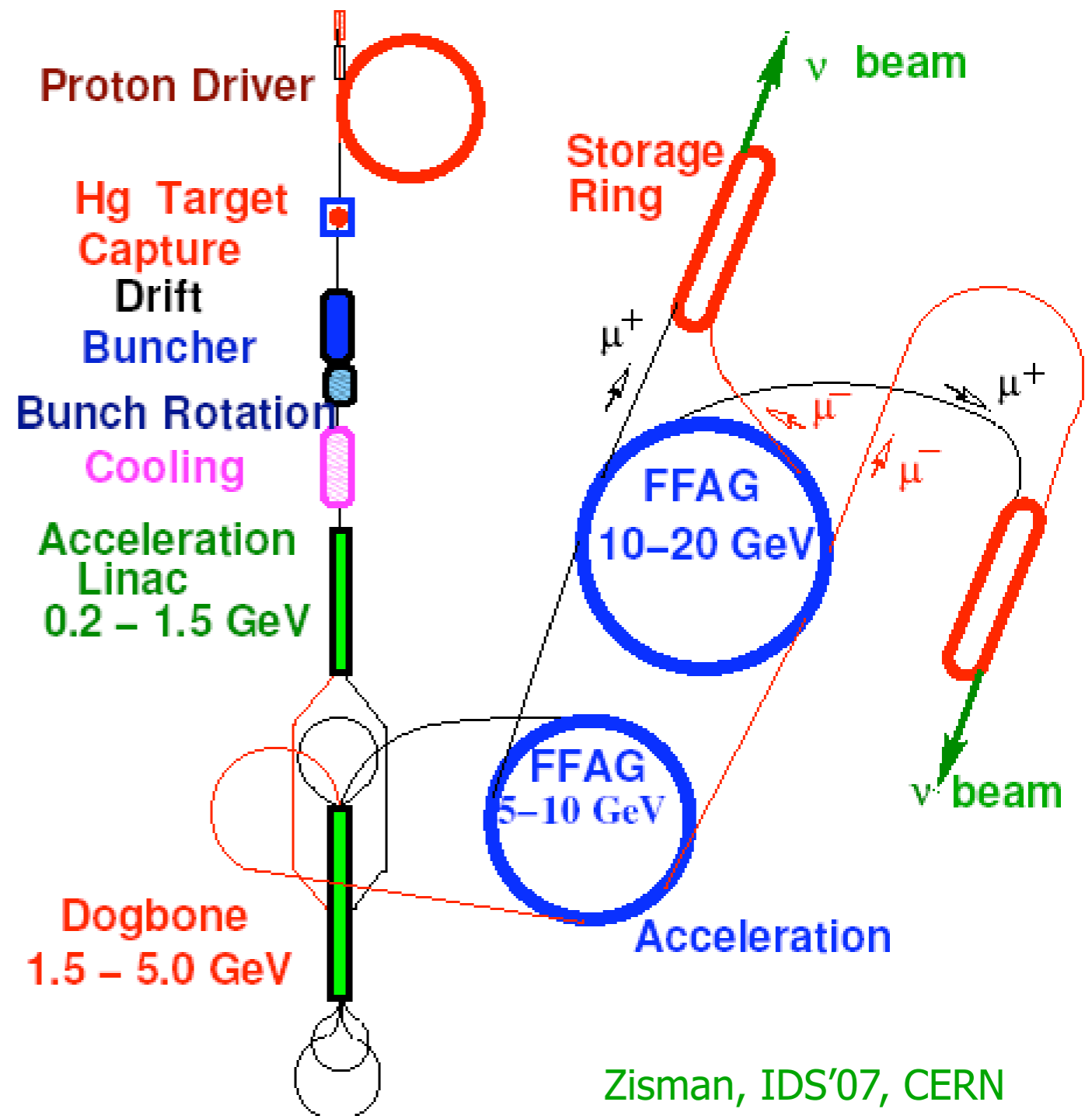
reduce transverse emittance

## Acceleration (LINAC/FFAG)

130 MeV 20-40 GeV

## Decay Ring

store for ~500 turns; long straight section



Zisman, IDS'07, CERN

# The Neutrino Factory

## Proton Driver

primary beam on production target

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### Bunching

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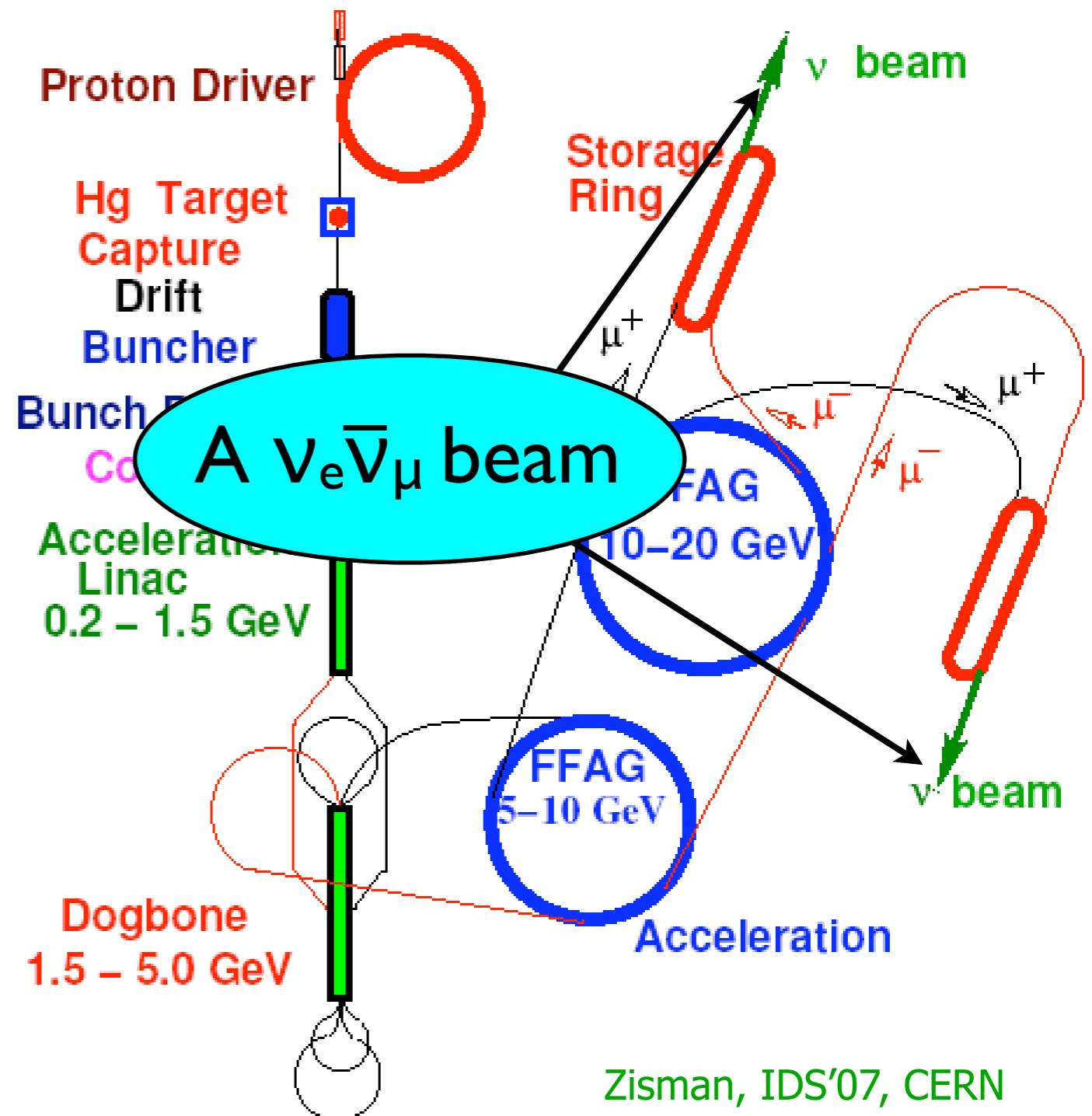
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Zisman, IDS'07, CERN

# The Neutrino Factory

A  $\nu_\mu$  beam

## Proton Driver

primary beam on production target

## Target, Capture, Decay

### Bunching

Phase Rotation reduce E of bunch

## Cooling

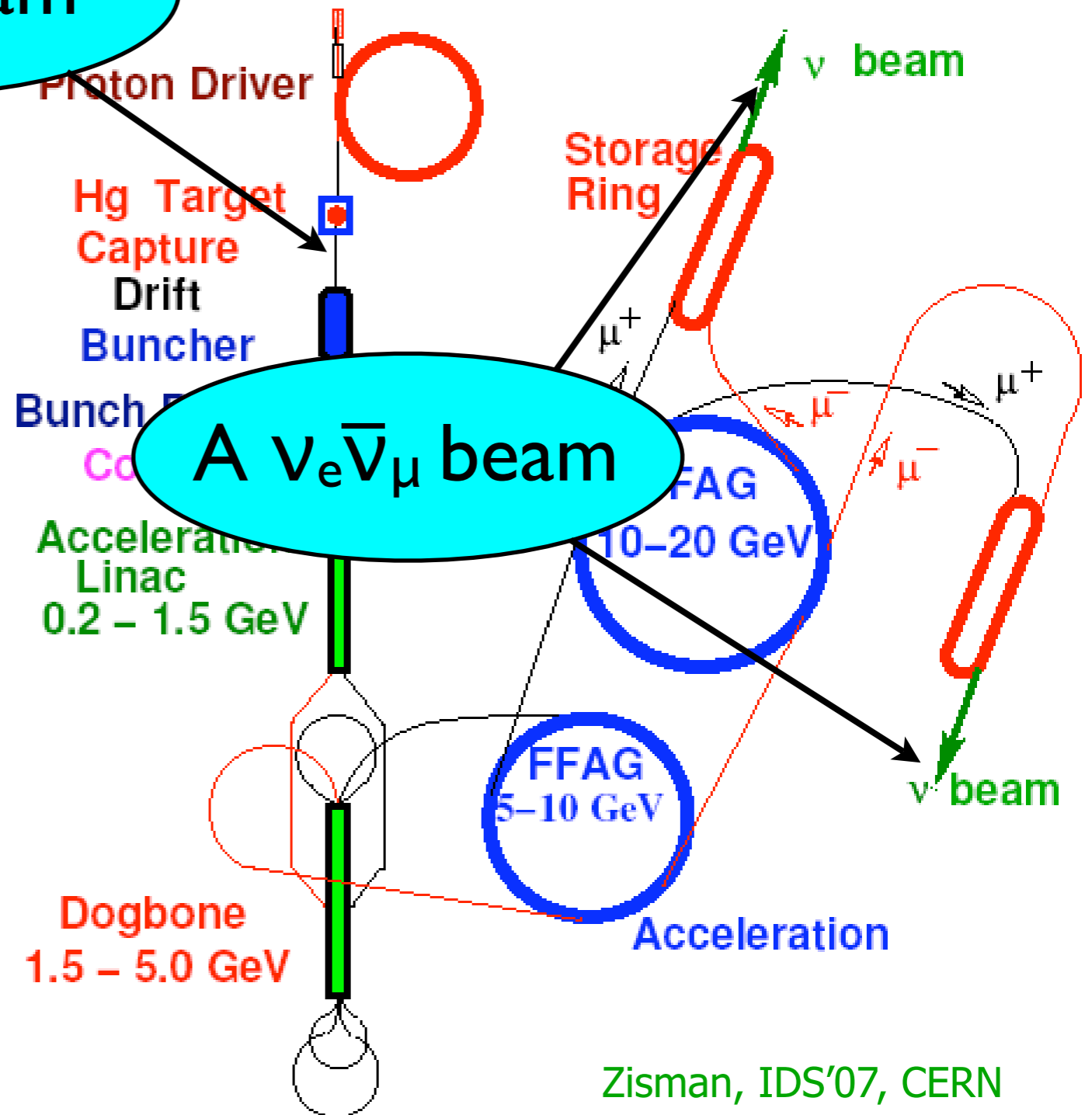
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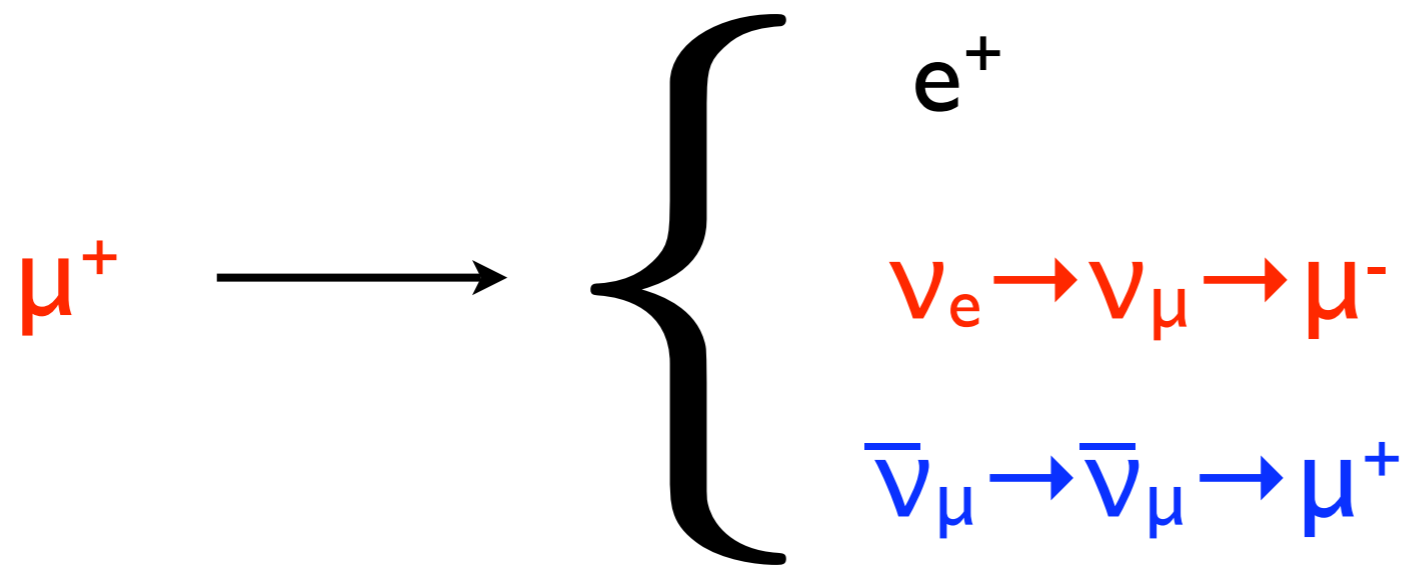
store for ~500 turns; long straight section



Zisman, IDS'07, CERN

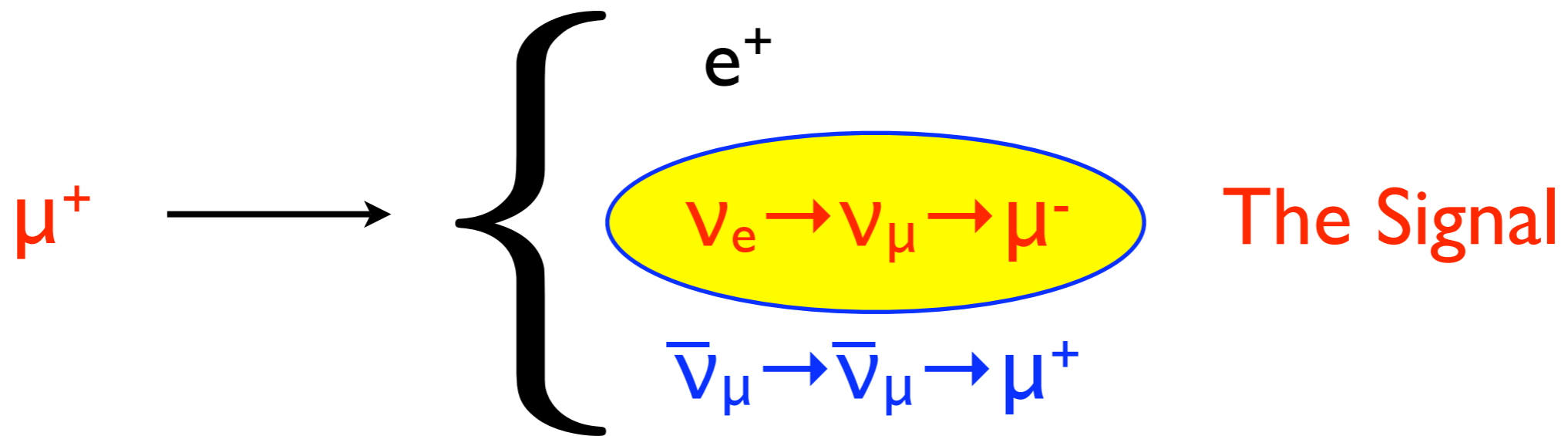
# The Golden Channel

A. Cervera et al, hep-ph/0002108



# The Golden Channel

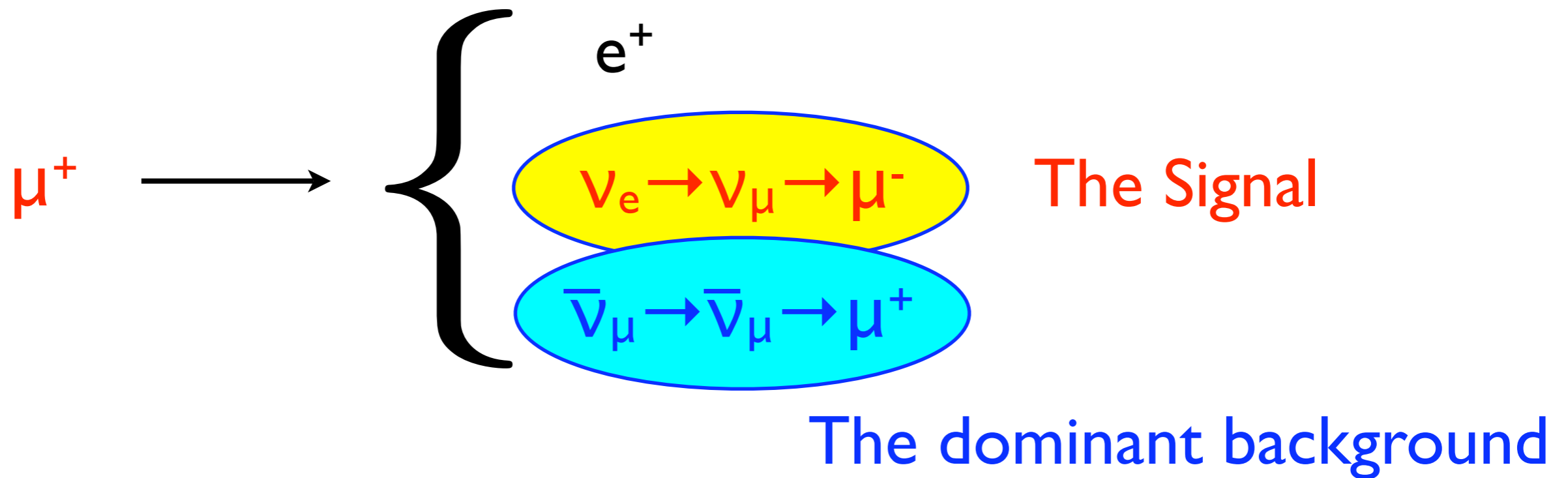
A. Cervera et al, hep-ph/0002108





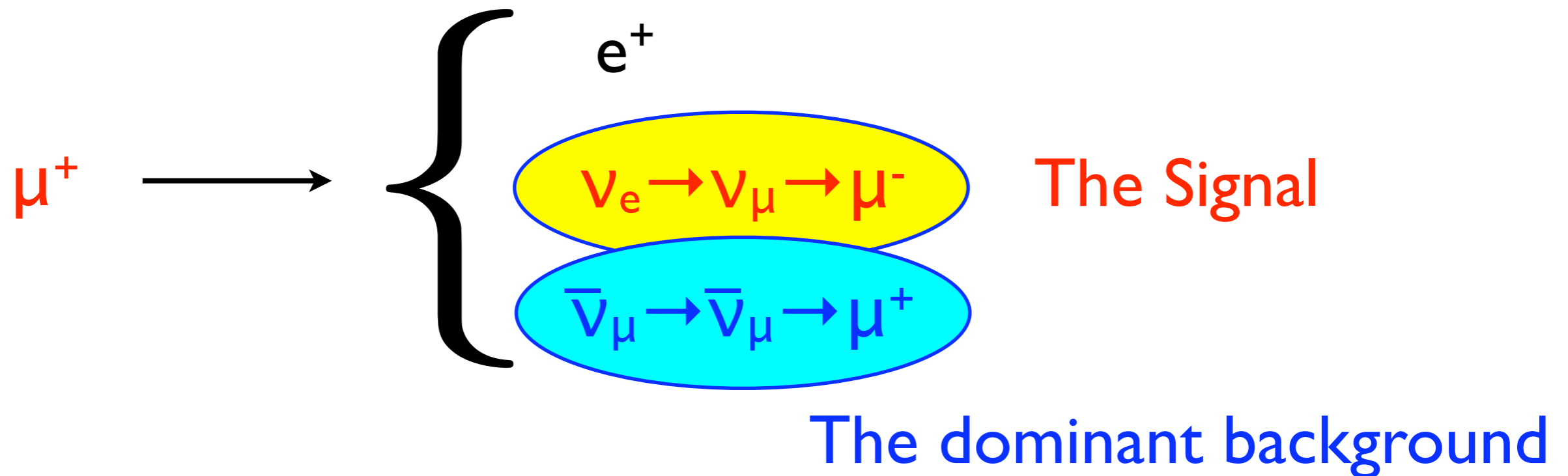
# The Golden Channel

A. Cervera et al, hep-ph/0002108



# The Golden Channel

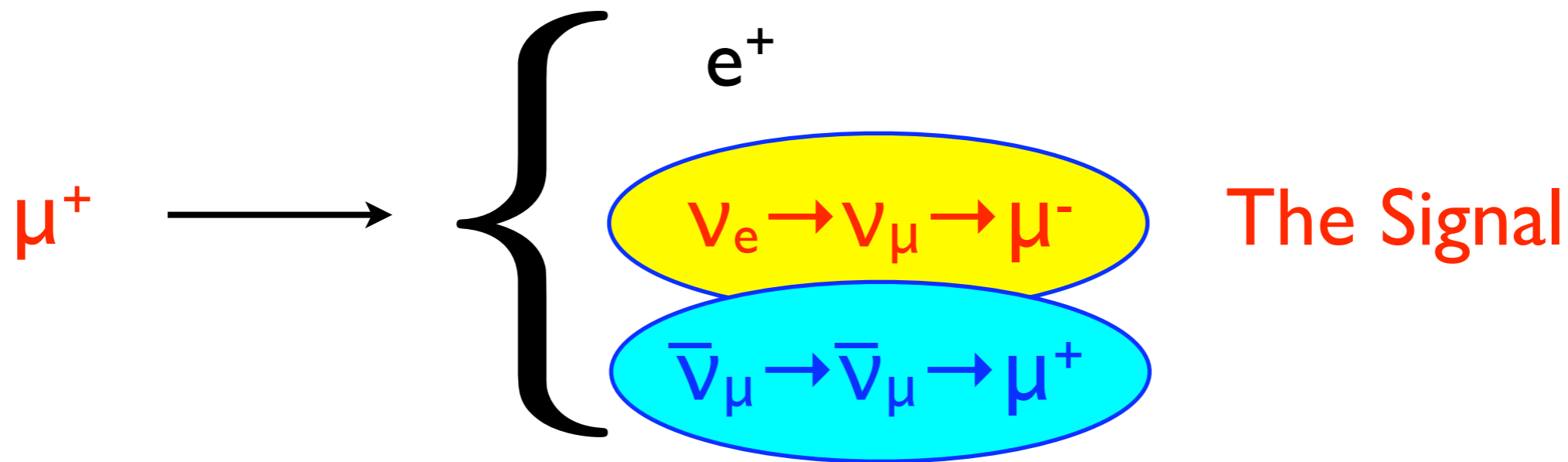
A. Cervera et al, hep-ph/0002108



To look for the signal, at the Neutrino  
Factory we need  $\mu$  charge identification

# The Golden Channel

A. Cervera et al, hep-ph/0002108



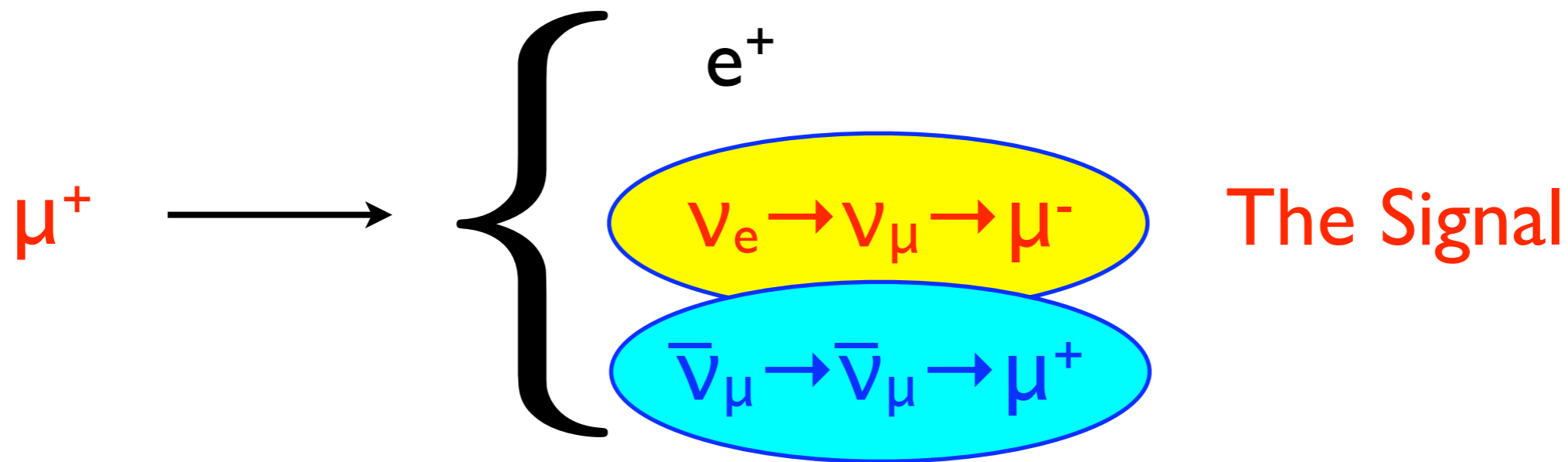
The dominant background

To look for the signal, at the Neutrino Factory we need  $\mu$  charge identification



# The Golden Channel

A. Cervera et al, hep-ph/0002108



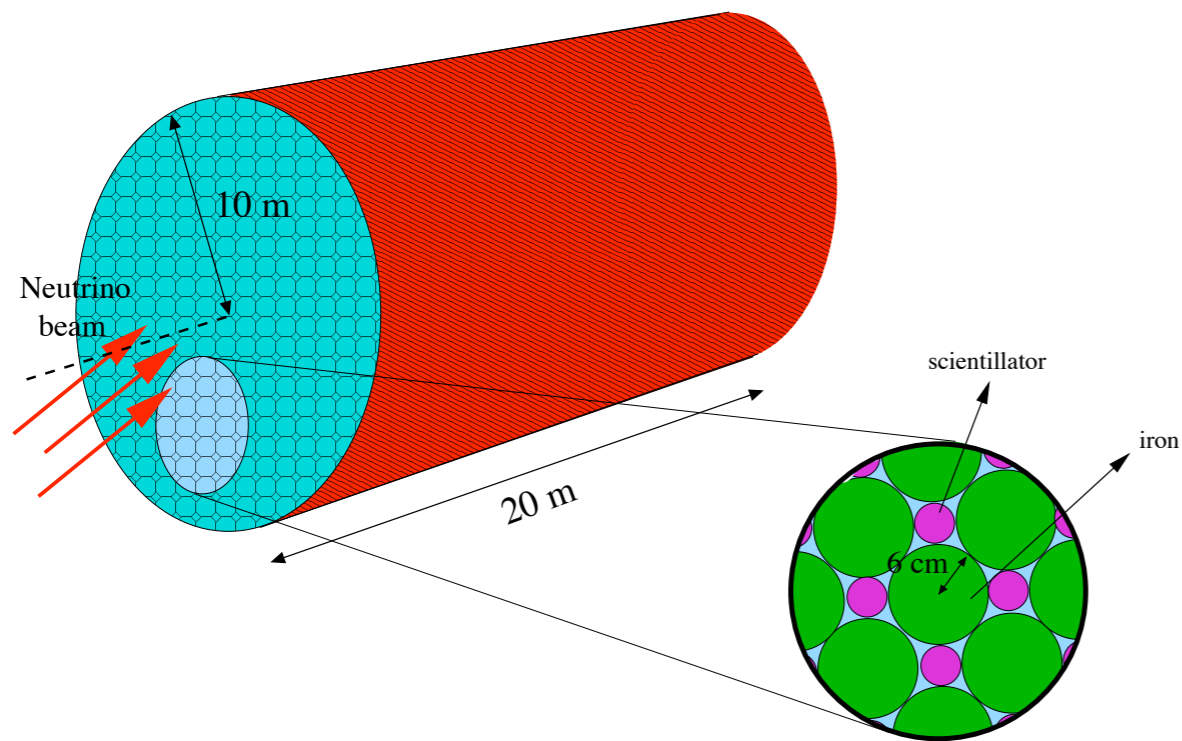
The dominant background

To look for the signal, at the Neutrino Factory we need  $\mu$  charge identification



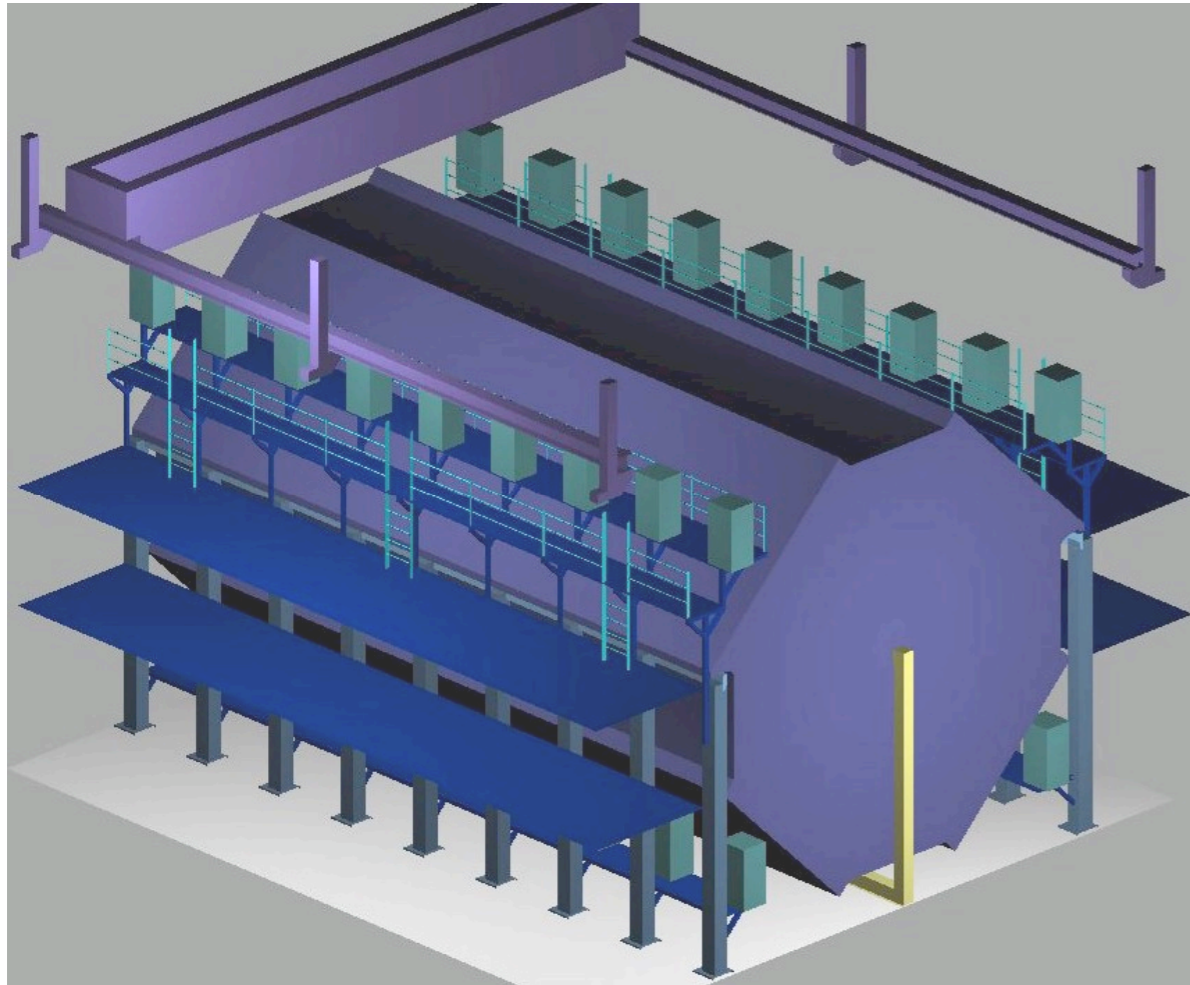
# Magnetized Iron Detector

40-50 Kton Mass



Good Muon Charge  
Identification

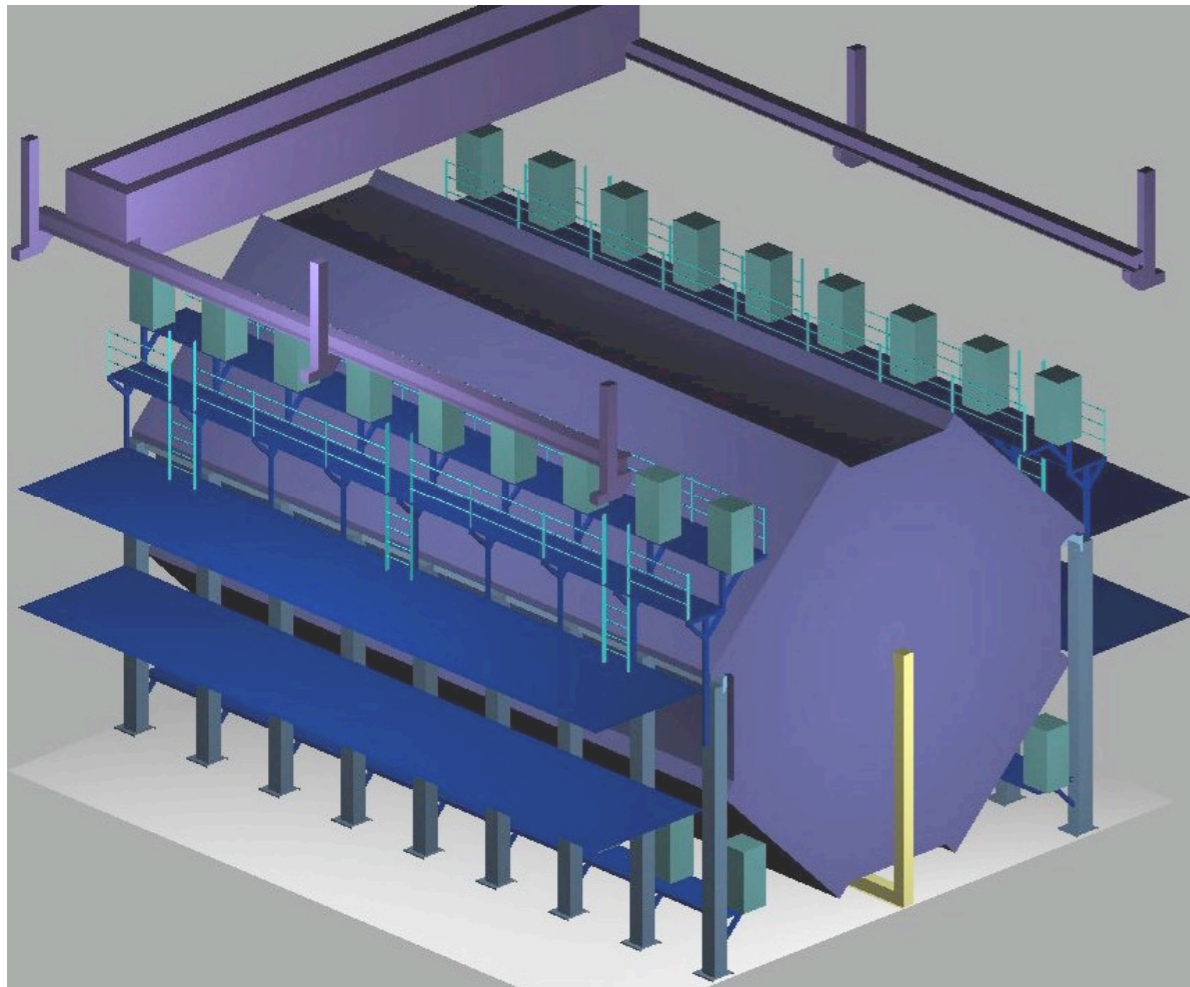
# Magnetized Iron Detector



40-50 Kton Mass

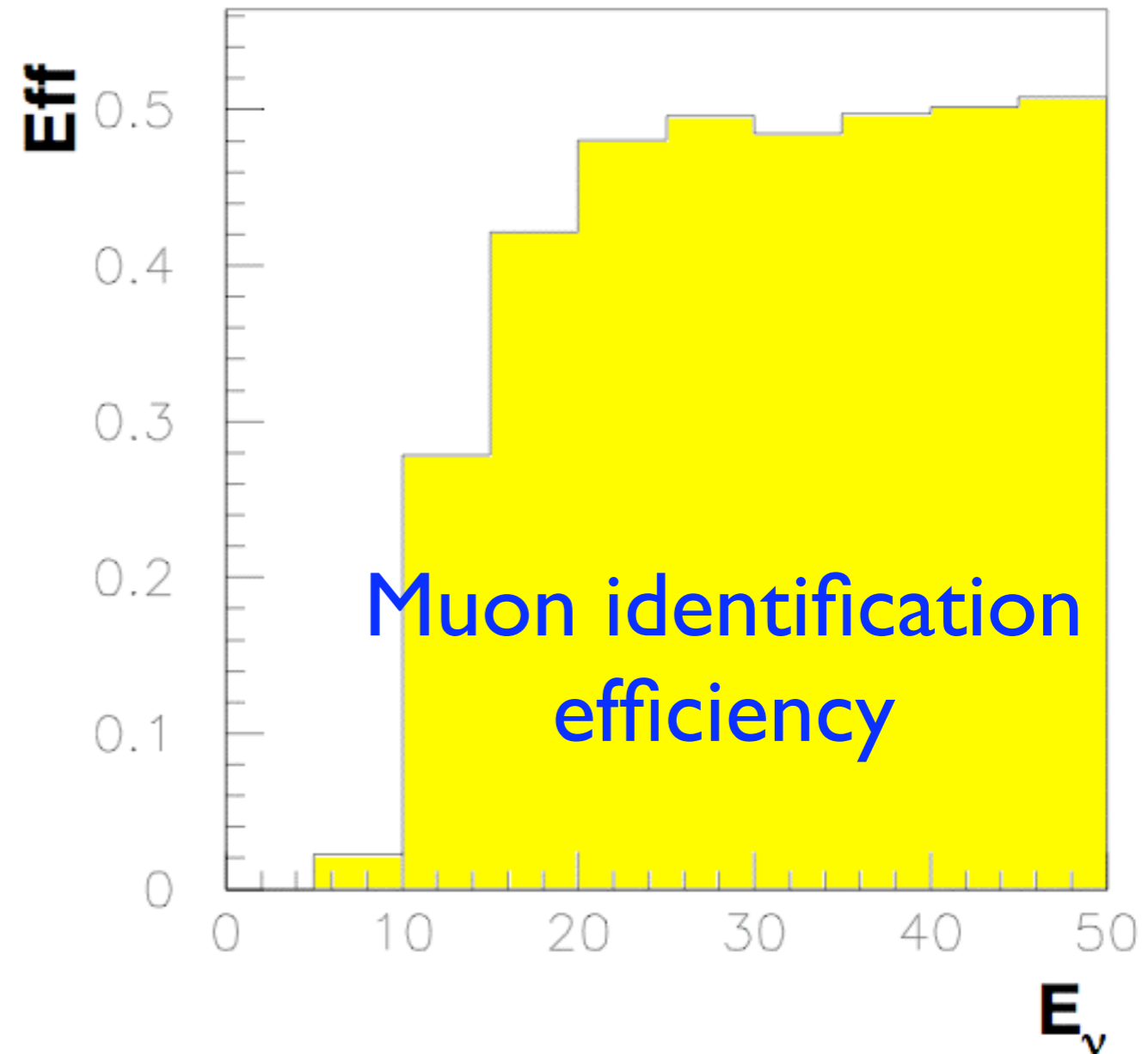
Good Muon Charge  
Identification

# Magnetized Iron Detector

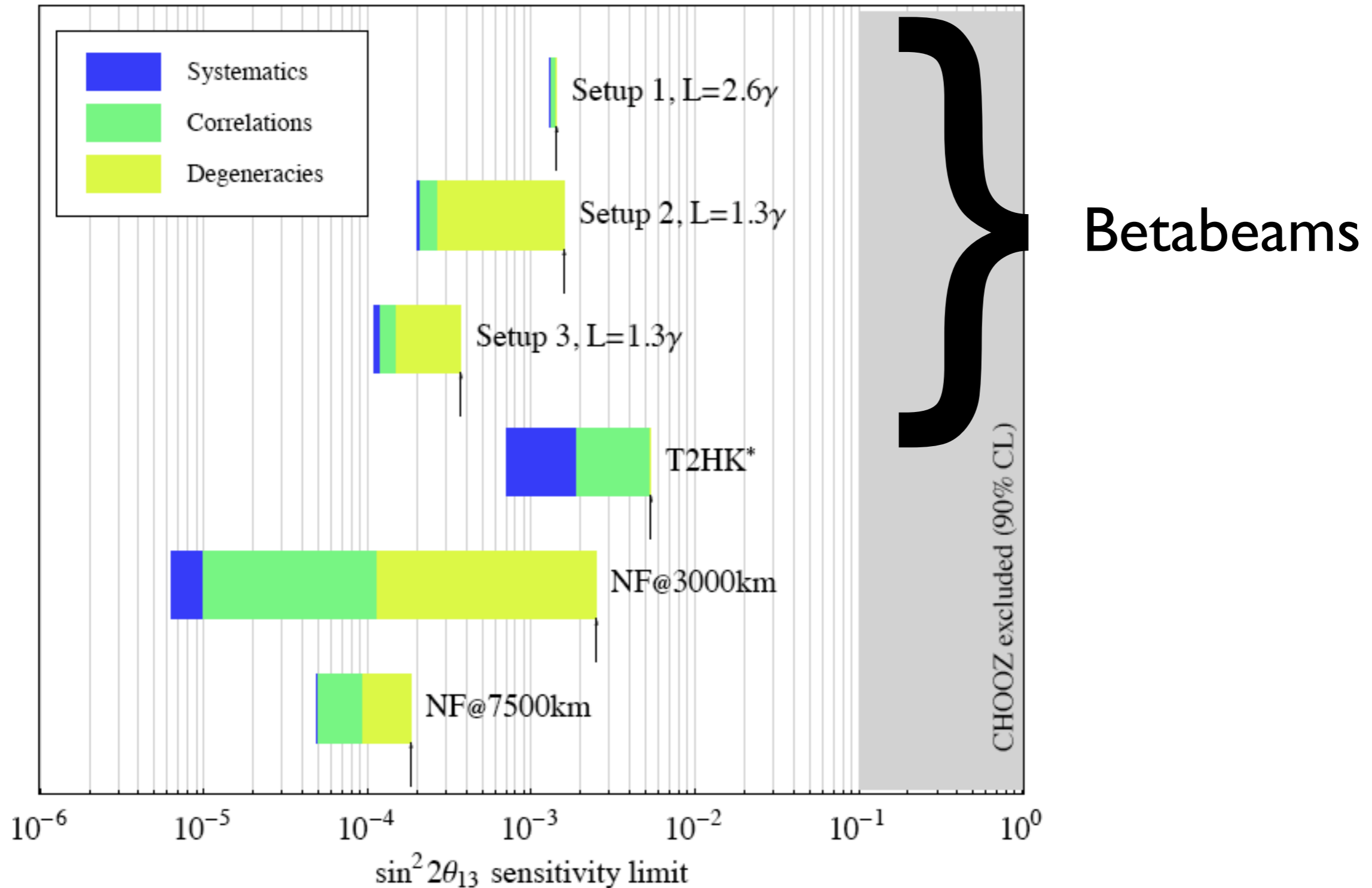


Good Muon Charge Identification

40-50 Kton Mass



# Solving degeneracies





# Solving degeneracies

- Combining channels: Silver and Platinum
- Combining baselines: the Magic baseline
- Combining energies: improving the detector

# The Silver Channel

$$P_{e\tau}^{\pm} = X_{\tau}^{\pm} \sin^2 2\theta_{13} - (Y_c^{\pm} \cos\delta \mp Y_s^{\pm} \sin\delta) \sin 2\theta_{13} + Z_{\tau}$$

$$X_{\tau}^{\pm} = \frac{c_{23}^2}{s_{23}^2} X_{\mu}^{\pm} \quad Z_{\tau} = \frac{s_{23}^2}{c_{23}^2} Z_{\mu}$$

Donini, Meloni and Migliozzi '02

# The Silver Channel

$$P_{e\tau}^{\pm} = X_{\tau}^{\pm} \sin^2 2\theta_{13} - (Y_c^{\pm} \cos\delta \mp Y_s^{\pm} \sin\delta) \sin 2\theta_{13} + Z_{\tau}$$

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Donini, Meloni and Migliozzi '02

Same sensitivities as the Golden Channel

# The Silver Channel

$$P_{e\tau}^{\pm} = X_{\tau}^{\pm} \sin^2 2\theta_{13} - (Y_c^{\pm} \cos\delta \mp Y_s^{\pm} \sin\delta) \sin 2\theta_{13} + Z_{\tau}$$

$$X_{\tau}^{\pm} = \frac{c_{23}^2}{s_{23}^2} X_{\mu}^{\pm}$$

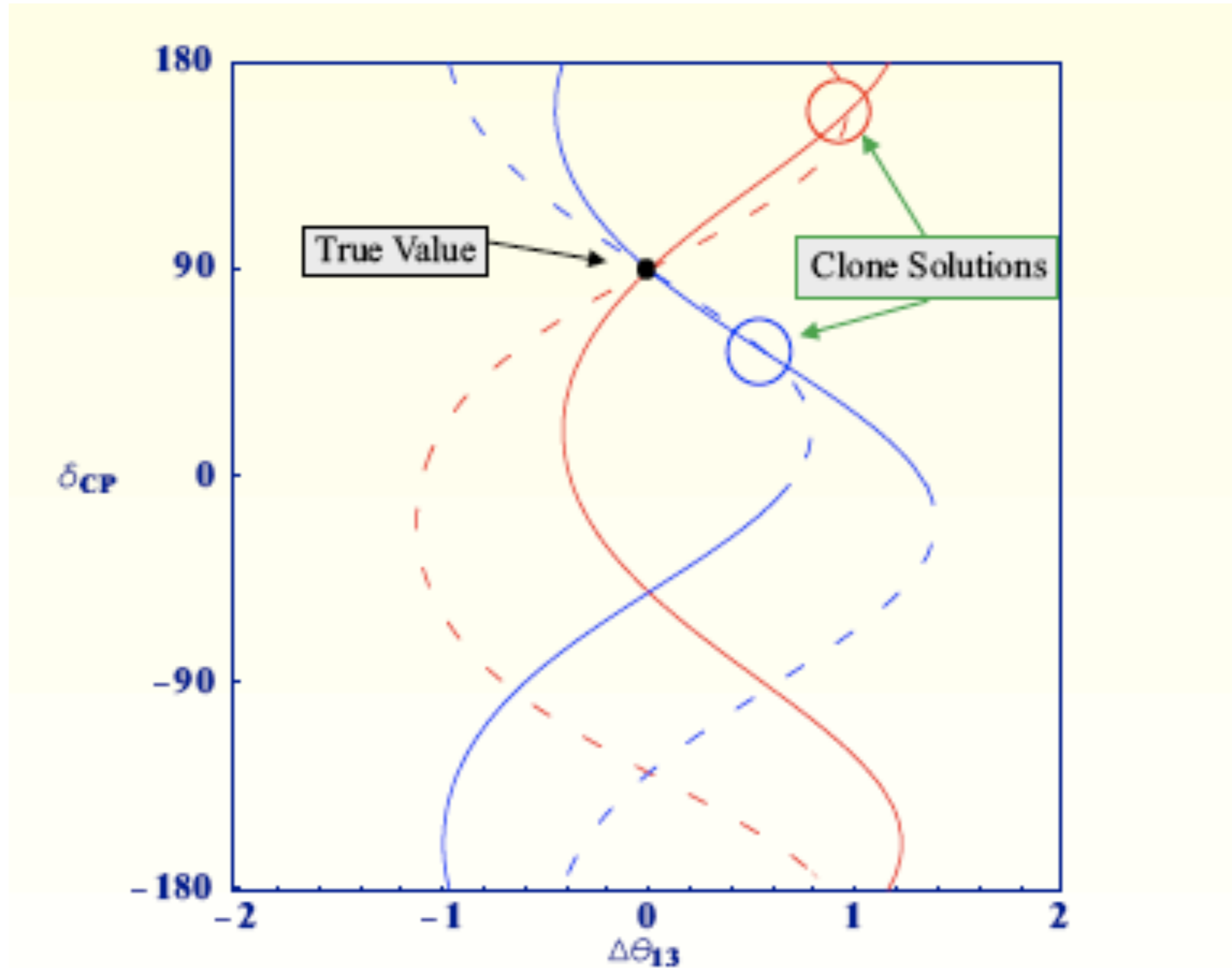
$$Z_{\tau} = \frac{s_{23}^2}{c_{23}^2} Z_{\mu}$$

Donini, Meloni and Migliozzi '02

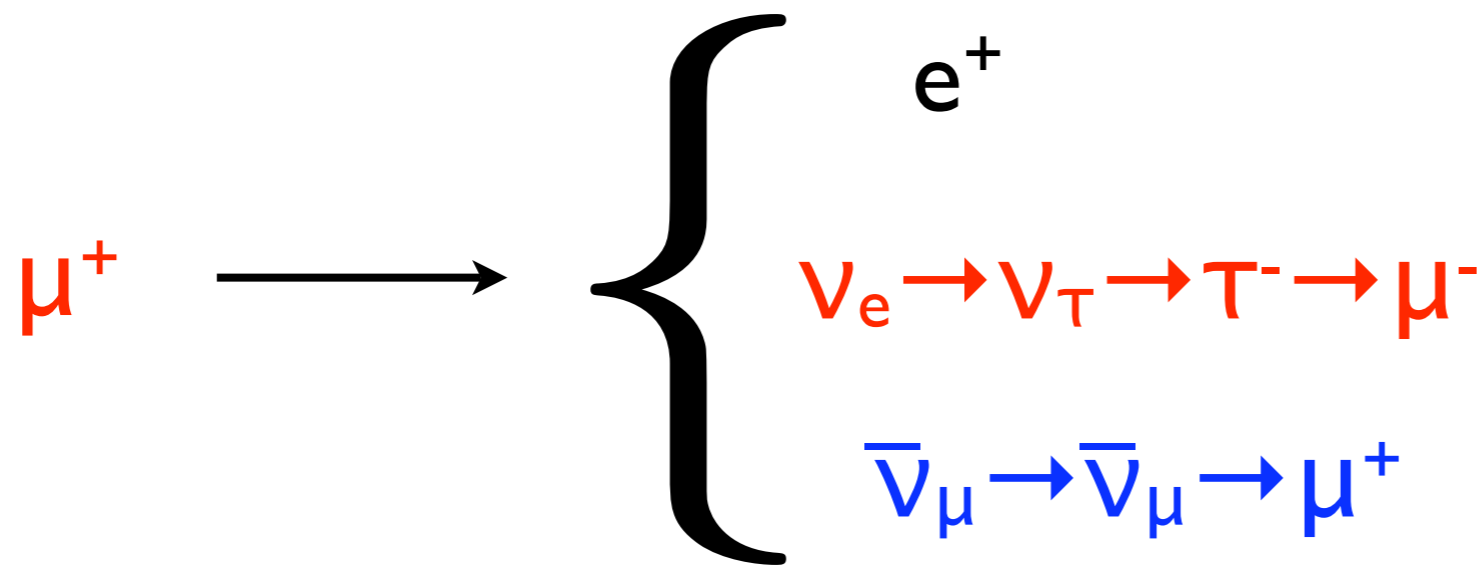
Different  $\theta_{13}$ - $\delta$  correlation

Same sensitivities as the Golden Channel

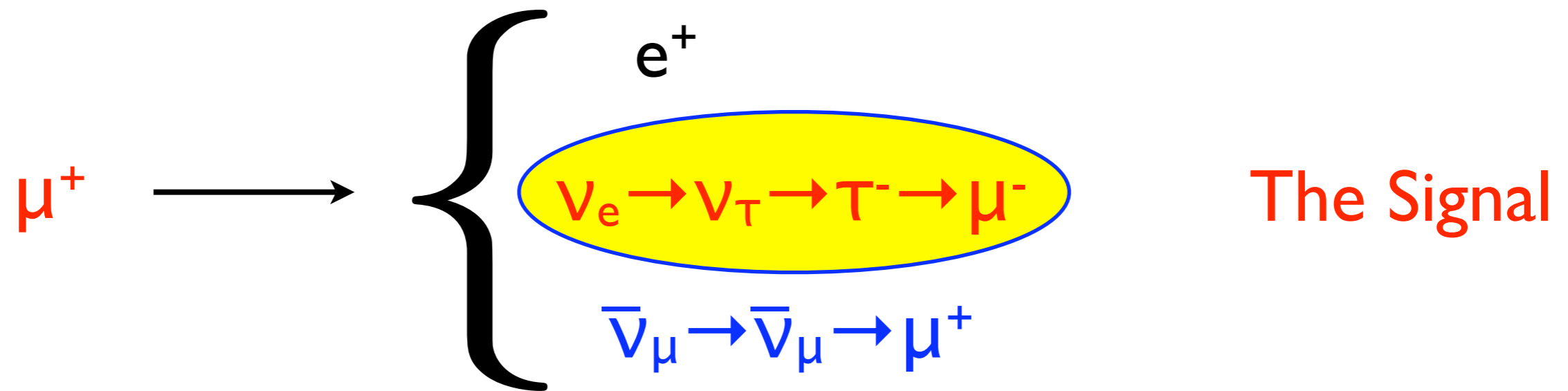
# How the silver channel solve the intrinsic degeneracy



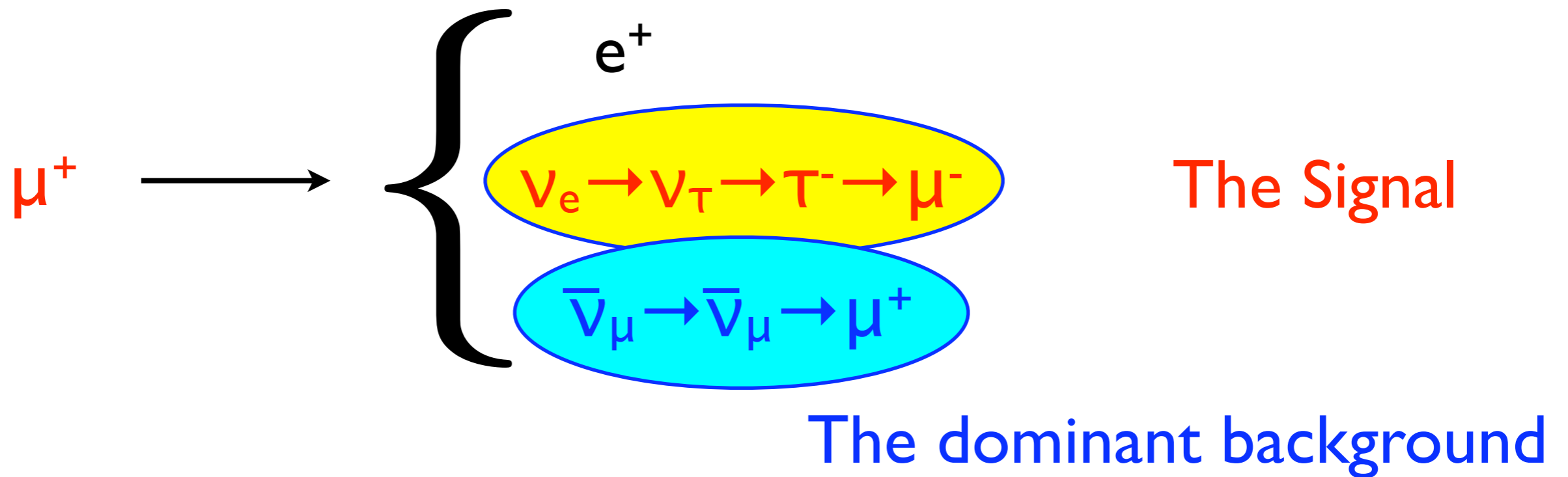
# The Silver Channel



# The Silver Channel

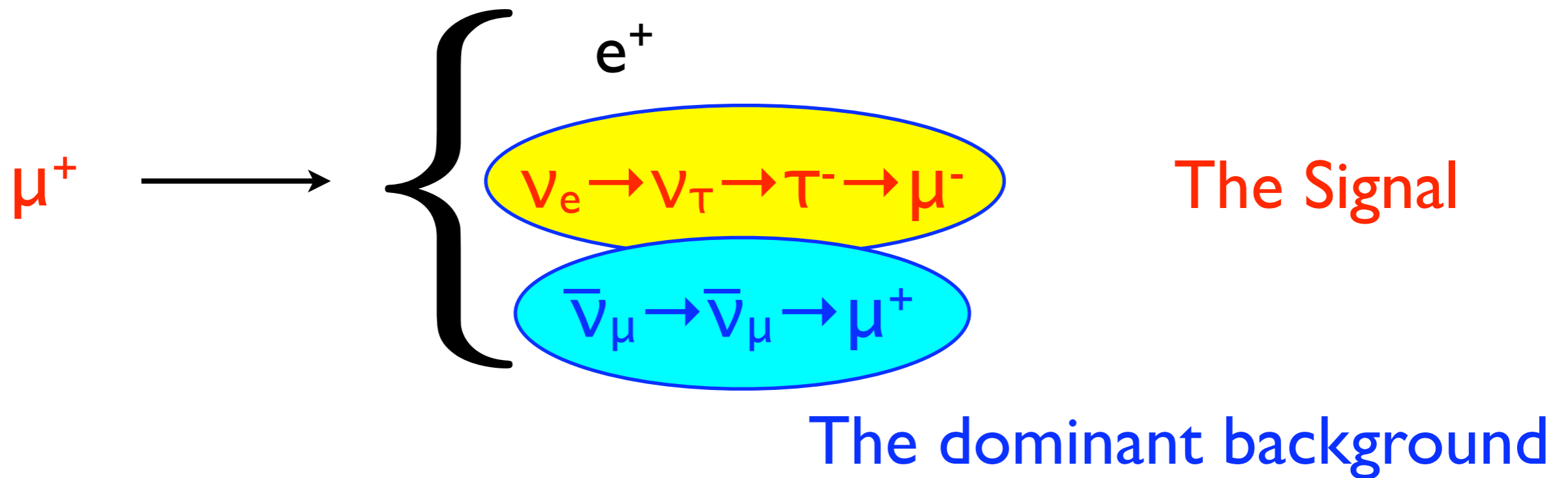


# The Silver Channel



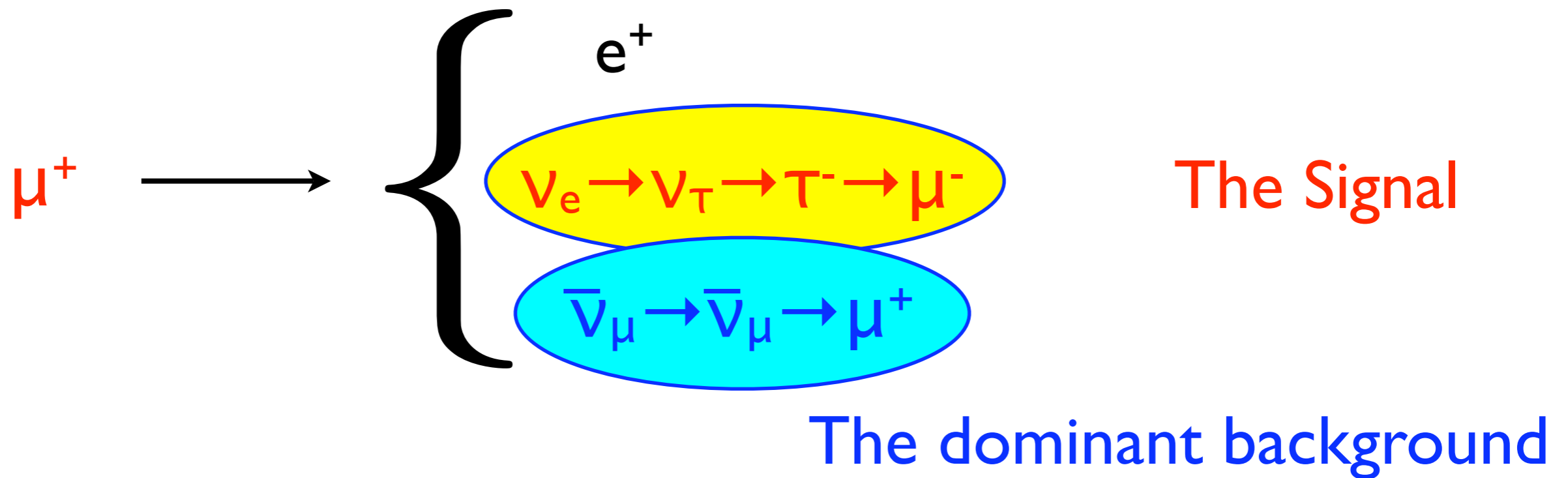


# The Silver Channel



To look for the signal, we need  $\mu$  charge identification and  $\tau$  decay vertex identification

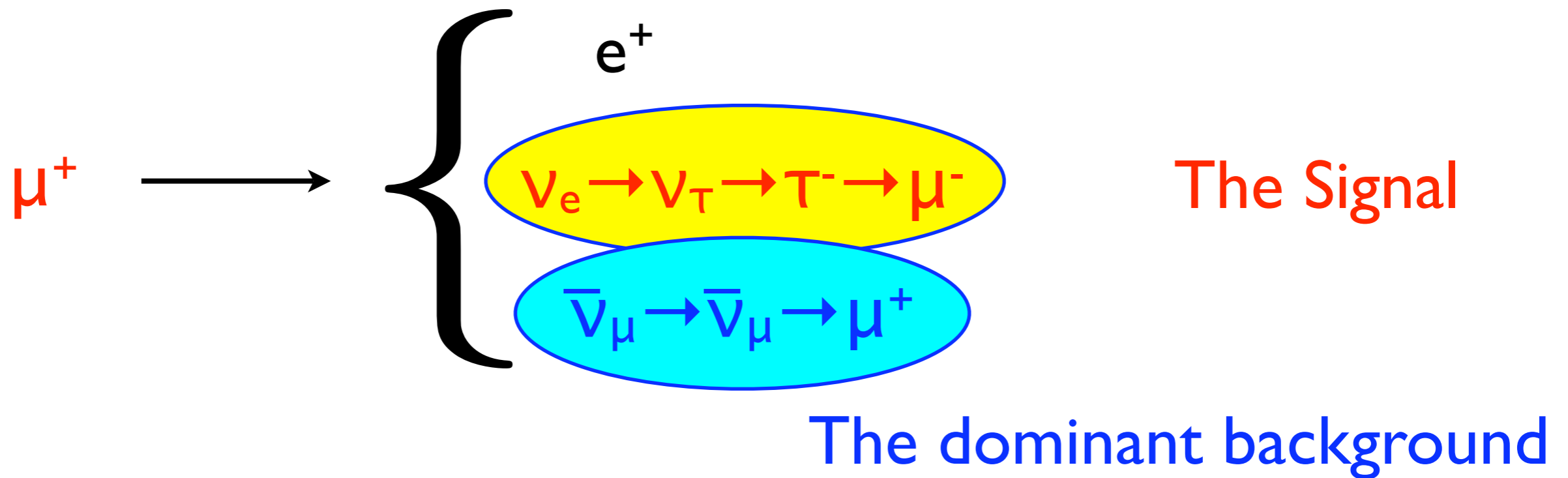
# The Silver Channel



To look for the signal, we need  $\mu$  charge identification and  $\tau$  decay vertex identification



# The Silver Channel

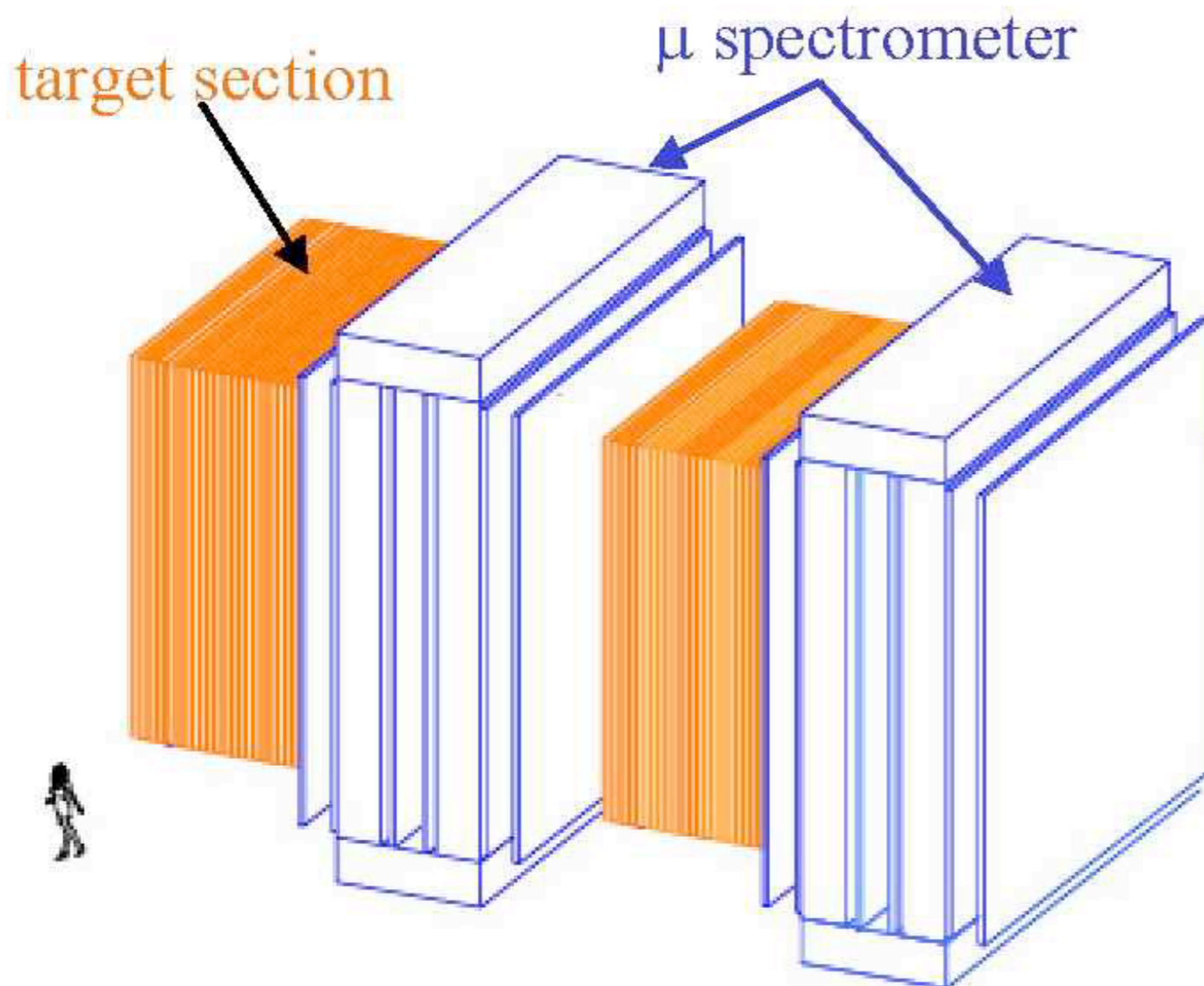


To look for the signal, we need  $\mu$  charge identification and  $\tau$  decay vertex identification



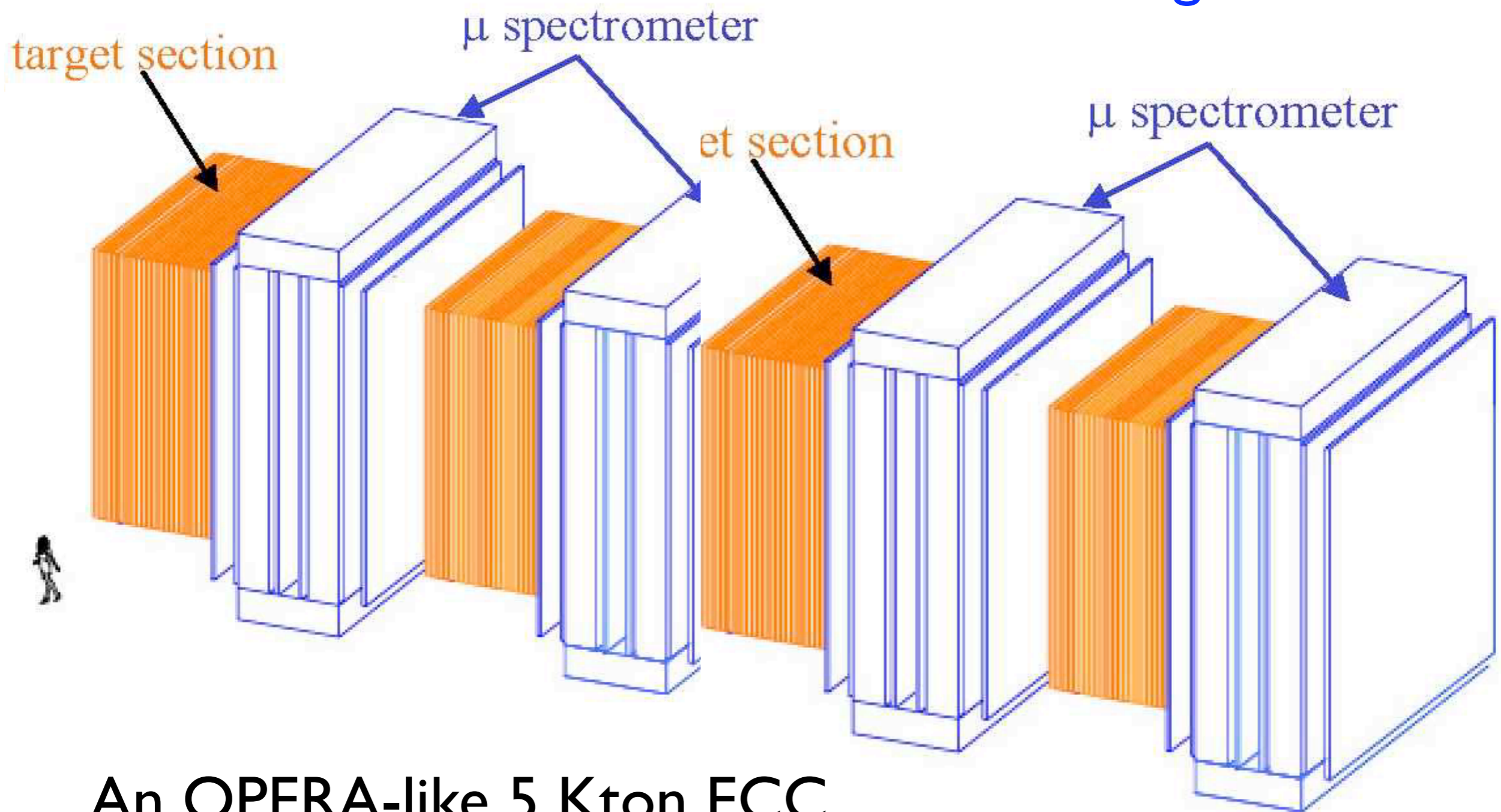
# Emulsion Cloud Chamber

Evolution: Magnetized ECC



# Emulsion Cloud Chamber

Evolution: Magnetized ECC



An OPERA-like 5 Kton ECC

# The Platinum Channel

$$P_{\mu e}^{\pm} = X_{\mu}^{\mp} \sin^2 2\theta_{13} + (Y_c^{\mp} \cos\delta \pm Y_s^{\mp} \sin\delta) \sin 2\theta_{13} + Z_{\mu}$$

$$X_{\mu}^{\pm} \rightarrow X_{\mu}^{\mp} \quad Y_{s,c}^{\pm} \rightarrow Y_{s,c}^{\mp}$$

Bueno, Campanelli and Rubbia '00

Same sensitivities as the Golden Channel

# The Platinum Channel

$$P_{\mu e}^{\pm} = X_{\mu}^{\mp} \sin^2 2\theta_{13} + (Y_c^{\mp} \cos \delta \pm Y_s^{\mp} \sin \delta) \sin 2\theta_{13} + Z_{\mu}$$

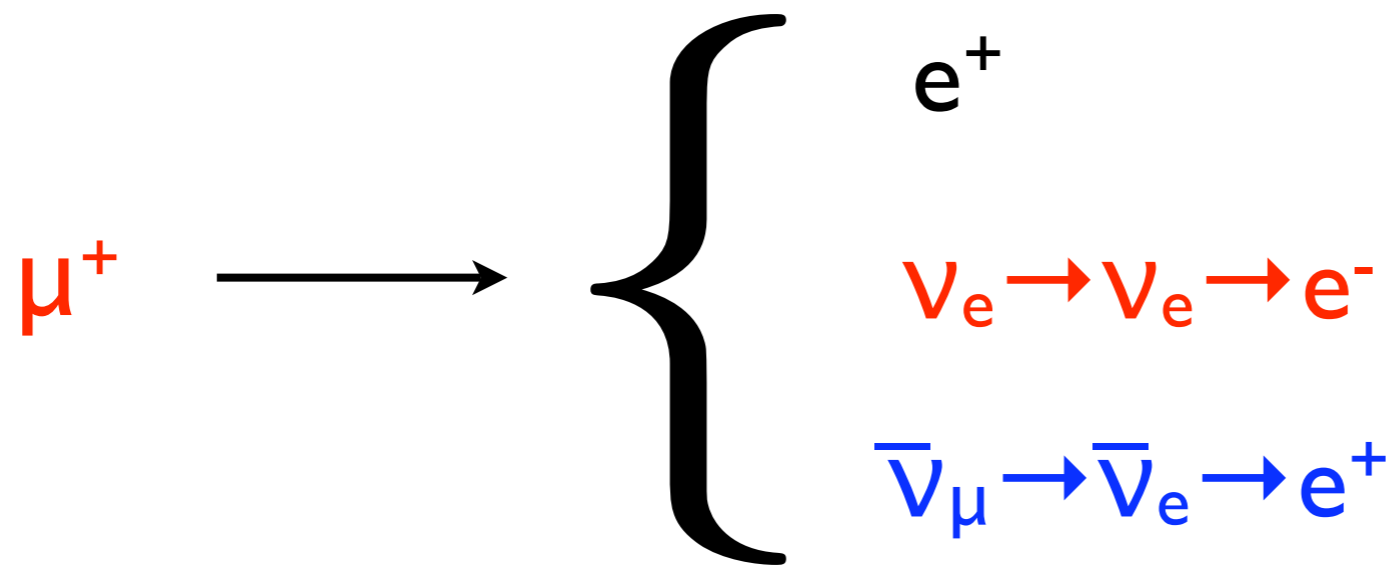
$$X_{\mu}^{\pm} \rightarrow X_{\mu}^{\mp} \quad Y_{s,c}^{\pm} \rightarrow Y_{s,c}^{\mp}$$

Bueno, Campanelli and Rubbia '00

Different  $\theta_{13}$ - $\delta$  correlation

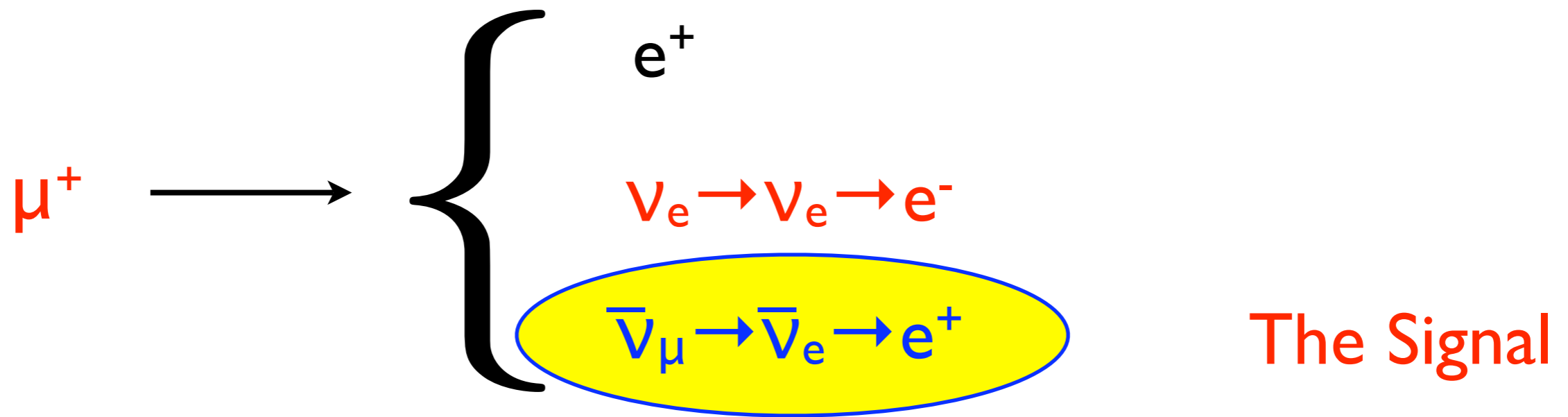
Same sensitivities as the Golden Channel

# The Platinum Channel

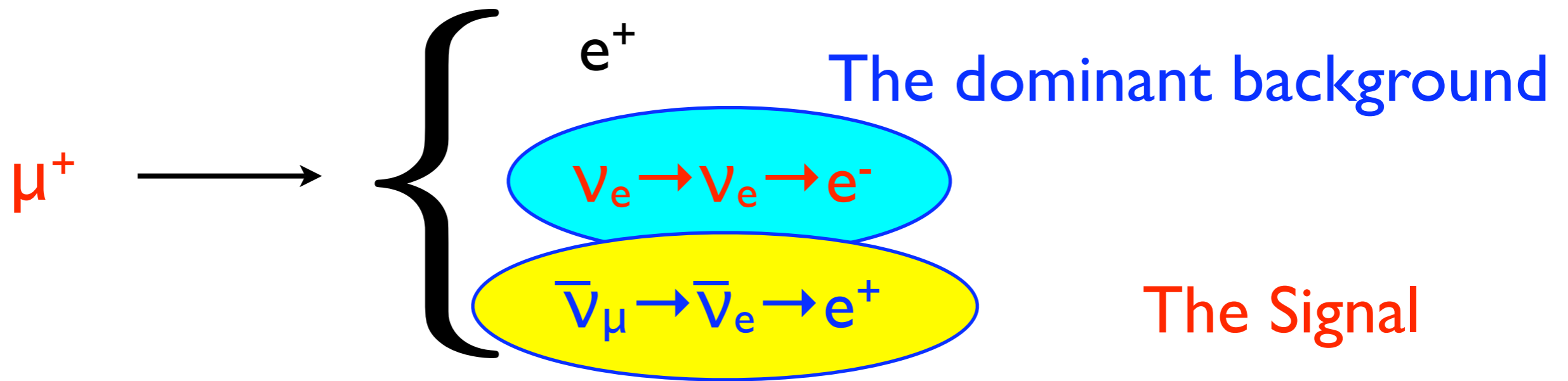




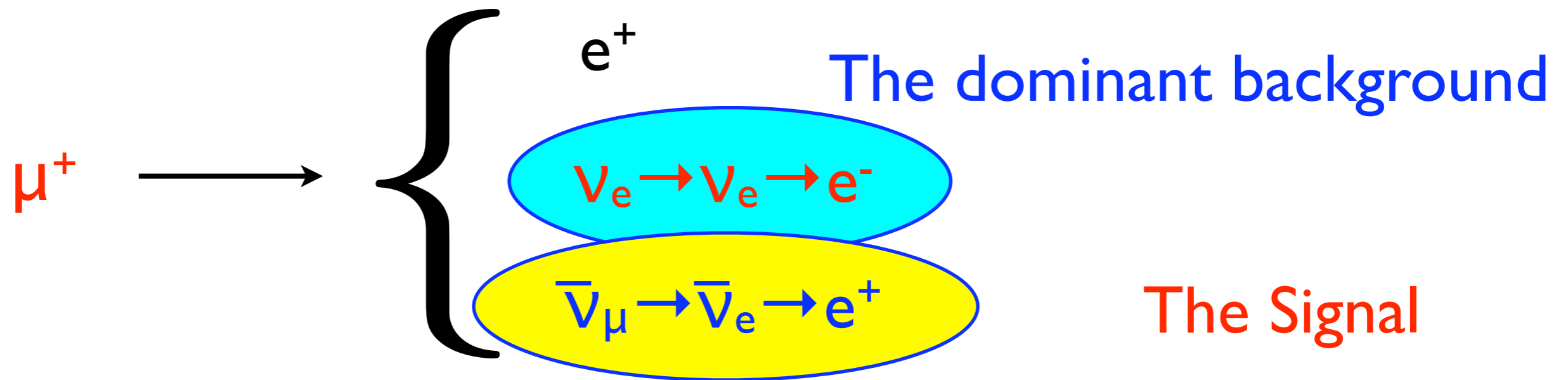
# The Platinum Channel



# The Platinum Channel

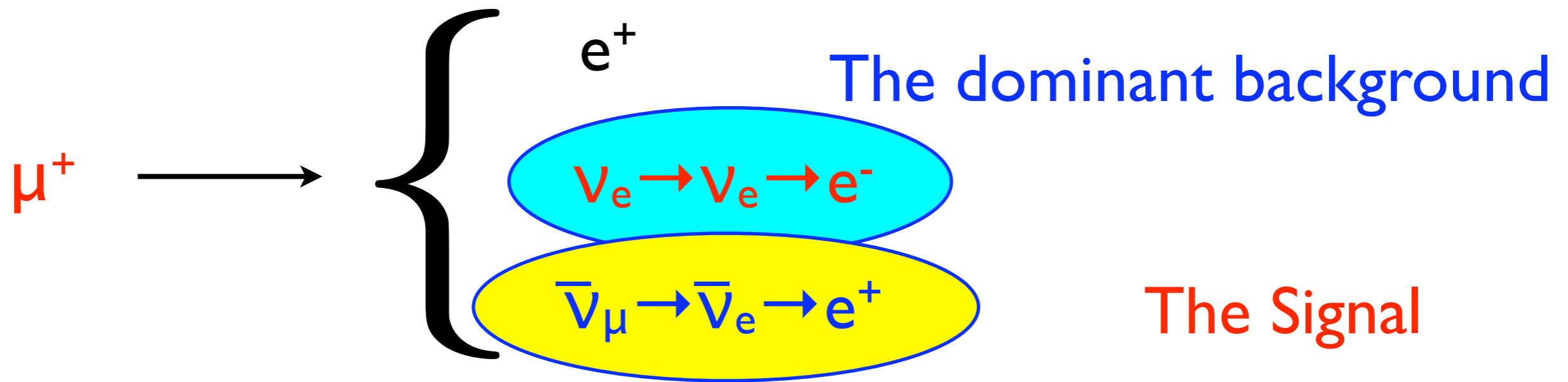


# The Platinum Channel



To look for the signal, we need **e charge identification**

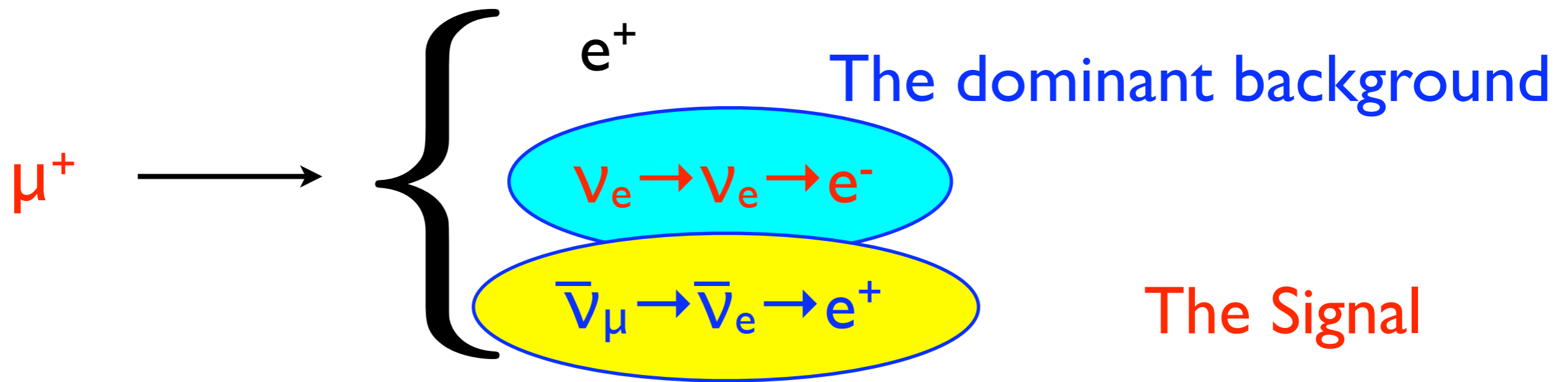
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# The Platinum Channel

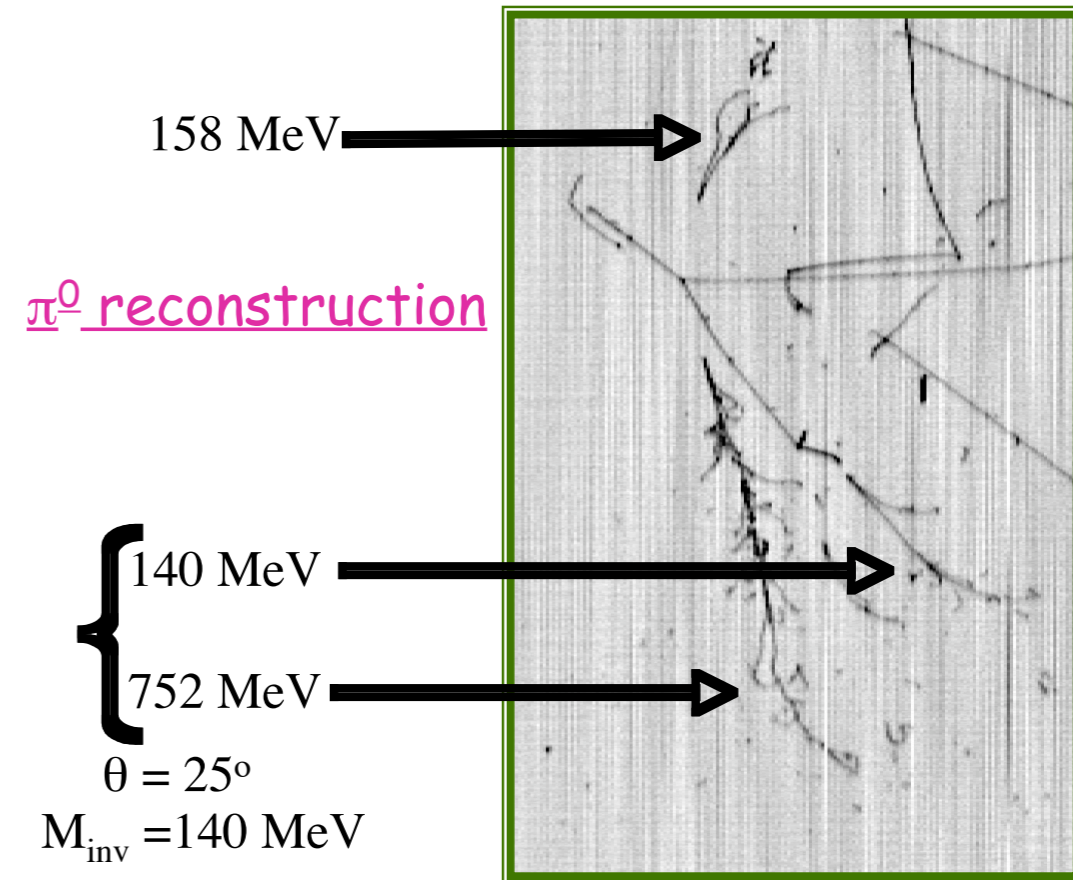
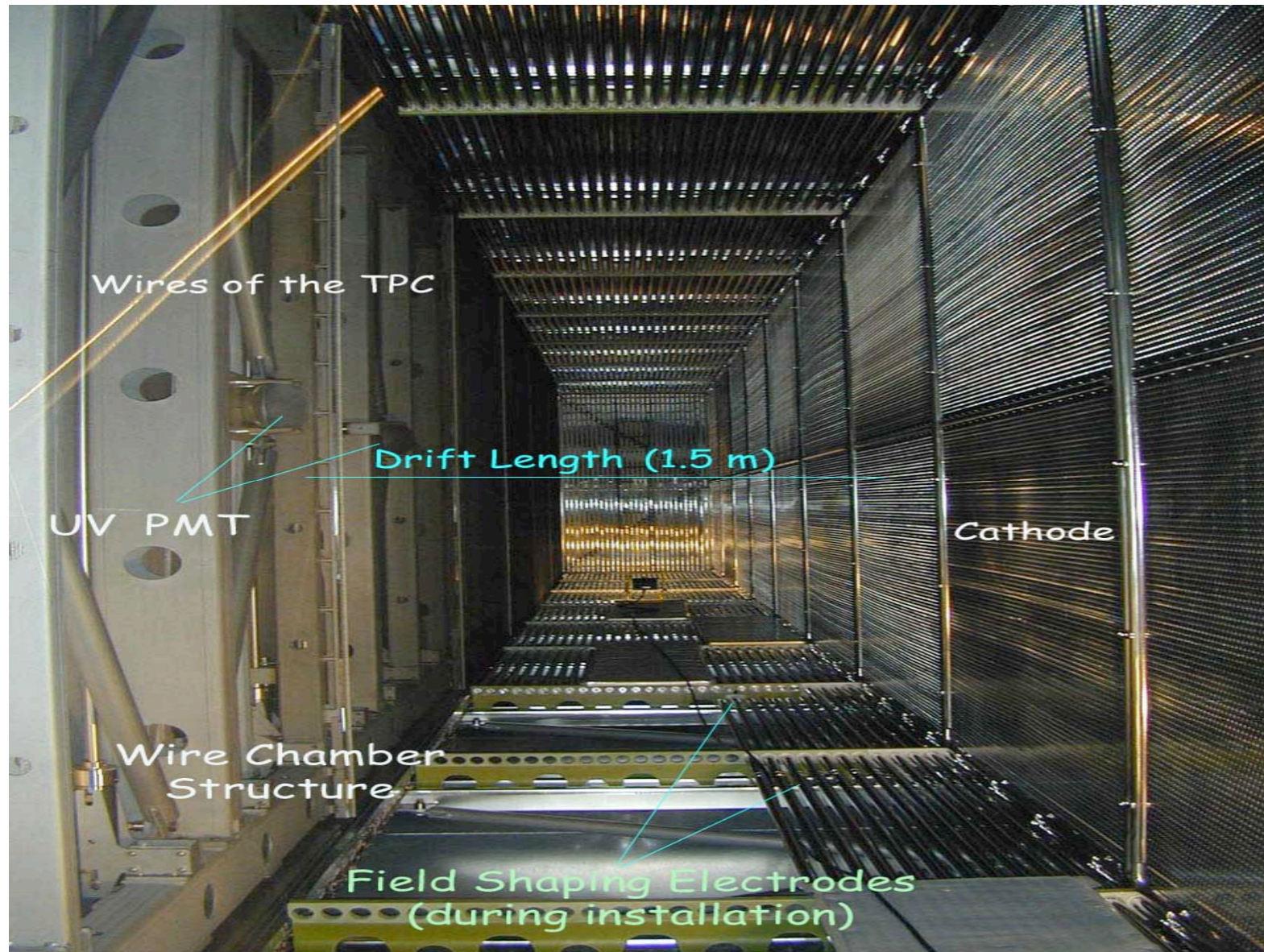


To look for the signal, we need **e charge identification**



# Liquid Argon TPC

Feasibility proved at T600

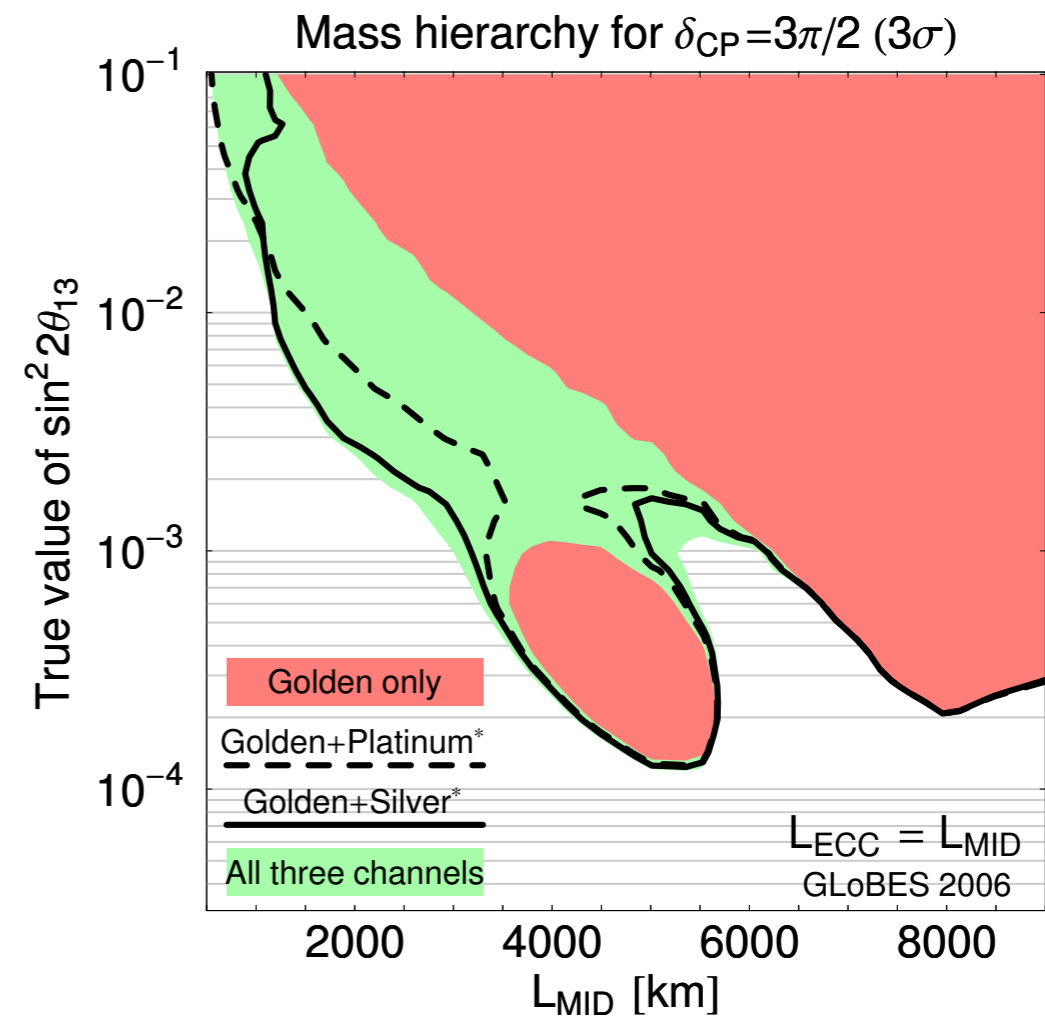
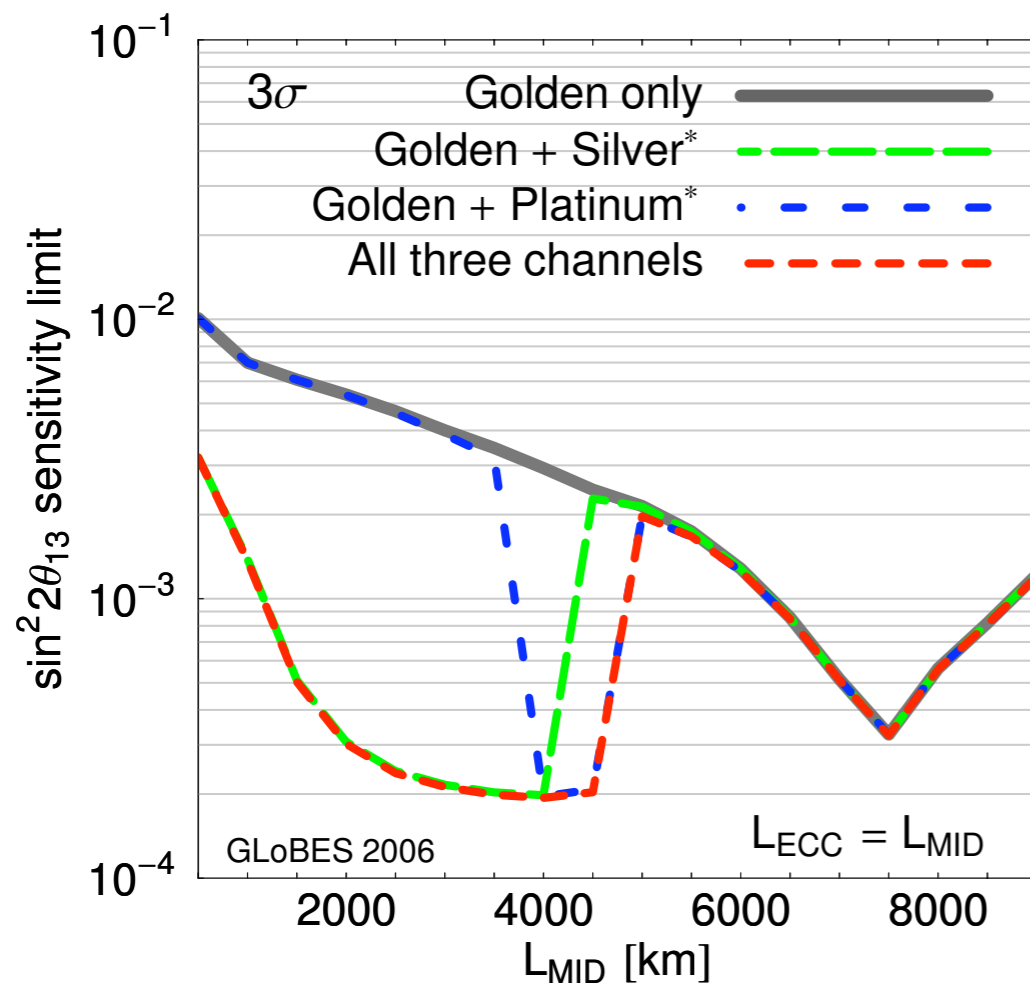


T600 test @ Pavia:  
Run 201 - Evt 12

10-100 Kton Mass

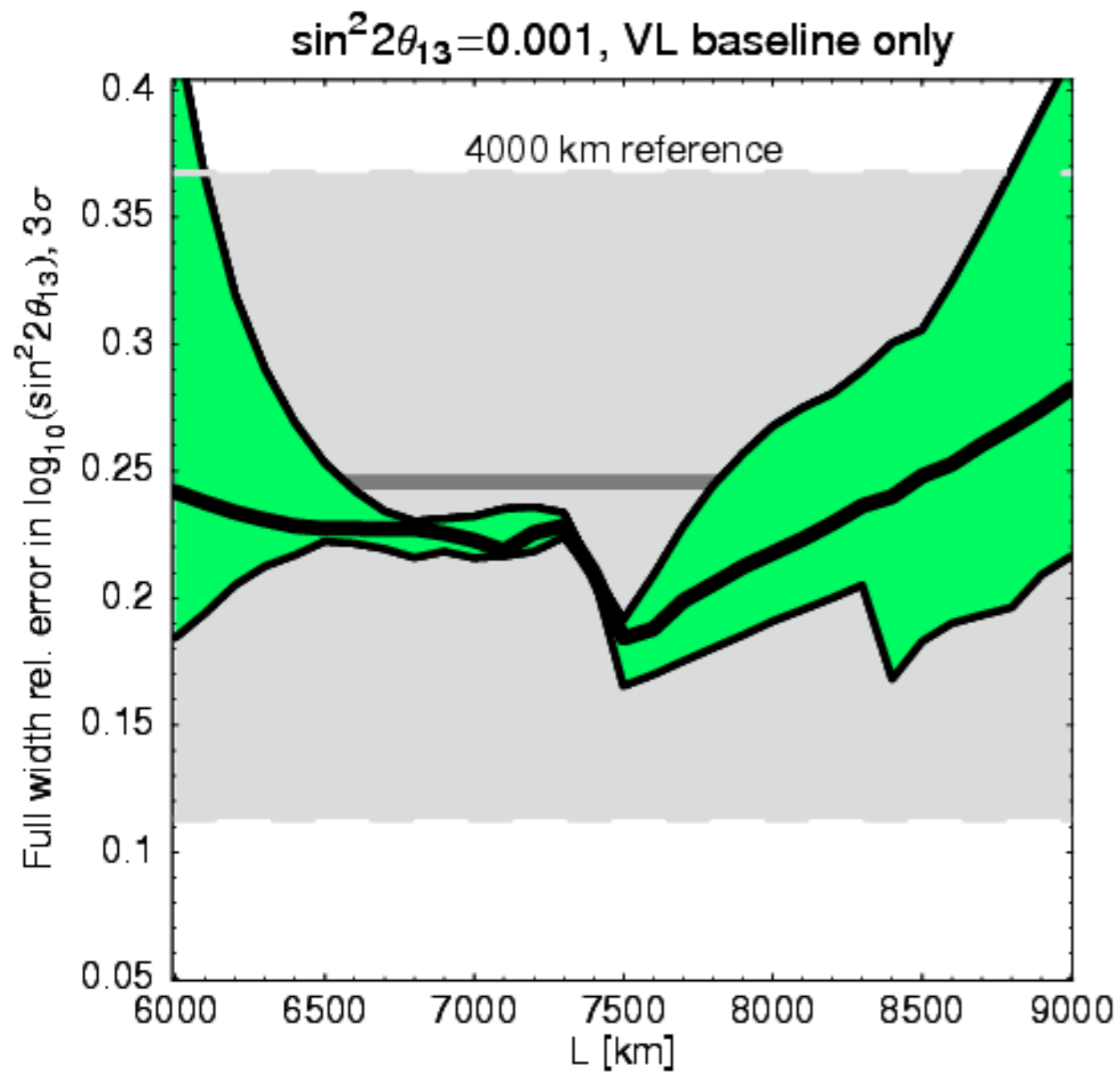
# Channels Combination

The main limitation of silver and platinum channels is **statistics**



Huber, Lindner, Rolinec and Winter '06

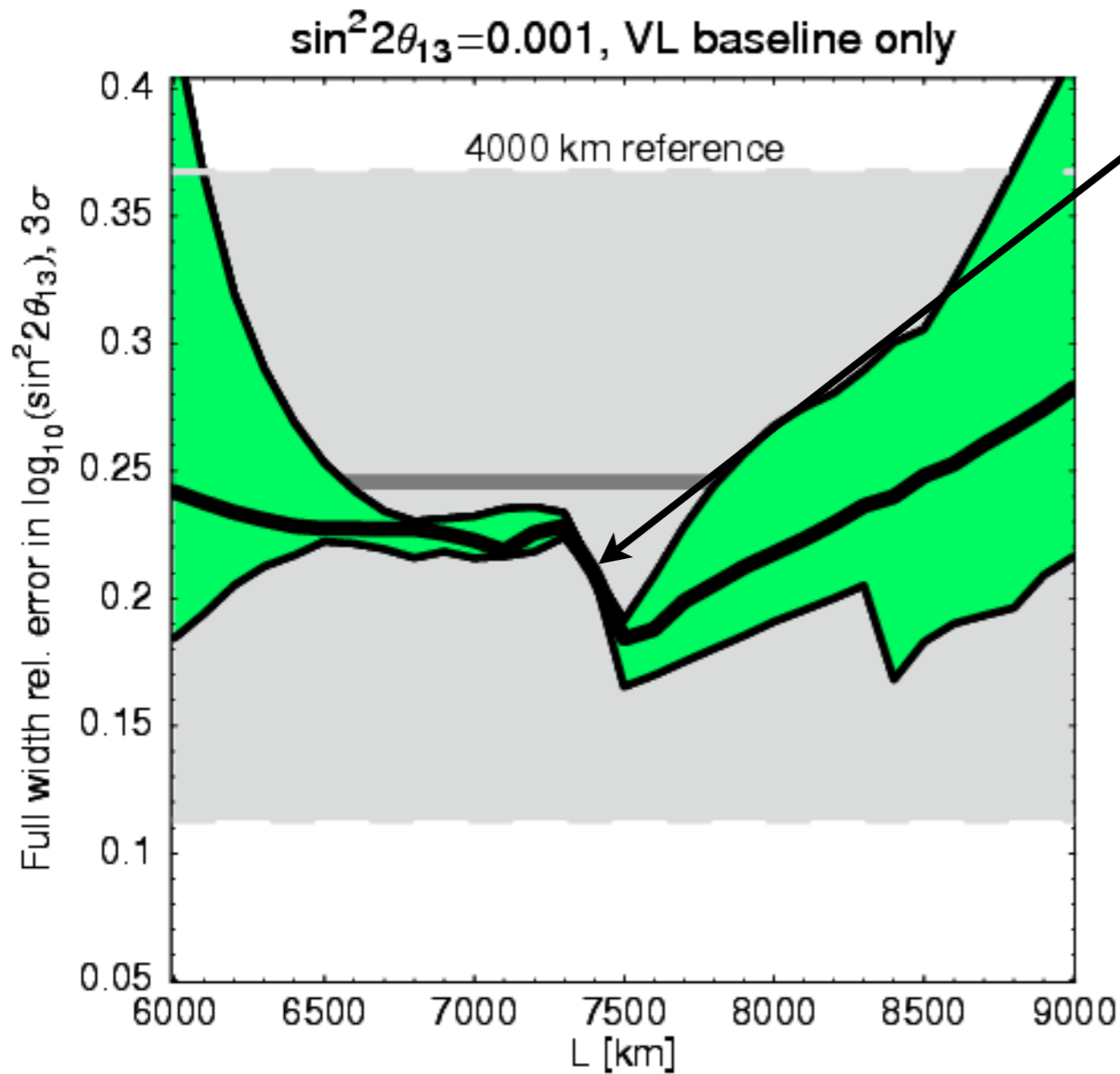
# The Magic Baseline



Huber and Winter '03



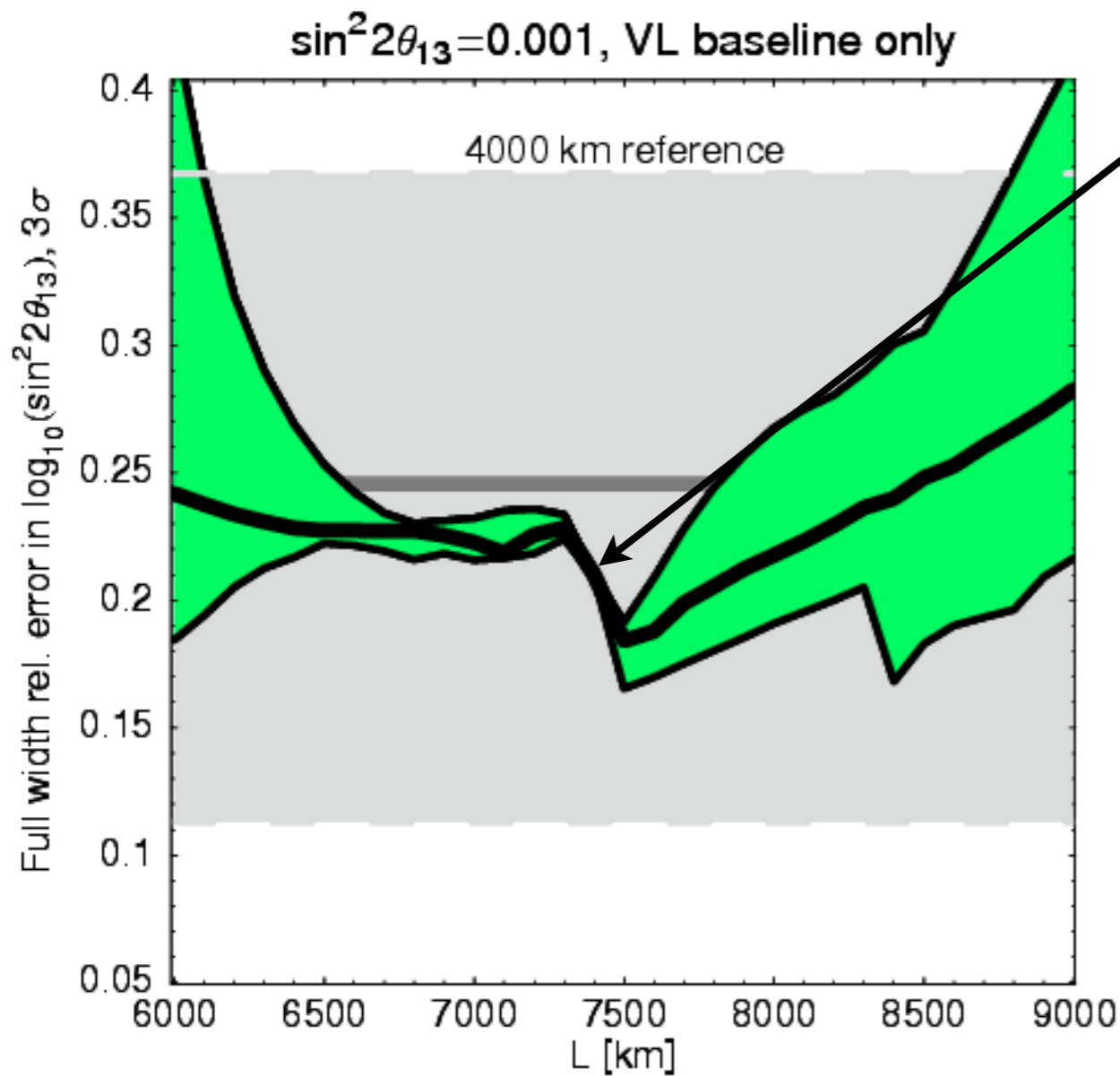
# The Magic Baseline



At this baseline, no dependence on  $\delta$

Huber and Winter '03

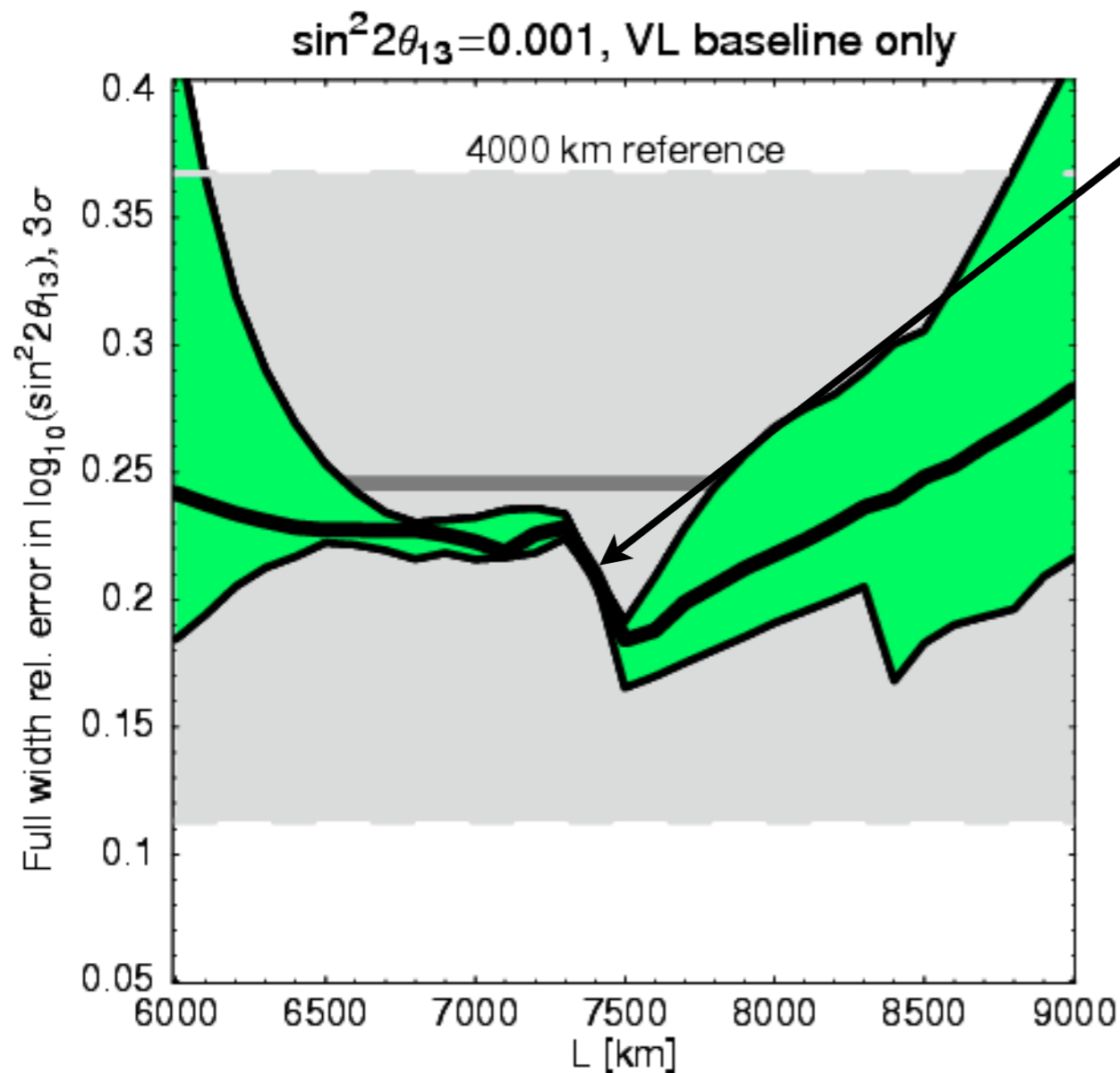
# The Magic Baseline



At this baseline, no  
dependence on  $\delta$   
Also, no sensitivity at all....

Huber and Winter '03

# The Magic Baseline

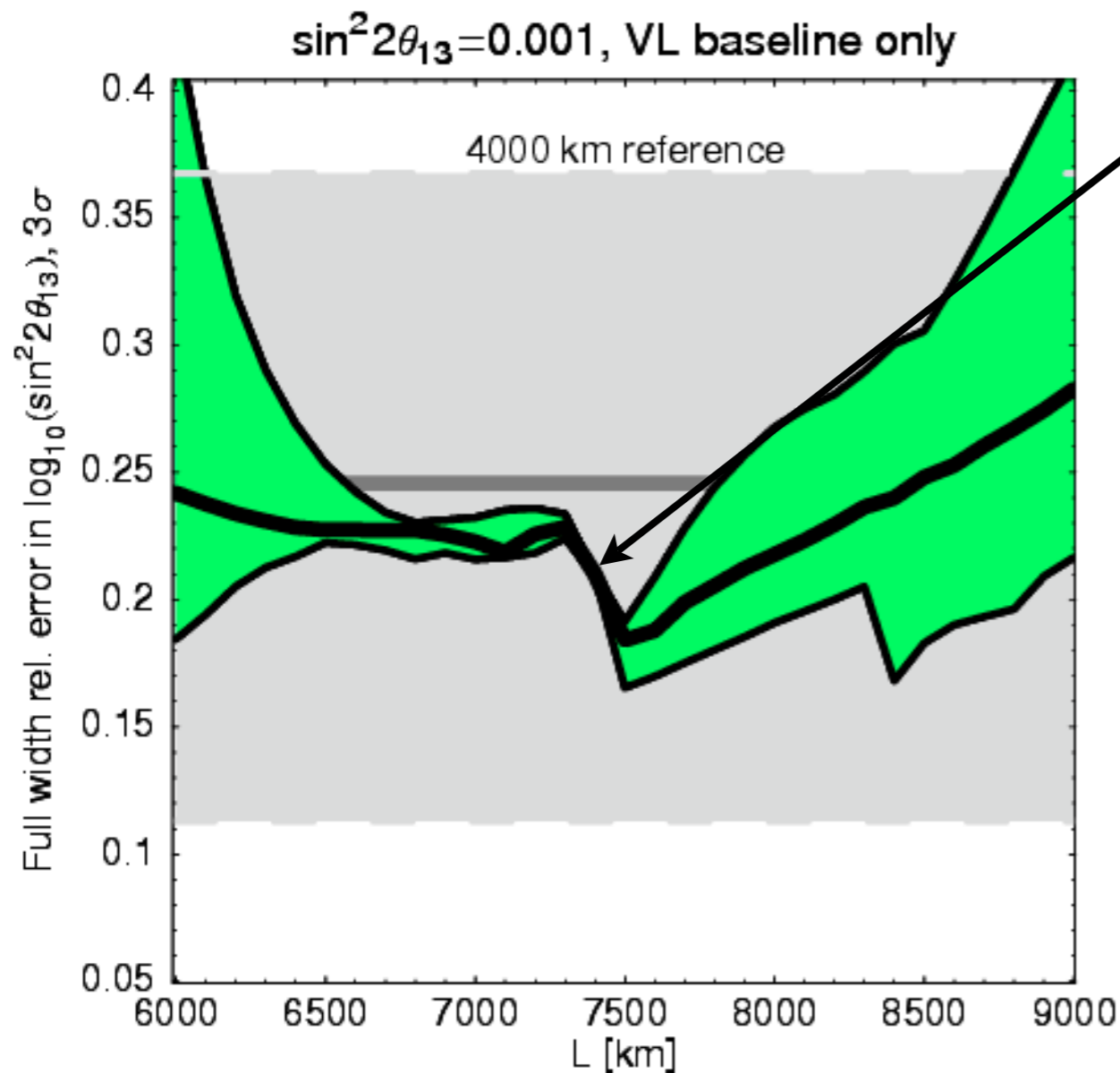


At this baseline, no dependence on  $\delta$   
Also, no sensitivity at all...

Good to measure  $\theta_{13}$   
and the sign of  $\Delta m^2_{13}$

Huber and Winter '03

# The Magic Baseline



Huber and Winter '03

At this baseline, **no dependence on  $\delta$**   
Also, **no sensitivity at all...**

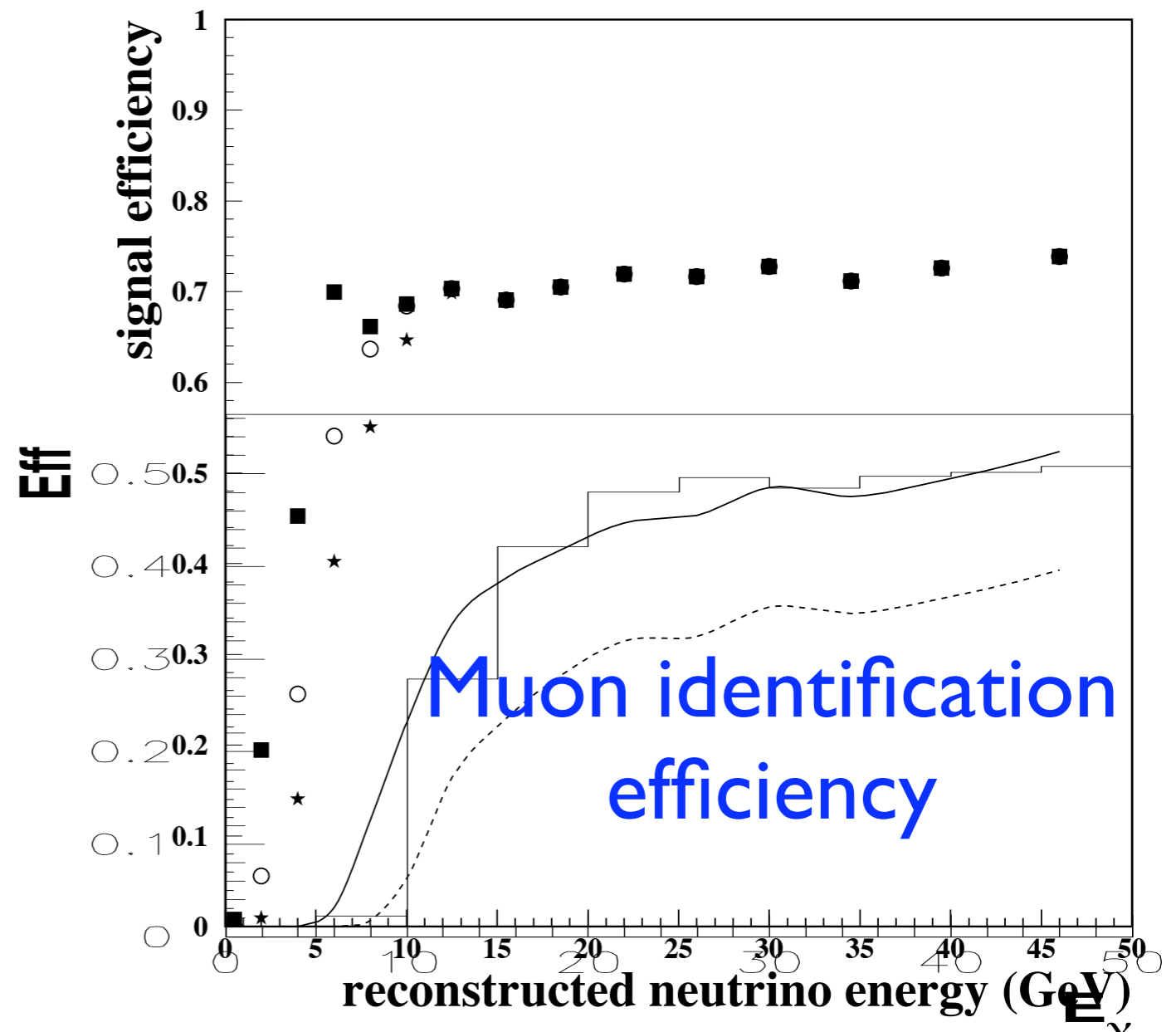
**Good to measure  $\theta_{13}$**   
**and the sign of  $\Delta m^2_{13}$**

Combined with  
another baseline,  
acts as a **degeneracy-solver**

# Enlightened MINDs

The crucial improvement is  
to lower the threshold  
for muon identification

From the ISS Detector Group Final Report



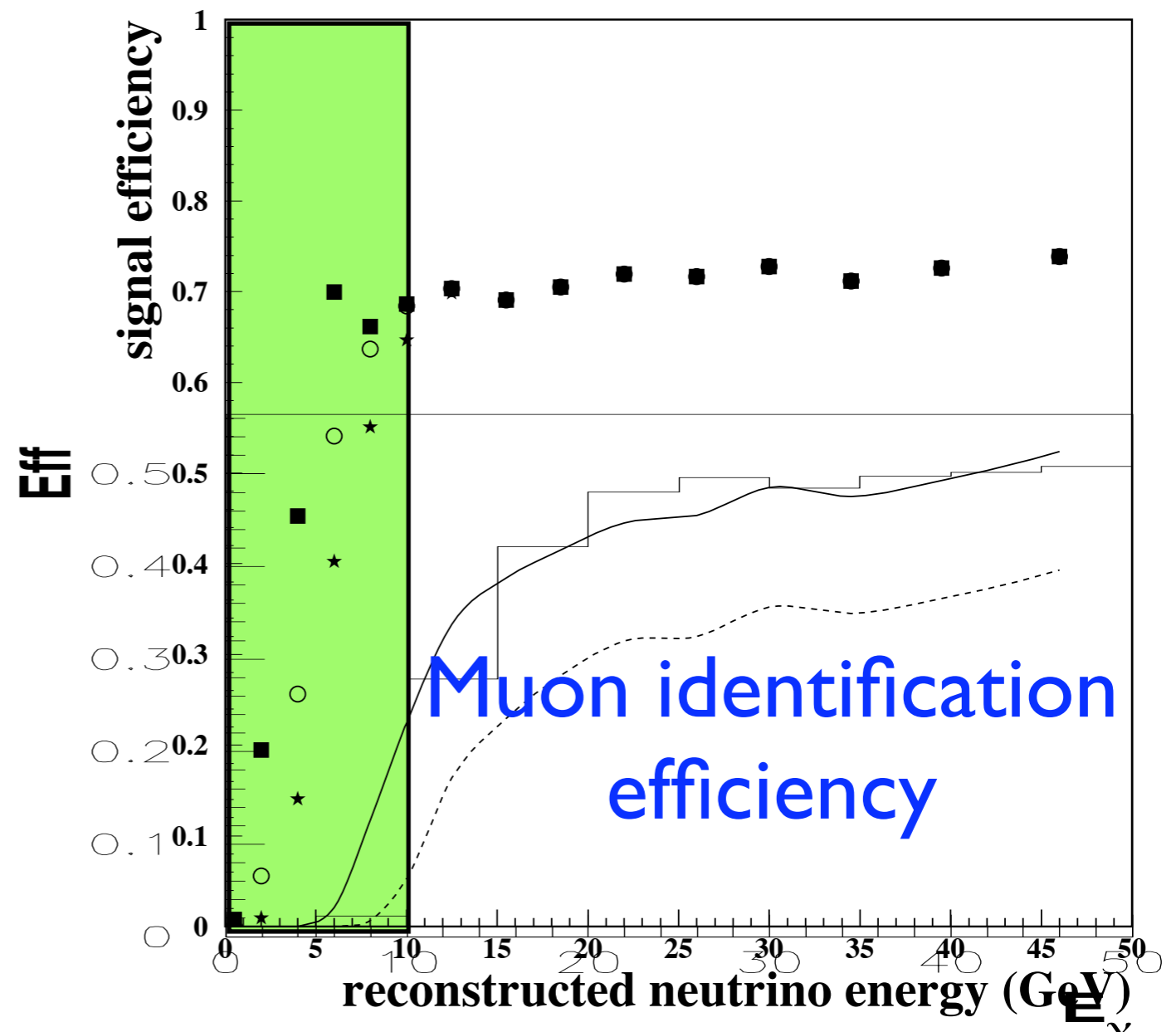
# Enlightened MINDs

The crucial improvement is to lower the threshold for muon identification

For the standard NF setup, the first oscillation peak is around 7 GeV:

a good efficiency below this value acts as a degeneracy-solver

From the ISS Detector Group Final Report





## The $\nu_\mu$ disappearance channel

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - (\sin^2 2\theta_{23} - s_{23}^2 \sin^2 2\theta_{13} \cos^2 2\theta_{23}) \sin^2\left(\frac{\Delta_{atm} L}{2}\right) \\ - \left(\frac{\Delta_{sol} L}{2}\right) [s_{12}^2 \sin^2 2\theta_{23} + \tilde{J} s_{23}^2 \cos \delta] \sin(\Delta_{atm} L) \\ - \left(\frac{\Delta_{sol} L}{2}\right)^2 [c_{23}^4 \sin^2 2\theta_{12} + s_{12}^2 \sin^2 2\theta_{23} \cos(\Delta_{atm} L)]$$

Where

$$\tilde{J} = \cos \theta_{13} \sin 2\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \qquad \Delta_{sol} = \frac{\Delta m_{12}^2}{2E}$$
$$\sin 2\theta_{13} < 0.4 \qquad \Delta_{atm} = \frac{\Delta m_{23}^2}{2E} \qquad \left(\frac{\Delta_{sol} L}{2}\right) \cong 0.05$$



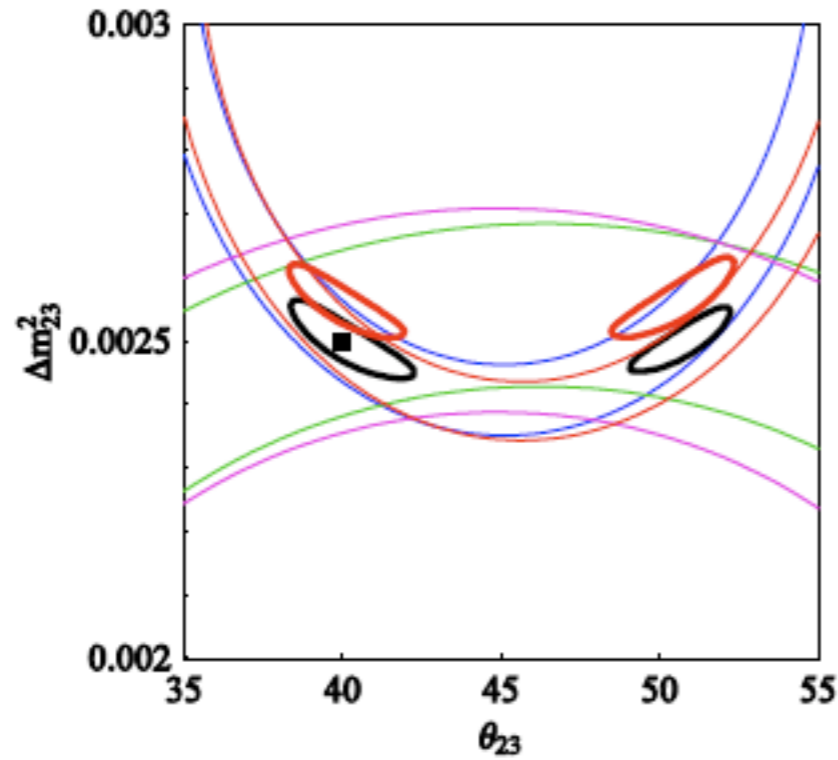
## Preliminar analysis at the NuFactory

5yr  $\nu_\mu$  + 5yr  $\bar{\nu}_\mu$  exposure with a 40Kt iron calorimeter for the NF

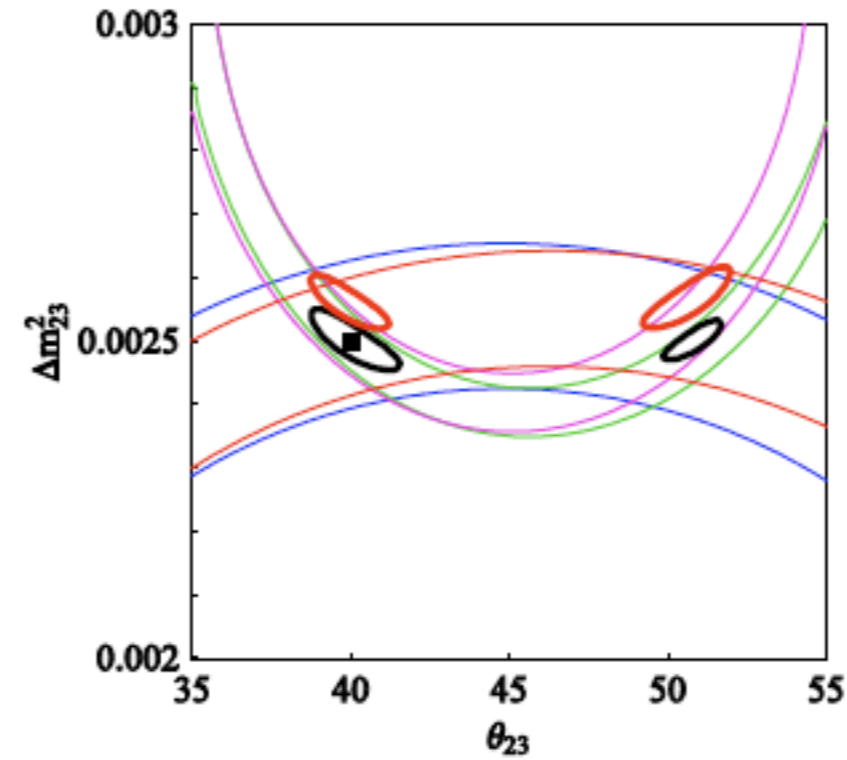
- Possible Setups:
  - L = 3000Km E = 20, 50 GeV
  - L = 7000Km E = 50 GeV
- 5 GeV bins considered
- Efficiency:
  - $\varepsilon_\mu = 0.5$  for neutrinos "Cervera *et al.* hep-ph/0002108"
  - $\varepsilon_\mu = 0.33$  for antineutrinos
- Systematics = 2%

See e.g. Bueno *et al.* hep-ph/0005007 for an Icarus analysis



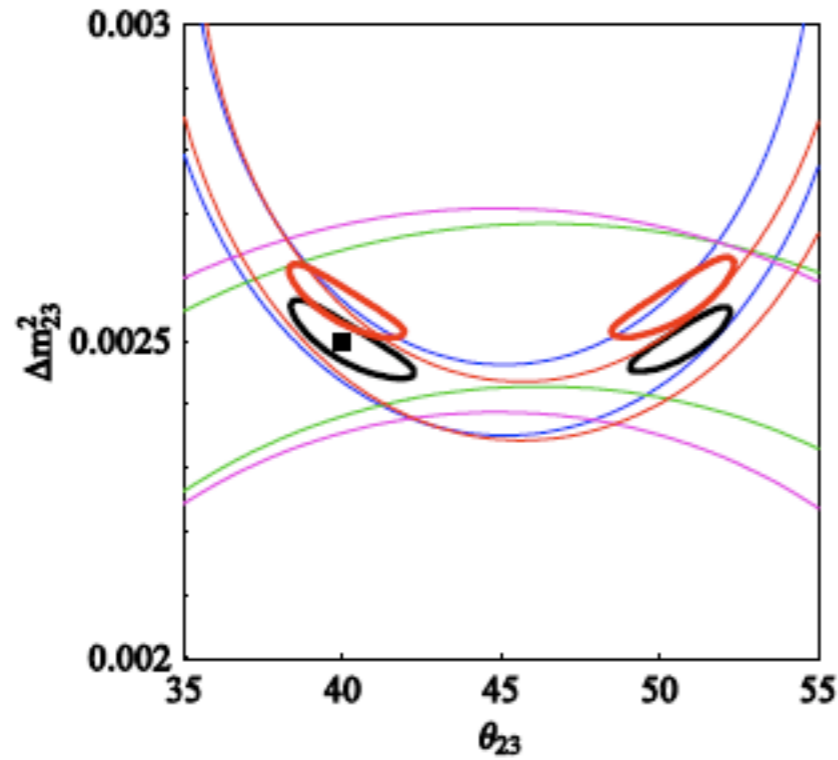


$E = 50$  GeV  
 $L = 3000$  Km

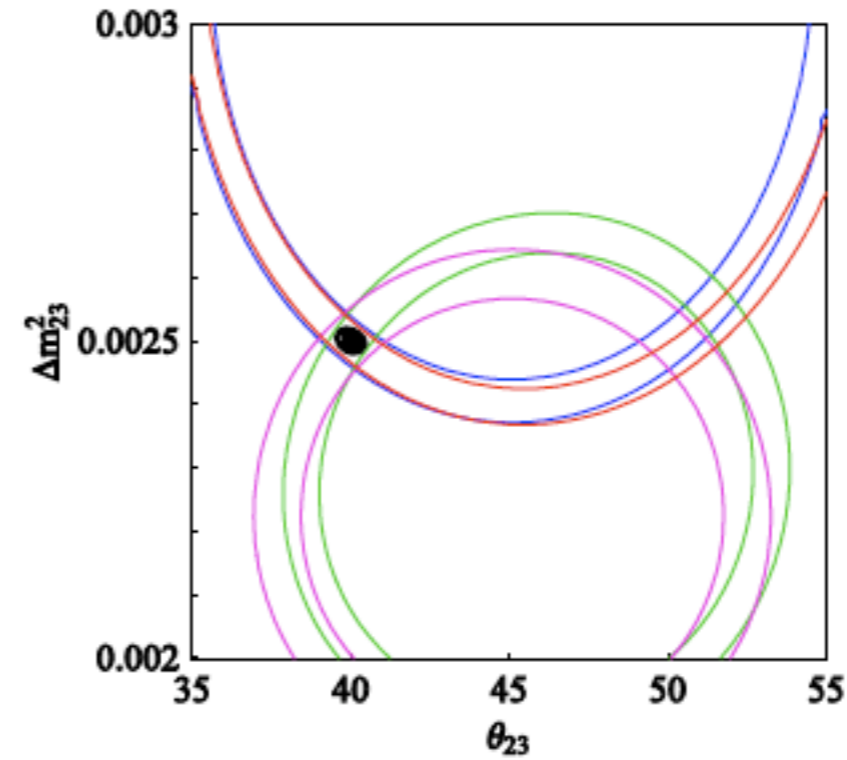


$E = 20$  GeV  
 $L = 3000$  Km

Input:  $\theta_{23} = 40^\circ$ ,  $\theta_{13} = 6^\circ$ ,  $\delta = 0^\circ$

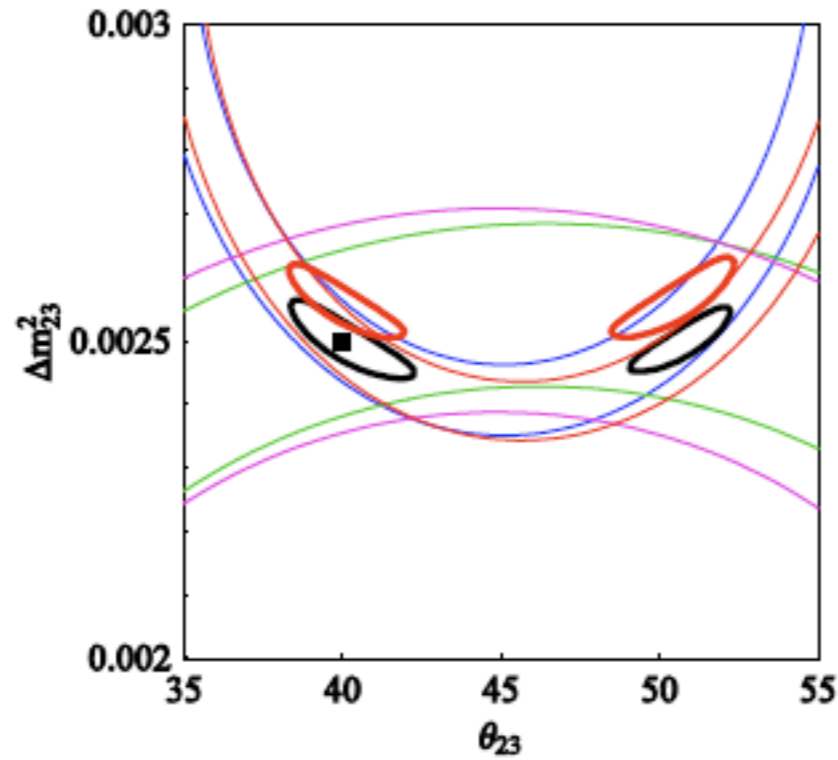


$E = 50 \text{ GeV}$   
 $L = 3000 \text{ Km}$

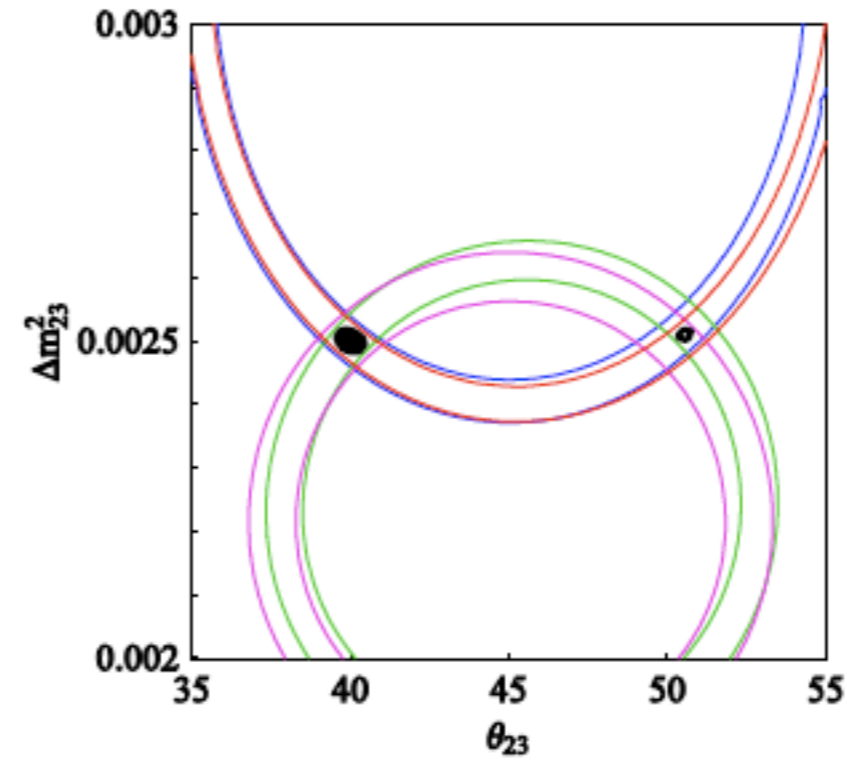


$E = 50 \text{ GeV}$   
 $L = 7000 \text{ Km}$

Input:  $\theta_{23} = 40^\circ$ ,  $\theta_{13} = 6^\circ$ ,  $\delta = 0^\circ$

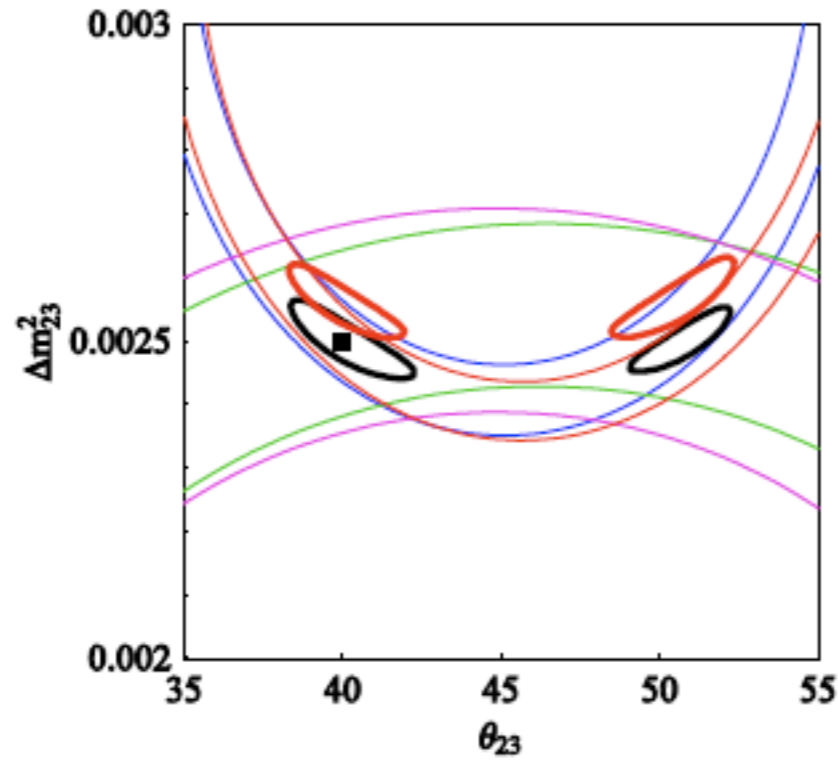


$E = 50 \text{ GeV}$   
 $L = 3000 \text{ Km}$

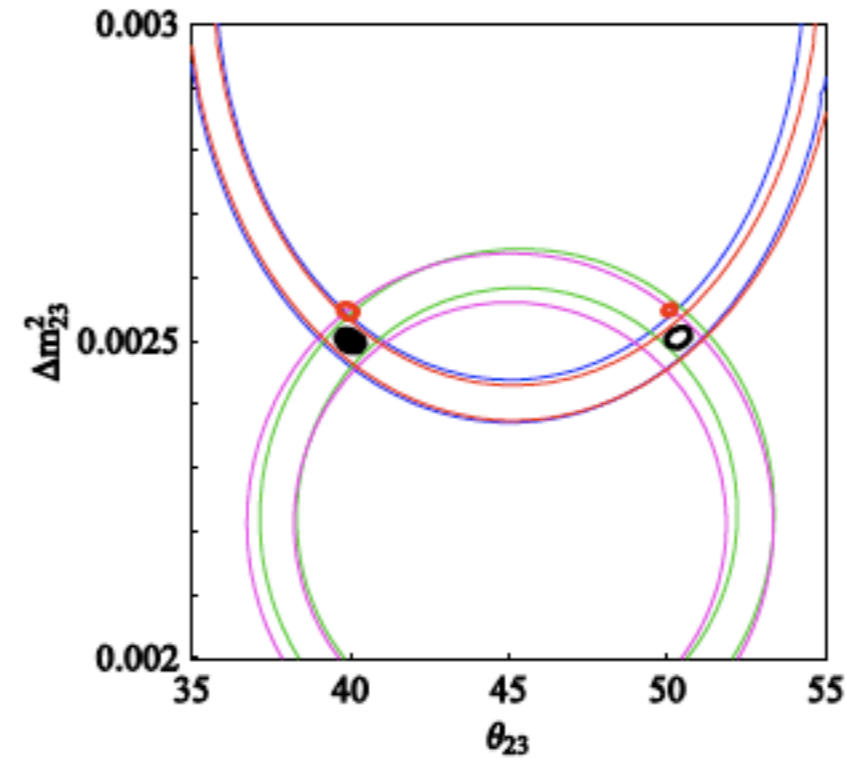


$E = 50 \text{ GeV}$   
 $L = 7000 \text{ Km}$

Input:  $\theta_{23} = 40^\circ$ ,  $\theta_{13} = 4^\circ$ ,  $\delta = 0^\circ$

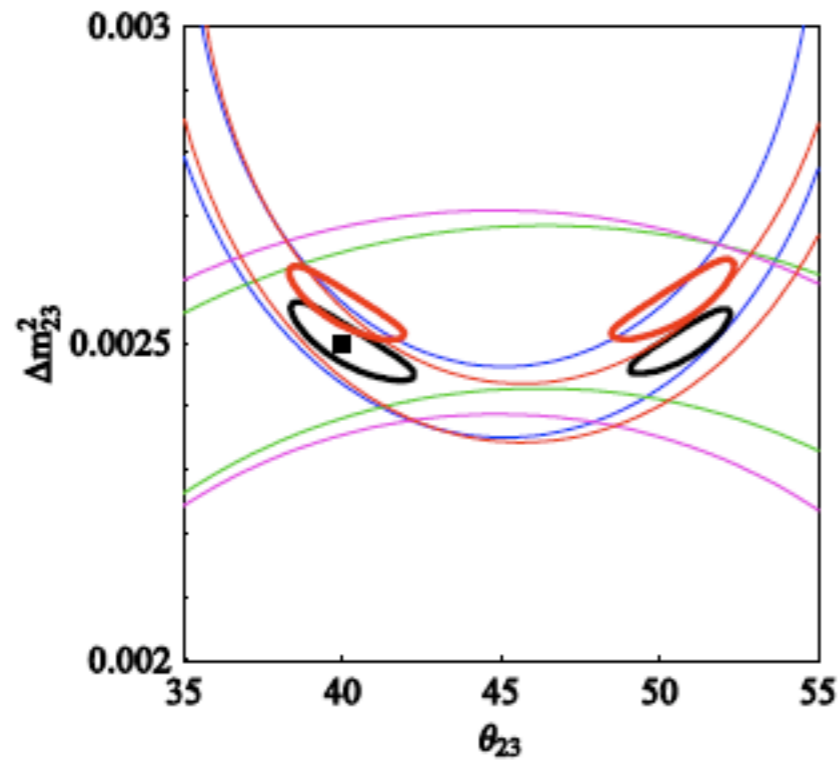


$E = 50 \text{ GeV}$   
 $L = 3000 \text{ Km}$

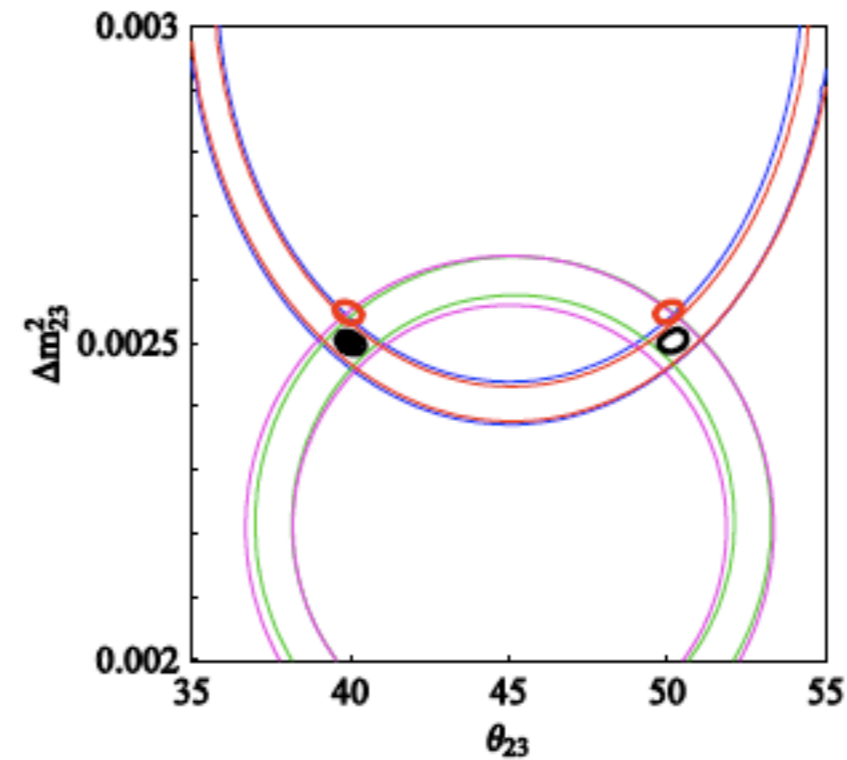


$E = 50 \text{ GeV}$   
 $L = 7000 \text{ Km}$

Input:  $\theta_{23} = 40^\circ$ ,  $\theta_{13} = 3^\circ$ ,  $\delta = 0^\circ$



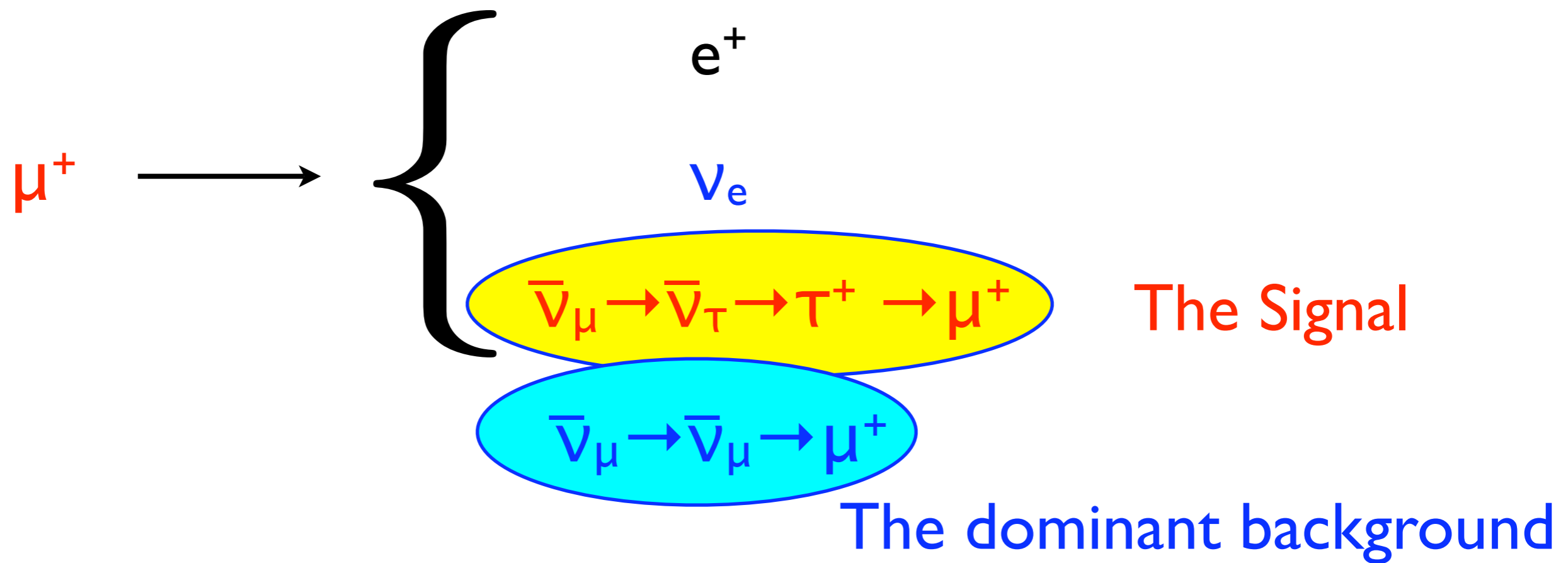
$E = 50 \text{ GeV}$   
 $L = 3000 \text{ Km}$



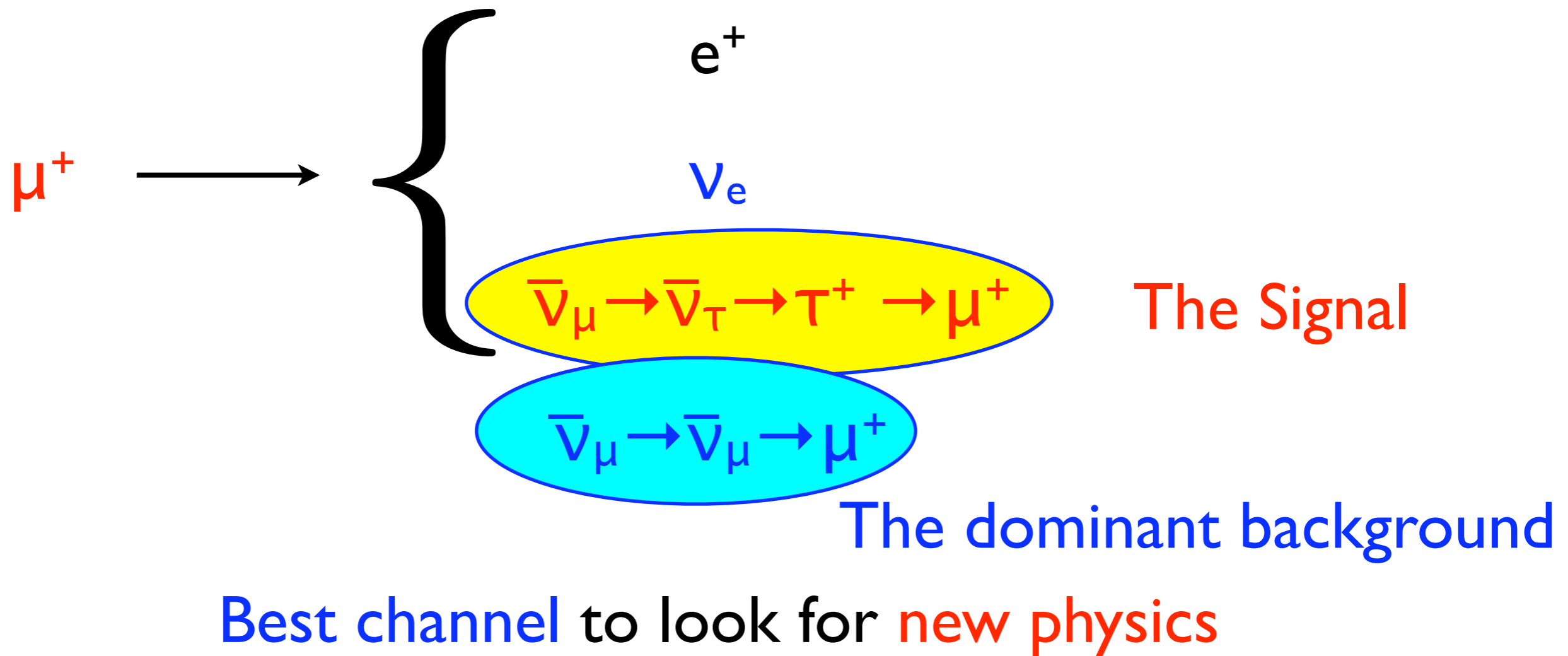
$E = 50 \text{ GeV}$   
 $L = 7000 \text{ Km}$

Input:  $\theta_{23} = 40^\circ$ ,  $\theta_{13} = 2^\circ$ ,  $\delta = 0^\circ$

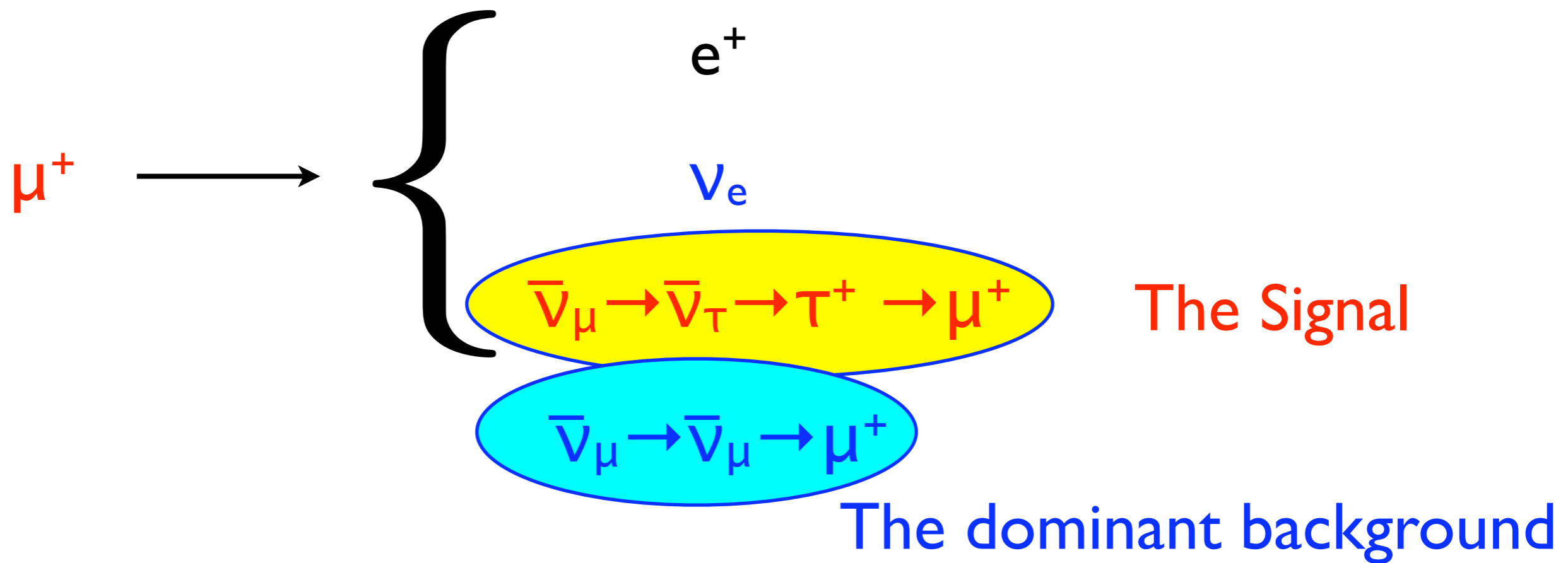
(...the forgotten channel...)



(...the forgotten channel...)



(...the forgotten channel...)

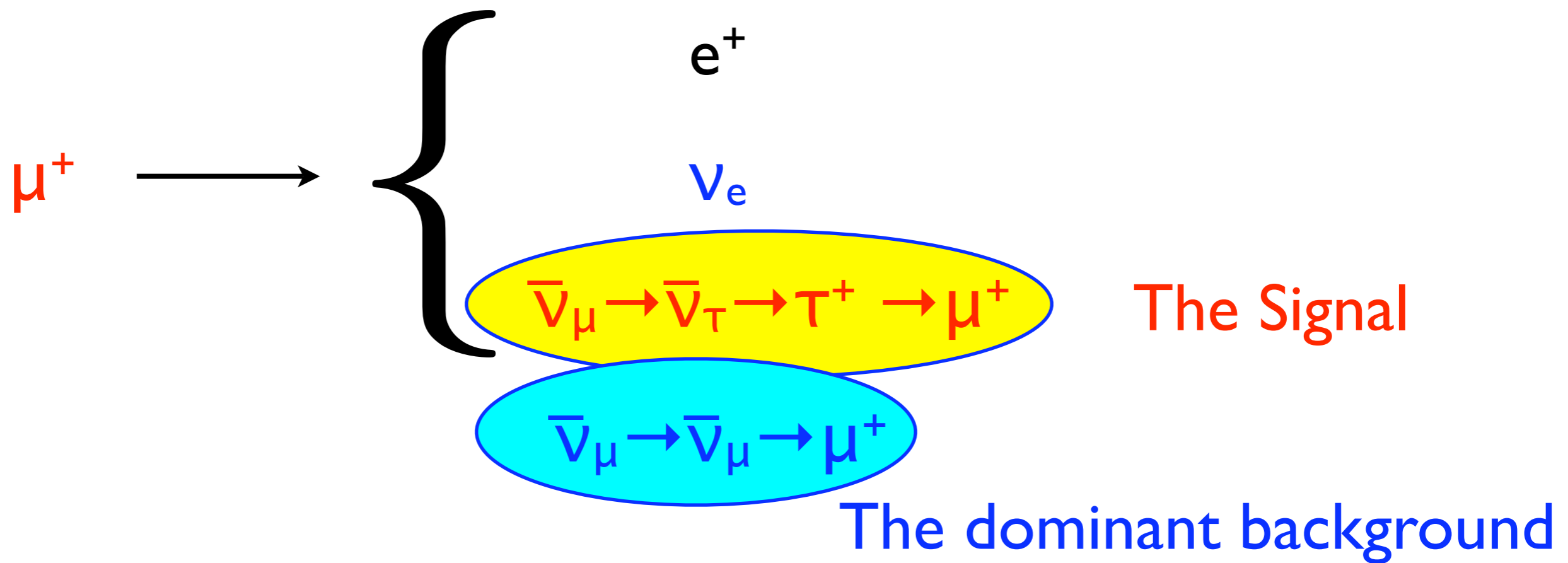


Best channel to look for **new physics**





(...the forgotten channel...)

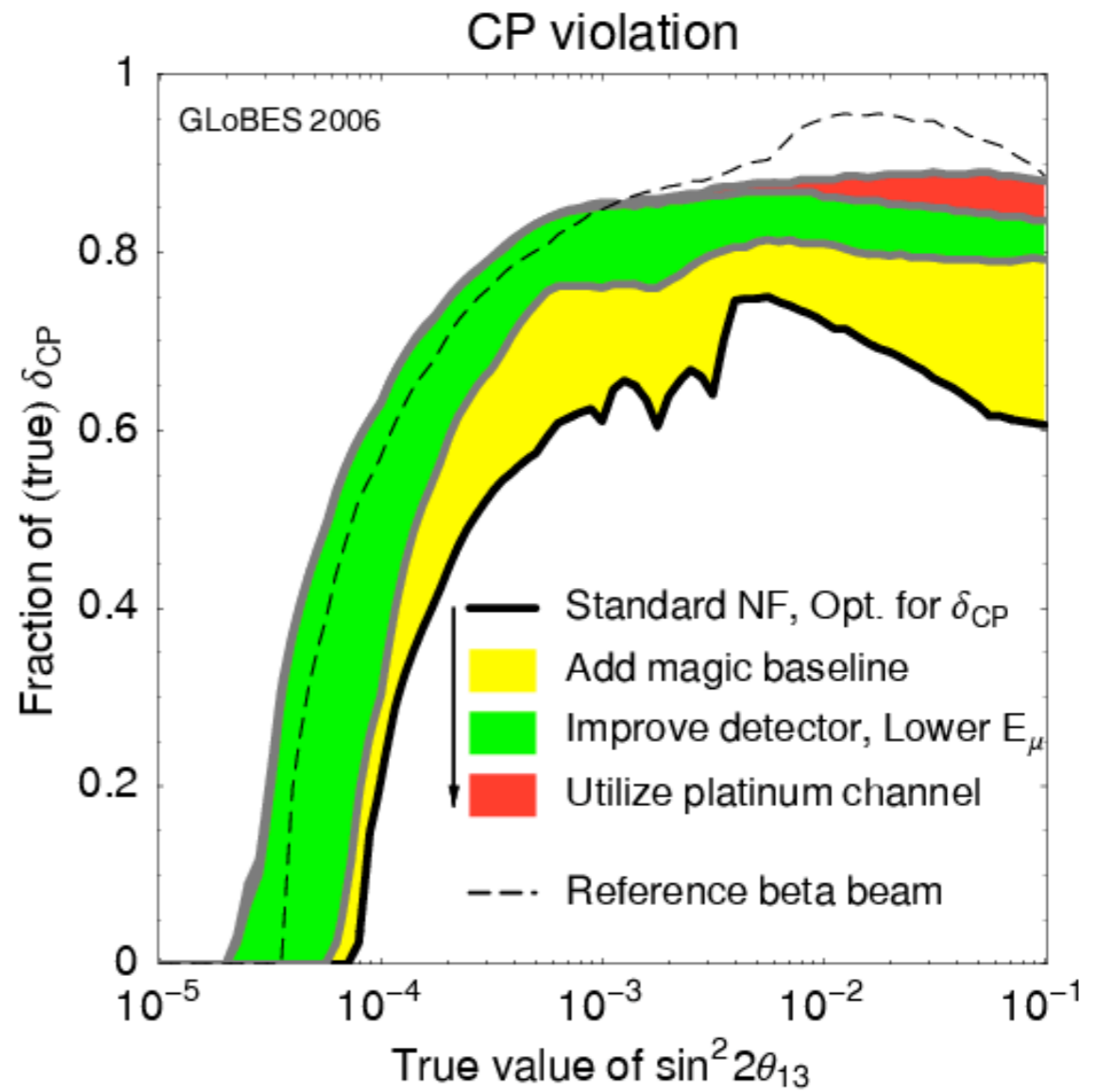
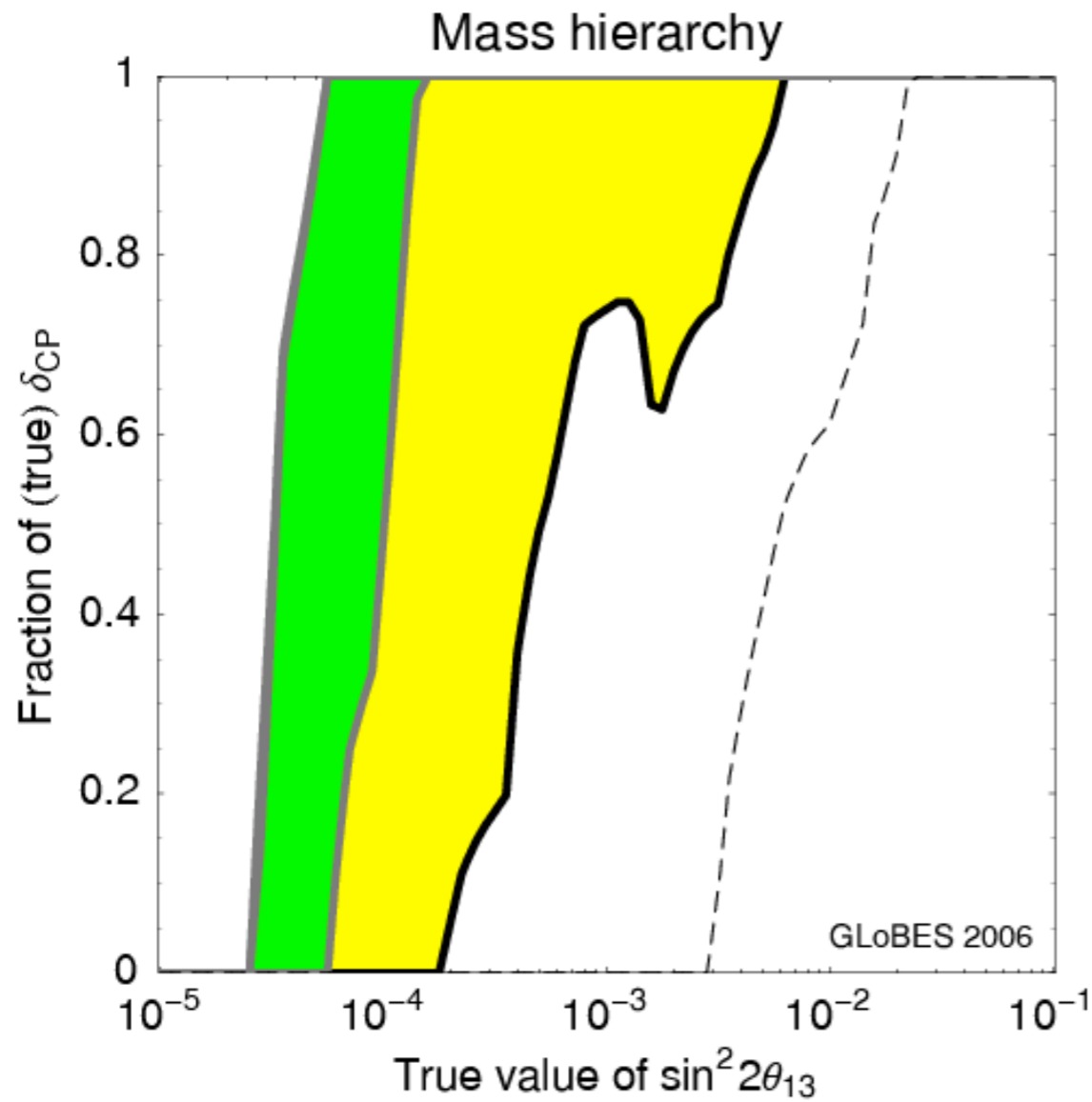


Best channel to look for **new physics**



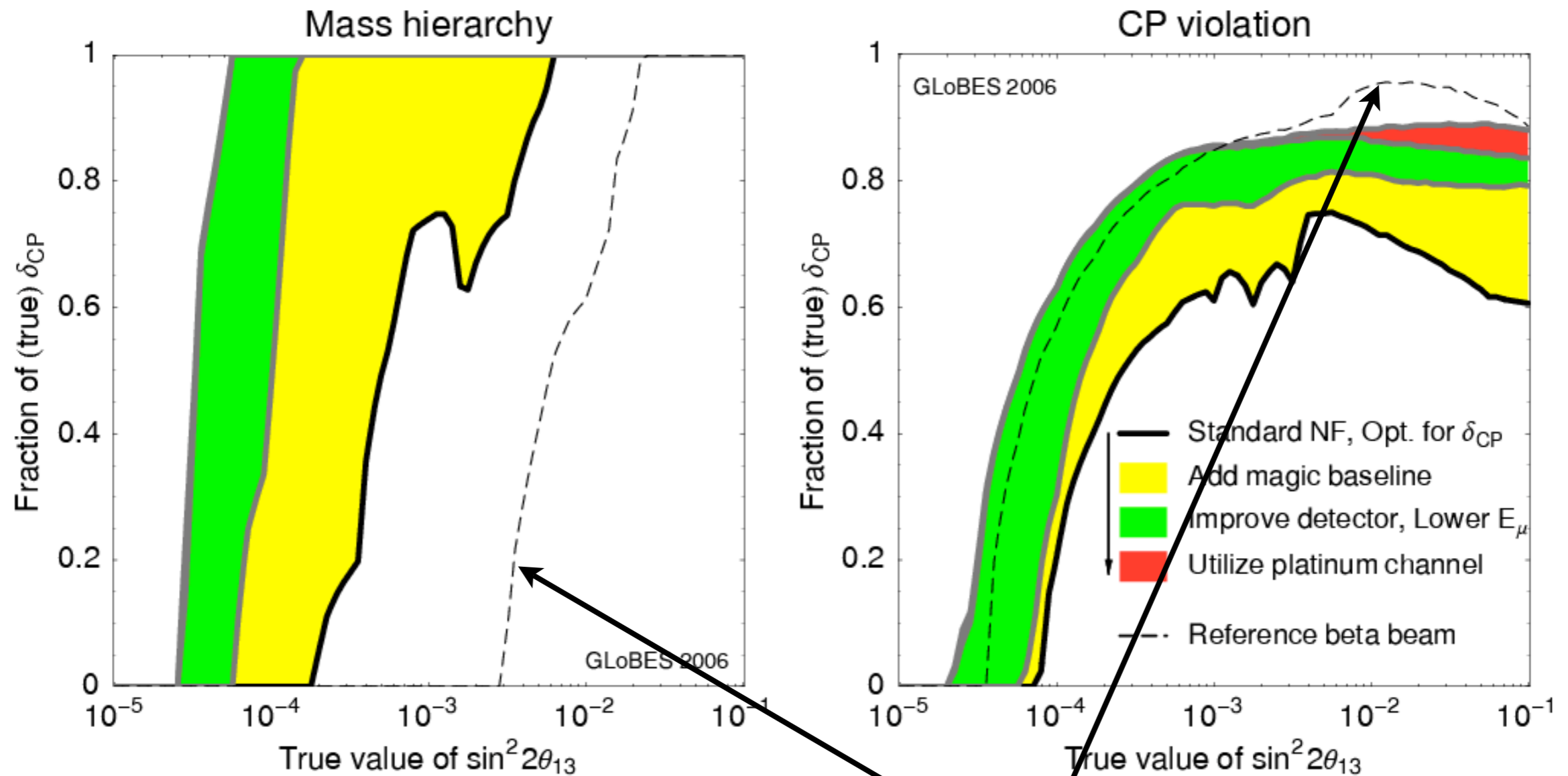
# The NuFact Sensitivity

Huber, Lindner, Rolinec and Winter '06



# The NuFact Sensitivity

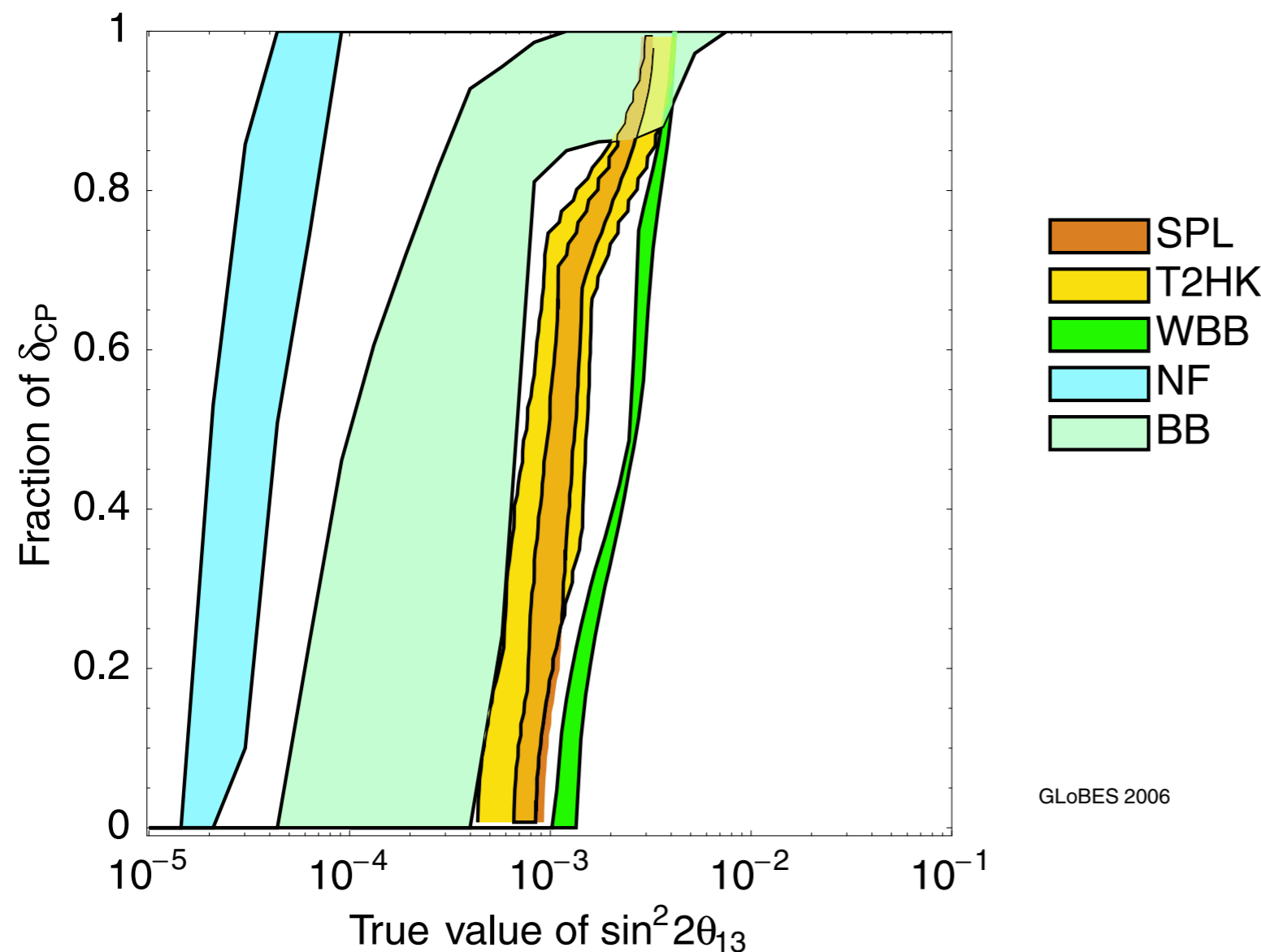
Huber, Lindner, Rolinec and Winter '06



Burguet-Castell, Casper, Couce, Gómez-Cadenas and Hernández '05

# The NuFact Sensitivity

## Discovery reach in $\sin^2 2\theta_{13}$



GLoBES 2006

ISS final report:

25 GeV muons

Two E-MIND detectors

1.  $L = 3000-4000$  Km

2.  $L = 7500$  Km

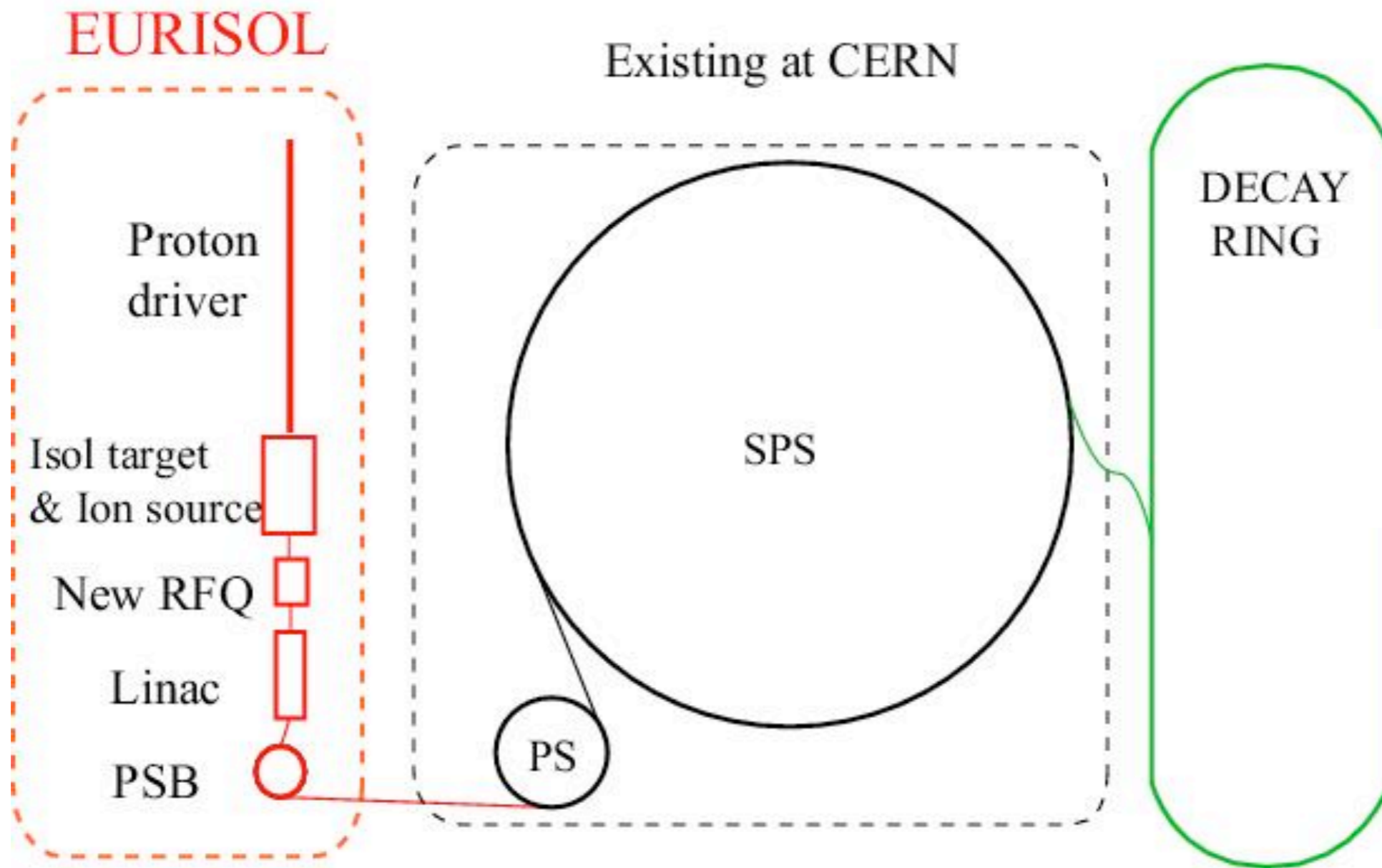
$(0.5/1) 10^{21}$  useful muons

per year per baseline

From the ISS Physics Group Final Report

# BETABEAMS

1. with  ${}^6\text{He}/{}^{18}\text{Ne}$



$\langle E_\nu \rangle = 300 \text{ MeV}$

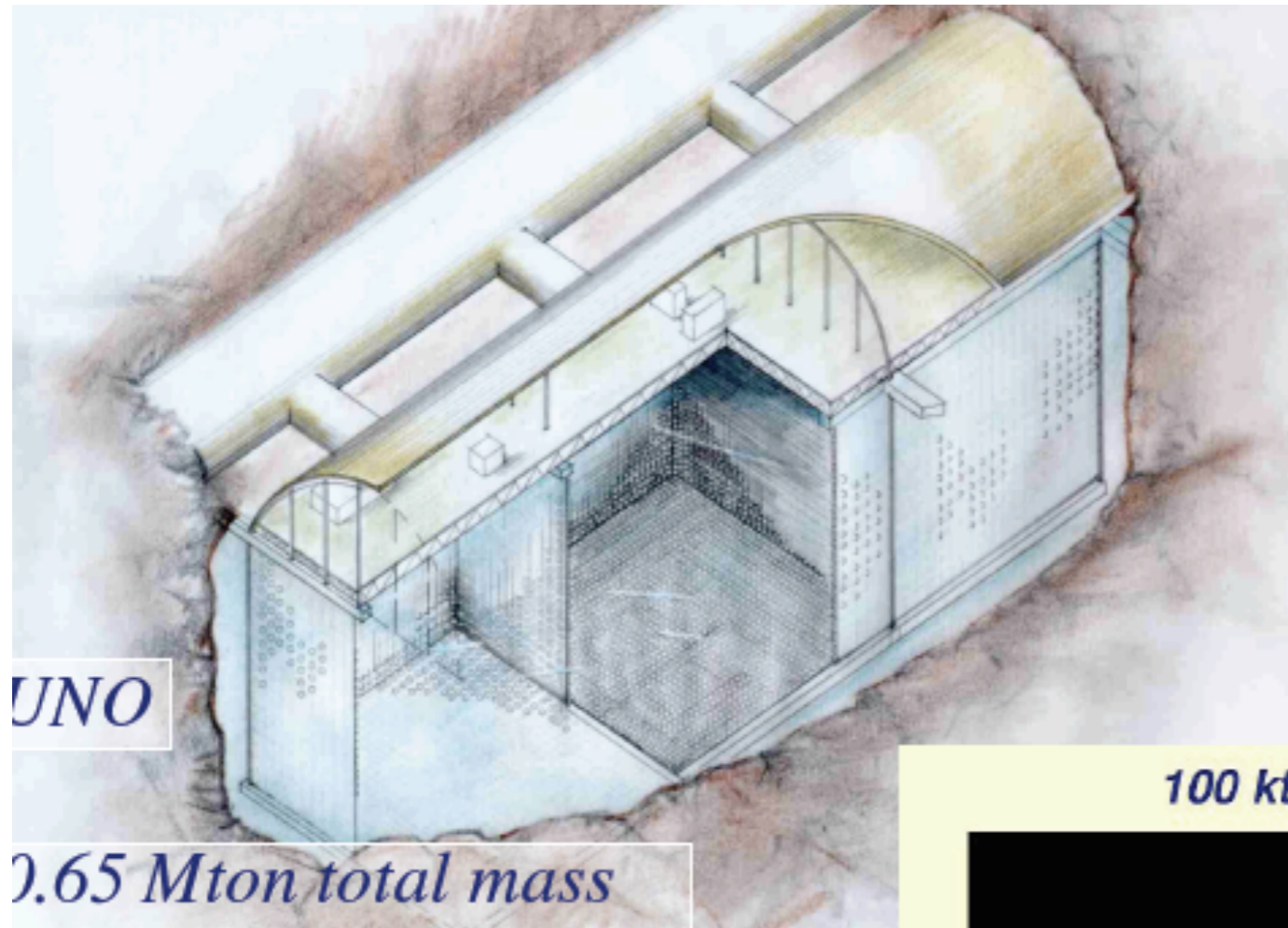
$\gamma \sim 100$

P. Zucchelli hep-ph/0107006

$L = 130 \text{ Km}$

# The CERN-Memphys project

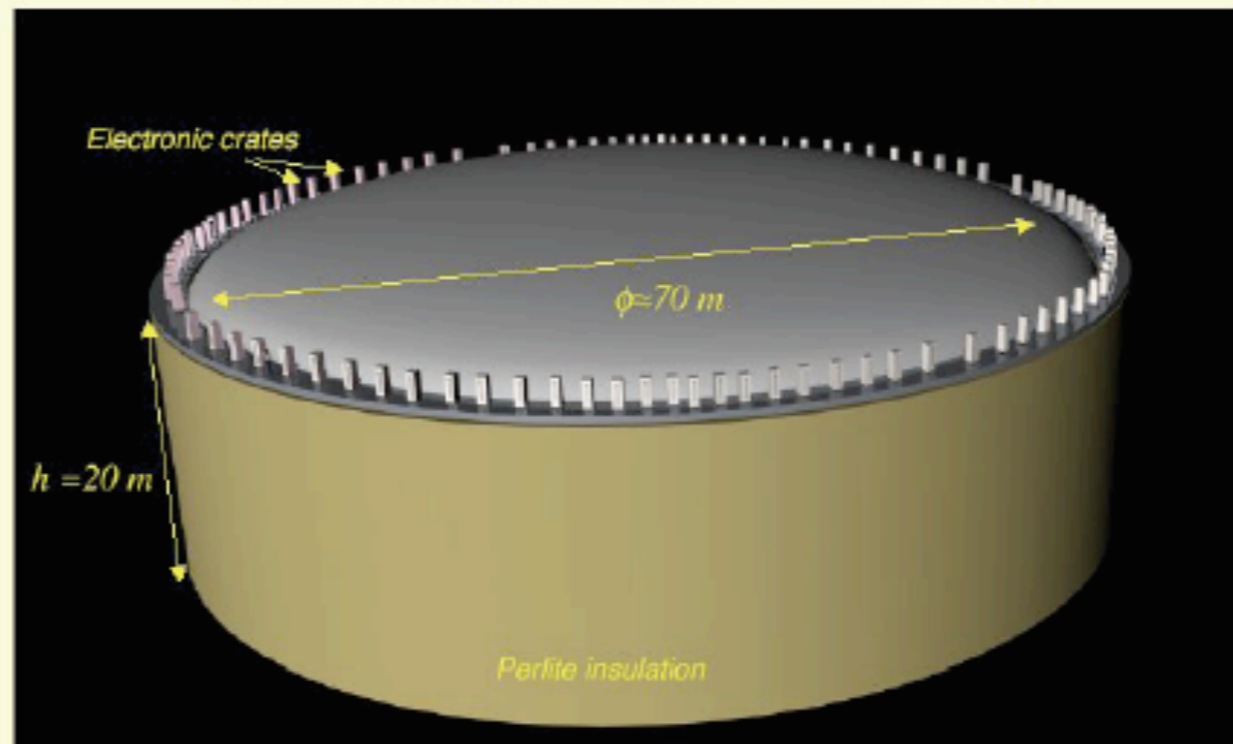
## *Detector options*



UNO

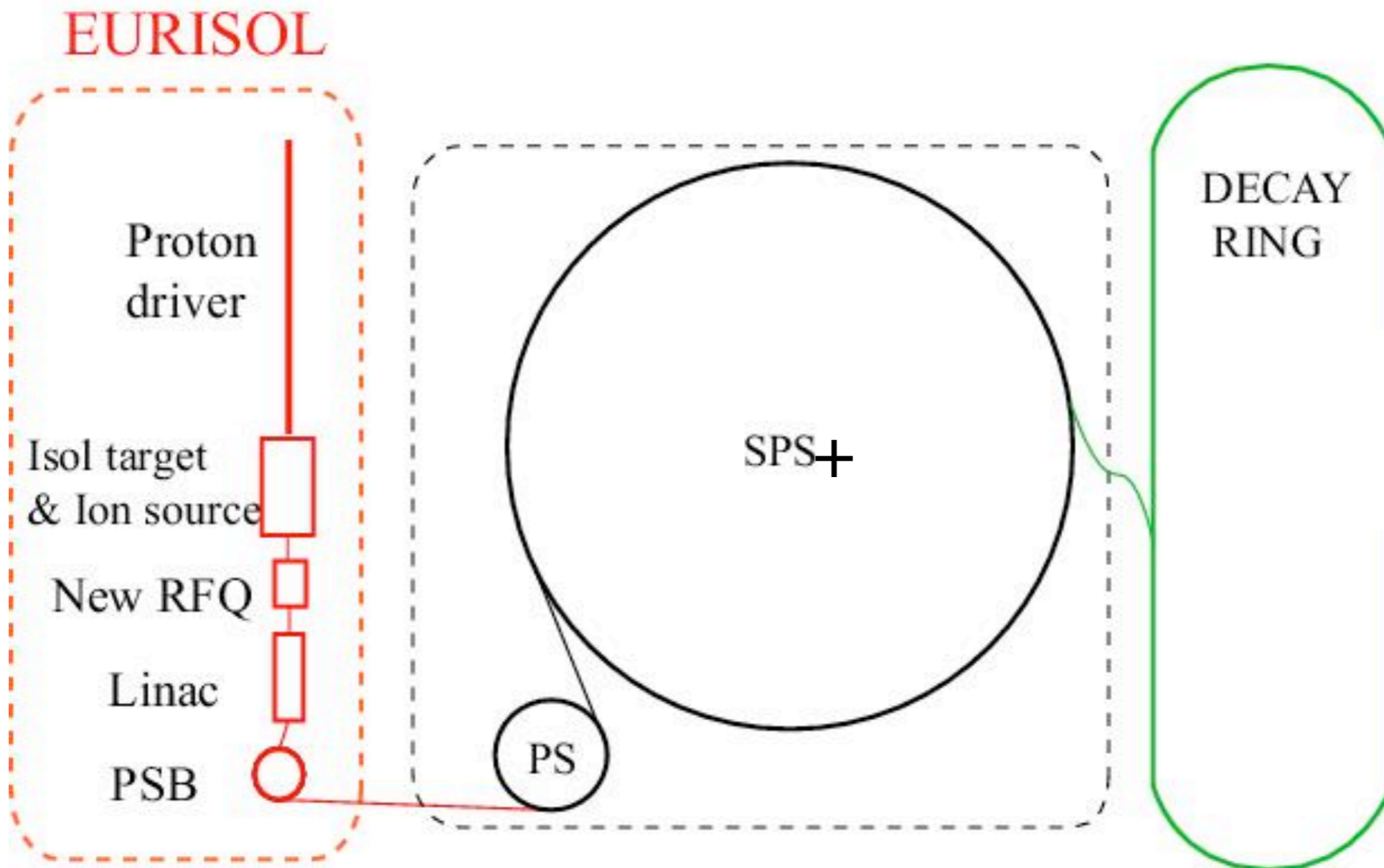
0.65 Mton total mass

### 100 kton liquid Argon TPC detector



Experiments for CP violation: a giant liquid Argon scintillation, Cerenkov and charge imaging experiment.

A.Rubbia, Proc. II Int. Workshop on Neutrinos in Venice, 2003, hep-ph/0402110



$\langle E_\nu \rangle = 1.2 \text{ GeV}$

$L = 650 \text{ Km}$

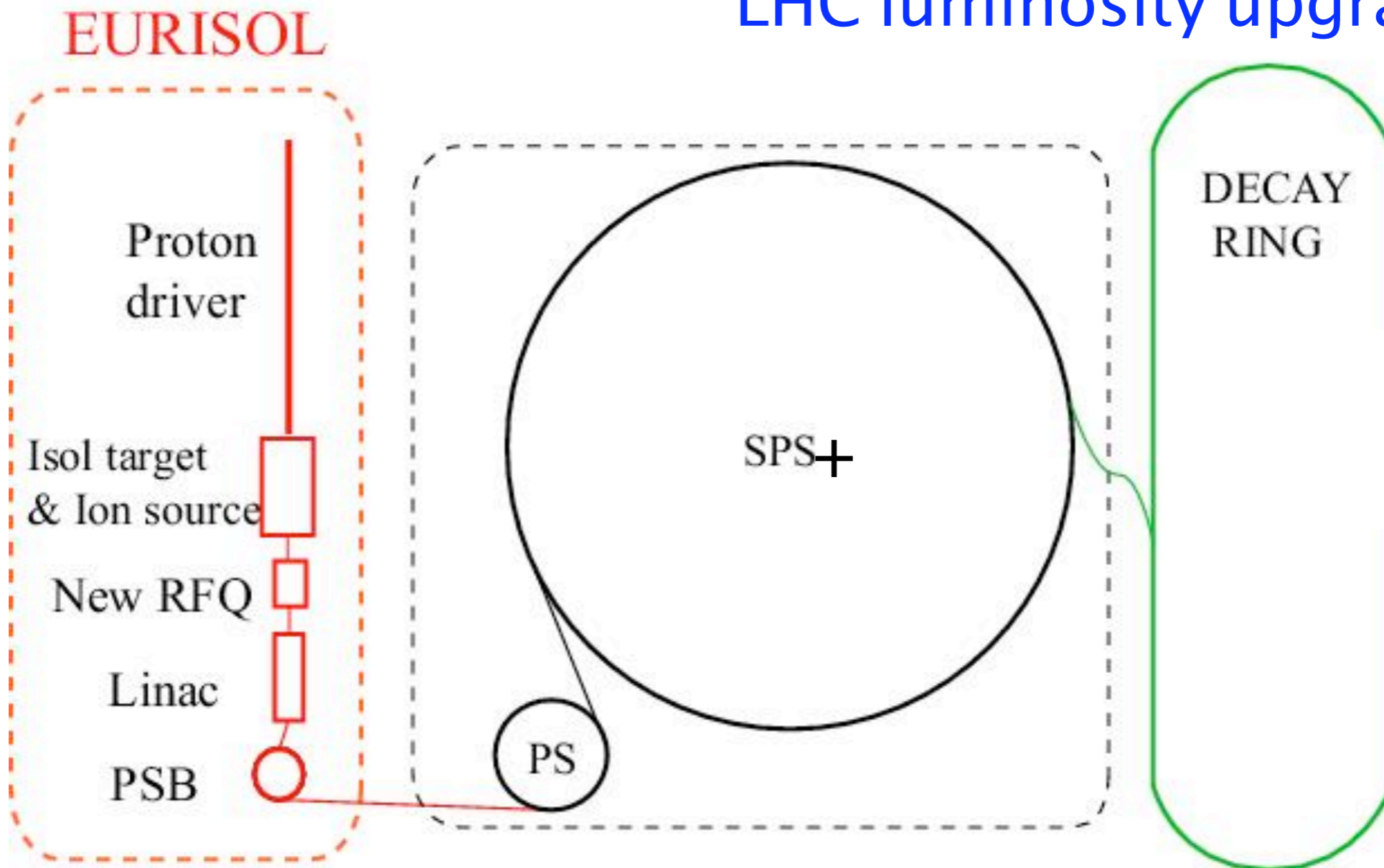
$\gamma \sim 350$

J. Burguet-Castell et al. hep-ph/0312068

J. Burguet-Castell et al. hep-ph/0503021



LHC luminosity upgrade



$\langle E_\nu \rangle = 1.2 \text{ GeV}$

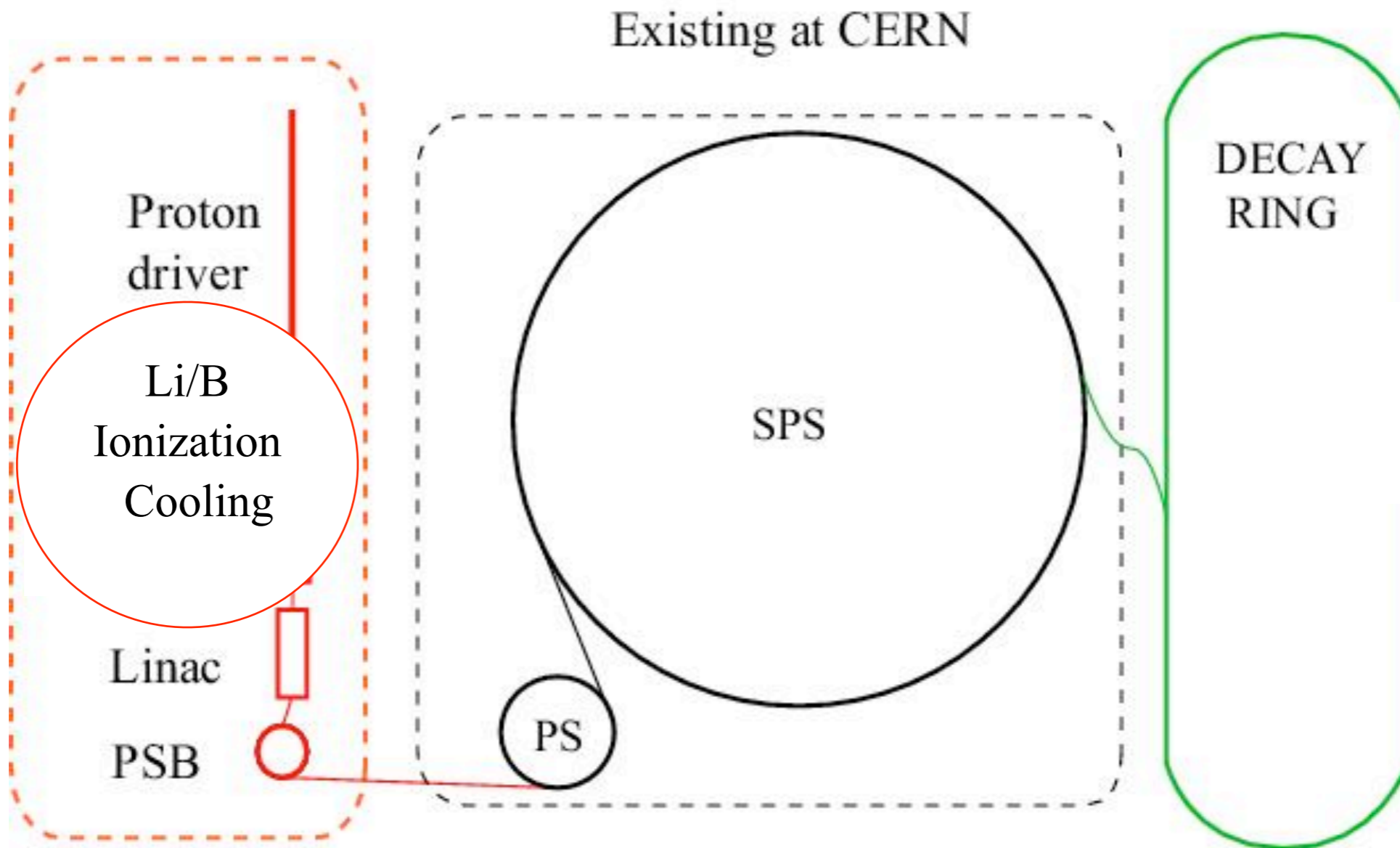
$L = 650 \text{ Km}$

$\gamma \sim 350$

J. Burguet-Castell et al. hep-ph/0312068

J. Burguet-Castell et al. hep-ph/0503021

3. with  $^8\text{Li}/^8\text{B}$



$\langle E_\nu \rangle = 1.3 \text{ GeV}$

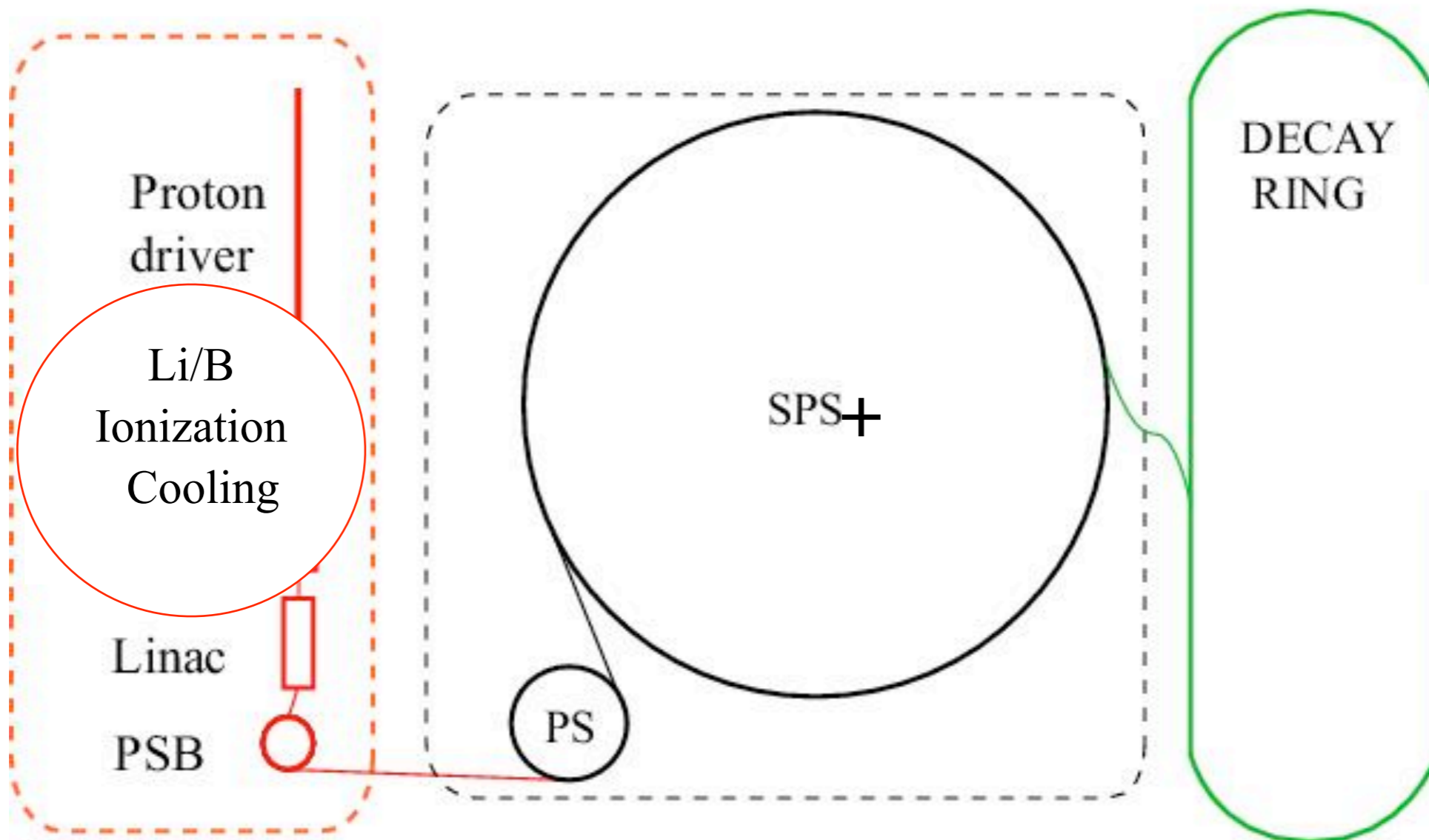
$L = 650 \text{ Km}$

$\gamma \sim 100$

C. Rubbia et al. hep-ph/0602032

C. Rubbia et al. hep-ph/0609235

4. with  $^8\text{Li}/^8\text{B}$



$\langle E_\nu \rangle = 4.5 \text{ GeV}$

$L = 7000 \text{ Km}$

**Magic Baseline!**

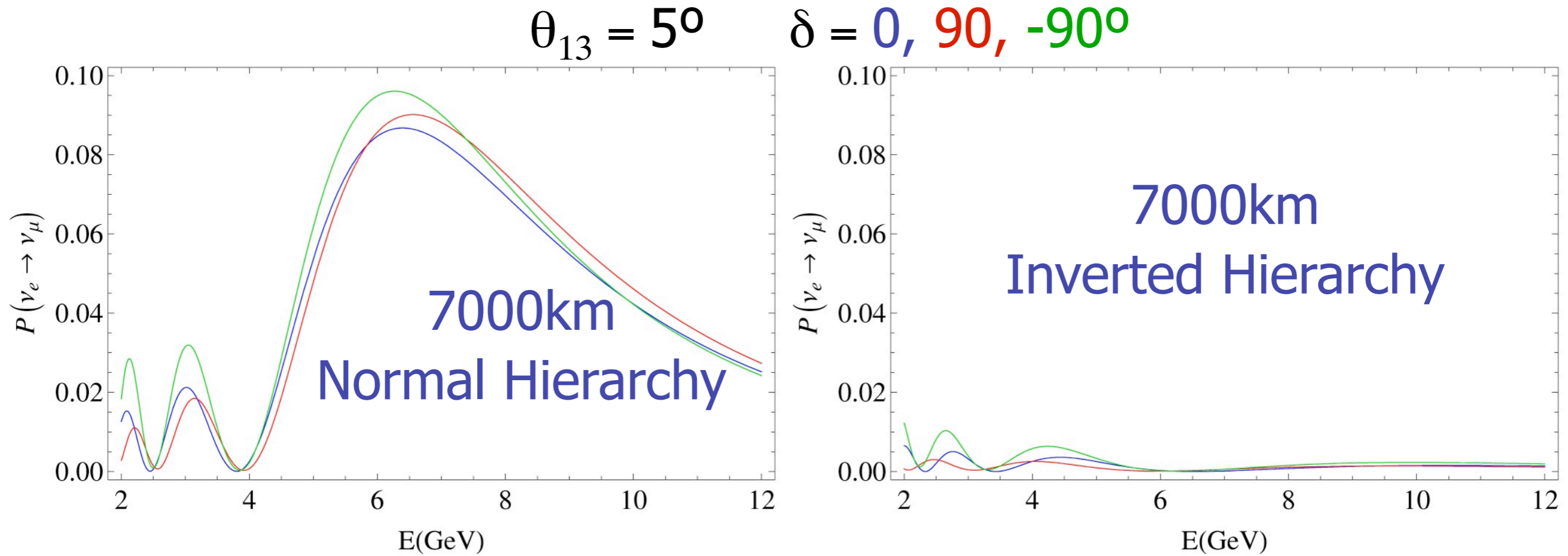
$\gamma \sim 350$

S. K. Agarwalla et al. hep-ph/0610333

S. K. Agarwalla et al. hep-ph/0611233

S. K. Agarwalla et al. arXiv:0711.1459

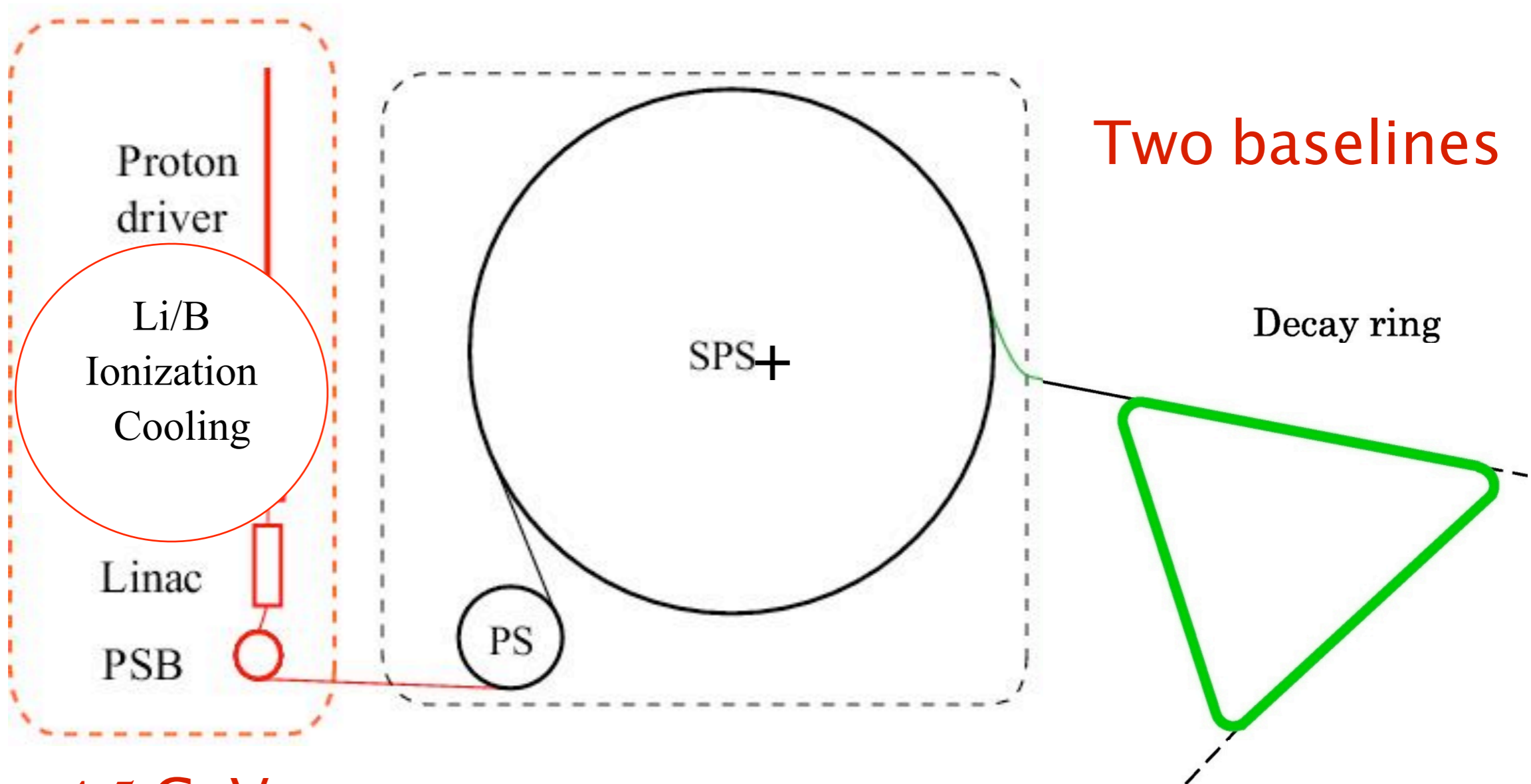
# Resonant enhancement at the MB



Resonant enhancement depending on the hierarchy

Sensitivity to the mass hierarchy  
down to  $\sin^2 2\theta_{13} = 10^{-3}$  for  $\gamma = 350$

4. with  $^8\text{Li}/^8\text{B}$



$\langle E_\nu \rangle = 4.5 \text{ GeV}$

$L \sim 1500 \text{ Km}$

$L = 7000 \text{ Km}$

$\gamma \sim 350$

S. K. Agarwalla et al. hep-ph/0610333

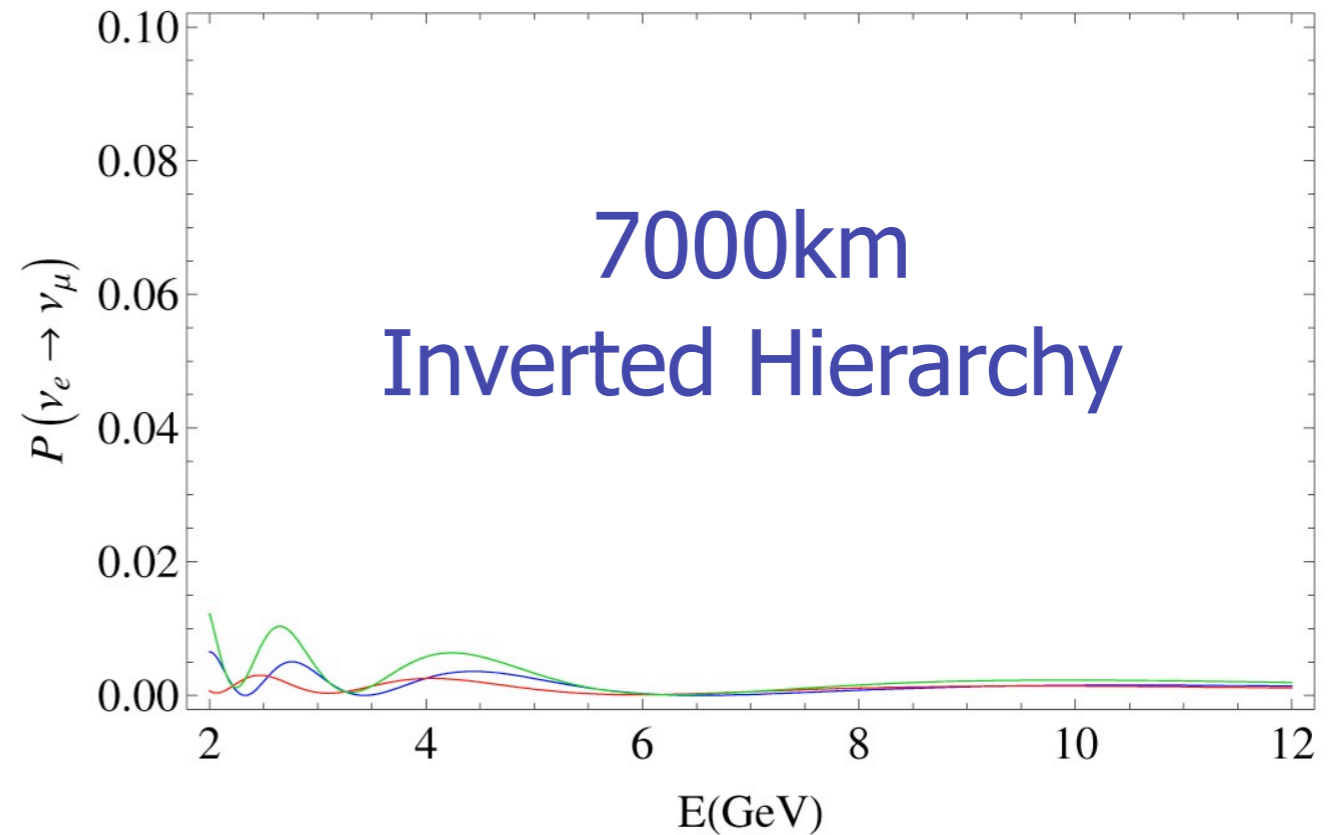
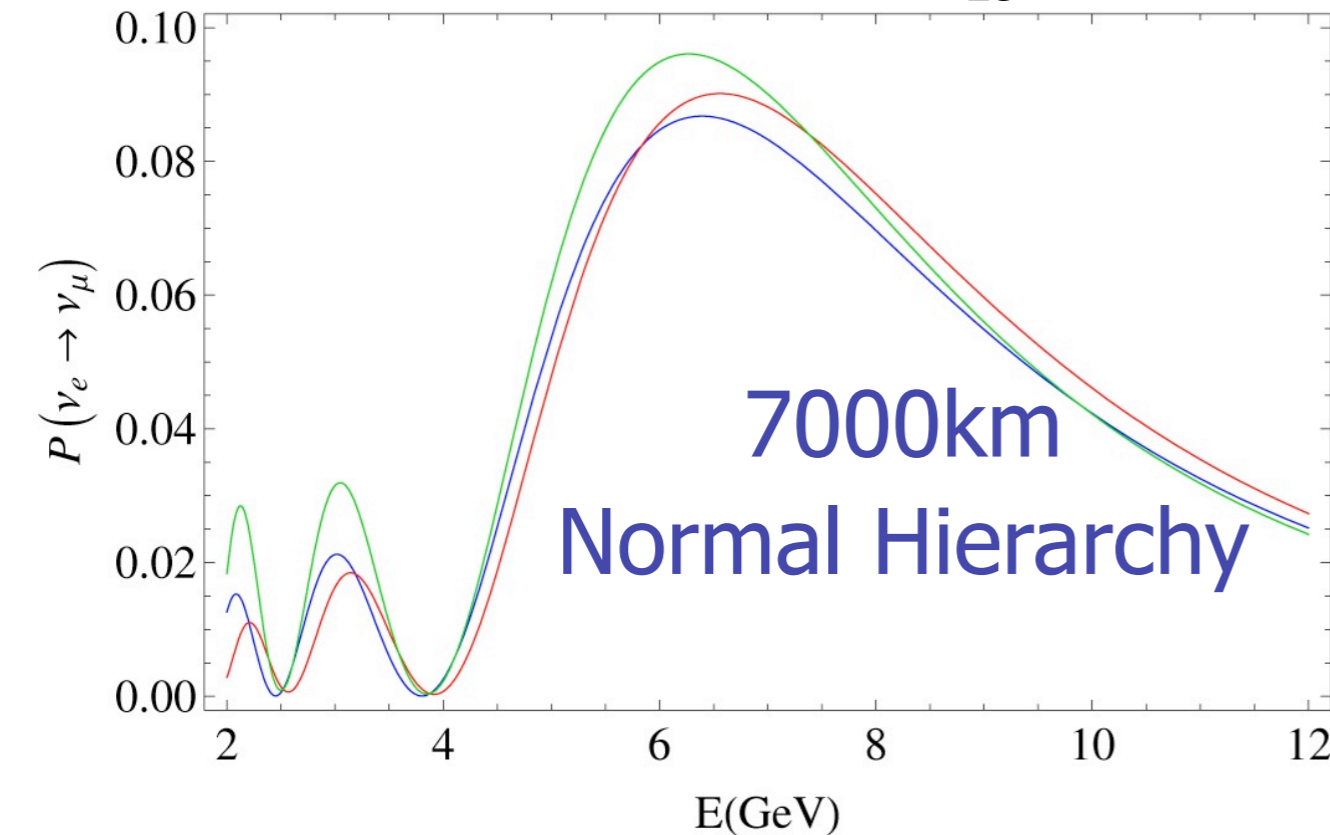
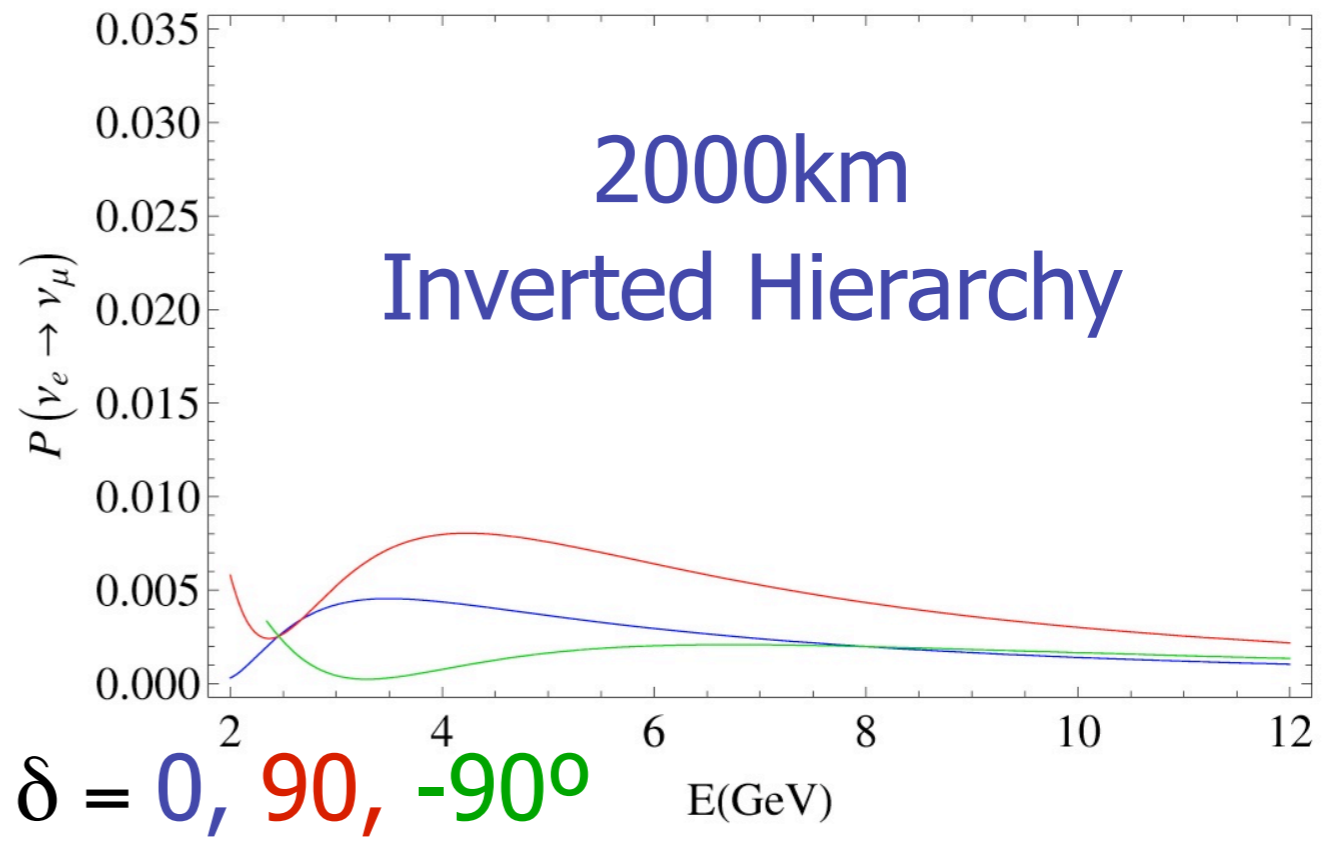
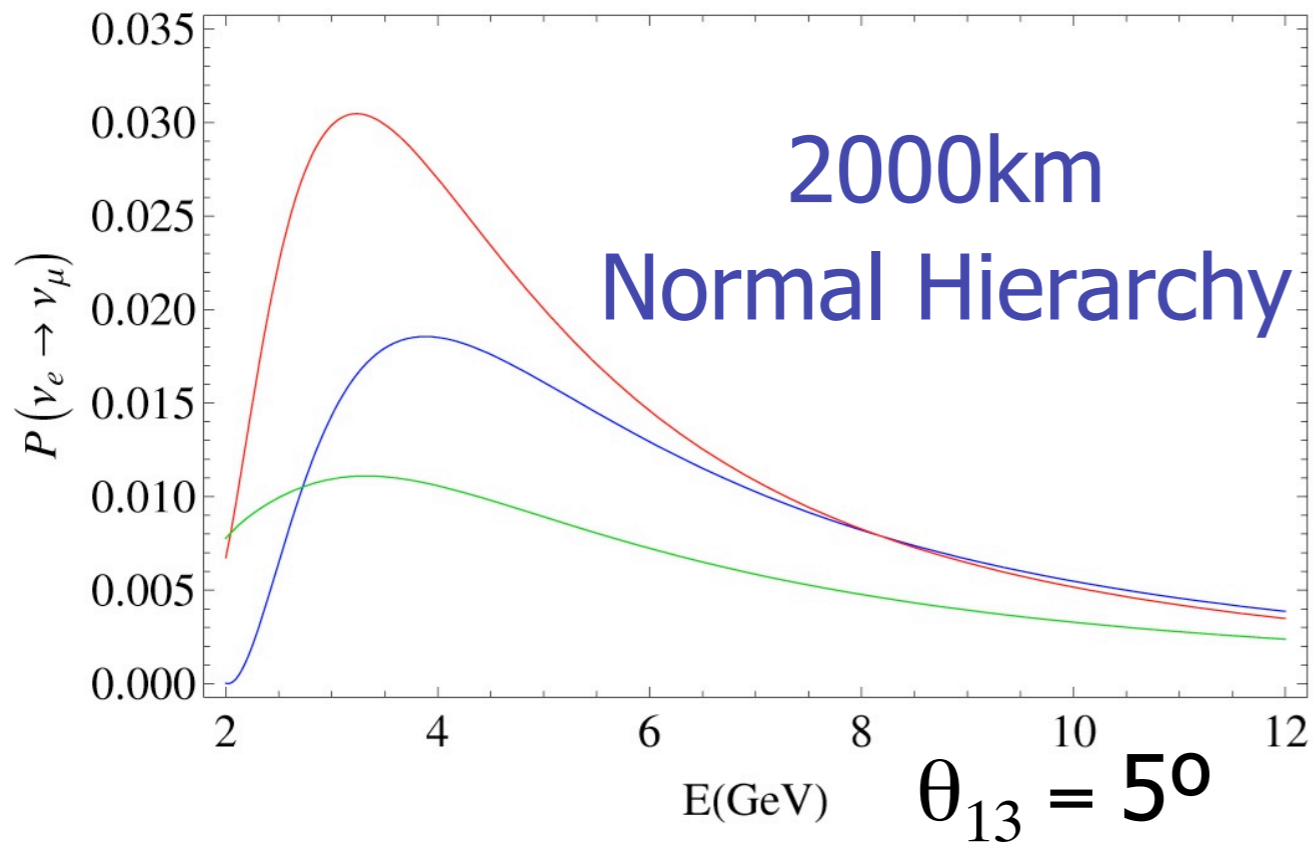
S. K. Agarwalla et al. hep-ph/0611233

S. K. Agarwalla et al. arXiv:0711.1459

P. Coloma et al. arXiv:0712.0796

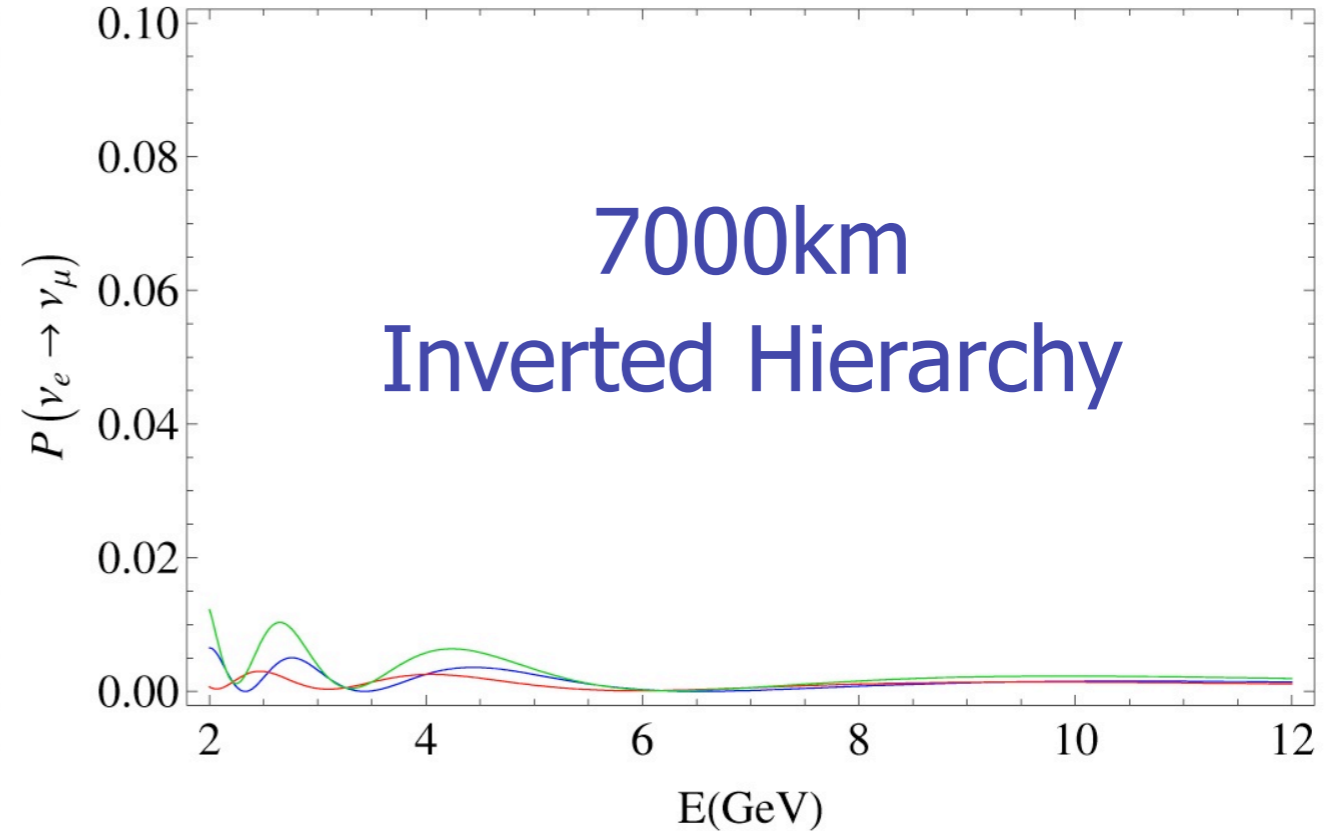
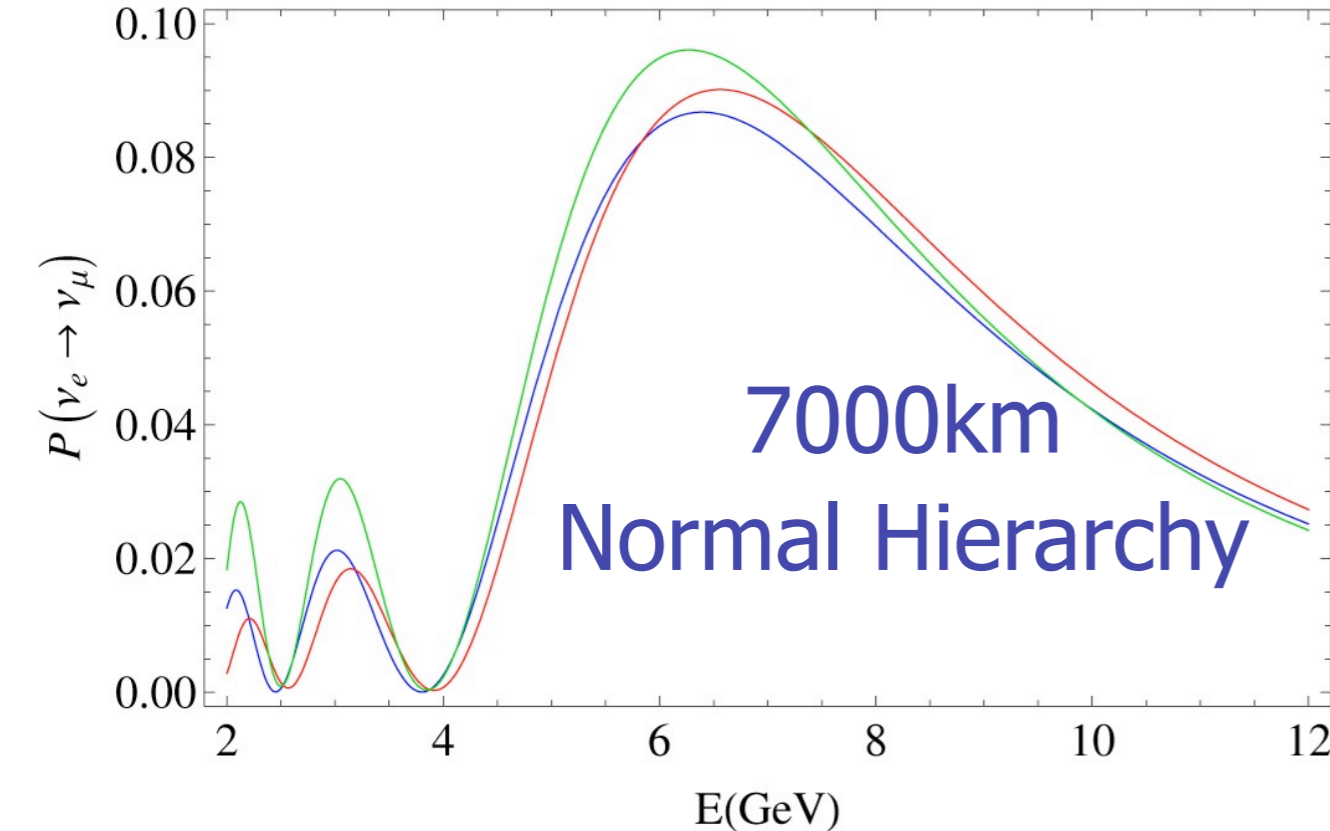
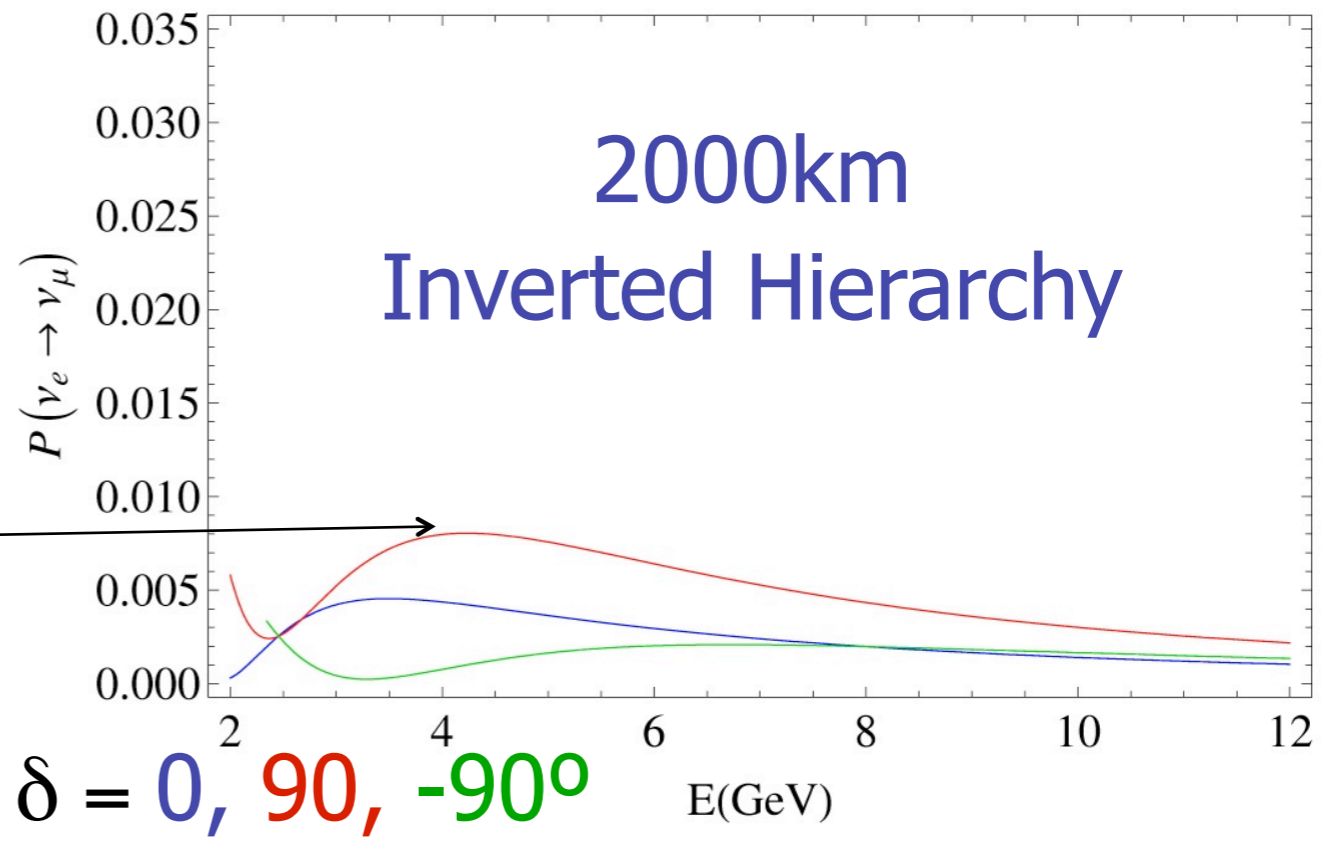
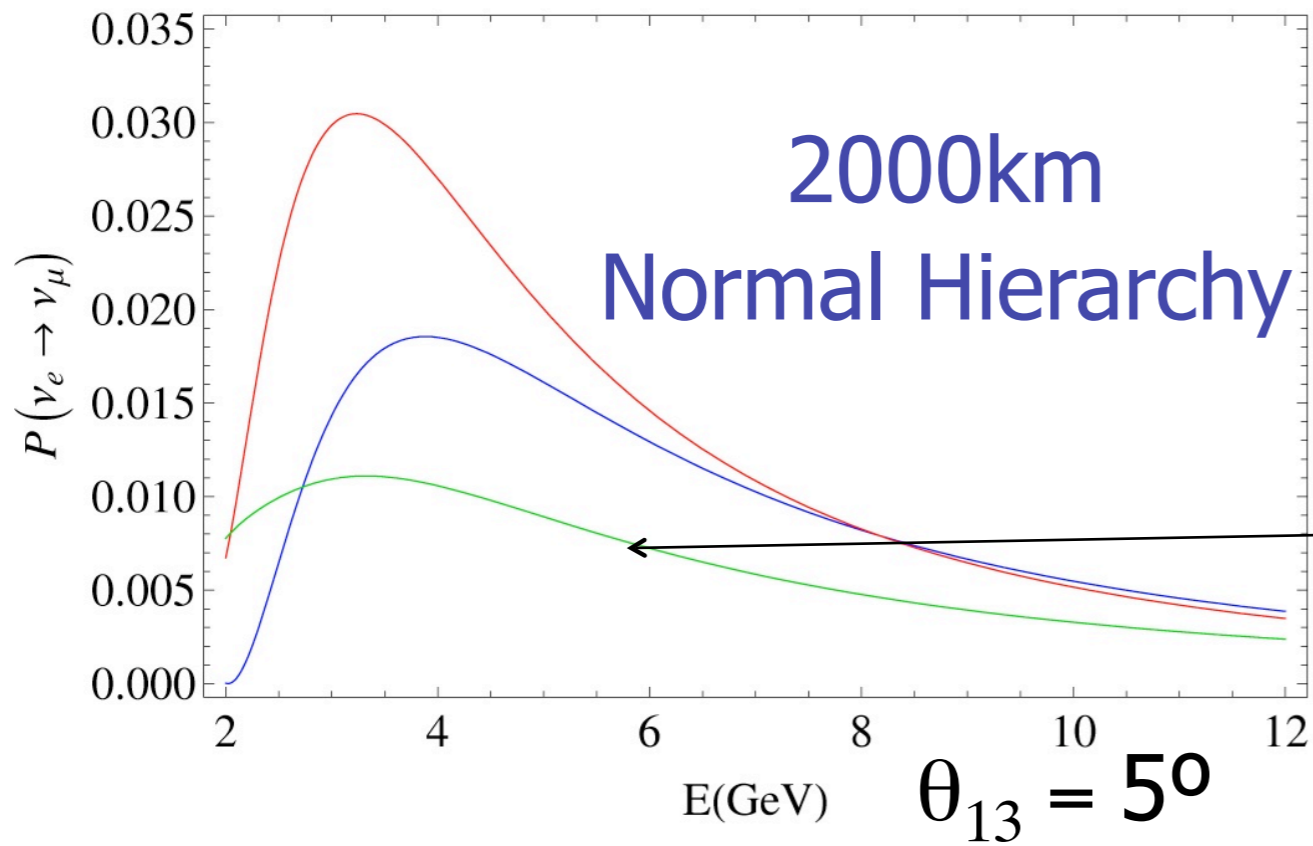


# Add a second baseline and look for $\delta$

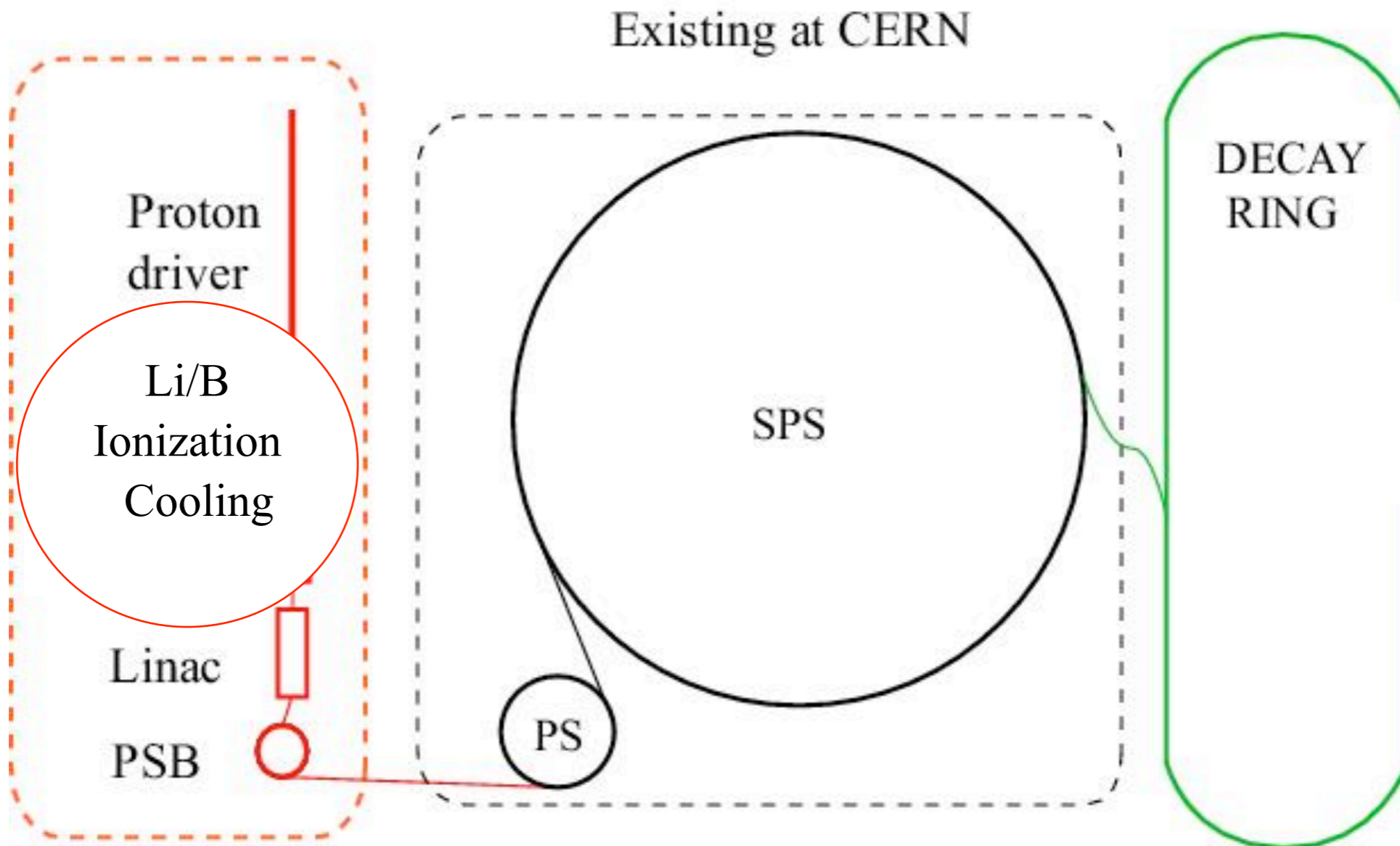




# Add a second baseline and look for $\delta$



## 5. A “cocktail” of $^8\text{Li}/^8\text{B}$ and $^6\text{He}/^{18}\text{Ne}$



$$\langle E_\nu \rangle = 1.2/1.3 \text{ GeV}$$

$$L = 650 \text{ Km}$$

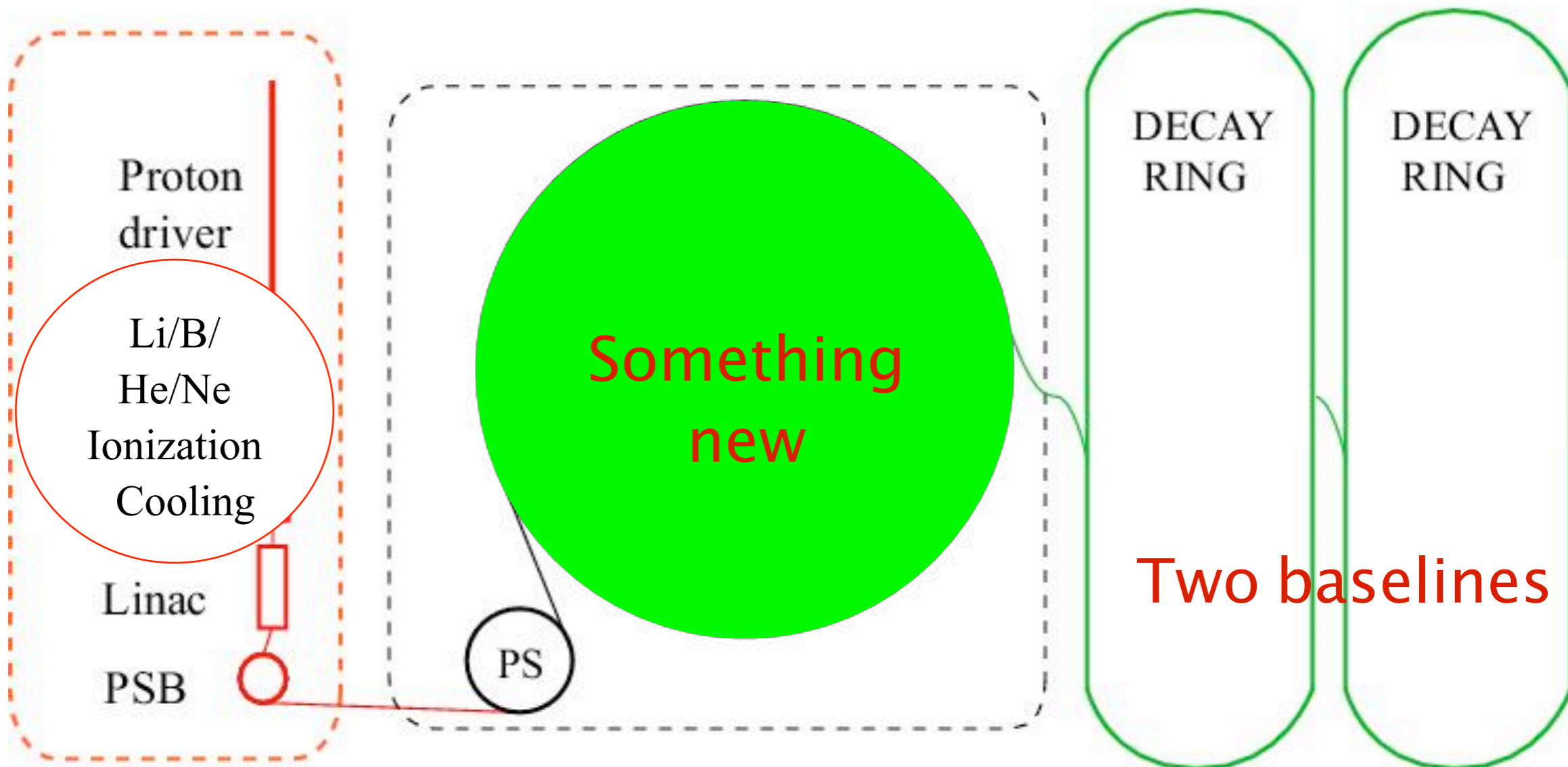
$$\gamma \sim 100$$

A. Donini and E. Fernández Martínez hep-ph/0603261

First and second peak at the same baseline



## 6. A “cocktail” of $^8\text{Li}/^8\text{B}$ and $^6\text{He}/^{18}\text{Ne}$



$$\langle E_\nu \rangle = 2/8 \text{ GeV}$$

$$L = 1000 \text{ Km}$$

$$L = 7000 \text{ Km}$$

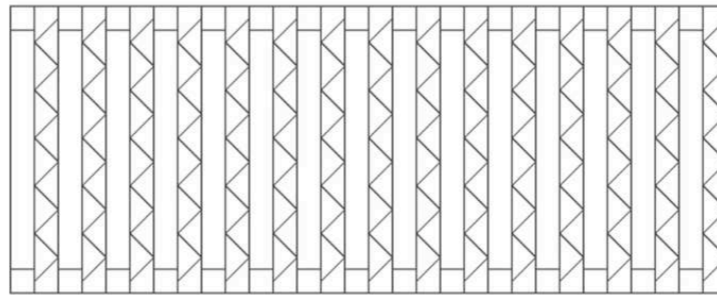
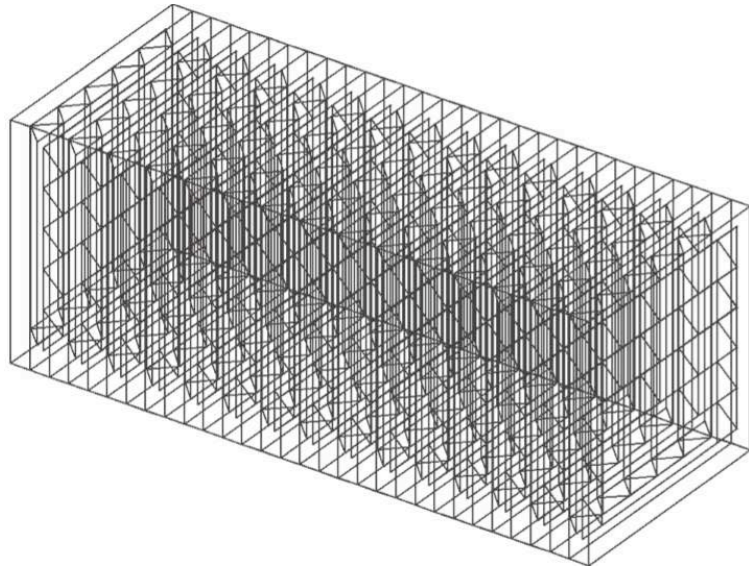
$$\gamma \sim 100$$

$$\gamma \sim 650$$

A. Donini and E. Fernández Martínez hep-ph/0603261

S. K. Agarwalla et al. arXiv:0804.3007

# TASD

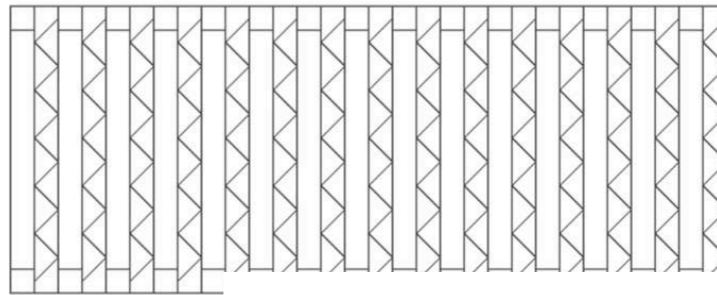
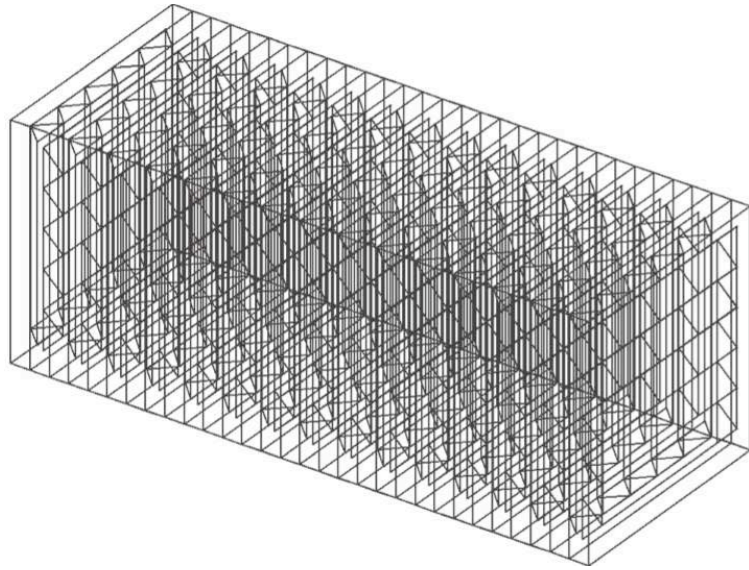


22.5 Kton Mass

An extrapolation of  
MinerVa

Suited for low energy  
muons

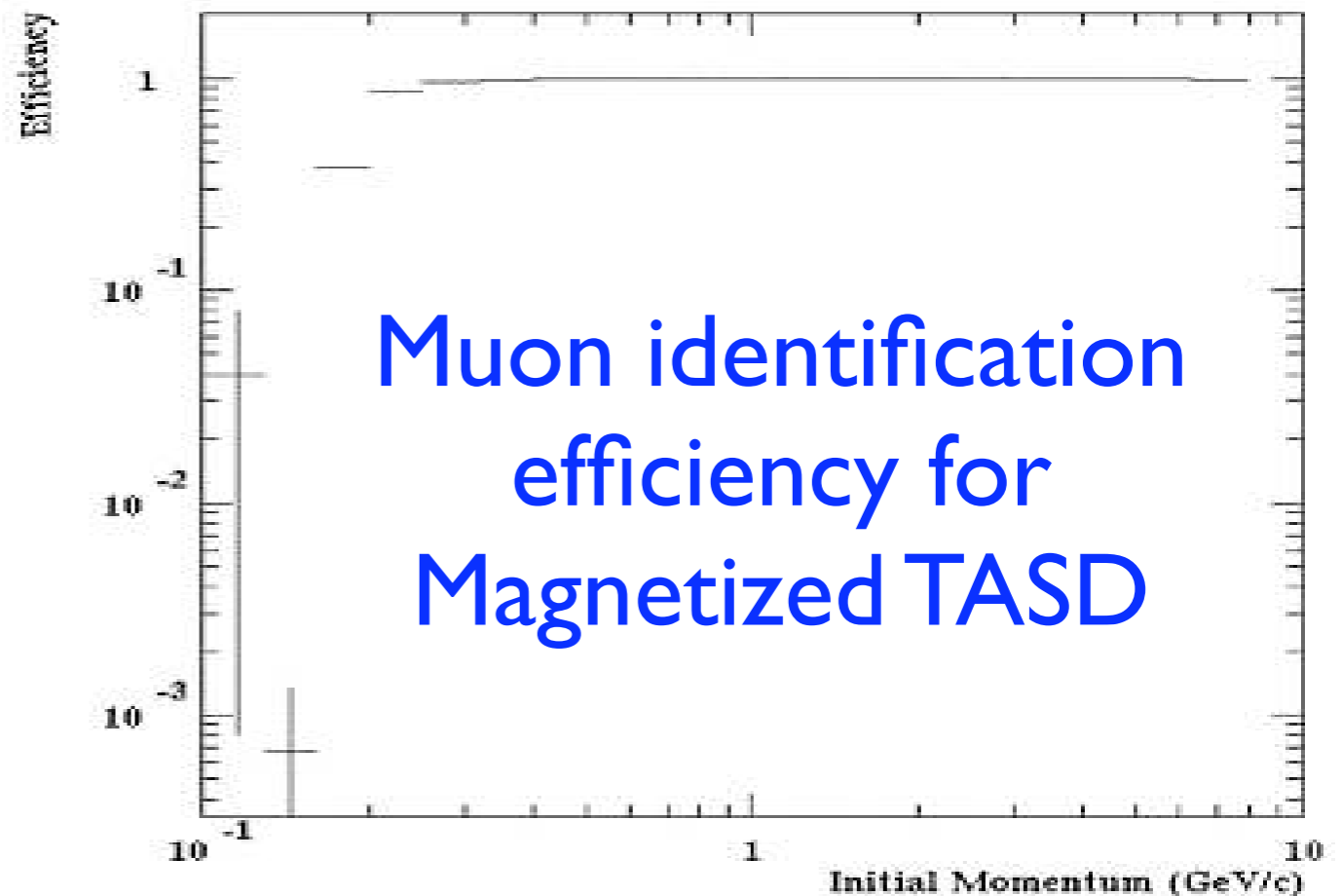
# TASD



22.5 Kton Mass

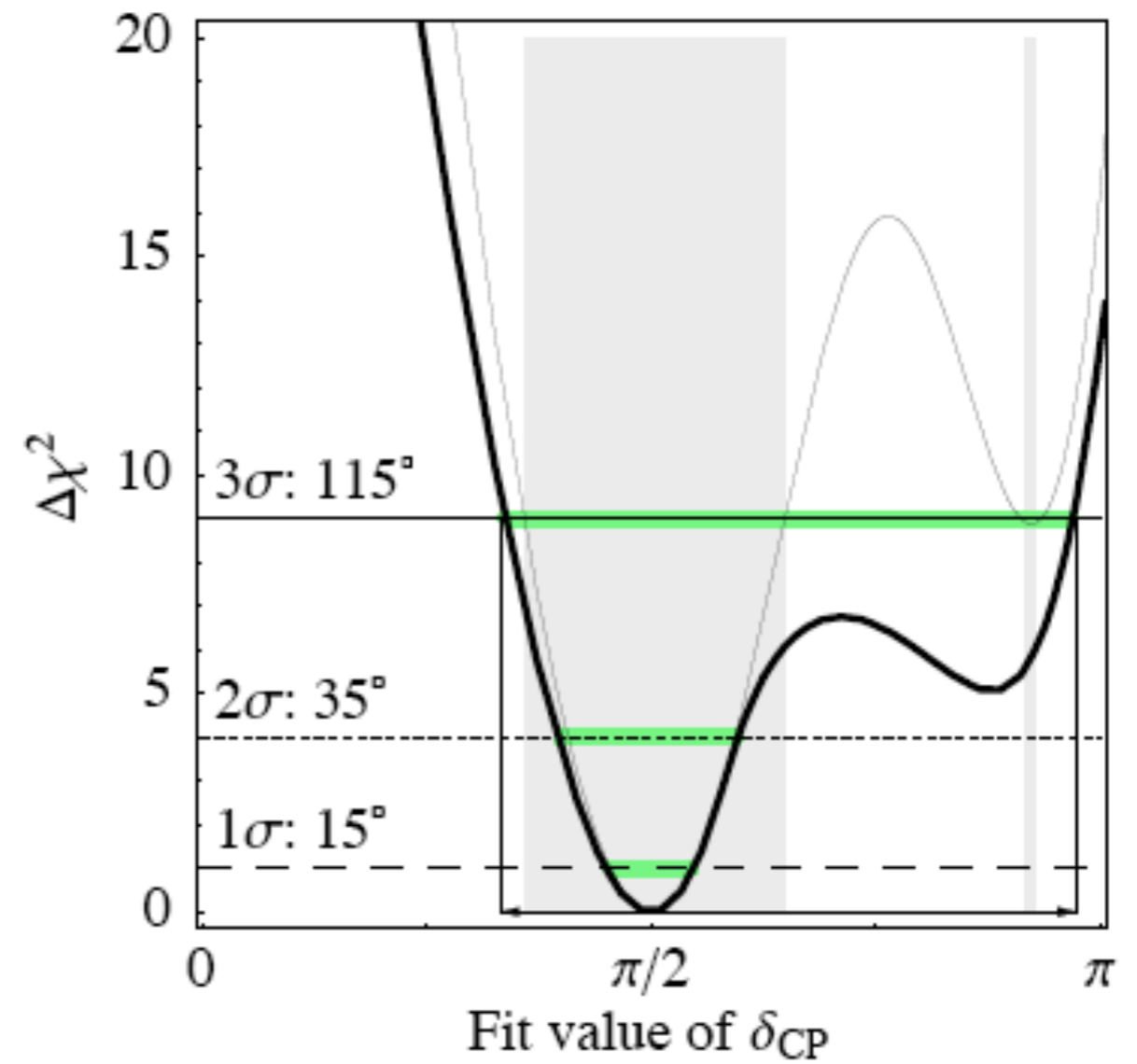
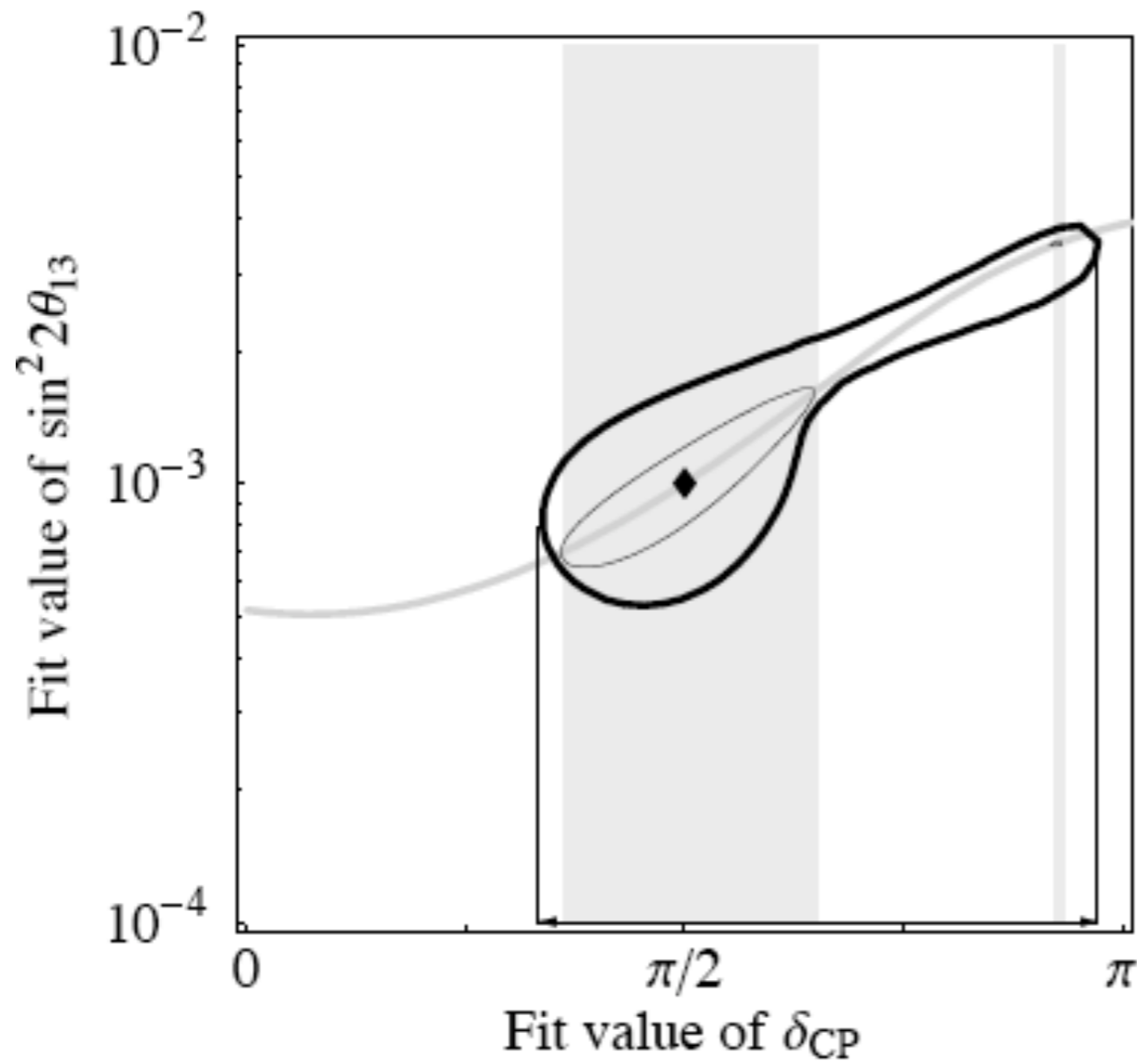
An extrapolation of  
MinerVa

Suited for low energy  
muons

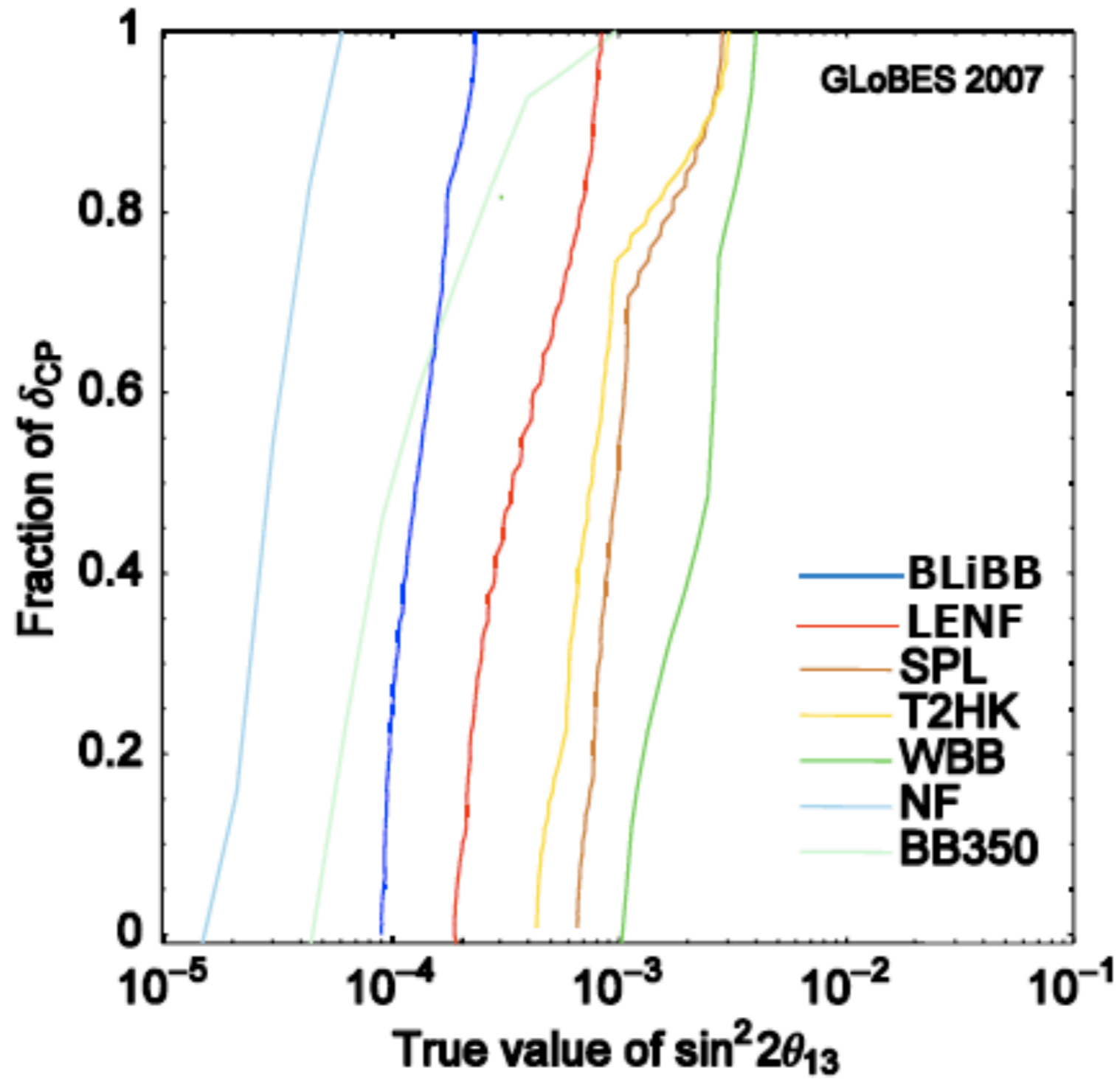


# CONCLUSIONS

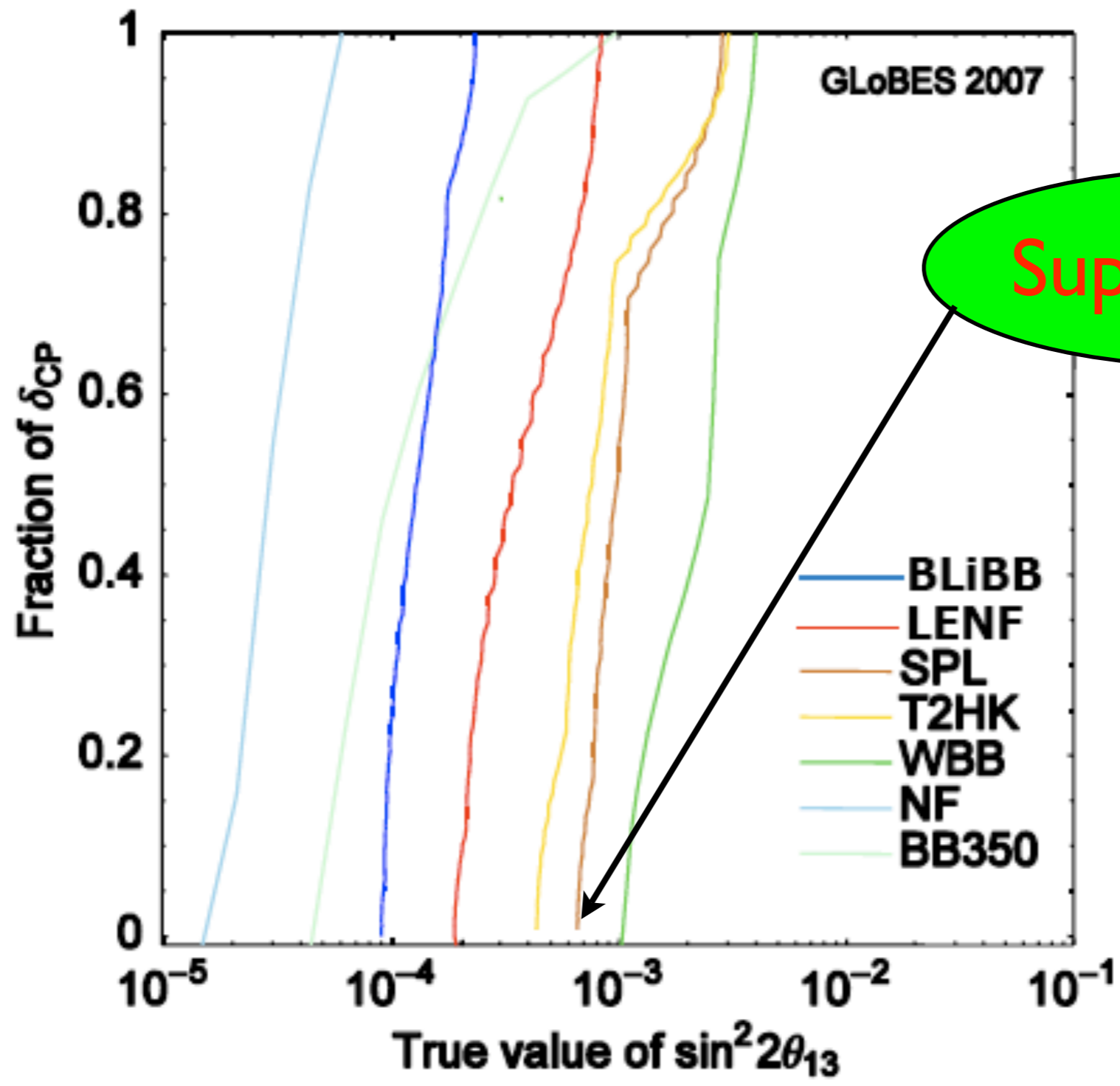
# Definition of the CP-fraction



# Sensitivity to $\sin^2 2\theta_{13}$

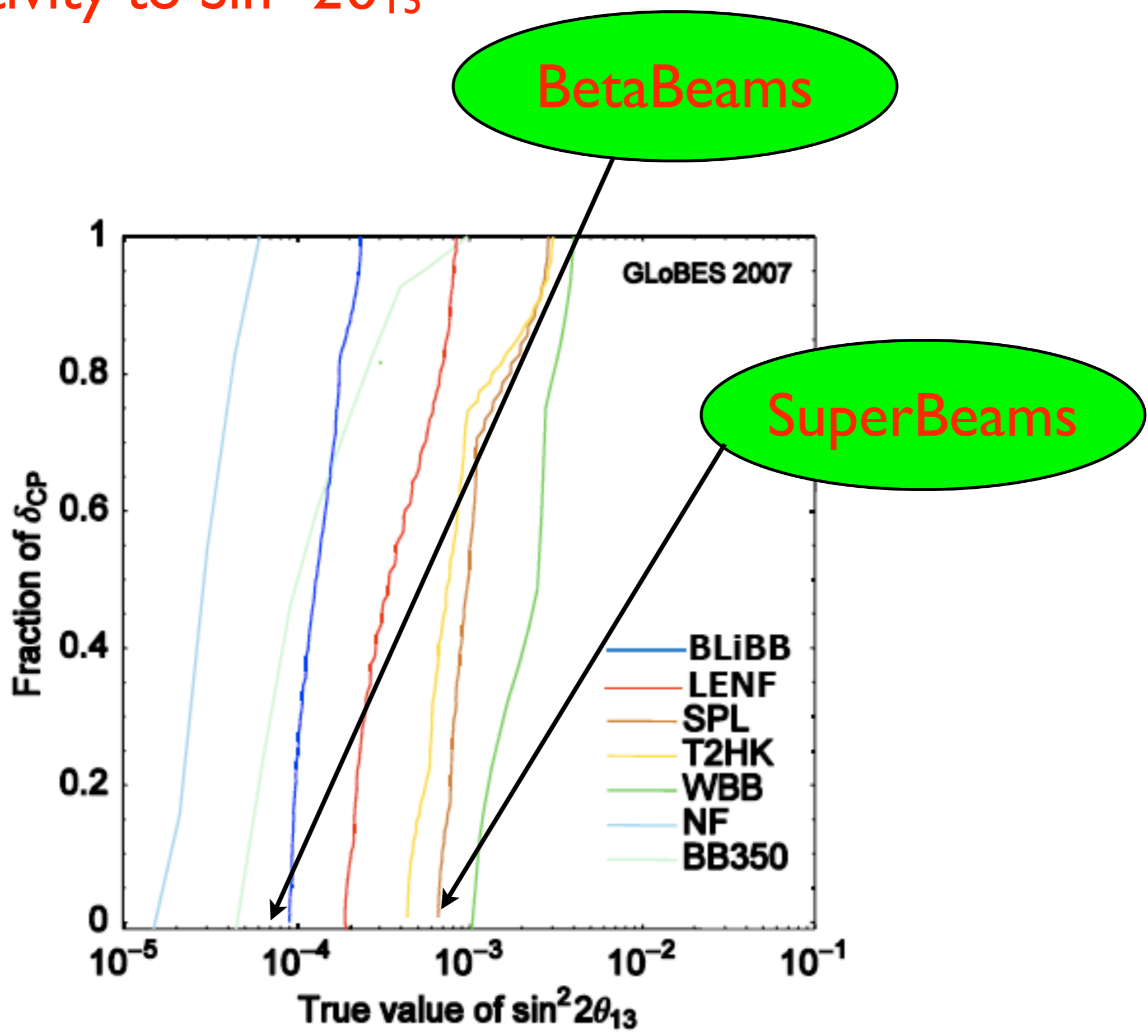


# Sensitivity to $\sin^2 2\theta_{13}$



SuperBeams

# Sensitivity to $\sin^2 2\theta_{13}$



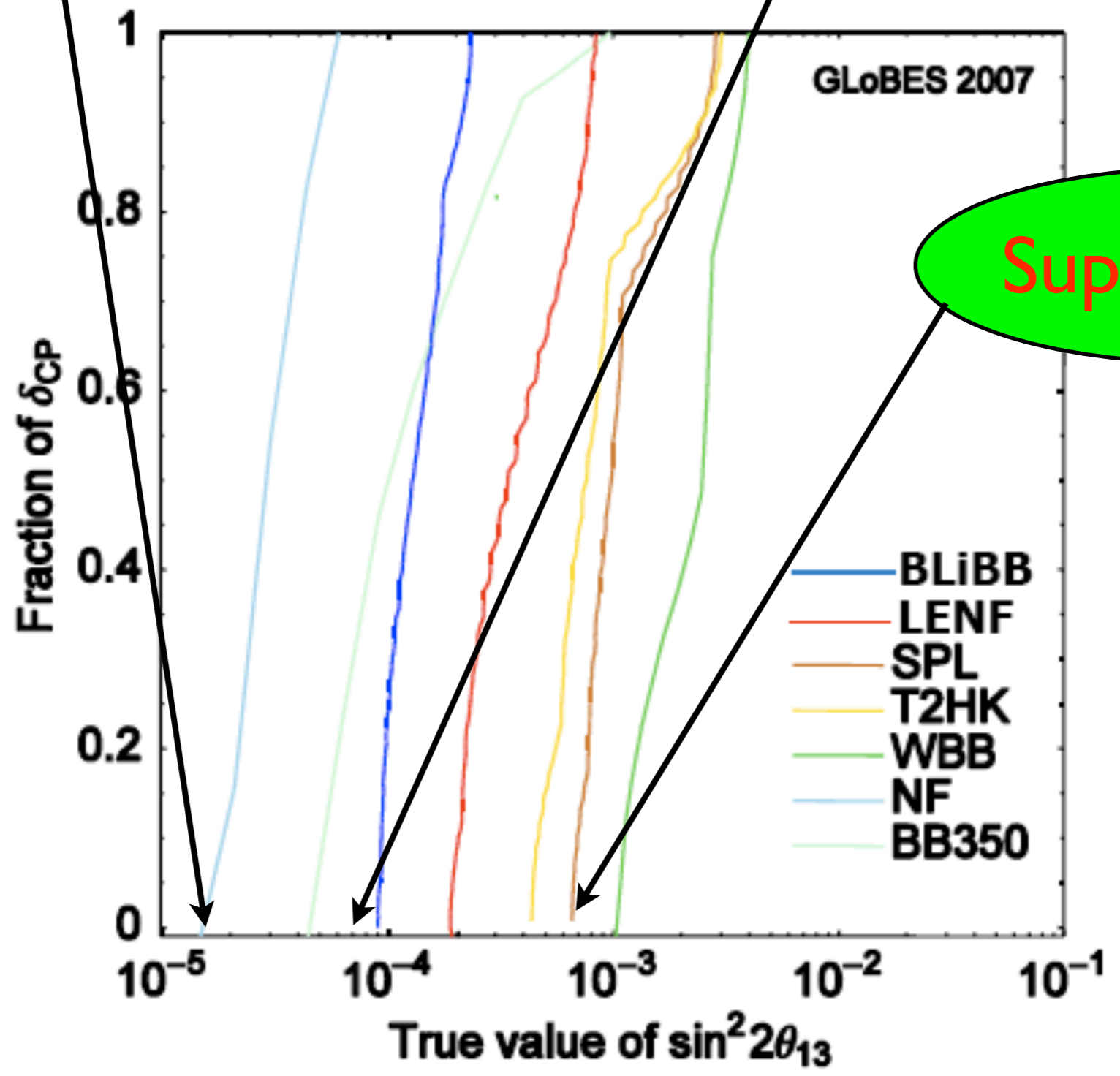


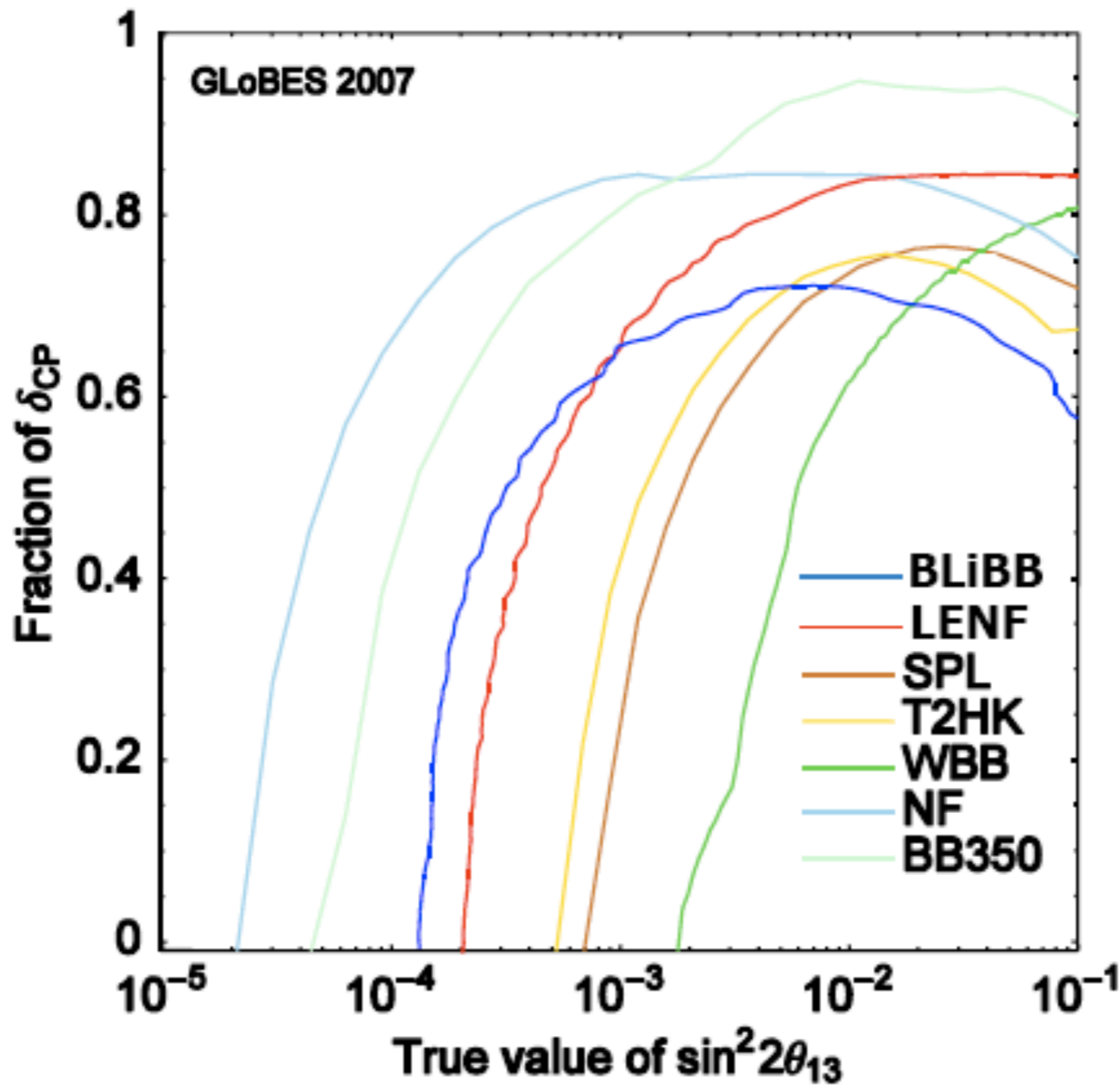
# Sensitivity to $\sin^2 2\theta_{13}$

Neutrino Factory

BetaBeams

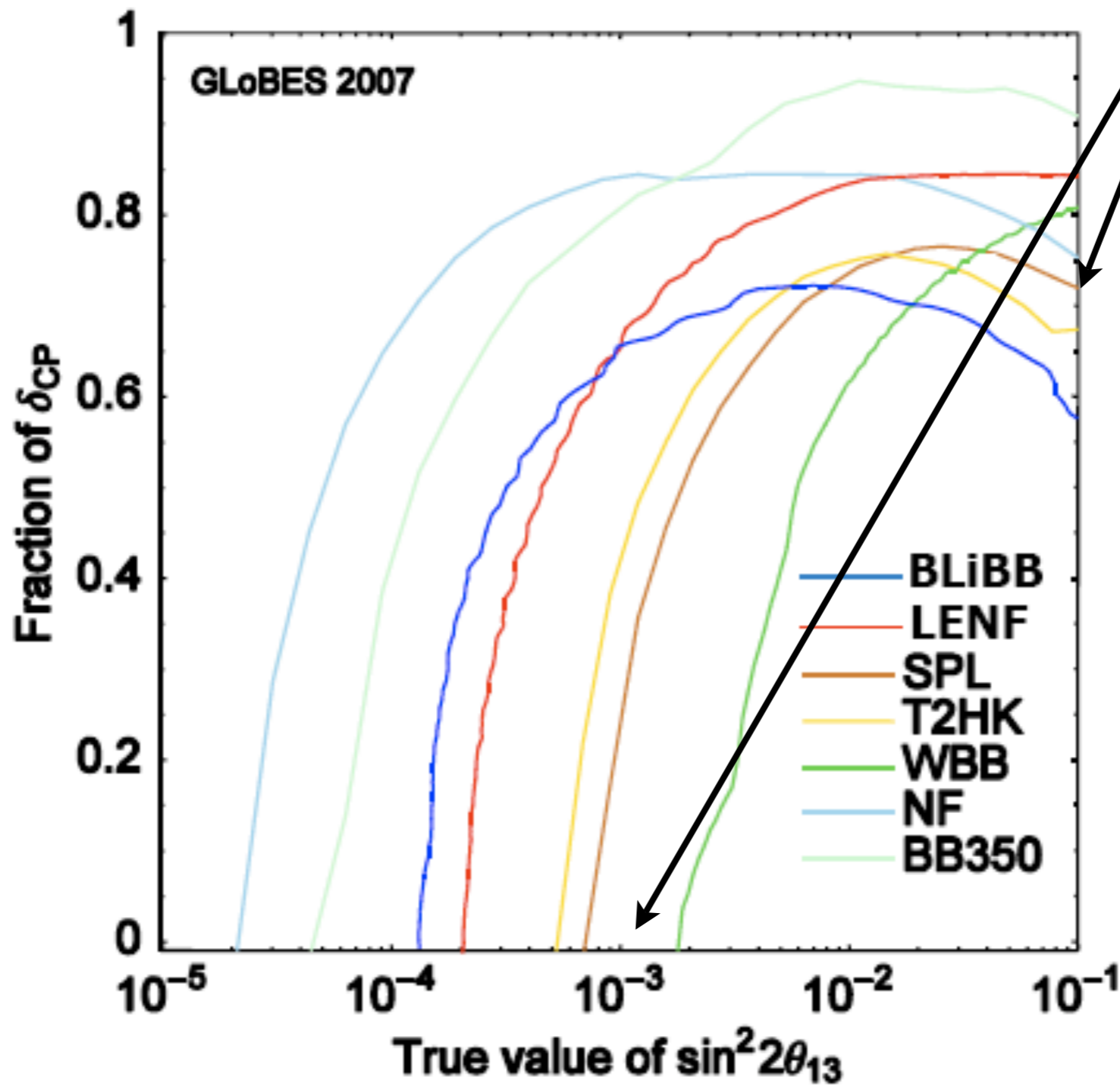
SuperBeams





Sensitivity to  $\delta$

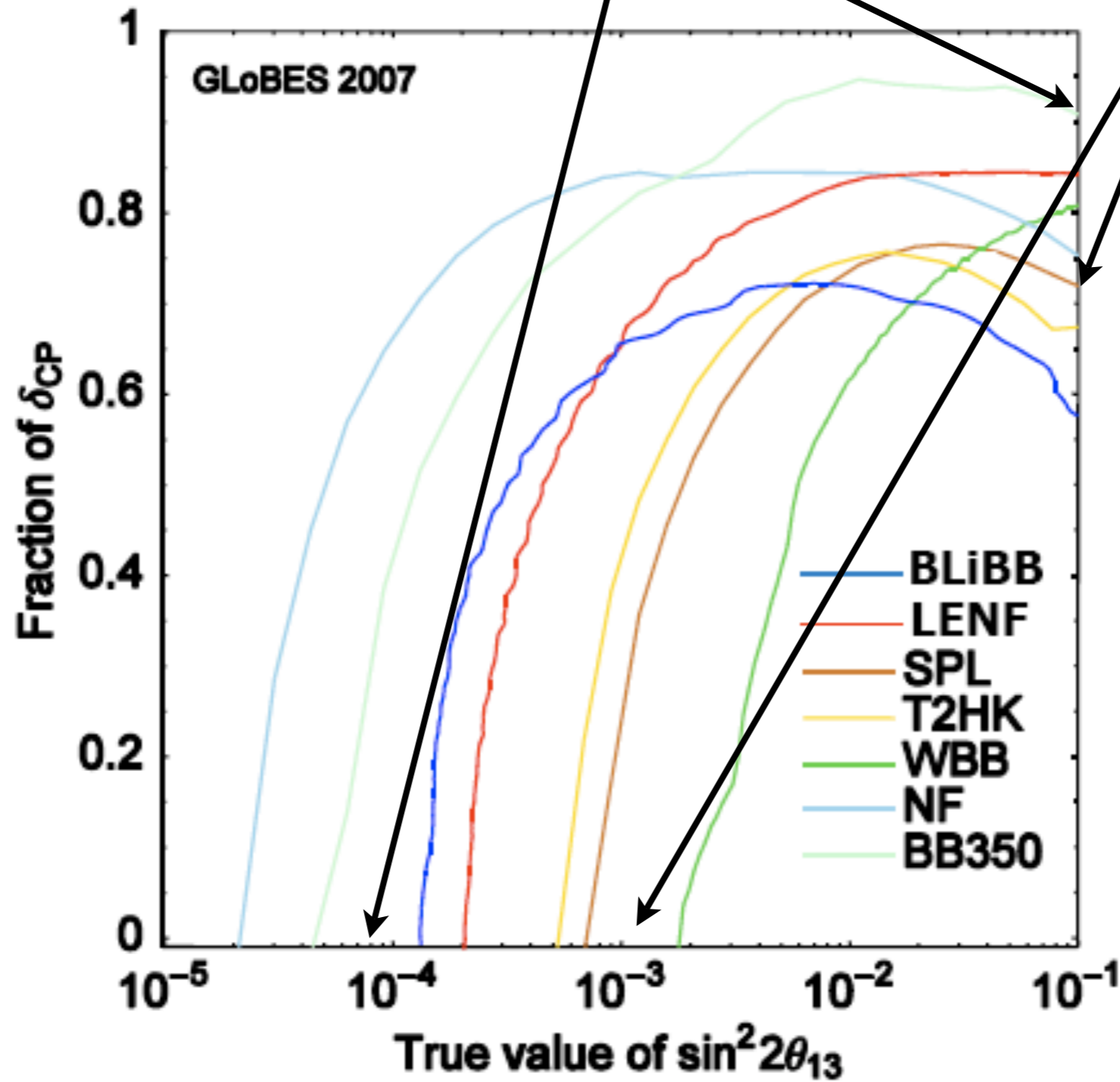
SuperBeams



Sensitivity to  $\delta$

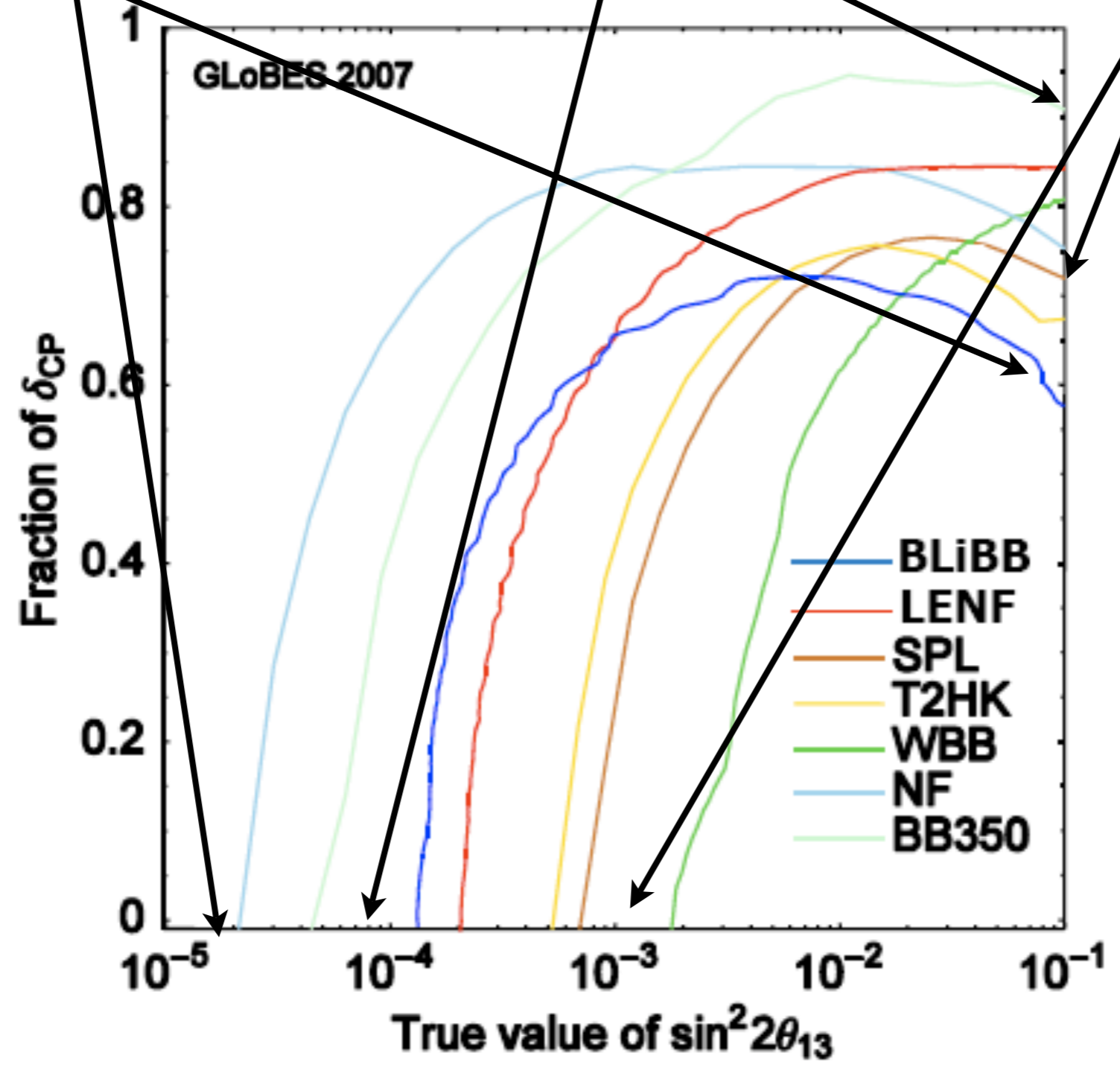
BetaBeams

SuperBeams

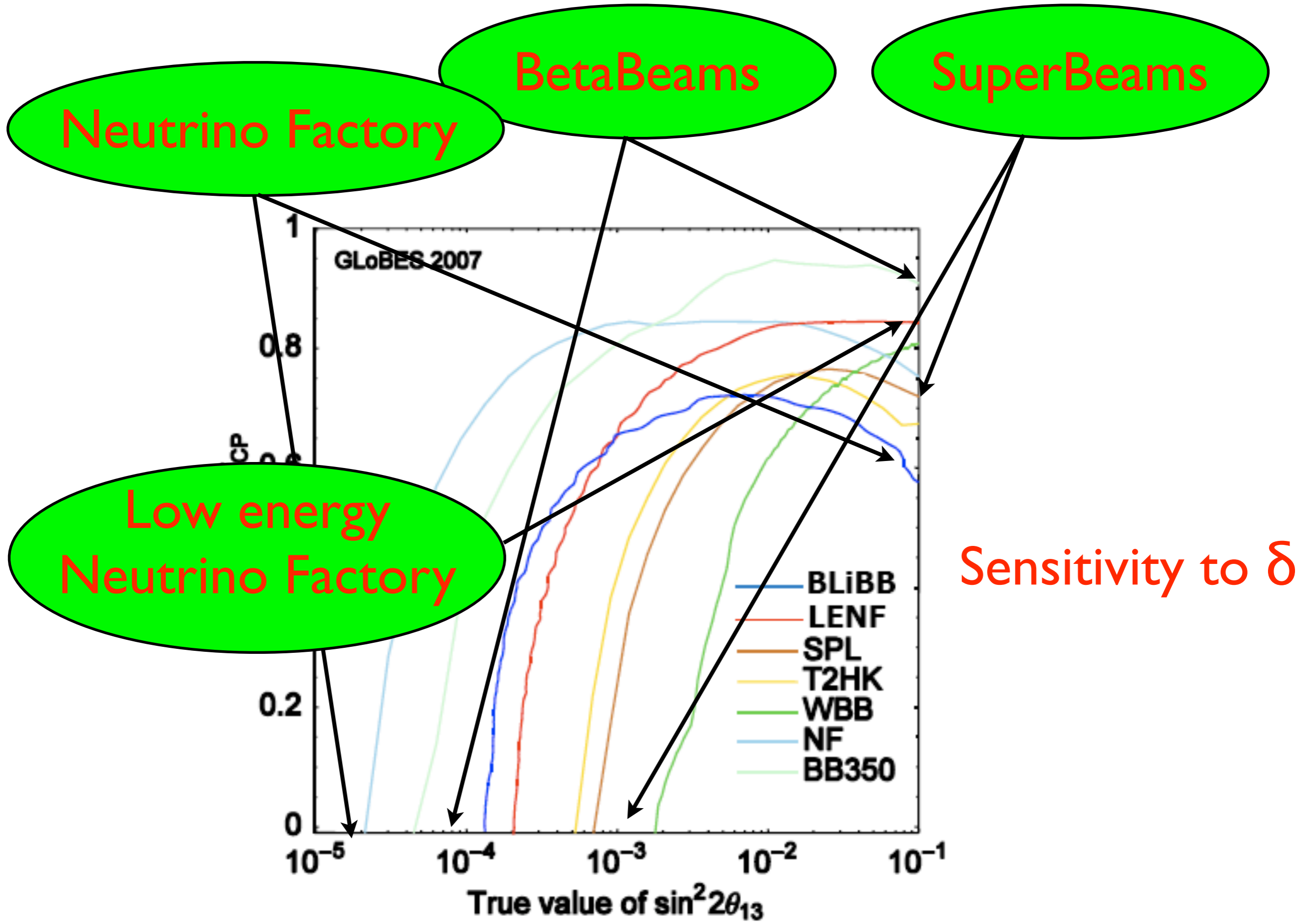


Sensitivity to  $\delta$

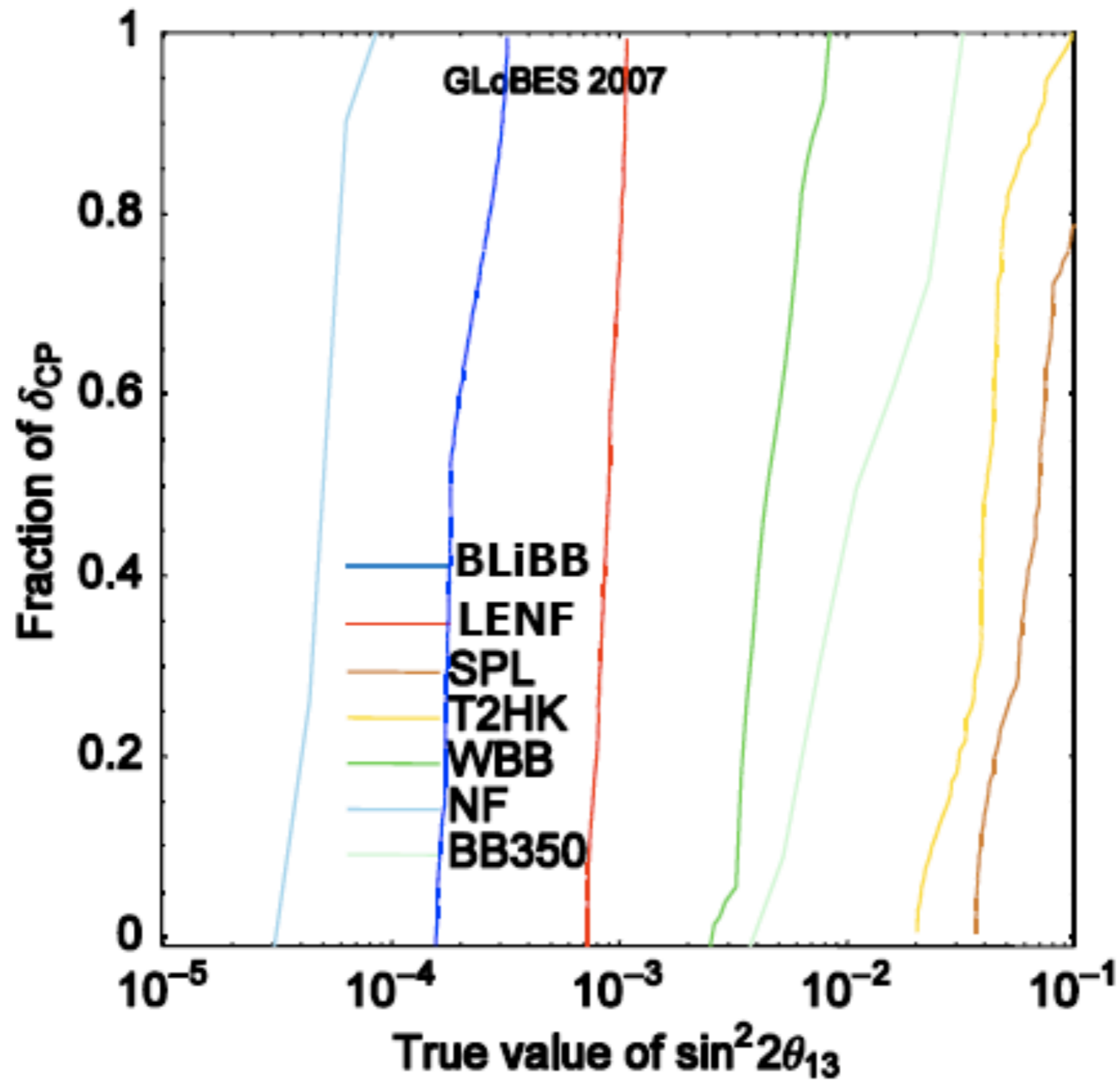
Neutrino Factory      BetaBeams      SuperBeams



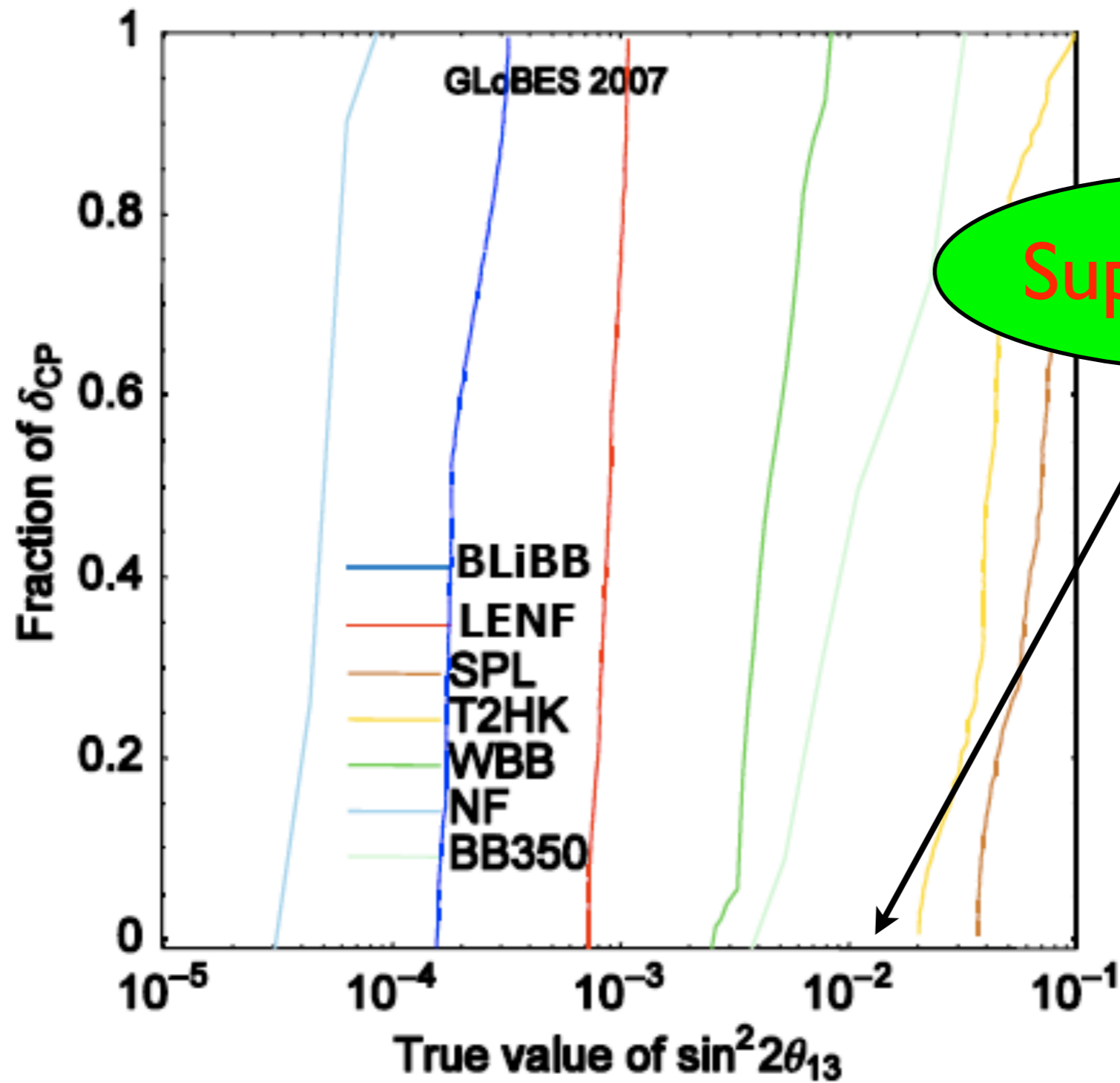
Sensitivity to  $\delta$



# Sensitivity to the hierarchy

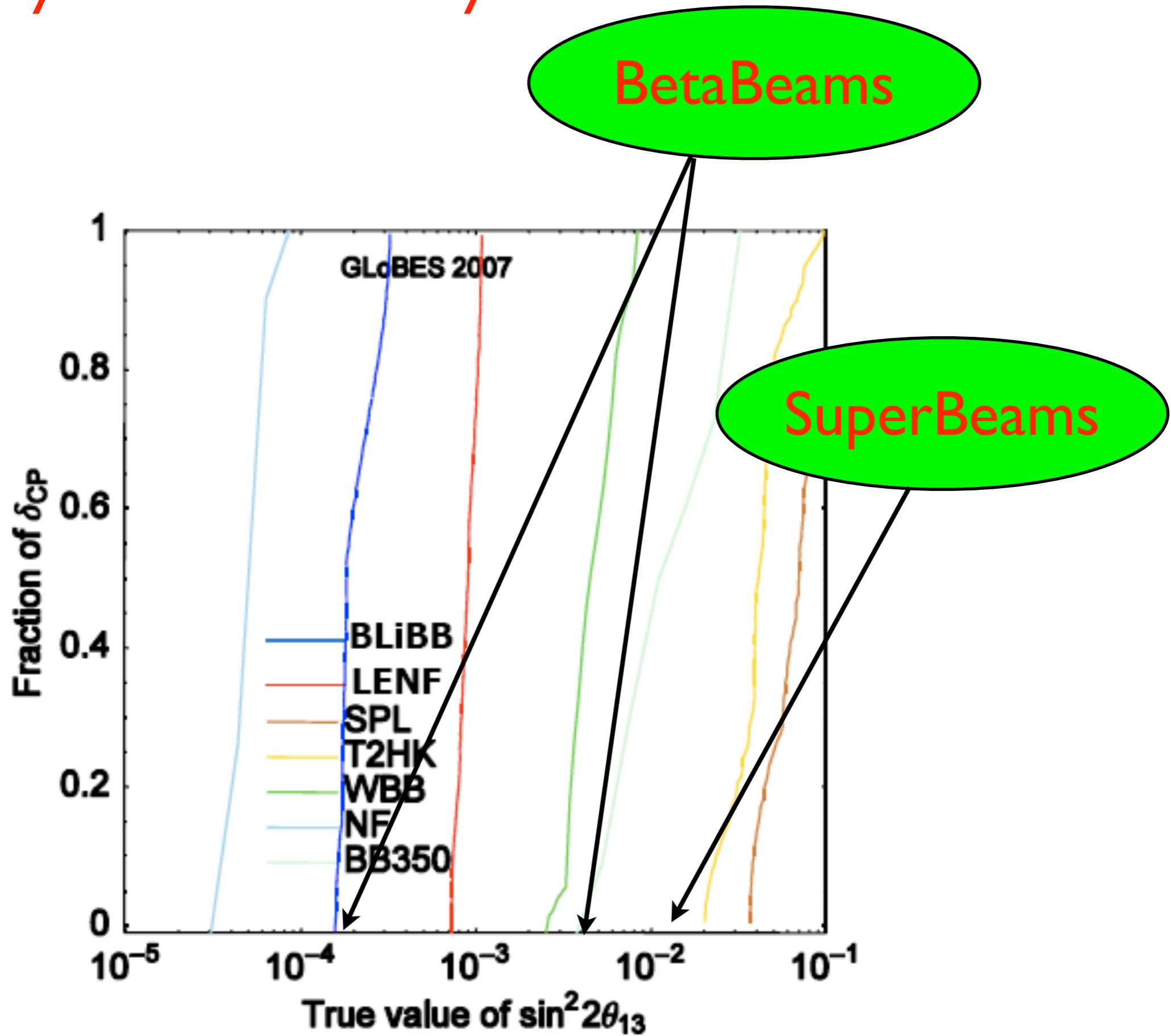


# Sensitivity to the hierarchy

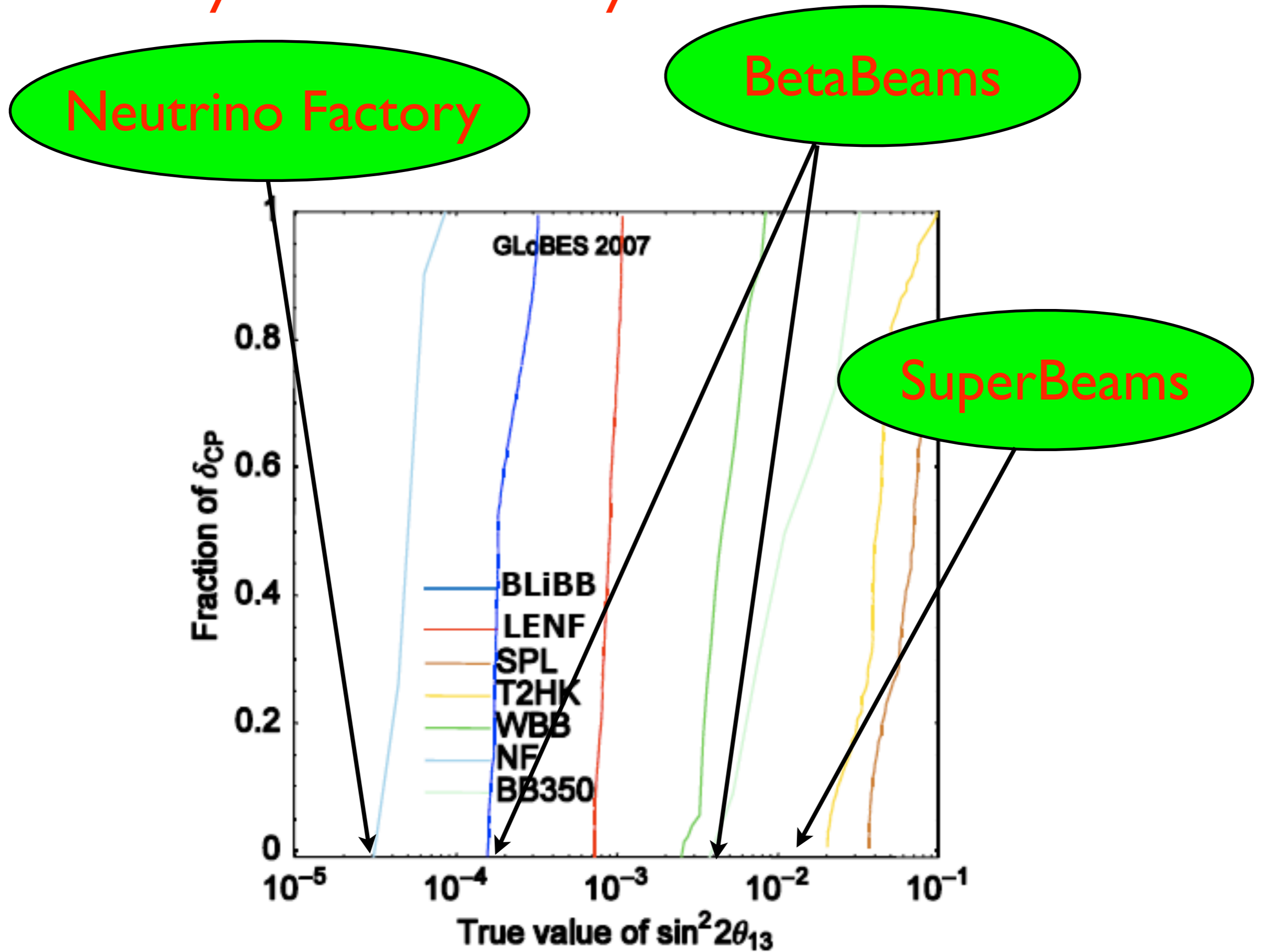




# Sensitivity to the hierarchy



# Sensitivity to the hierarchy



- The goal: measure **at the same time** the four parameters that we do not yet know:  **$\theta_{13}$ ,  $\delta$ , the sign of  $\Delta m^2_{23}$  and the  $\theta_{23}$ -octant**
- A plethora of possibilities (and we are still thinking...). It is crucial to take a decision to see which are the results of D-Chooz, T2K and NOvA.
- If  **$\theta_{13}$**  is large, then it is time for precision physics **AND** to look for new physics

# $\mu \rightarrow e \gamma$ in supersymmetric models with heavy right-handed neutrinos

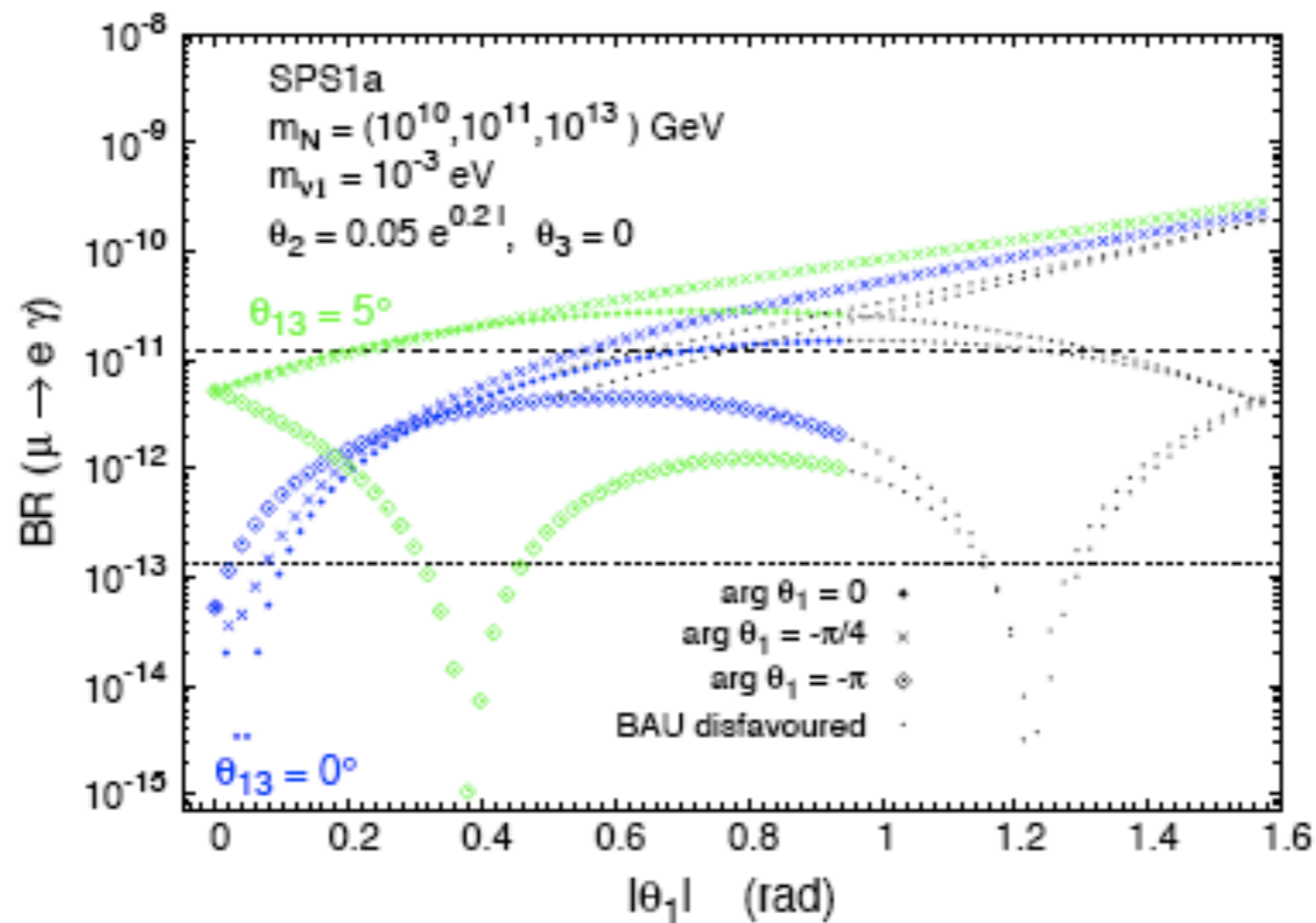


Figure 7:  $BR(\mu \rightarrow e \gamma)$  as a function of  $|\theta_1|$ , for  $\arg \theta_1 = \{0, -\pi/4, -\pi\}$  (dots, times, diamonds, respectively) and  $\theta_{13} = 0^\circ, 5^\circ$  (blue/darker, green/lighter lines). BAU is enabled by the choice  $\theta_2 = 0.05 e^{0.2i}$  ( $\theta_3 = 0$ ). In all cases black dots represent points associated with a disfavoured BAU scenario and a dashed(dotted) horizontal line denotes the present experimental bound (future sensitivity).

E. Arganda et al. hep-ph/0607263



- It is also crucial that accelerator studies continue to understand the feasibility of the more extreme setups, such as the Neutrino Factories or the (high- $\gamma$ ) BetaBeams
- The european neutrino community must take a decision by 2012, according to what we have signed in the FP7 of the EU