

IceCube



# Neutrino Astrophysics

Teresa Montaruli

University of Wisconsin - Madison and University of  
Bari Italy

[tmontaruli@icecube.wisc.edu](mailto:tmontaruli@icecube.wisc.edu)

**The real voyage is not to travel to new landscapes,  
but to see with new eyes...**

**Marcel Proust**

# Lectures contents

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## Lecture 1

- Introduction to neutrino astronomy
- connections with cosmic rays and gamma-astronomy
- calculation of neutrino fluxes from gamma fluxes
- candidate sources: galactic sources
- UHECR and Auger

## Lecture 2

- Extra-galactic sources: AGNs and GRBs
- Calculation of rates
- Detection Technique
- Main Parameters of Detectors
- Existing detectors

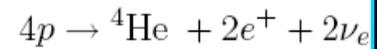
## Lecture 3

- Event topologies and reconstructions
- Example of analyses
- Point-source analysis and current results
- Atmospheric neutrino analysis
- Current physics results
- SN collapse

# The Birth of Neutrino Astronomy

## Neutrinos from thermonuclear reactions in the Sun

R. Davis



$$\sim 6 \times 10^{10} \nu \text{ cm}^{-2} \text{ s}^{-1}$$
$$E_\nu \sim 0.1 - 20 \text{ MeV}$$

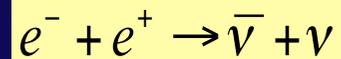
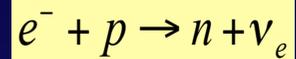
**~ 10 s bursts of 10 MeV  $\nu$ s from stellar collapse**

Nobel Prize in Physics 2002

M. Koshiba

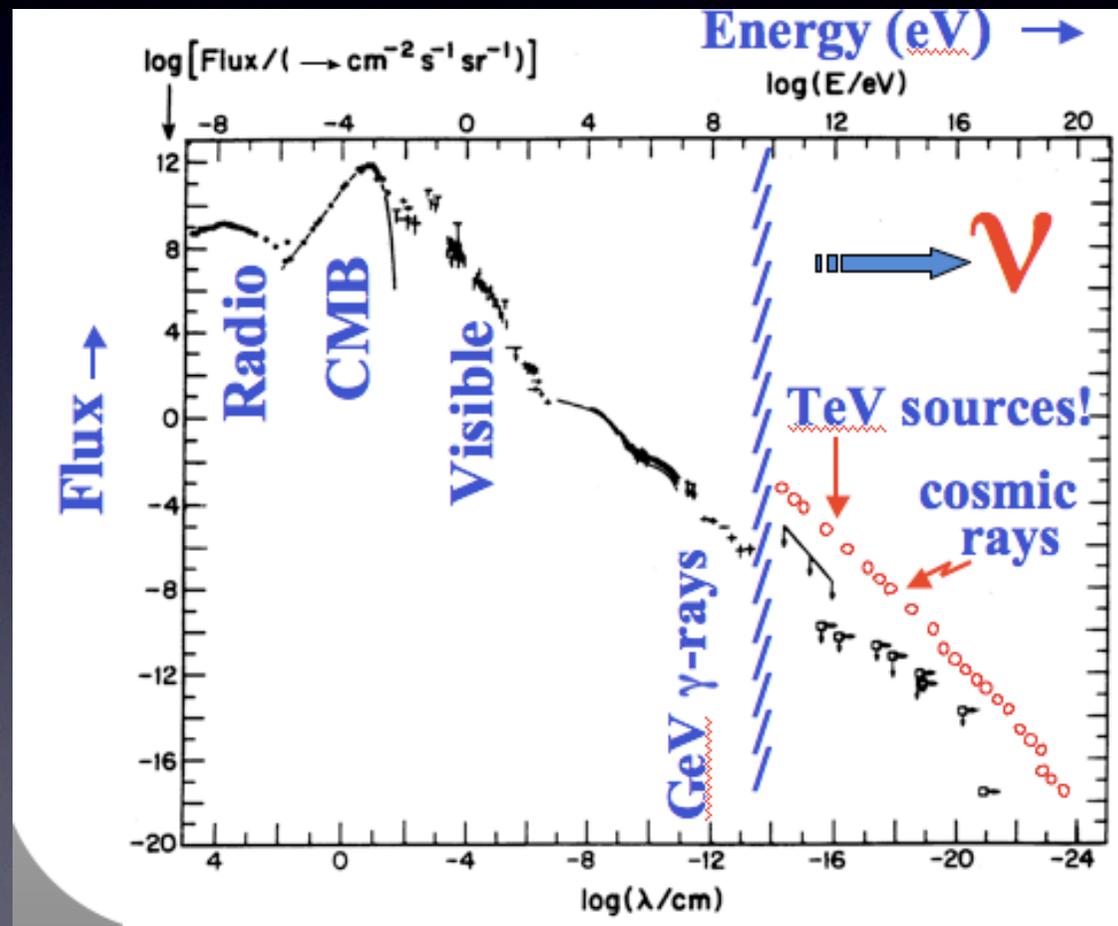


**Neutronization  
Thermalization:**

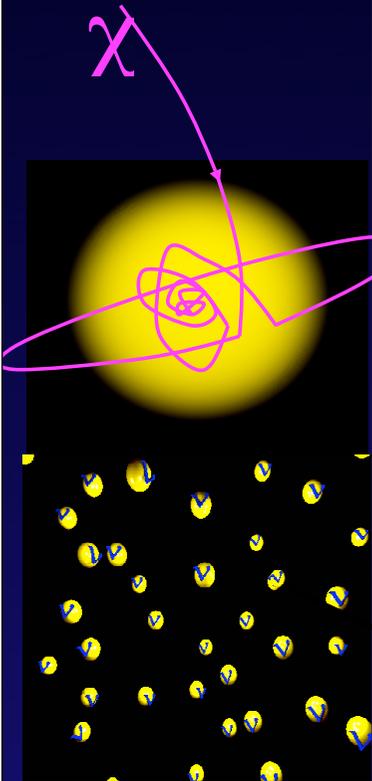
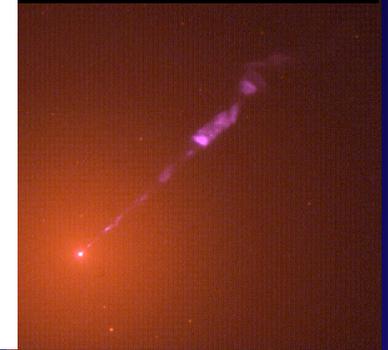
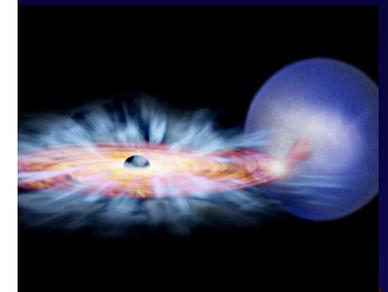
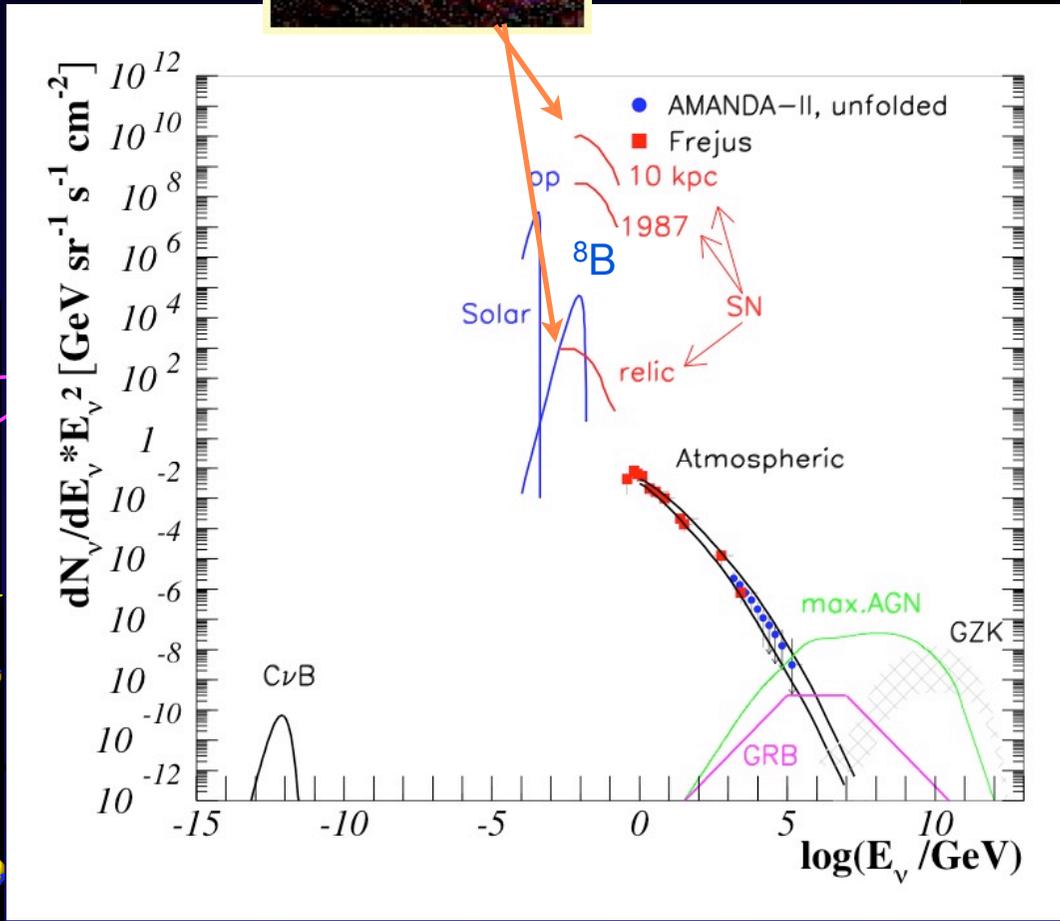
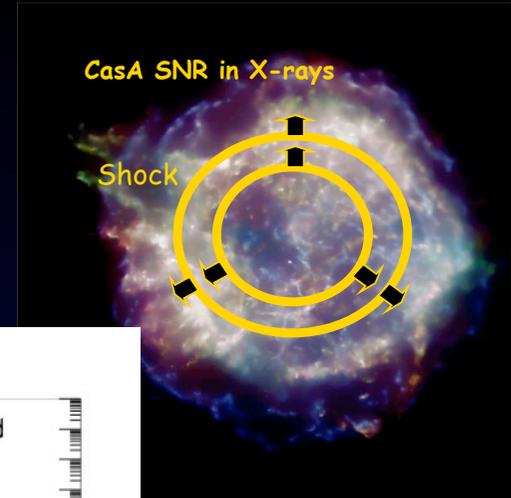
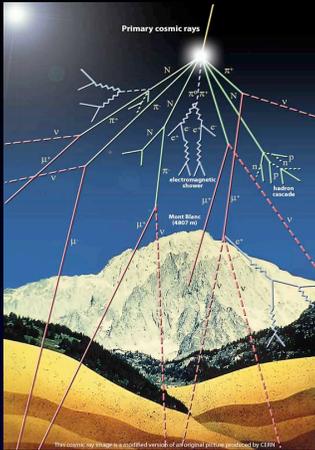


SN1987A

# CRs and Neutrinos



# Neutrino Fluxes



# Messengers of the universe

## absorption

$\gamma$ -rays:  $\gamma + \gamma_{2.7k}$

proton:  $p + \gamma_{2.7k} \rightarrow \pi^0 + X$

neutrinos:  $\nu + \nu_{1.95K} \rightarrow Z+X$

## cut-off

$>10^{14}eV$

$>5 \cdot 10^{19}eV$

$>4 \cdot 10^{22}eV$

## mean free path

10 Mpc

50 Mpc

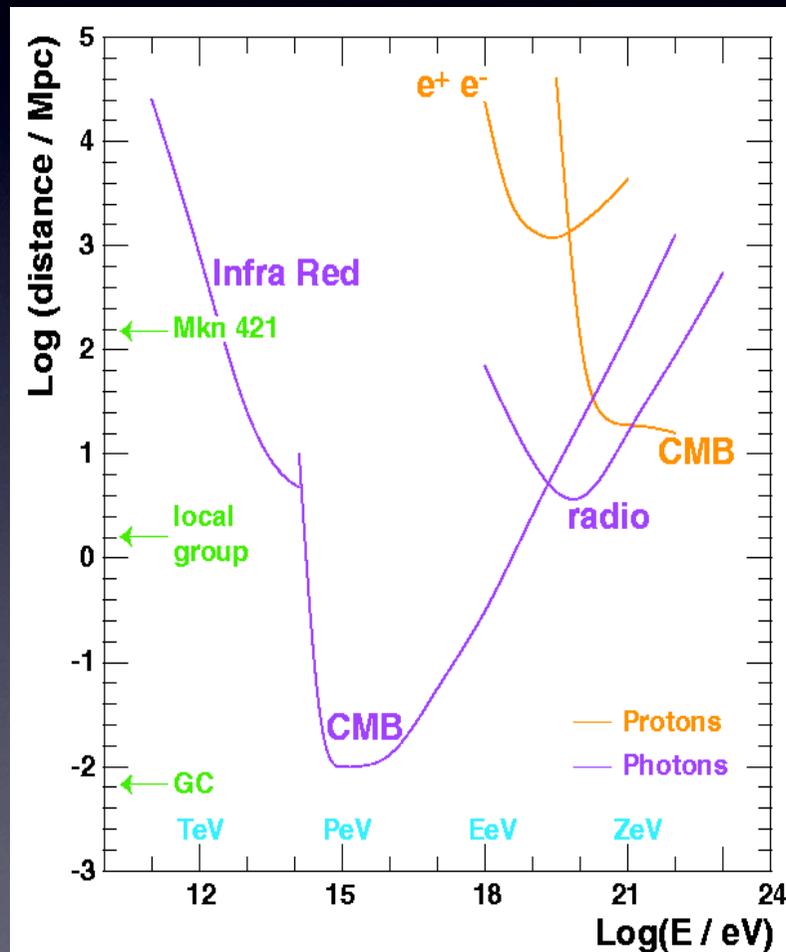
(40 Gpc)

$1pc = 3.26 ly = 3.1 \cdot 10^{13} km$

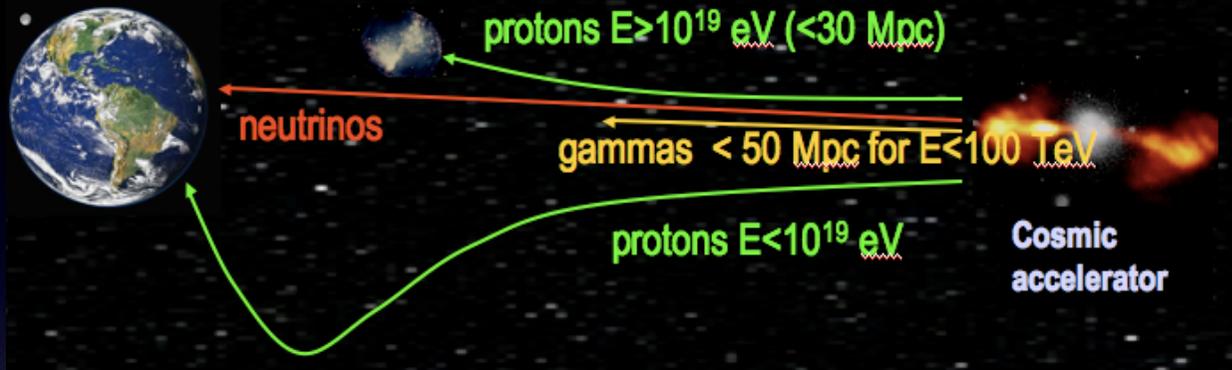
$1 Mpc \sim 3.1 \times 10^{24} cm$

$p$  and gamma astronomy  
have not access to the  
entire Universe

Particles are  
messengers if the point  
back to sources  
(neutral or UHE)

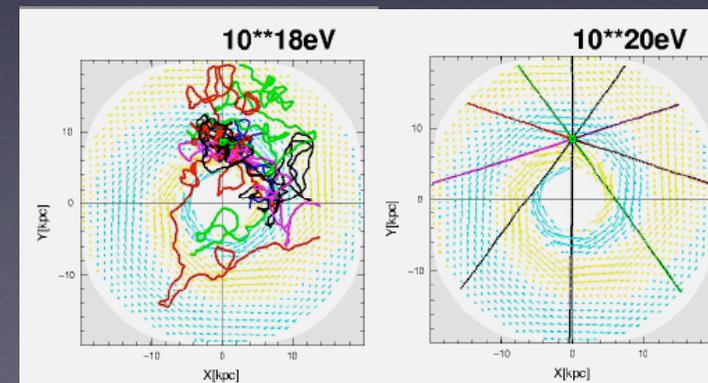


# Astronomy



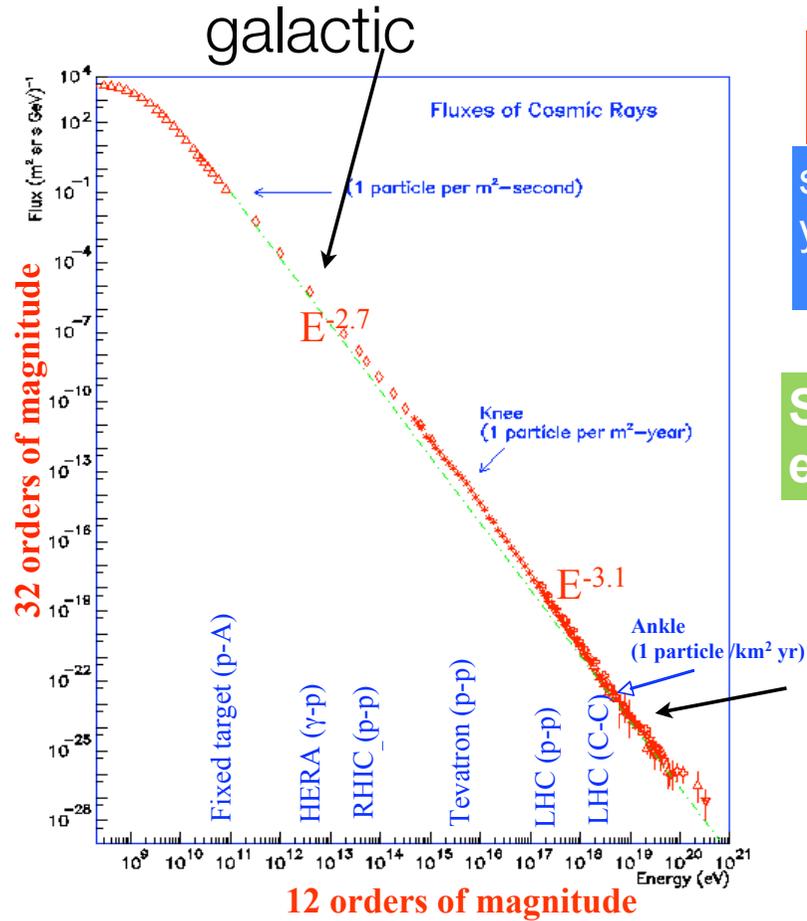
- **Neutrons:** decay  $\gamma_{ct} = E/m c t \approx 10 \text{ kpc}$  for  $E \sim E_{\text{TeV}}$
- **Photons:** currently provide most information on the Universe but they are **reprocessed in sources** and **interact during propagation with extra-galactic backgrounds**. For  $E > 500 \text{ GeV}$  they do not survive the journey from the Galactic Centre
- **Protons:** directions **scrambled** by the galactic and intergalactic magnetic fields

$$\vartheta \cong \frac{d}{R_{\text{gyro}}} = \frac{dB}{E} \Rightarrow \frac{\vartheta}{0.1^\circ} = \frac{\left[ \frac{d}{1 \text{ Mpc}} \right] \left[ \frac{B}{1 \text{ nG}} \right]}{\left[ \frac{E}{3 \times 10^{20} \text{ eV}} \right]}$$



# Cosmic Rays

1 TeV = 1.6 erg  
 1 EeV = 0.16 Joule



Below the knee (galactic CRs):

observed energy density of galactic CR:  
 $\sim 10^{-12}$  erg/cm<sup>3</sup>

supernova remnants: 10<sup>50</sup> ergs every 30 years  
 $\sim 10^{-12}$  erg/cm<sup>3</sup>

SNRs provide the environment and energy to explain the galactic CRs!

Who are the sources of the highest energy CRs?  
 A 320 EeV CR has 50 J (energy of a tennis ball!)

# The knee

- Acceleration cutoff  $E_{\max} \sim ZBL \sim Z \times 100 \text{ TeV (SNR)}$ , change in acceleration mechanisms
- A-dependent knee (cannonball model) not preferred respect to Z (Kascade)
- Rigidity dependent cutoff due to confinement of CRs in the galaxy
- Change in interaction properties (eg. onset of a channel where energy goes into unseen

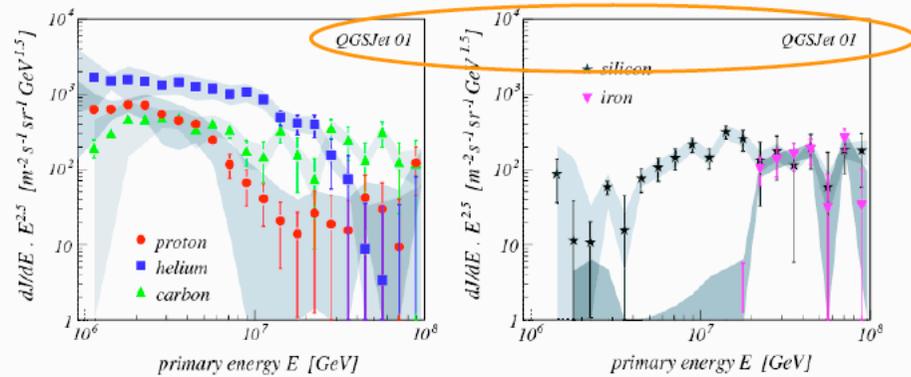


Fig. 14. Unfolded energy spectra for H, He, C (left panel) and Si, Fe (right panel) based on QGSJet simulations. The shaded bands are an estimate of the systematic uncertainties due to the used parameterizations and the applied unfolding method (Gold algorithm).

Observed knee for p at about 4000 TeV  
 Z dependent knee favored by data  
 Depends on interaction models

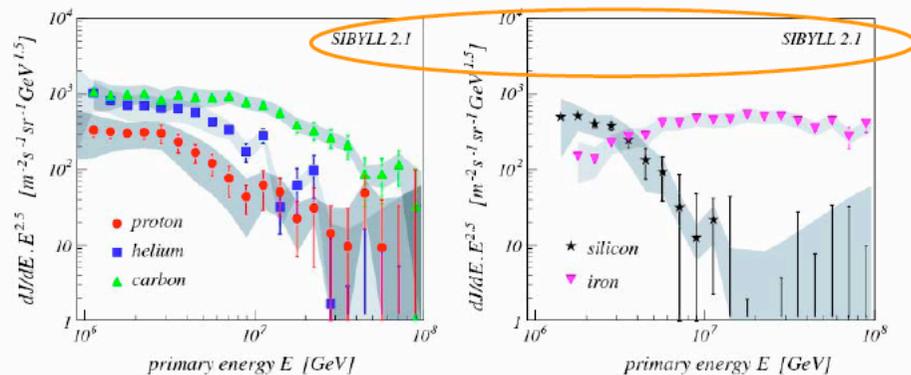
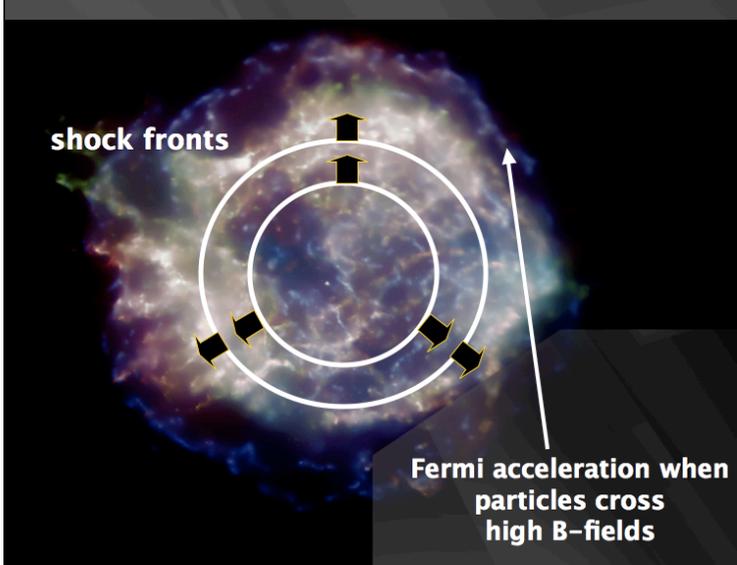


Fig. 15. Unfolded energy spectra for H, He, C (left panel) and Si, Fe (right panel) based on SIBYLL simulations. The shaded bands are estimates of the systematic uncertainties due to the used parameterizations and the applied unfolding method (Gold algorithm).

# Supernova remnants and shock acceleration

Cas A supernova remnant in X-rays



In 1<sup>st</sup> order Fermi particles are efficiently accelerated since energy increases on both directions across shock

- conserve  $m, E, p$  across the shock front
- Energy gain crossing shock in either direction

**A shock is a transition layer where the velocity field of the fluid suddenly decreases**

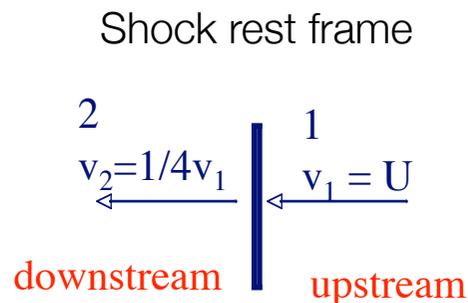
Continuity equation (conservation of mass across shock):  $\rho_1 v_1 = \rho_2 v_2$

For ionized gas  $R =$  compression ratio  $= \rho_2 / \rho_1 = v_1 / v_2 = 4$

4 gas theory

Increase of energy for particle crossing the shock front in both directions:  $\Delta E/E \sim U/c$

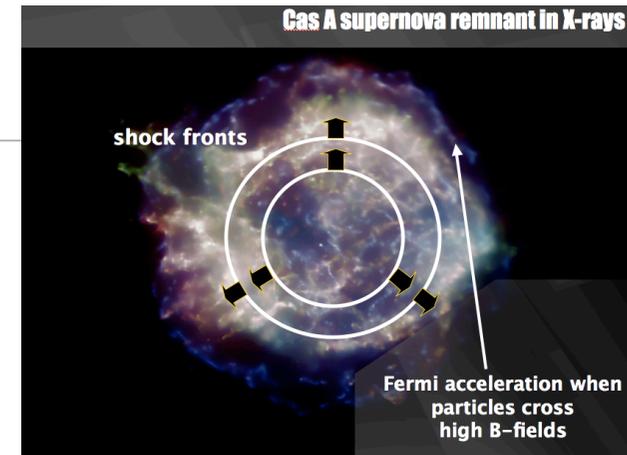
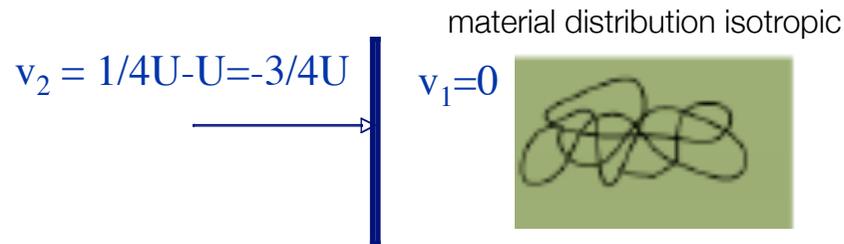
**1<sup>nd</sup> order in the velocity of the shock**



Shock front at rest: upstream gas flows into shock with velocity  $v_1 = U$  and leaves the shock with smaller velocity  $v_2 = U/4$

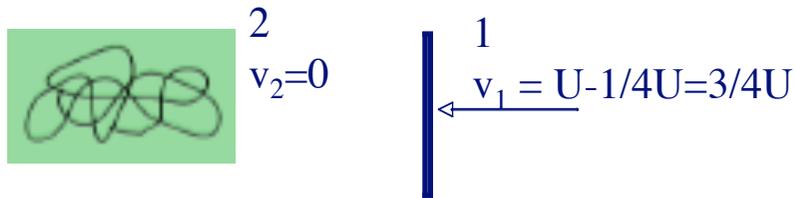
# Supernova remnants and shock acceleration

Upstream material rest frame



Let's consider the particles **upstream with the front**. Here the particle distribution is isotropic. The shock advances through the medium at velocity  $U$ , but the gas behind the shock travels at velocity  $3/4U$  relative to the upstream gas. When a high energy particle crosses the shock front, it obtains a small increase in the energy of the order of  $\Delta E/E \sim U/c$

Downstream material frame



Let us consider the opposite process of a particle diffusing from behind the shock (**downstream**) to the upstream region. The velocity distribution of particles is isotropic downstream the shock and when they cross the shock front they encounter gas moving towards the shock front with the velocity  $3/4U$ . The particle undergoes exactly the same process of receiving a small increase in the energy on crossing the shock from downstream to upstream. **So every time the particle crosses the shock it receives an increase of energy and the increment is the same in both directions**

Increase of energy for particle crossing the shock front in both directions:  $\Delta E/E \sim U/c$

# Spectrum from 1<sup>st</sup> Fermi acceleration

Total flux of particles that cross the shock

- $(E-E_0)/E_0 \sim U/c \Rightarrow \beta = E/E_0 = 1+U/c$

- For  $U \ll c$  (non relativistic shock)  $\ln \beta = \ln(1+U/c) \sim U/c$

- Average particles lost across the shock  $\sim U/c$

- Probability remains in acceleration region and will cross the shock again:  $P \sim 1-U/c \Rightarrow \ln(1+P) \sim -U/c$  ( $U \ll c$ )

- $\ln P / \ln \beta \sim -1$

integral spectral index

- After  $k$  collisions:

$$\left. \begin{aligned} \frac{E}{E_0} = \beta^k &\Rightarrow k \ln \beta = \ln \frac{E}{E_0} \\ \frac{N}{N_0} = P^k &\Rightarrow k \ln P = \ln \frac{N}{N_0} \end{aligned} \right\} \Rightarrow k = \frac{\ln \frac{E}{E_0}}{\ln \beta} = \frac{\ln \frac{N}{N_0}}{\ln P} \Rightarrow$$

$$\ln \frac{N}{N_0} = \frac{\ln P}{\ln \beta} \times \ln \frac{E}{E_0} = \ln \left( \frac{E}{E_0} \right)^{\ln P / \ln \beta} \Rightarrow \frac{N}{N_0} = \left( \frac{E}{E_0} \right)^{\ln P / \ln \beta}$$

differentiating  $dN \propto E^{\ln P / \ln \beta - 1} dE \Rightarrow \frac{dN}{dE} \propto E^{-2}$

$$\Phi_+ = \frac{1}{4\pi} \int d\Omega \Phi_i \cos\theta = \frac{\rho c}{4}$$

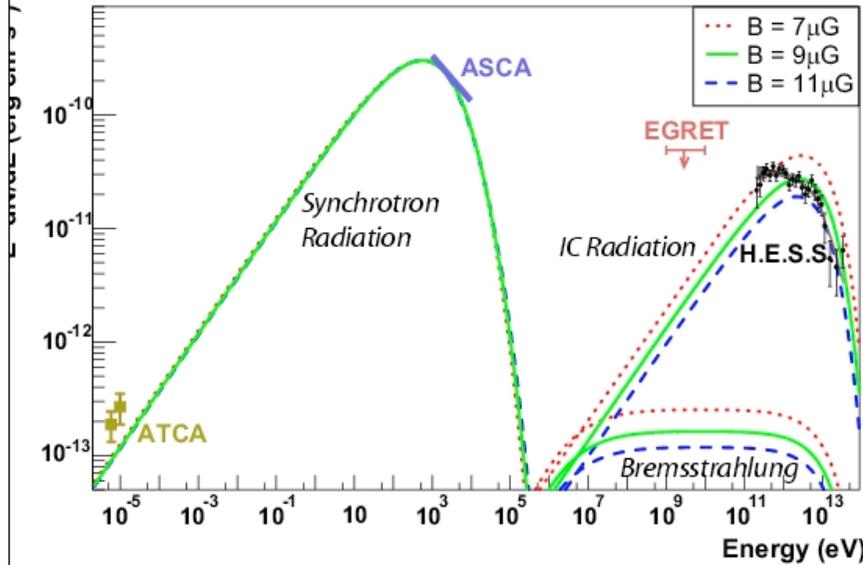
$\rho$  = density of particles.

Flux of particles that cannot cross again the shock  $\rho v_1 = \rho U$

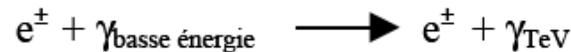
So the fraction of particles lost is  $(\rho U) / (1/4\rho c) \sim U/c$

# RX J1713.7-39.46

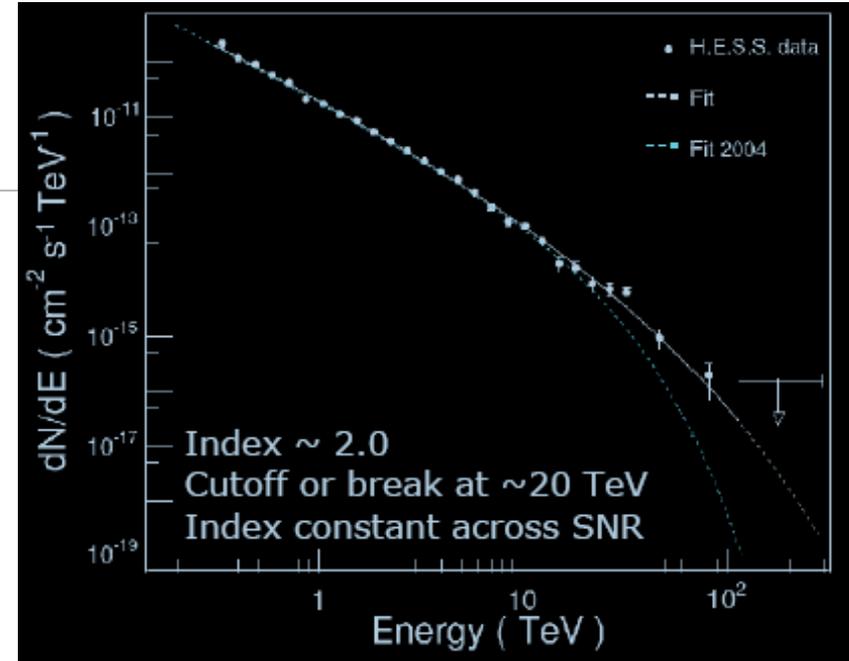
**IC model:** B-field cannot exceed 10  $\mu\text{G}$  and ...  
does not provide good spectral fit



Electrons emit synchrotron radiation. Relativistic electrons make Inverse Compton scattering on ambient photons that are seen then at higher energies.



For high B-fields synch losses dominate over IC losses. Large  $E_{e,\text{max}}$  ( $> 100 \text{ TeV}$ ) can be achieved only for  $B \leq 10 \mu\text{G}$



- Particles up to  $>100 \text{ TeV}$
- If hadrons  
primary energy  $>200 \text{ TeV}$
- If leptons  
primary energy  $>100 \text{ TeV (KN)}$

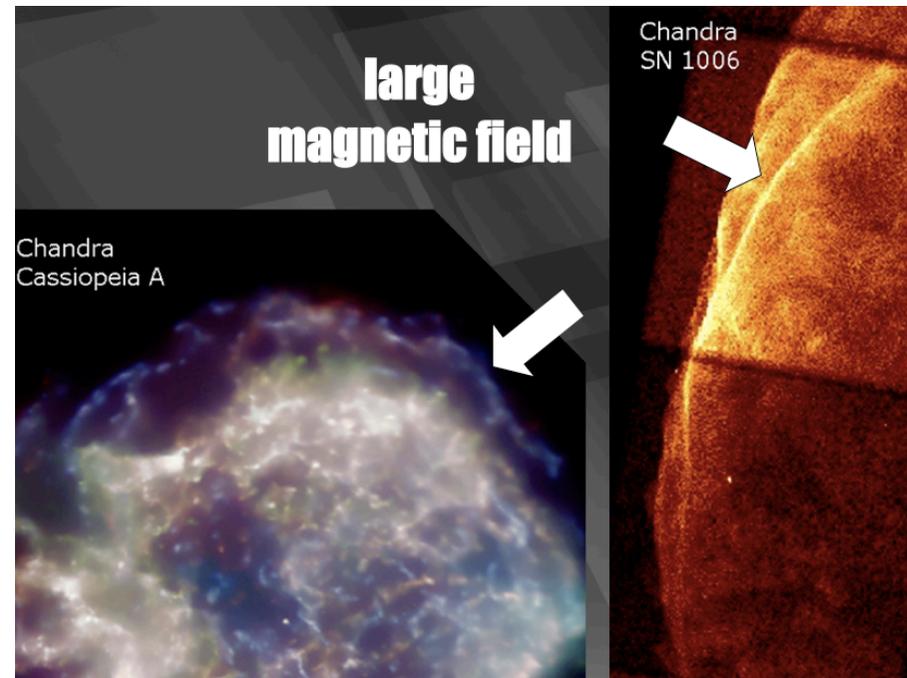
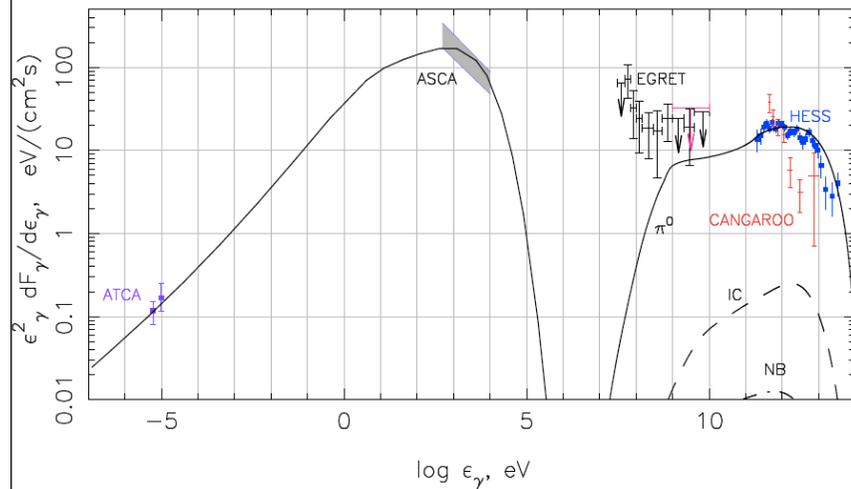
$$E_e^{\text{max}} = 2,3 \cdot 10^4 \frac{v_1}{c} \left( \frac{B}{1 \text{ G}} \right)^{-\frac{1}{2}} \text{ GeV} \quad v_1 = \text{velocity of particle upstream shock}$$

$$B \sim 10 \mu\text{G} \text{ et } v_1 \sim 10^8 \text{ cm} \cdot \text{s}^{-1} \quad 2,2 \cdot 10^5 \text{ GeV}$$

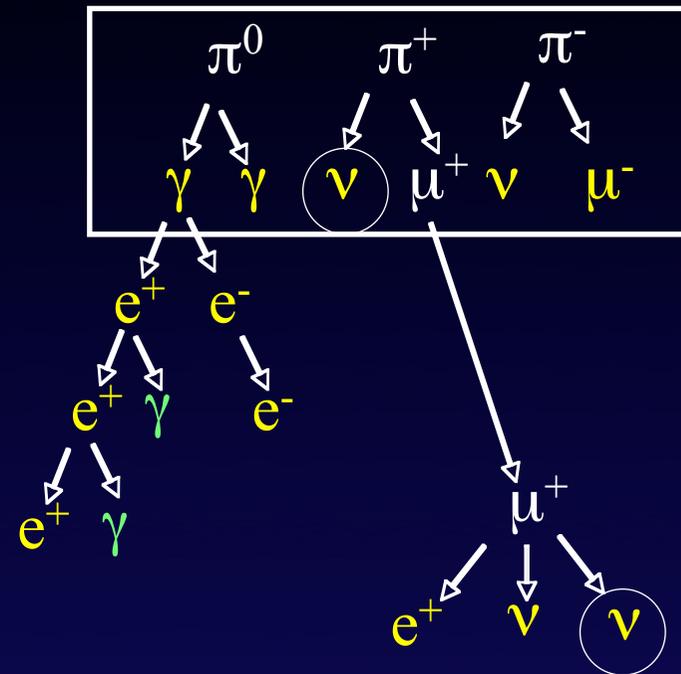
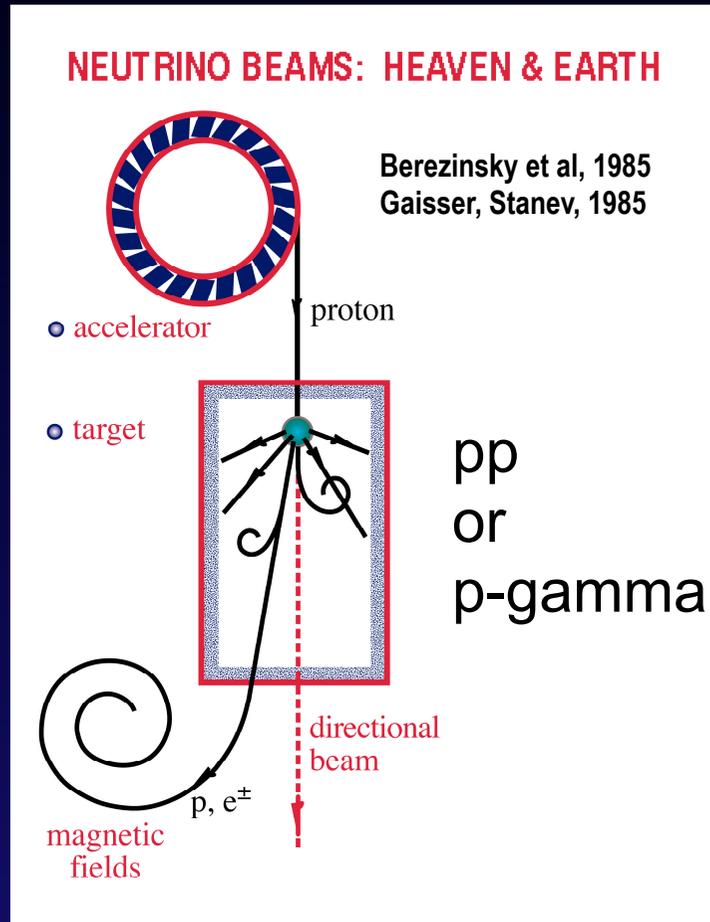
# Hadrons in SNRs?

SED of RX J1713.7-3946  
Berezhko, Volks ICRC2007  
B-field required for fit is  $126\mu\text{G}$  for pion production. In models with magnetic field amplification the energy at which SNR accelerate can be as high as  $Z \times 10^3 \text{ TeV}$  at early stages of SNR evolutions.

High resolution X-ray observations of SNR rims: brightness profiles connected to intensity of B-fields  $\sim 100\mu\text{G}$



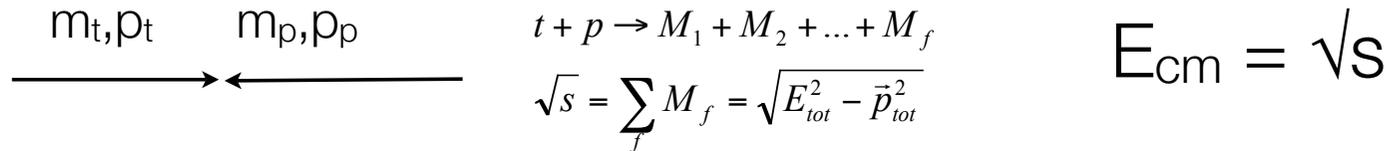
# The generic source of neutrinos



Connection with gamma  
 Same order of magnitude for  
 neutrino flux and gamma flux if no  
 attenuation of gammas

# Reminder on reaction thresholds

CM frame

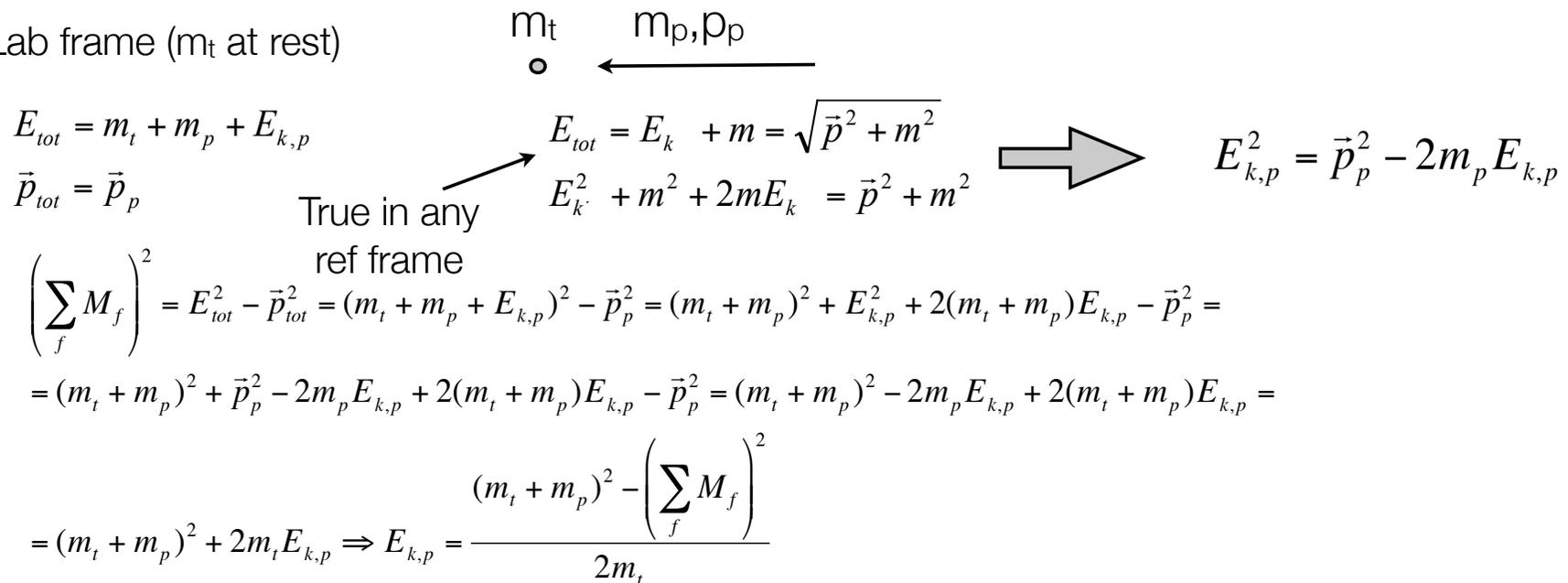


$$m_t, p_t \quad m_p, p_p \quad t + p \rightarrow M_1 + M_2 + \dots + M_f \quad E_{\text{cm}} = \sqrt{s}$$

$$\sqrt{s} = \sum_f M_f = \sqrt{E_{\text{tot}}^2 - \vec{p}_{\text{tot}}^2}$$

energy of projectile available to produce particles at rest in final state:

Lab frame ( $m_t$  at rest)



$$E_{\text{tot}} = m_t + m_p + E_{k,p}$$

$$\vec{p}_{\text{tot}} = \vec{p}_p$$

$$E_{\text{tot}} = E_k + m = \sqrt{\vec{p}^2 + m^2}$$

$$E_k^2 + m^2 + 2mE_k = \vec{p}^2 + m^2 \Rightarrow E_{k,p}^2 = \vec{p}_p^2 - 2m_p E_{k,p}$$

True in any ref frame

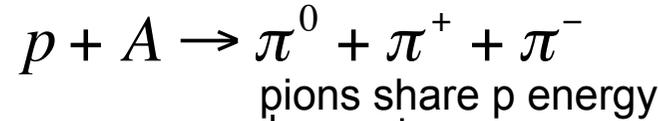
$$\left( \sum_f M_f \right)^2 = E_{\text{tot}}^2 - \vec{p}_{\text{tot}}^2 = (m_t + m_p + E_{k,p})^2 - \vec{p}_p^2 = (m_t + m_p)^2 + E_{k,p}^2 + 2(m_t + m_p)E_{k,p} - \vec{p}_p^2 =$$

$$= (m_t + m_p)^2 + \vec{p}_p^2 - 2m_p E_{k,p} + 2(m_t + m_p)E_{k,p} - \vec{p}_p^2 = (m_t + m_p)^2 - 2m_p E_{k,p} + 2(m_t + m_p)E_{k,p} =$$

$$= (m_t + m_p)^2 + 2m_t E_{k,p} \Rightarrow E_{k,p} = \frac{(m_t + m_p)^2 - \left( \sum_f M_f \right)^2}{2m_t}$$

# The photon $\leftrightarrow$ neutrino connection

pp interactions



2 photons with:  $E_\gamma \approx E_\pi/2 \approx E_p/6$

$e + 2\nu_\mu + \nu_e$

For each gamma 2 muon neutrinos with:  $E_\nu \approx E_\pi/4 \approx E_p/12$

Hence energy in photons and gammas is the same:

After oscillations:  $\nu_\mu/\gamma \sim 0.5$

$$\int_{E_\gamma^{\min}}^{E_\gamma^{\max}} E_\gamma \frac{dN_\gamma}{dE_\gamma} dE_\gamma = K \int_{E_\nu^{\min}}^{E_\nu^{\max}} E_\nu \frac{dN_\nu}{dE_\nu} dE_\nu, \quad K \sim 0.5$$

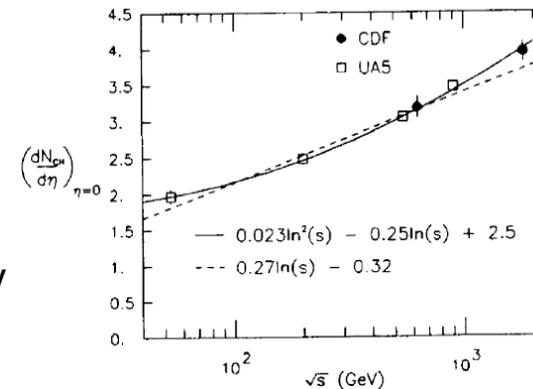
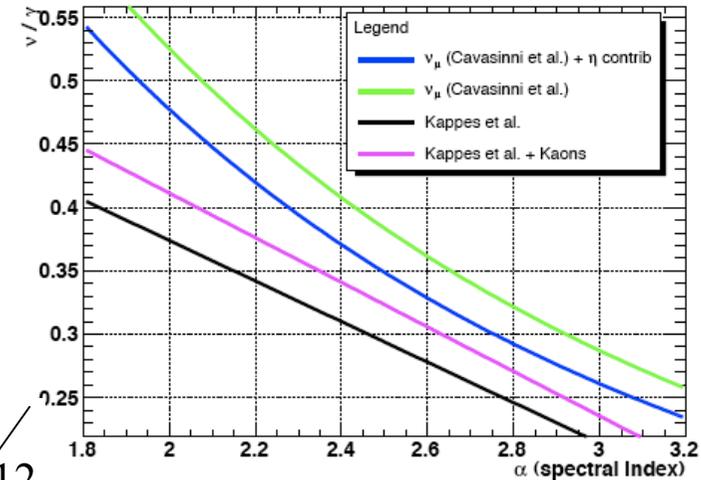
particle multiplicity in pp

$$E_p^{\max} = 6E_\gamma^{\max}, \quad E_\nu^{\max} = \frac{1}{12} E_p^{\max},$$

$$p + p \rightarrow p + p + \pi^0$$

$$E_p^{\min} = \Gamma \frac{(2m_p + m_\pi)^2 - 2m_p^2}{2m_p} \simeq \Gamma \times 1.23 \text{ GeV}, \quad p + p \rightarrow p + n + \pi^+$$

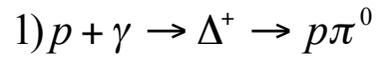
$\nu/\gamma$  after oscillations



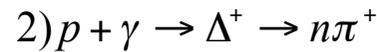
Minimum proton energy fixed by threshold for  $\pi$  production ( $\Gamma = E/m$  is the Lorentz factor of the p jet respect to the observer)

# The photon $\leftrightarrow$ neutrino connection

## py interactions



BR = 2/3



BR = 1/3

E of gammas in lab (p at rest)

$$E_{k,p} = \frac{\left(\sum_f M_f\right)^2 - (m_i + m_p)^2}{2m_i} = \frac{(m_N + m_\pi)^2 - m_p^2}{2m_p} \sim 150 \text{ MeV}$$

$$E_\gamma = \gamma_p \varepsilon_\gamma = 150 \text{ MeV}$$

Energy of gammas p rest frame      Energy of gammas in CM

$$E_{p,thr} = \gamma_p m_p = 150 \text{ MeV} \times m_p / \varepsilon_\gamma = \left(\frac{1 \text{ MeV}}{\varepsilon_\gamma}\right) \times 150 \text{ GeV}$$

2 gammas with  $2/3 \times 0.1 E_p = 4/3 \times 0.1 E_p$   
 2 muon neutrinos (if muon decays) with  $1/3 \times 0.1 E_p / 2 = 1/3 \times 0.1 E_p$

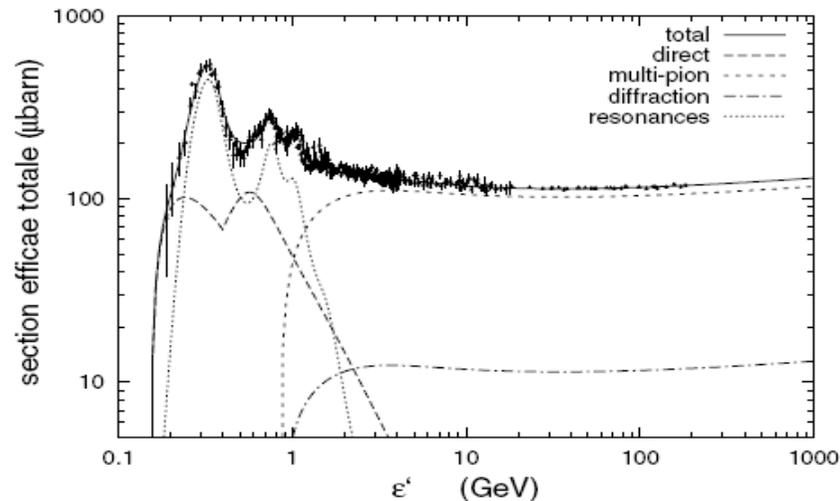
$$E_\gamma = \frac{E_p \langle x_{p \rightarrow \pi} \rangle}{2} = 10\% E_p$$

$$E_\nu = \frac{E_p \langle x_{p \rightarrow \pi} \rangle}{4} = 5\% E_p$$

$$\langle x_{p \rightarrow \pi} \rangle \approx 0.2$$

$$\int_{E_\gamma \min}^{E_\gamma \max} E_\gamma \frac{dN_\gamma}{dE_\gamma} dE_\gamma = K \int_{E_\nu \min}^{E_\nu \max} E_\nu \frac{dN_\nu}{dE_\nu} dE_\nu$$

K = 2 after oscillations are accounted for



Halzen and Hooper, astro-ph/0502449

# Current scenario

Giunti

- The relation between flavor states and mass ones contains a  $3 \times 3$  matrix  $V = U A$ ,  $A$  relevant only if neutrino is Majorana and  $U = \text{MNSP}$  matrix

B. Pontecorvo, Sov. Phys. JETP 7, 172 (1958) [Zh. Eksp. Teor. Fiz. 34, 247 (1957)],  
Z. Maki, M. Nakagawa and S. Sakata, Prog. Theor. Phys. 28 870 (1962)

$$A = \begin{pmatrix} e^{i\alpha} & 0 & 0 \\ 0 & e^{i\beta} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

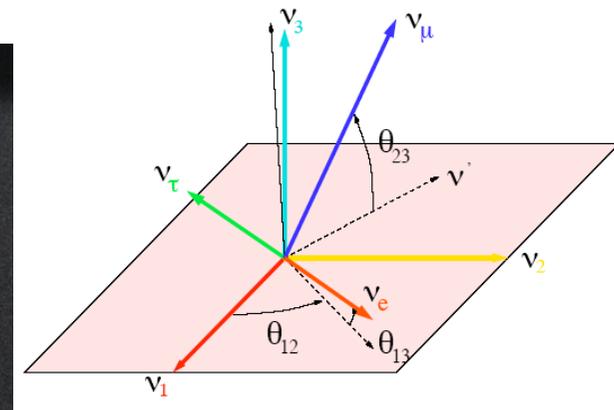
solar  $U_{e1}, U_{e2} \leftrightarrow \theta_{12}$ , CHOOZ  $U_{e3} \leftrightarrow \theta_{13}$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

atmospheric  $U_{e3} \leftrightarrow \theta_{13}$ ,  $U_{\mu 3}, U_{\tau 3} \leftrightarrow \theta_{23}$

$$s_{ij} \equiv \sin \theta_{ij}, c_{ij} \equiv \cos \theta_{ij}$$

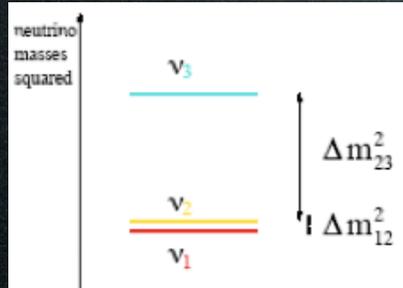
Neutrino scenario depends on 3 angles ( $\theta_{12}$ ,  $\theta_{23}$  and  $\theta_{13}$ ), 2 square mass differences ( $\Delta m_{12}^2$  and  $\Delta m_{23}^2$ ) and a CP violation phase  $\delta$



# Astrophysical neutrino oscillations

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_i |U_{\alpha,i}|^2 |U_{\beta,i}|^2 + 2 \sum_{i < j} U_{\alpha,i} U_{\beta,i} U_{\alpha,j} U_{\beta,j} \cos\left(\frac{\Delta m_{ij}^2 L}{2E}\right)$$

$$\Delta m_{31}^2 \sim \Delta m_{32}^2 \gg \Delta m_{21}^2$$



$2 \times 10^{-3} \text{ eV}^2$  atmospheric

$7 \times 10^{-5} \text{ eV}^2$  solar

$$\theta_{13} = 0$$

For astrophysical source @1 kpc emitting  $\nu$ s of 10 TeV:  
**COS $\phi$  averages to zero** since the extension of sources  
 about 1 pc and distance 1 kpc so L known with precision 1/1000 not 1/10<sup>8</sup>

$$\phi \sim 3 \cdot 10^8 \left( \frac{\Delta m^2}{8 \cdot 10^{-5} \text{ eV}^2} \right) \left( \frac{L}{1 \text{ kpc}} \right) \left( \frac{10 \text{ TeV}}{E_\nu} \right)$$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_i |U_{\alpha,i}|^2 |U_{\beta,i}|^2$$

$$P(\nu_e \rightarrow \nu_e) = \sum_i |U_{ei}|^2 |U_{ei}|^2 = |U_{e1}|^4 + |U_{e2}|^4 + |U_{e3}|^4 = 0.82^4 + 0.57^4 + 0 = 0.56$$

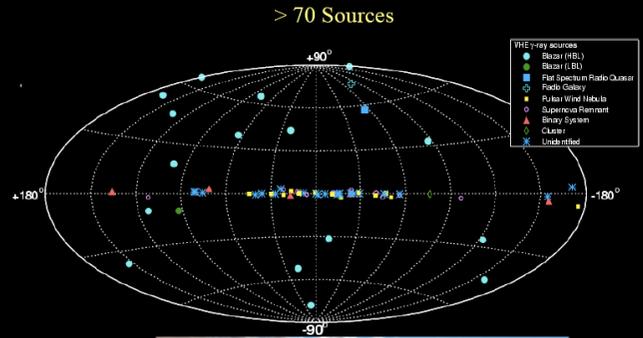
$$P(\nu_e \rightarrow \nu_\mu) = \sum_i |U_{ei}|^2 |U_{\mu i}|^2 = |U_{e1}|^2 |U_{\mu 1}|^2 + |U_{e2}|^2 |U_{\mu 2}|^2 + |U_{e3}|^2 |U_{\mu 1}|^2 = 0.82^2 \cdot 0.4^2 + 0.57^2 \cdot 0.58^2 + 0 = 0.22$$

$$P(\nu_e \rightarrow \nu_\tau) = \sum_i |U_{ei}|^2 |U_{\tau i}|^2 = |U_{e1}|^2 |U_{\tau 1}|^2 + |U_{e2}|^2 |U_{\tau 2}|^2 + |U_{e3}|^2 |U_{\tau 1}|^2 = 0.82^2 \cdot 0.4^2 + 0.57^2 \cdot 0.58^2 + 0 = 0.22$$

$\nu_\alpha \backslash \nu_\beta$	$\nu_e$	$\nu_\mu$	$\nu_\tau$
$\nu_e$	60%	20%	20%
$\nu_\mu$	20%	40%	40%
$\nu_\tau$	20%	40%	40%

# Current VHE $\gamma$ -ray Instruments

3 TeV sources in 1995  
> 70 in 2008



MILAGRO



STACEE



MAGIC



TIBET



Brenda  
Dingus' talk

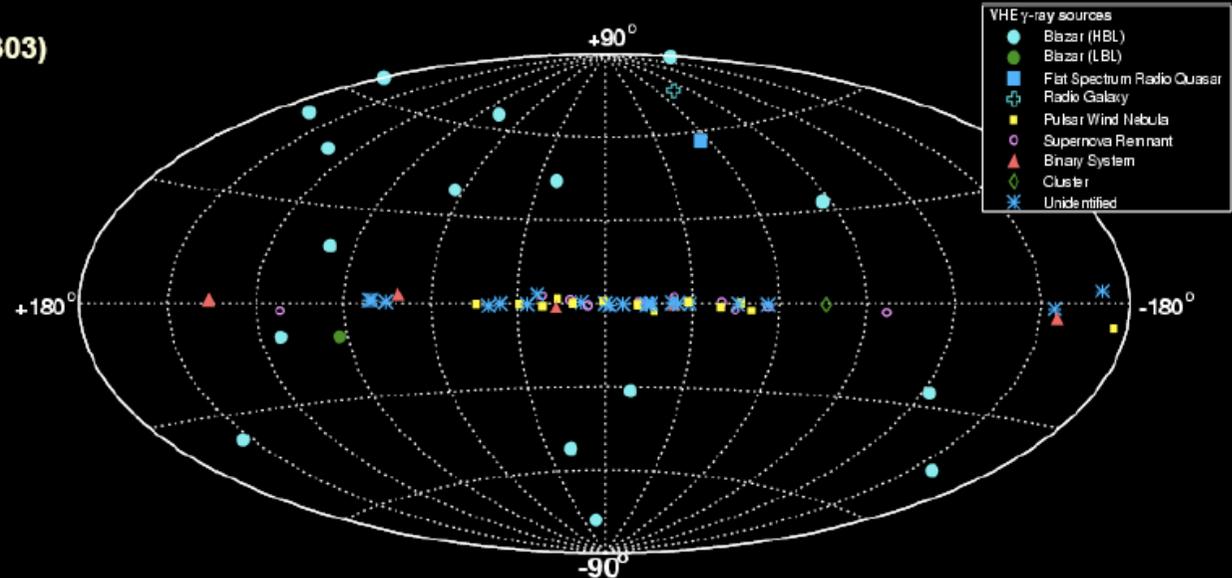


# TeV Sky 2008

## GALACTIC :

- Young Shell type Supernova Remnants
- Older and/or Interacting SNRs
- Composite SNRs
- Pulsar Wind Nebulae (PWN)
- Binary Systems (LS 5039, LSI +61 303)
- Variable PWN in binary
- Open Stellar Clusters
- Galactic Center
- Galactic diffuse emission
- Unidentified sources ...

> 70 Sources

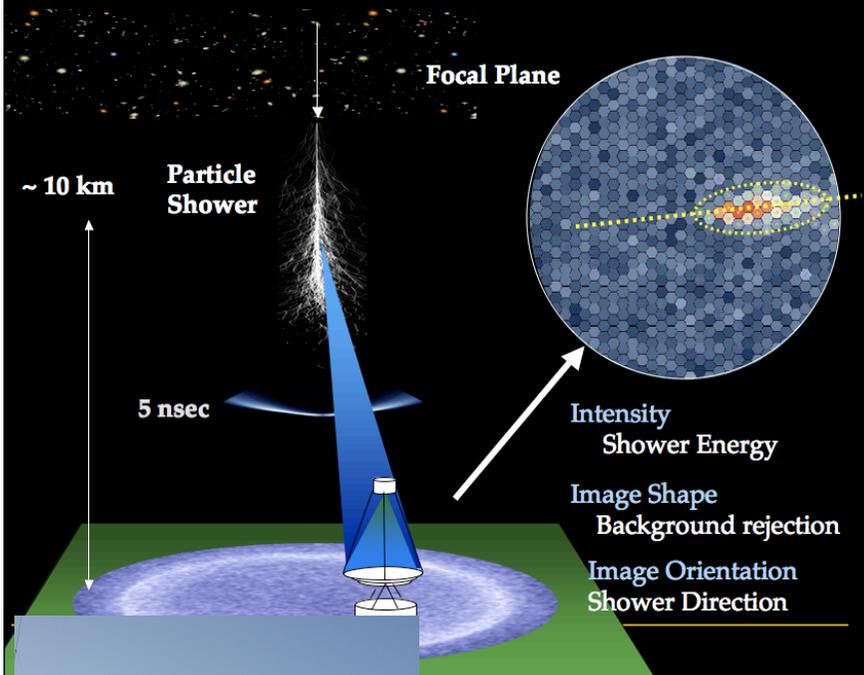


2007-09-15 - Up-to-date plot available at <http://www.mppmu.mpg.de/~rwagner/sources/>

## EXTRAGALACTIC :

- Blazars
- Radiogalaxies (FR II: M87+?)
- Flat Spectrum Radio Quasars (3C 273, recent)
- Extragalactic Background Light (EBL)
- Multiwave-length campaigns
- Starburst Galaxies (UL)
- GRBs (UL)
- ...

# Detection technique of IACT



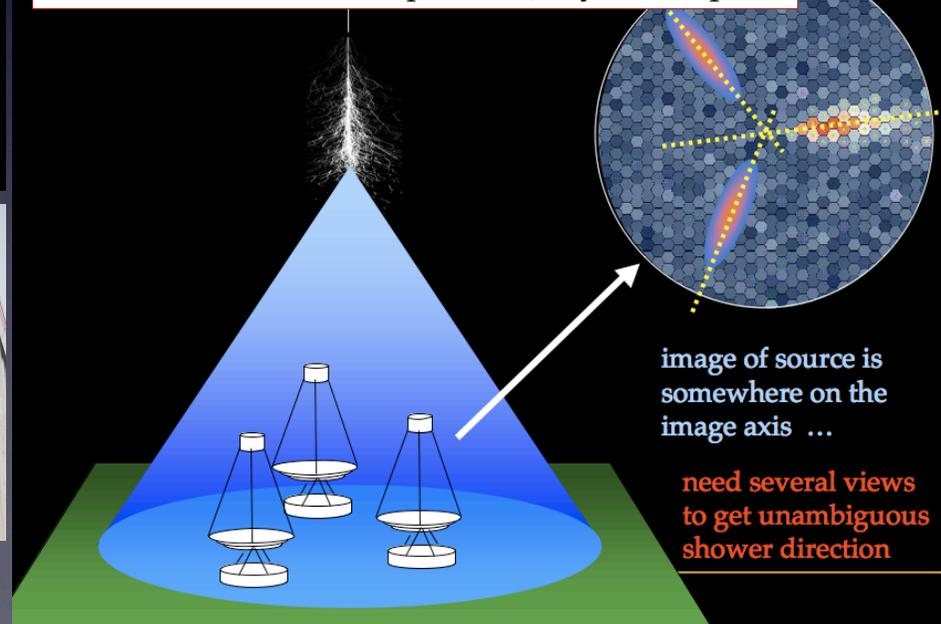
$$I_{\text{Crab}} = 3 \times 10^{-11} \text{ erg/cm}^2\text{s}$$

$$= 1.9 \times 10^{-11} \text{ TeV/cm}^2\text{s} \text{ (100 GeV-10 TeV)}$$

$$1 \text{ TeV} = 1.6 \text{ erg}$$

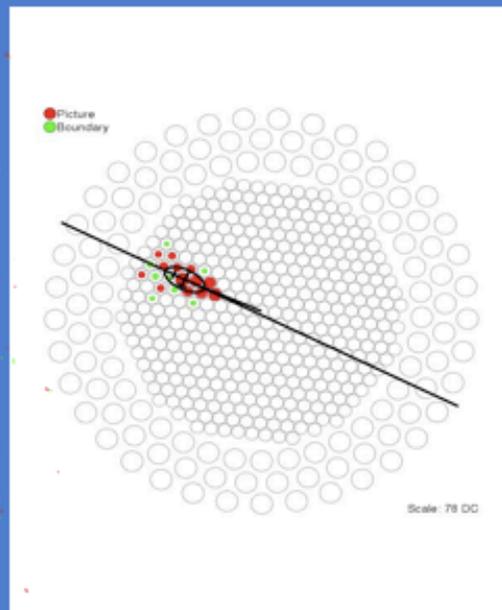
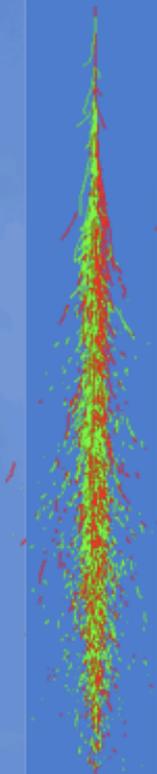
Stereoscopic IACT arrays

as perfect  $\gamma$ -ray-telescopes!

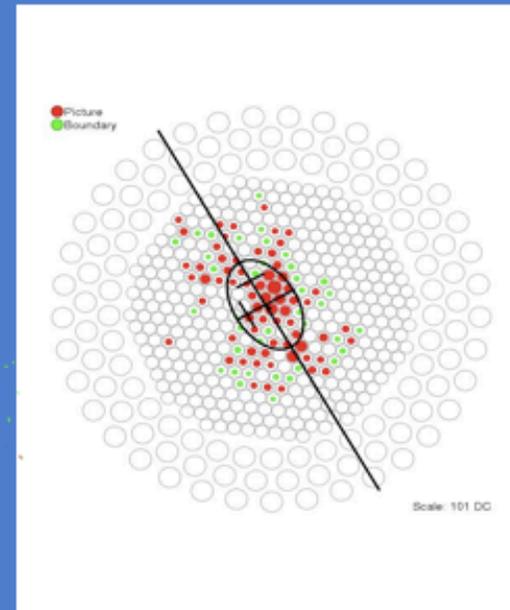
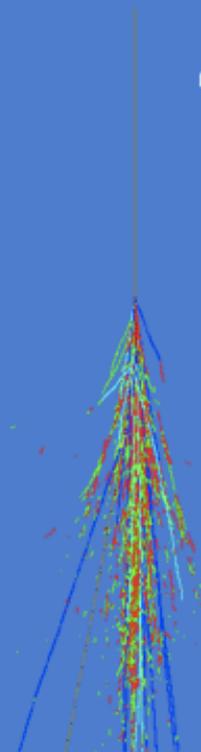


# Air shower images

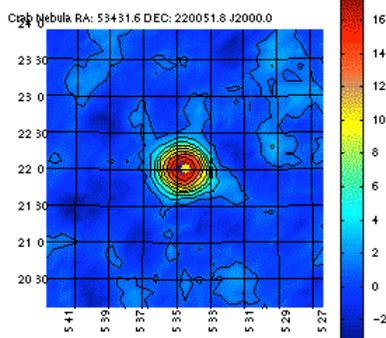
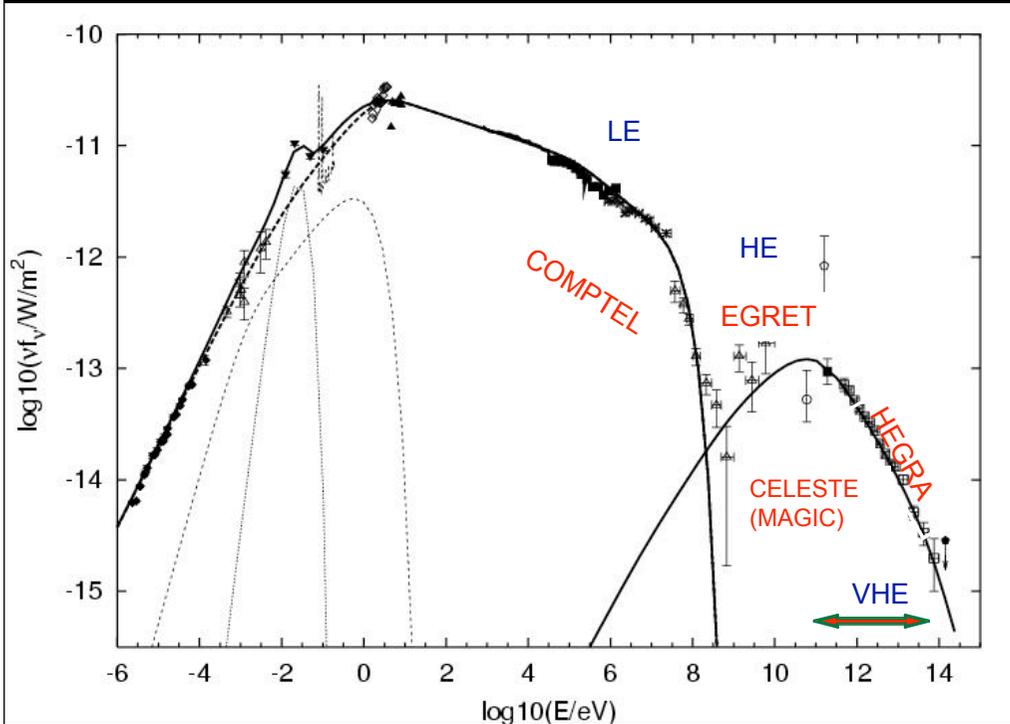
$\gamma$  primary



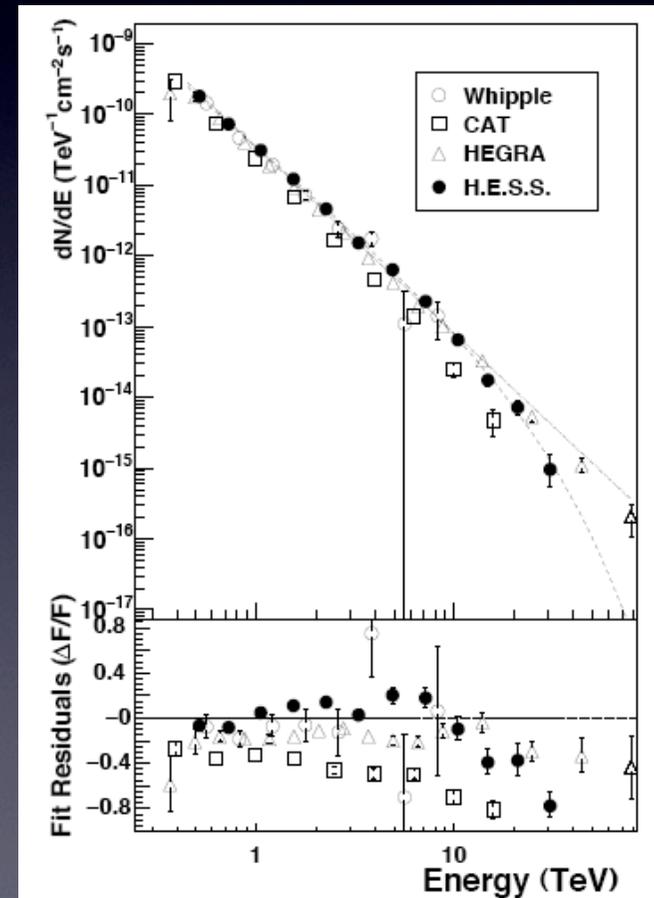
“hadron” primary



# Standard Candle: Crab



HESS 2006  
 cut-off at  $14.3 \pm 2.1 \text{ stat} \pm 2.8 \text{ sys TeV}$   
 spectral index =  $2.39 \pm 0.03 \text{ stat} \pm 0.09 \text{ sys}$   
 flux  $> 1 \text{ TeV}$   
 $2.26 \pm 0.08 \text{ stat} \pm 0.45 \text{ sys} \times 10^{-11} \text{ cm}^{-2} \text{ s}^{-1}$



# Neutrino fluxes from SNRs

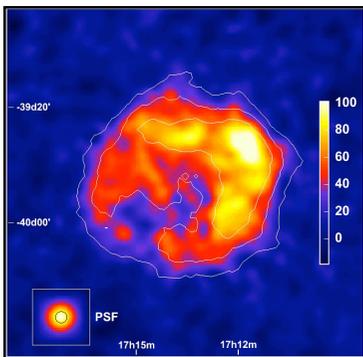
a SNR at  $d = 1$  kpc transfers  $W = 10^{50}$  erg to cosmic rays interacting with molecular clouds with density  $n = 1 \text{ cm}^{-3}$

$$E \frac{dN_\gamma}{dE} (> 1 \text{ TeV}) =$$

$$= 10^{-11} \sim 10^{-12} \frac{\text{photons}}{\text{cm}^2 \text{ s}} \frac{W}{10^{50} \text{ erg}} \frac{n}{1 \text{ cm}^3} \left(\frac{d}{1 \text{ kpc}}\right)^{-2} \text{ km}^3 \text{ detector } 5 \text{ yr}$$

$$\frac{dN_\nu}{dt} = \int dE_\nu A_\nu^{\text{eff}} \frac{dN_\nu}{dE_\nu}$$

$$\frac{dN_\nu}{dE_\nu} = A_\nu \cdot E_\nu^{-\alpha_\nu} \cdot \exp\left(-\frac{E_\nu}{E_{\text{max}}}\right)$$



cut-off in gamma may be due to absorption not only acceleration mechanism

Kappes et al, astro-ph/0607286  
pp - interactions

